Social Network Analysis Journal

M.Sc Part I Computer Science

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1 Practical 01

1.1 Aim: Write a program to compute the following for a given a network: (i) number of edges, (ii) number of nodes; (iii) degree of node; (iv) node with lowest degree; (v) the adjacency list; (vi) matrix of the graph.

```
[1]: library(igraph)

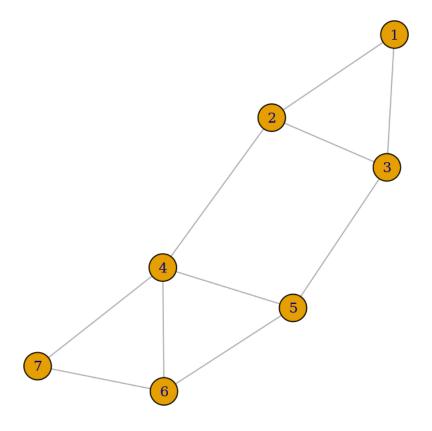
Attaching package: 'igraph'

The following objects are masked from 'package:stats':
    decompose, spectrum

The following object is masked from 'package:base':
    union

[2]: g <- graph.formula(1-2, 1-3, 2-3, 2-4, 3-5, 4-5, 4-6,4-7, 5-6, 6-7)

[3]: plot(g)</pre>
```



1.1.1 1)no of edges

[4]: ecount(g)

10

1.1.2 2)no of nodes

[5]: vcount(g)

7

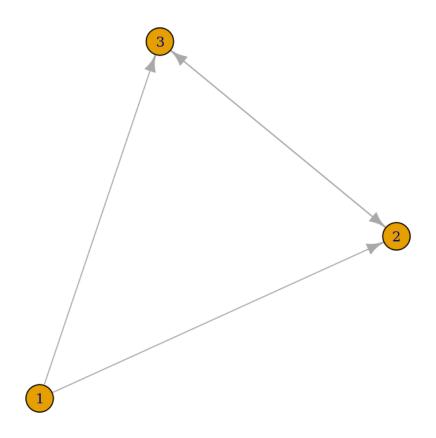
1.1.3 3)Degree Of nodes

[6]: degree(g)

1 2 2 3 3 3 4 4 5 3 6 3 7 2

[7]: dg <- graph.formula(1-+2, 1-+3, 2++3)

[8]: plot(dg)



[9]: degree(dg, mode="in")

1 0 **2** 2 **3** 2

```
[10]: degree(dg, mode="out")
     1
                          2 2
                                                1 3
                                                                       1
     1.1.4 4) a) Node with lowest degree
[11]: V(dg) name [degree(dg) == min(degree(dg))]
     '1'
     1.1.5 4) b) Node with lowest degree
[12]: V(dg) name [degree(dg) == max(degree(dg))]
     1. '2' 2. '3'
     1.1.6 5) To find neighbours / adjacency list:
[13]: neighbors(g,5)
     + 3/7 vertices, named, from 881bcb9:
     [1] 3 4 6
[14]: get.adjlist(dg)
     $`1`
     + 2/3 vertices, named, from d90acba:
     [1] 2 3
     $`2`
     + 3/3 vertices, named, from d90acba:
     [1] 1 3 3
     $`3`
     + 3/3 vertices, named, from d90acba:
     [1] 1 2 2
     1.1.7 6) Adjacency Matrix
[15]: get.adjacency(g)
     7 x 7 sparse Matrix of class "dgCMatrix"
       1 2 3 4 5 6 7
     1 . 1 1 . . . .
     21.11...
     3 1 1 . . 1 . .
     4 . 1 . . 1 1 1
     5 . . 1 1 . 1 .
```

```
6 . . . 1 1 . 1
7 . . . 1 . 1 .
```

2 Practical 02

2.1 Aim:

Perform following tasks:

- (i) View data collection forms and/or import onemode/two-mode datasets;
- (ii) Basic Networks matrices transformations

[1]: library(igraph)

Attaching package: 'igraph'

The following objects are masked from 'package:stats':

decompose, spectrum

The following object is masked from 'package:base':

union

- [2]: nodes <- read.csv("/kaggle/input/network-analysis-data-from-various-sources/

