## Traffic Sign Project Report

April 20, 2018

#### 1 Project Goal

The goal of this project is to build a convolutional neural network to classify traffic signs in the German Traffic Sign dataset[1], and evaluate its performance.

#### 2 Data Exploration

The dataset consists of three subsets.

	Training	Validation	Test
Example Count	34799	4410	12630

The images in the dataset are in 32x32x3 RGB format. The total number of sign classes is 43.

We first verify that the class label distribution in each subset are consistent. See Figure 1 for a bar chart of class label count per subset. As we can see, the classes are not distributed evenly, which might cause some labels to be predicted more accurately later on, but the distribution is consistent in all three subsets, so evaluation with the validation and test sets should properly reflect model performance.

We also check if the colour distribution is consistent in three subsets. in Figure 2 we see that the RGB distribution is consistent in all three datasets.

### 3 Image Preprocessing

Before we train our network on the images, we first need to preprocess the data to provide a normalised input for the network. the easiest approach is to subtract the mean from the images half the range, but we observed that some images have larger range of colour and brightness variations than others, therefore a per-image normalisation is used to ensure consistent variation ranges for all images.

We also perform a data augmentation step for all training data by adding some random noise to the images. During training, before the network consumes the input, the input images are randomly perturbed in hue, brightness, saturation and contrast by a small amount. This helps increase the robustness of the network and reduce overfitting. We do not expand the original training set. Instead, we perform this perturbation each passthrough so that each epoch, the network trains on slightly different versions of each training example. Luckily, we can incorporate this step into the Tensorflow computation graph.

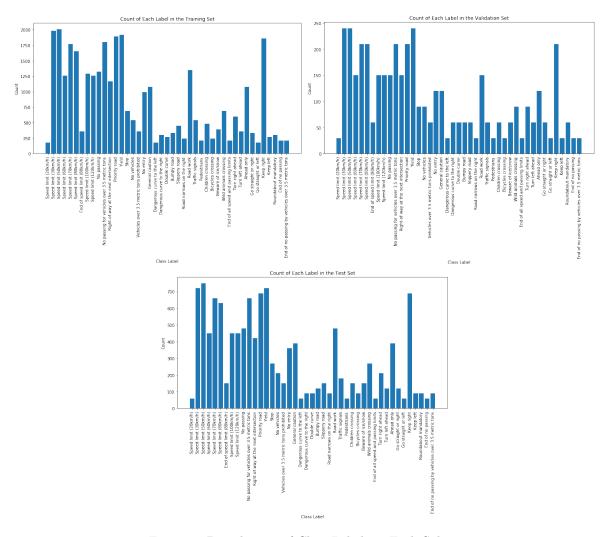


Figure 1: Distribution of Class Labels in Each Subset

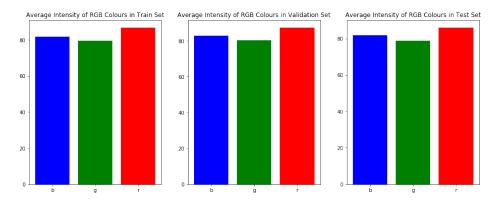


Figure 2: Distribution of RGB colours in Each Subset

#### 4 Model Architecture

Our network uses the following architecture:

Layer No.	Layer Type	Dimensionality	Activation	Note
1	Conv2D	16x[3, 3]	ReLU	Valid Padding, L1 Regularisation (0.1)
2	MaxPooling	[2, 2]	None	Stride=2
3	Conv2D	32x[3, 3]	ReLU	Valid Padding, L1 Regularisation (0.1)
4	MaxPooling	[2, 2]	None	Stride=2
5	Dense	512	ReLU	Batch Normalisation
6	Dropout	-	None	Drop Rate=0.7
7	Dense	512	ReLU	Batch Normalisation
8	Dropout	-	None	Drop Rate=0.7
9	Dense	43	Linear / Softmax	Output

The computation graph has an auxiliary boolean input is\_training to inform the network whether to perform noise adding and dropout in forward passthrough. The whole forward pass architecture can be seen in Appendix Figure 10.

