## Prediction Market 1 CSCI 1440/2440 2025-04-14

## 1 Prediction Markets

A **prediction market** is a market in which securities are traded based on the predicted outcomes of future events. Prediction markets can be based on the future outcomes of sporting events, elections, or even the weather. They are interesting because they effectively aggregate the beliefs of all participants, so that the market price conveys the collective belief/probability of an outcome.

## 2 Market with One Decoy

In today's market, we will flip two fair coins: *C*, the true coin; and *D*, the decoy coin. We will then independently and uniformly at random choose one of the two coin flips to reveal to each student in lab.

You, the students, will then begin trading contracts that are worth \$100 if the true coin is heads, and \$0, if it is tails. Once trading subsides, we will reveal the value of *C* and *D*, and settle all contracts.

50% chance of seeing decoy

HT TH

## 3 Questions

For all questions, assume that you are told "heads".

- 1. What is the probability that *C* is heads? (1/2\*1)+(1/2\*1/2)=1/2+1/4=3/4
- 2. Let's say you find out that another person was also told "heads". What is the probability that C is heads? (1/2\*1)+(1/2\*1/2)=1/2+1/4=3/4

If I and they saw true: (1/2\*1/2\*1) = 1/4If one of us saw true: 2\*(1/2\*1/2\*1) = 1/2If we both saw fake: (1/2\*1/2\*1/2) = 1/8

- 3. Let's say you find out that one other person was told "tails". What is the probability that *C* is heads?
- 4. Let's say you find out that 1000000 other people were told "tails". What is the probability that *C* is heads?

Either HT or TH I saw true: (1/2.1,000,000\*1) + they saw true 0

I saw true: (1/2 \* 1/2\*1) + they saw true 0

probability of C = heads and D = tails: 1/4

- 5. Let  $f_H$  be the fraction of other people that are told heads. What are the two most likely values for  $f_H$ , keeping in mind that you were told heads.
- 6. How might you infer what other people were told from how they behave in the market?

If price of contract goes down or if there is a lot of selling, true coin must