 →InputFileNodes.csv", header=T, , as.is=T)
- [3]: head(nodes)

		id	media	media.type	type.label	audience.size
		<chr></chr>	<chr $>$	<int $>$	<chr $>$	<int $>$
	1	s01	NY Times	1	Newspaper	20
A data.frame: 6×5	2	s02	Washington Post	1	Newspaper	25
A data.frame. 0 × 5	3	s03	Wall Street Journal	1	Newspaper	30
	4	s04	USA Today	1	Newspaper	32
	5	s05	LA Times	1	Newspaper	20
	6	s06	New York Post	1	Newspaper	50

- [4]: links <- read.csv("/kaggle/input/network-analysis-data-from-various-sources/

 →InputFileEdges.csv", header=T, as.is=T)
- [5]: head(links)

```
from
                                            weight
                                                     type
                                   to
                          <chr>
                                   <chr>
                                            <int>
                                                     <chr>
                                                     hyperlink
                          s01
                                   s02
                                            10
                          s01
                                   s02
                                                     hyperlink
                                            12
A data.frame: 6 \times 4
                                            22
                                                     hyperlink
                          s01
                                   s03
                          s01
                                   s04
                                            21
                                                     hyperlink
                      5
                                            22
                                                     mention
                          s04
                                   s11
                      6
                         s05
                                   s15
                                            21
                                                     mention
```

```
[6]: net <- graph.data.frame(d=links, vertices=nodes, directed=T)
```

```
[7]: net <- graph.data.frame(d=links, vertices=nodes, directed=T)
m=as.matrix(net)

g <- graph.adjacency(m, mode="directed")

# Get adjacency matrix
A <- as.matrix(get.adjacency(g))
A</pre>
```

s02

s03

s04

s05

s06

s07

s08

s09

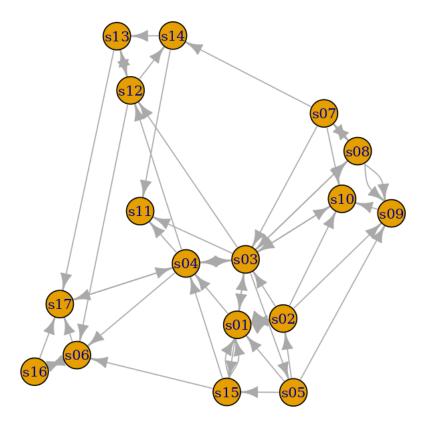
s10

s11

s12

	s01	0	2	1	1	O	0	0	0	0	0	O	0	0	0
	s02	1	0	1	0	0	0	0	0	1	1	0	0	0	0
	s03	1	0	0	1	1	0	0	1	0	1	1	1	0	0
	s04	0	0	1	0	0	1	0	0	0	0	1	1	0	0
	s05	1	1	0	0	0	0	0	0	1	0	0	0	0	0
	s06	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	s07	0	0	1	0	0	0	0	1	0	1	0	0	0	1
A matrix: 17×17 of type dbl	s08	0	0	1	0	0	0	1	0	2	0	0	0	0	0
A matrix. 17 × 17 of type doi	s09	0	0	0	0	0	0	0	0	0	1	0	0	0	0
	s10	0	0	1	0	0	0	0	0	0	0	0	0	0	0
	s11	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	s12	0	0	0	0	0	1	0	0	0	0	0	0	1	1
	s13	0	0	0	0	0	0	0	0	0	0	0	1	0	0
	s14	0	0	0	0	0	0	0	0	0	0	1	0	1	0
	s15	2	0	0	1	0	1	0	0	0	0	0	0	0	0
	s16	0	0	0	0	0	1	0	0	0	0	0	0	0	0
	s17	0	0	0	1	0	0	0	0	0	0	0	0	0	0

[8]: plot(net)



[]:

3 Practical 03

3.1 Aim:

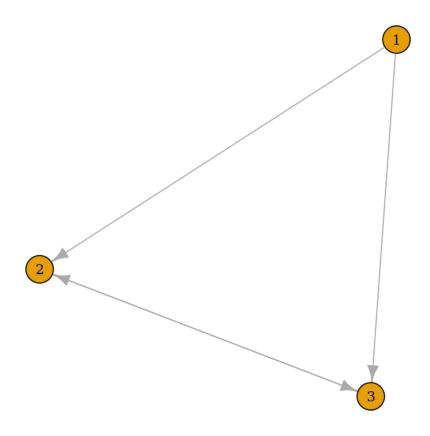
Compute the following node level measures: (i) Density; (ii) Degree; (iii) Reciprocity; (iv) Tra