[3, 3] kernels are found to perform better than [5, 5] kernels, likely due to the fact that the details in traffic signs exhibit difference on a small scale. L1 regularisation here is used to induce sparsity in the convolution kernels so they focus on different aspects of the input image. A pair of high dimensional dense layers are used in conjunction with a high dropout rate to achieve a balance between expressiveness and overfitting control. Batch normalisation is employed to combat rapid overfitting during training, in addition to the high dropout rate. An additional convolutional layer is found to be contributing little to the validation accuracy, so only two convolutional layers are used in this model.

#### 5 Training and Evaluation

The network is trained on the training dataset with a batch size of 32 over 20 epochs. Input images are shuffled each epoch. The network is trained with an Adam optimiser with a learning rate of  $5 \times 10^{-4}$ . Loss and accuracy are evaluated per epoch on both the training and validation set. The training vs validation loss over training steps is shown in figure 3.

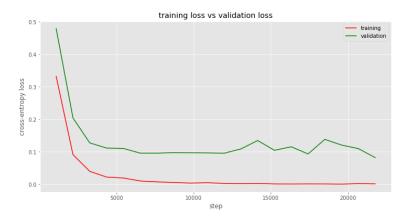


Figure 3: training vs validation loss

The final training accuracies are 99.96% on the training set and 98.18% on the validation set. The network achieves 96.22% accuracy on the test dataset.

### 6 Performance Analysis

To analyse the performance of the network in more detail, we acquired five new German traffic sign images from Google Image Search and predicted their top 5 labels with the classifier. Here are the results:

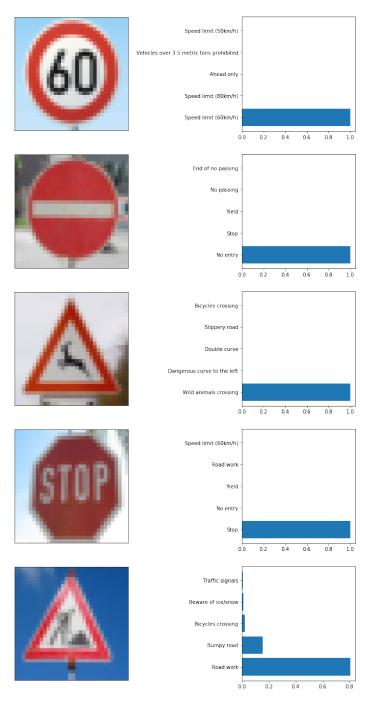


Figure 4: Prediction with New Images

As we see, the network is able to provide correct predictions for all images. In addition, it is able to provide "confident" predictions for all images except "Road Work". However, we will show later that the softmax probability is not a good measure of the network's confidence.

Since the network is able to correctly classify all new images, we have to examine the misclassified images in the test dataset to figure out how it behaves when it fails to classify correctly. Here are some of the examples of misclassification:

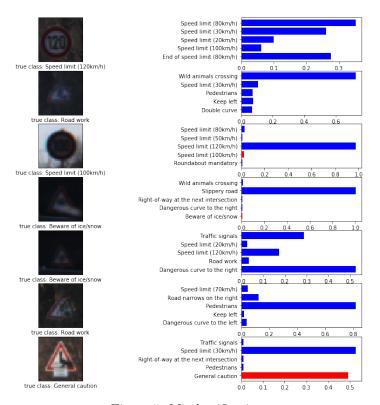


Figure 5: Misclassifications

Here, we see that in some cases, the softmax probability reflects the uncertainty of the classifier (such as the first image), whereas in some other cases, even though the image is so blurry that eeven a human cannot easily label it, the network provides an extremely "confident" output that is quite wrong. Is there another way to estimate the uncertainty of the network? Recall that we do not include the noise adding and dropout steps in the evaluation pipeline. One idea is to add these stochastic elements back into the network, let it predict with uncertainty, and examine a sample of its prediction to gauge its confidence. As an example, we take the sixth image ("Road work") and run it through the network 10000 times with noise and dropout enabled (Figure 6).