[1]: library(igraph)

Attaching package: 'igraph'

```
The following objects are masked from 'package:stats':
         decompose, spectrum
     The following object is masked from 'package:base':
         union
     3.1.1 1) Density
[2]: g <- graph.formula(1-2, 1-3, 2-3, 2-4, 3-5, 4-5, 4-6,4-7, 5-6, 6-7)
[3]: nodes <- read.csv("/kaggle/input/network-analysis-data-from-various-sources/
      links <- read.csv("/kaggle/input/network-analysis-data-from-various-sources/</pre>
      net <- graph.data.frame(d=links, vertices=nodes, directed=T)</pre>
[4]: vcount(g)
     7
[5]: ecount(g)
     10
[6]: ecount(g)/(vcount(g)*(vcount(g)-1)/2)
     0.476190476190476
     3.1.2 2) Degree
[7]: degree(net)
     \mathbf{s01}\ 10\ \mathbf{s02}\ 7\ \mathbf{s03}\ 13\ \mathbf{s04}\ 9\ \mathbf{s05}\ 5\ \mathbf{s06}\ 6\ \mathbf{s07}\ 5\ \mathbf{s08}\ 6\ \mathbf{s09}\ 5\ \mathbf{s10}\ 5\ \mathbf{s11}\ 3\ \mathbf{s12}\ 6\ \mathbf{s13}\ 4\ \mathbf{s14}\ 4\ \mathbf{s15}\ 6
     s16
                                     3 s17
                                                                      5
     3.1.3 3) Reciprocity
[8]: dg <- graph.formula(1-+2, 1-+3, 2++3)
     plot(dg)
     reciprocity(dg)
```

0.5



3.1.4 Formula

[9]: dyad.census(dg)

\$mut 1

sym 2

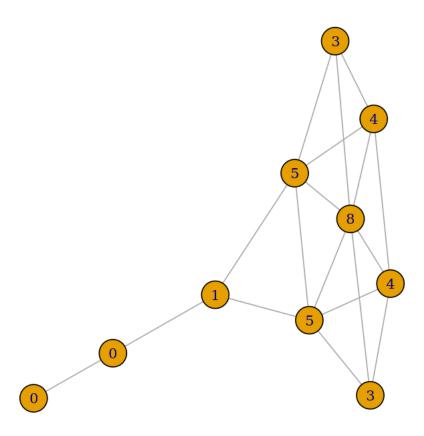
null 0

[10]: 2*dyad.census(dg)\$mut/ecount(dg)

0.5

3.1.5 4) Transitivity

```
[11]: kite <- graph.famous("Krackhardt_Kite")
atri <- adjacent.triangles(kite)
plot(kite, vertex.label=atri)</pre>
```



```
[12]: transitivity(kite, type="local")
```

1. 0.66666666666666 2. 0.66666666666666 3. 1 4. 0.5333333333333 5. 1 6. 0.5 7. 0.5 8. 0.33333333333333 9. 0 10. NaN

Formula

[13]: adjacent.triangles(kite) / (degree(kite) * (degree(kite)-1)/2)

1. 0.66666666666667 2. 0.66666666666667 3. 1 4. 0.533333333333 5. 1 6. 0.5 7. 0.5 8. 0.3333333333333 9. 0 10. NaN

3.1.6 5) Centralization

Degree of centrality

```
[14]: centralization.degree(net, mode="in", normalized=T)
```

\$res 1. 5 2. 3 3. 6 4. 4 5. 1 6. 4 7. 1 8. 2 9. 4 10. 4 11. 3 12. 3 13. 2 14. 2 15. 2 16. 1 17. 4

\$centralization 0.1875

\$theoretical max 272

Closeness Centralization

```
[15]: closeness(net, mode="all", weights=NA)
    centralization.closeness(net, mode="all", normalized=T)
```

\$centralization 0.375359630727278

\$theoretical max 7.74193548387097

Betweeness Centrality

```
[16]: betweenness(net, directed=T, weights=NA)
  edge.betweenness(net, directed=T, weights=NA)
  centralization.betweenness(net, directed=T, normalized=T)
```

```
$res 1. 26.8571428571429 2. 6.23809523809524 3. 126.511904761905 4. 92.6428571428571 5. 13
         16. 0 17. 58.5
     $centralization 0.443932911706349
     tan 3840
     Eigenvector centrality
[17]: centralization.evcent(net, directed=T, normalized=T)
     $vector 1.
                0.777185829200523
                                 2.
                                     0.569523129226997
                                                       3.
                                                           1
                                                              4.
                                                                  0.821414404772152
         5. \ \ 0.306115118060718 \ \ 6. \ \ 0.605185074708371 \ \ \ 7. \ \ 0.103395270890436 \ \ 8. \ \ 0.337765973616263
         9. \ \ 0.47483664722783 \ \ 10. \ \ 0.657460289883597 \ \ 11. \ \ 0.627101587234399 \ \ 12. \ \ 0.638699752169925
         17. 0.574550689029643
     $value 3.26674489758997
     $options $bmat 'I'
         $n 17
         $which 'LR'
         $nev 1
         $tol 0
         $ncv 0
         \$ldv 0
         $ishift 1
         $maxiter 3000
         $nb 1
         $mode 1
         $start 1
         $sigma 0
         $sigmai 0
         $info 0
         $iter 7
         $nconv 1
         $numop 30
         $numopb 0
         $numreo 20
```

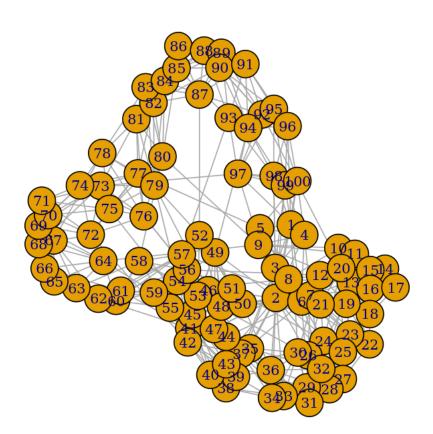
\$centralization 0.53110461741892

to 16

3.2 6) Clustering

```
[18]: # let's generate two networks and merge them into one graph.
g2 <- barabasi.game(50, p=2, directed=F)
g1 <- watts.strogatz.game(1, size=100, nei=5, p=0.05)
g <- graph.union(g1,g2)

#Let's remove multi-edges and loops
g <- simplify(g)
plot(g)</pre>
```



4 Practical 04

4.1 Aim:

For a given network find the following: (i) Length of the shortest path from a given node to and

```
[1]: library(igraph)

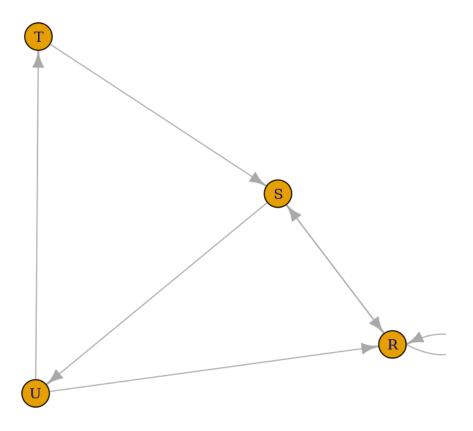
Attaching package: 'igraph'

The following objects are masked from 'package:stats':
    decompose, spectrum

The following object is masked from 'package:base':
    union
```

4.1.1 (i) Length of the shortest path from a given node to another node;

```
[3]: nms <- matt[,1 ]
  matt <- matt[, -1]
  colnames(matt) <- rownames(matt) <- nms
  matt[is.na(matt)] <- 0
  g <- graph.adjacency(matt, weighted=TRUE)
  plot(g)</pre>
```



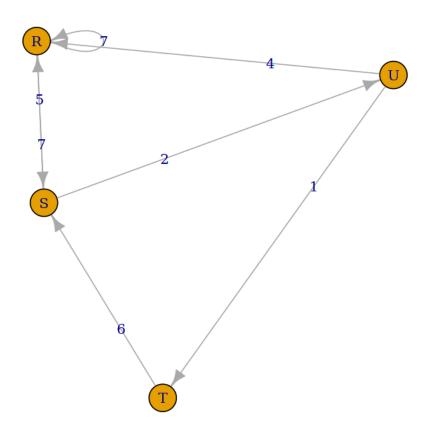
```
[4]: s.paths <- shortest.paths(g, algorithm = "dijkstra")
    print(s.paths)

    R S T U
    R 0 5 5 4
    S 5 0 3 2
    T 5 3 0 1
    U 4 2 1 0

[5]: shortest.paths(g, v="R", to="S")</pre>
```