As we see in the bar chart, even though the network is still unable to guess the correct label, the distribution of different labels in the sample is closer than the softmax probabilities to where the uncertainty should be.

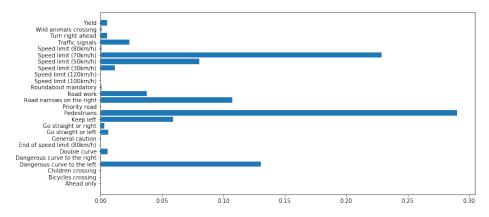


Figure 6: Stochastic Prediction Sample

We also calculate the per-class percision and recall in Appendix Table 1. The classes with the worst precision are **Speed limit (20km/h)**, **Pedestrians and Beware of ice/snow**, and the classes with the worst recall are **Speed limit (120km/h)**, **Pedestrians and Dangerous curve to the right**. Overall, the network is struggling the most with the class **Pedestrians**. We wonder why this is the case. Here are the classes that **Pedestrian** images are most commonly classified as:

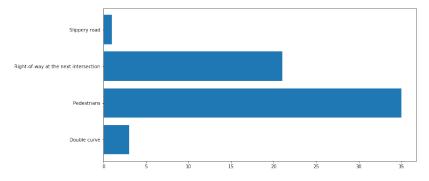


Figure 7: Pedestrian Class Prediction Outcome

It appears that the network frequently confuses **Pedestrian** with **Right-of-way at the next intersection**, which is indeed very similar in appearance. At the given image resolution, it is even difficult for humans to distinguish between the two.

#### 7 Activation Visualisation

Neural networks are often treated as black boxes, as the precise function of each layer and each node is difficult to pinpoint. However, sometimes it is possible to crudely estimate the function of a convolution kernel in a CNN by examining its activation patterns. Here, we visualise the mean activations of our convolutional layers for all circular-plate signs versus triangular-plate signs. We focus on the first convolutional layer, as the second layer is harder to interpret.

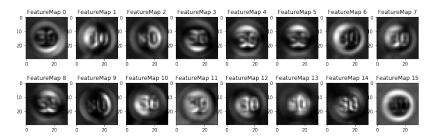


Figure 8: Conv Layer 1 for Circular Plates

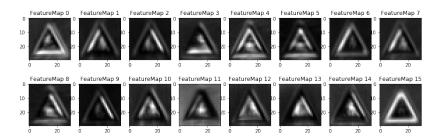


Figure 9: Conv Layer 1 for Triangular Plates

Notice that in both cases, the feature map 15 in the first convolution layer is always detecting the coloured stripe / ring around the sign, regardless of the shape of the sign, whereas feature map 13 in the first convolution layer always focuses on the interior of the sign. The different kernels focus on different aspects of the input images and create more meaningful features for the following layers.

### 8 Further Improvements

The current network architecture and data pipeline are not perfect and may still be improved. For example, the data augmentation step only used per-pixel noise-adding. By utilising other transformations such as rotation and translation, we may further improve the performance. The network also appears to struggle a little bit with some off-centre images or smaller signs, so some form of multiscale solution (such as parallel convolutional layers of different kernel sizes) can be helpful. Also, the training curve of the network shows that the validation loss has not yet stablised or "bounced back", so we may not have reached optimality during training yet. By tweaking the training parameters, we may be able to reach a better optimal point.

#### References

[1] STALLKAMP, J., SCHLIPSING, M., SALMEN, J., AND IGEL, C. The German Traffic Sign Recognition Benchmark: A multi-class classification competition. In *IEEE International Joint Conference on Neural Networks* (2011), pp. 1453–1460.