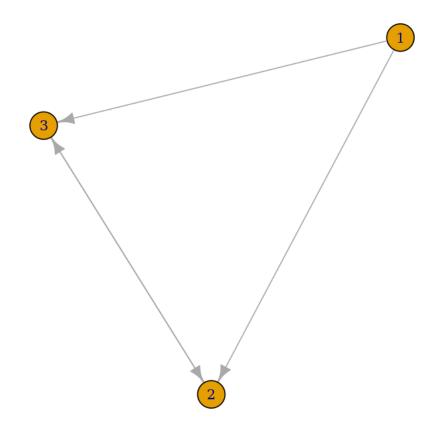
A matrix: 1 × 1 of type dbl $\frac{\mid S \mid}{\mid R \mid \mid 5}$

[6]: plot(g, edge.label=E(g)\$weight)



4.1.2 (ii) the density of the graph

0.444444444444444



[8]: graph.density(simplify(dg), loops=FALSE)

0.666666666666667

5 Practical 05

5.1 Aim:

Write a program to distinguish between a network as a matrix, a network as an edge list, and a nature of the state of the

[1]: library(igraph)

```
Attaching package: 'igraph'

The following objects are masked from 'package:stats':

decompose, spectrum

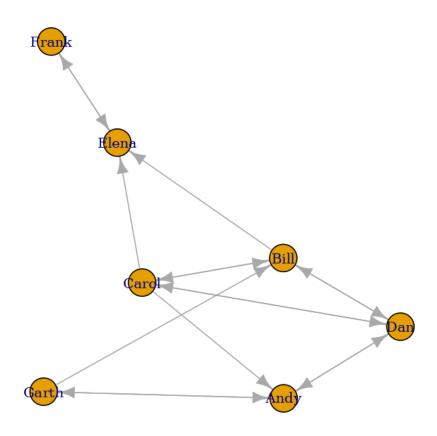
The following object is masked from 'package:base':

union
```

5.1.1 (i) Length of the shortest path from a given node to another node;

```
[2]: ng<-graph.

formula(Andy++Garth,Garth-+Bill,Bill-+Elena,Elena++Frank,Carol-+Andy,Carol-+Elena,Carol++Dan,Carol++Dan,Carol-+Elena,Carol++Dan,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Dan,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol-+Elena,Carol
```



2) a network as a matrix,

[4]: get.adjacency(ng)

7 x 7 sparse Matrix of class "dgCMatrix"

Andy Garth Bill Elena Frank Carol Dan

	J						
Andy	•	1	•	•	•		1
Garth	1		1				
Bill	•		•	1		1	1
Elena					1		
Frank				1			
Carol	1		1	1			1
Dan	1		1			1	

```
[5]: E(ng)
    + 16/16 edges from 9022c9b (vertex names):
     [1] Andy ->Garth Andy ->Dan
                                   Garth->Andy Garth->Bill Bill ->Elena
     [6] Bill ->Carol Bill ->Dan
                                   Elena->Frank Frank->Elena Carol->Andy
    [11] Carol->Bill Carol->Elena Carol->Dan Dan ->Andy Dan ->Bill
    [16] Dan ->Carol
[6]: get.adjedgelist(ng,mode="in")
    $Andy
    + 3/16 edges from 9022c9b (vertex names):
    [1] Garth->Andy Carol->Andy Dan ->Andy
    $Garth
    + 1/16 edge from 9022c9b (vertex names):
    [1] Andy->Garth
    $Bill
    + 3/16 edges from 9022c9b (vertex names):
    [1] Garth->Bill Carol->Bill Dan ->Bill
    $Elena
    + 3/16 edges from 9022c9b (vertex names):
    [1] Bill ->Elena Frank->Elena Carol->Elena
    $Frank
    + 1/16 edge from 9022c9b (vertex names):
    [1] Elena->Frank
    $Carol
    + 2/16 edges from 9022c9b (vertex names):
    [1] Bill->Carol Dan ->Carol
    $Dan
    + 3/16 edges from 9022c9b (vertex names):
    [1] Andy ->Dan Bill ->Dan Carol->Dan
```

6 Practical 05

iii) a network as an edge list.

6.1 Aim:

Write a program to distinguish between a network as a matrix, a network as an edge list, and a n 1) a network as a sociogram (or 'network graph')

```
[1]: install.packages("sna")
    install.packages("network")

Installing package into '/usr/local/lib/R/site-library'
    (as 'lib' is unspecified)

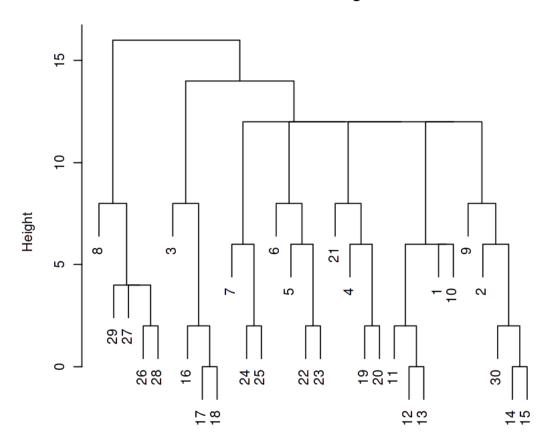
Installing package into '/usr/local/lib/R/site-library'
    (as 'lib' is unspecified)

[4]: library(sna)
    library(igraph)

6.1.1 (i) i) structural equivalence

[6]: links2 <- read.csv("/kaggle/input/sna-edges/edges1.csv", header=T, row.names=1)
    eq<-equiv.clust(links2)
    plot(eq)</pre>
```

Cluster Dendrogram

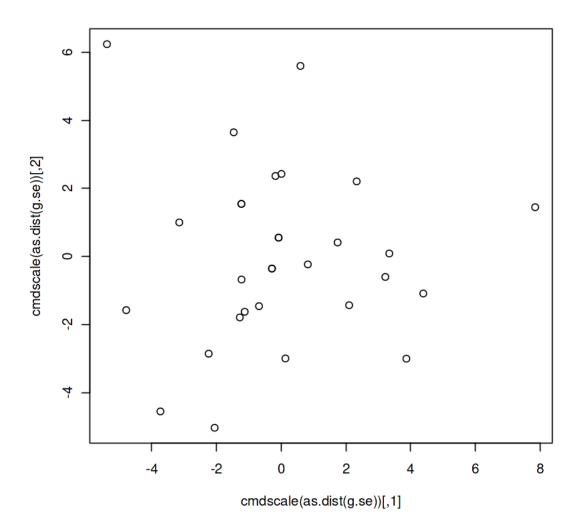


as.dist(equiv.dist) hclust (*, "complete")

6.2 ii) automorphic equivalence,

```
[7]: g.se<-sedist(links2)

#Plot a metric MDS of vertex positions in two dimensions
plot(cmdscale(as.dist(g.se)))
```

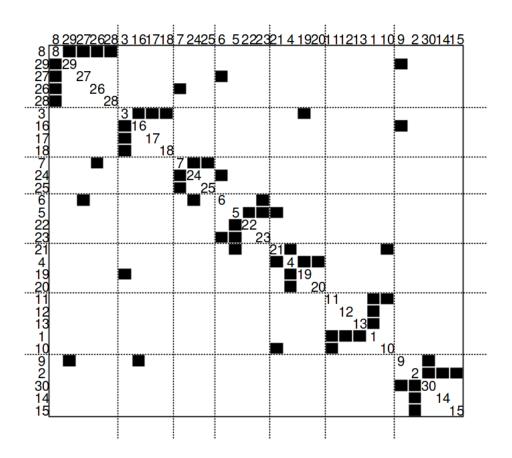


6.3 3) regular equivalence from a network.