# Appendix

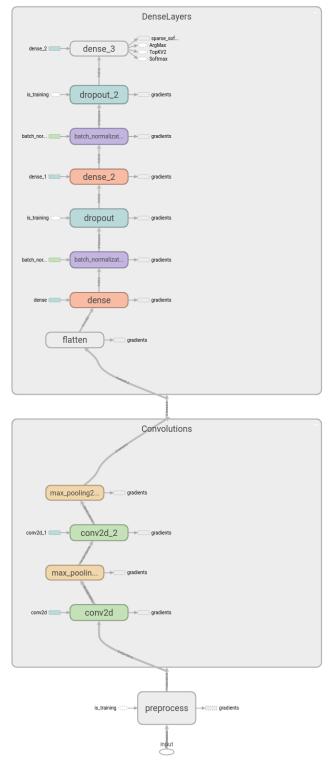


Figure 10: Network Architecture

Table 1: Per-class Precision and Recall

0     0     Speed limit (20km/h)     0.566667     1.000000     42       1     1     Speed limit (30km/h)     0.988889     0.966079     15       2     2     Speed limit (50km/h)     0.980000     0.965834     18       3     3     Speed limit (60km/h)     0.935556     0.972286     32       4     4     Speed limit (80km/h)     0.9953968     0.999228     28       6     6     End of speed limit (80km/h)     0.820000     0.991935     38       7     7     Speed limit (120km/h)     0.882222     0.985112     35       8     8     Speed limit (120km/h)     0.882222     0.985112     35       8     8     Speed limit (120km/h)     0.993333     0.807838     8       9     9     No passing     0.997500     0.979339     16       10     10     No passing for vehicles over 3.5 metric tons     0.975758     0.993827     22       11     11     Right-of-way at the next intersection     0.995652     0.984241     5 </th <th>0 26 27 24 12 35 10 15 42 22</th>	0 26 27 24 12 35 10 15 42 22
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3     Speed limit (60km/h)     0.935556     0.972286     32       4     4     Speed limit (70km/h)     0.966667     0.990683     23       5     5     Speed limit (80km/h)     0.953968     0.909228     28       6     6     End of speed limit (80km/h)     0.820000     0.991935     38       7     7     Speed limit (100km/h)     0.882222     0.985112     35       8     8     Speed limit (120km/h)     0.993333     0.809783     8       9     9     No passing     0.987500     0.979339     16       10     10     No passing for vehicles over 3.5 metric tons     0.997550     0.993827     22       11     11     Right-of-way at the next intersection     0.992857     0.892934     9       12     12     Priority road     0.995652     0.984241     5       13     13     Yield     0.997222     0.993084     3       14     14     Stop     0.996296     1.000000     4       15     15	12 35 10 15 42 22
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12     12     Priority road     0.995652     0.984241     5       13     13     Yield     0.997222     0.993084     3       14     14     Stop     0.996296     1.000000     4       15     15     No vehicles     1.000000     0.981308     2       16     16     Vehicles over 3.5 metric tons prohibited     0.993333     1.000000     7       17     17     No entry     0.991667     1.000000     12       18     18     General caution     0.935897     0.973333     31       19     19     Dangerous curve to the left     1.000000     0.983607     1       20     20     Dangerous curve to the right     0.977778     0.814815     20       21     21     Double curve     0.855556     0.905882     36       22     22     Bumpy road     0.950000     0.957983     30       23     23     Slippery road     0.980000     0.942308     19       24     24     Road narrows on	38
13     13     Yield     0.997222     0.993084     3       14     14     Stop     0.996296     1.000000     4       15     15     No vehicles     1.000000     0.981308     2       16     16     Vehicles over 3.5 metric tons prohibited     0.993333     1.000000     7       17     17     No entry     0.991667     1.000000     12       18     18     General caution     0.935897     0.973333     31       19     19     Dangerous curve to the left     1.000000     0.983607     1       20     20     Dangerous curve to the right     0.977778     0.814815     20       21     21     Double curve     0.855556     0.905882     36       22     22     Bumpy road     0.950000     0.957983     30       23     23     Slippery road     0.980000     0.942308     19       24     24     Road narrows on the right     0.954167     0.950207     27	16