Blockmodeling

```
[8]: b<-blockmodel(links2,eq,h=10)
plot(b)
```

Relation - 1



7 Practical 07

7.1 Aim:

Create sociograms for the persons-by-persons network and the committee-bycommittee network for a

[1]: library(igraph)

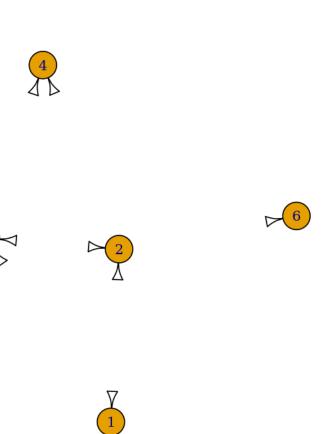
Attaching package: 'igraph'

The following objects are masked from 'package:stats':

```
The following object is masked from 'package:base':
        union
[2]: # Create sample data for data_Network_1
     data_Network_1 <- data.frame(</pre>
       Source = c(1, 1, 2, 2, 2, 2, 2, 3, 3, 3),
       Target = c(2, 3, 1, 3, 4, 5, 6, 2, 4, 5)
     # Create graph object
     g <- graph_from_data_frame(data_Network_1, directed = TRUE)</pre>
[3]: # Set binary code for edges to be displayed
     bytes <- "001111111111000000000"
     # Extract edges based on binary code
     edges <- which(strsplit(bytes, "")[[1]] == "1")</pre>
     # Get layout for visualization
     layout <- layout_with_kk(g)</pre>
[4]: library(dplyr)
     # Plot sociogram
     plot(g, layout = layout, edge.color = if_else(E(g)$id %in% edges, "red", "gray"))
    Attaching package: 'dplyr'
    The following objects are masked from 'package:igraph':
        as_data_frame, groups, union
    The following objects are masked from 'package:stats':
        filter, lag
    The following objects are masked from 'package:base':
```

decompose, spectrum

intersect, setdiff, setequal, union



[]:

8 Practical 08

8.1 Aim:

Perform SVD analysis of a network.

```
Attaching package: 'igraph'
    The following objects are masked from 'package:stats':
        decompose, spectrum
    The following object is masked from 'package:base':
        union
0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1), 9, 4)
[3]: print(a)
          [,1] [,2] [,3] [,4]
     [1,]
             1
                   1
                             0
     [2,]
             1
                   1
                        0
                             0
     [3,]
                   1
                             0
             1
                        0
     [4,]
                   0
                             0
             1
                        1
     [5,]
             1
                   0
                        1
                             0
     [6,]
             1
                   0
                        1
                             0
     [7,]
                   0
             1
                             1
     [8,]
             1
                   0
                        0
                             1
     [9,]
             1
                   0
                        0
                             1
[4]: svd(a)
    \$d 1. 3.46410161513775 2. 1.73205080756888 3. 1.73205080756888 4. 1.35973995551052e-16
                                                         -3.202997e-16
                                  -0.3333333
                                             0.4714045
                                                                       3.693981e-01
                                  -0.3333333
                                             0.4714045
                                                        -3.415341e-16
                                                                       4.459029e-01
                                  -0.3333333
                                             0.4714045
                                                         8.520300e-18
                                                                       -8.153010e-01
                                  -0.3333333
                                             -0.2357023
                                                        -4.082483e-01
                                                                       7.849070e-17
    $u A matrix: 9 \times 4 of type dbl -0.3333333
                                             -0.2357023
                                                        -4.082483e-01
                                                                       1.340019e-16
                                  -0.3333333
                                             -0.2357023
                                                        -4.082483e-01
                                                                      1.340019e-16
                                  -0.3333333
                                             -0.2357023
                                                         4.082483e-01
                                                                       1.182076e-16
                                  -0.3333333
                                             -0.2357023
                                                         4.082483e-01
                                                                       1.182076e-16
                                  -0.3333333
                                             -0.2357023
                                                         4.082483e-01
                                                                       1.182076e-16
```

[1]: library(igraph)

```
0.0000000
                                                                    -4.378026e-17
                                         -0.8660254
                                                                                     0.5
                                         -0.2886751
                                                      0.8164966
                                                                    -2.509507\mathrm{e}\text{-}16
                                                                                    -0.5
     v A matrix: 4 \times 4 of type dbl
                                         -0.2886751
                                                      -0.4082483
                                                                    -7.071068e-01
                                                                                    -0.5
                                         -0.2886751
                                                                    7.071068e-01
                                                      -0.4082483
                                                                                     -0.5
[]:
```