14     14     Stop     0.996296     1.000000     4       15     15     No vehicles     1.000000     0.981308     2       16     16     Vehicles over 3.5 metric tons prohibited     0.993333     1.000000     7       17     17     No entry     0.991667     1.000000     12       18     18     General caution     0.935897     0.973333     31       19     19     Dangerous curve to the left     1.000000     0.983607     1       20     20     Dangerous curve to the right     0.977778     0.814815     20       21     21     Double curve     0.855556     0.905882     36       22     22     Bumpy road     0.950000     0.957983     30       23     23     Slippery road     0.980000     0.942308     19       24     24     Road narrows on the right     0.950000     0.843750     34       25     25     Road work     0.954167     0.950207     27	8
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18   18   General caution   0.935897   0.973333   31     19   19   Dangerous curve to the left   1.000000   0.983607   1     20   20   Dangerous curve to the right   0.977778   0.814815   20     21   21   Double curve   0.855556   0.905882   36     22   22   Bumpy road   0.950000   0.957983   30     23   23   Slippery road   0.980000   0.942308   19     24   24   Road narrows on the right   0.900000   0.843750   34     25   25   Road work   0.954167   0.950207   27	1
19   19   Dangerous curve to the left   1.000000   0.983607   1     20   20   Dangerous curve to the right   0.977778   0.814815   20     21   21   Double curve   0.855556   0.905882   36     22   22   Bumpy road   0.950000   0.957983   30     23   23   Slippery road   0.980000   0.942308   19     24   24   Road narrows on the right   0.900000   0.843750   34     25   25   Road work   0.954167   0.950207   27	23
20     20     Dangerous curve to the right     0.977778     0.814815     20       21     21     Double curve     0.855556     0.905882     36       22     22     Bumpy road     0.950000     0.957983     30       23     23     Slippery road     0.980000     0.942308     19       24     24     Road narrows on the right     0.900000     0.843750     34       25     25     Road work     0.954167     0.950207     27	17
21     21     Double curve     0.855556     0.905882     36       22     22     Bumpy road     0.950000     0.957983     30       23     23     Slippery road     0.980000     0.942308     19       24     24     Road narrows on the right     0.900000     0.843750     34       25     25     Road work     0.954167     0.950207     27	40
22 22 Bumpy road 0.950000 0.957983 30   23 23 Slippery road 0.980000 0.942308 19   24 24 Road narrows on the right 0.900000 0.843750 34   25 25 Road work 0.954167 0.950207 27	36
23   23   Slippery road   0.980000   0.942308   19     24   24   Road narrows on the right   0.900000   0.843750   34     25   25   Road work   0.954167   0.950207   27	28
24 24 Road narrows on the right 0.900000 0.843750 34   25 25 Road work 0.954167 0.950207 27	33
25 25 Road work 0.954167 0.950207 27	39
	31
	14
	41
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	21
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	6
34 34 Turn left ahead 0.991667 0.952000 11	30
35 35 Ahead only 0.992308 0.992308 10	9
36 36 Go straight or right 0.966667 0.983051 25	19
37 37 Go straight or left 0.983333 0.983333 17	18
38 38 Keep right 0.989855 0.997080 13	5
39 39 Keep left 0.977778 0.956522 21	29
40 40 Roundabout mandatory 0.966667 0.988636 26	13
41 41 End of no passing 0.816667 1.000000 39	32
42 42 End of no passing by vehicles over 3.5 metric 0.988889 0.946809 14	