

Linked Lists

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Array

- ■Store an ordered list
- Using sequential mapping
 - Element(node) a_i is stored in the location L_i of the array
 - Next node is at the location L_i+1

■Pros:

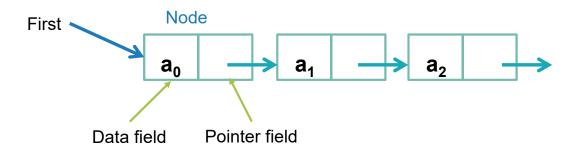
- Suitable for random access
- Efficient to insert/delete from the end
- Adequate for special data structures, Stack and Queue

■Con:

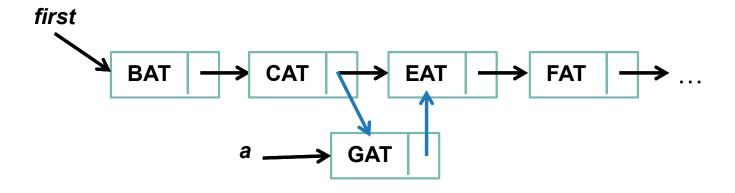
Difficult to insert/delete nodes at arbitrary location

Linked Lists

- ■Nodes are no longer continue in the memory
- ■Each node stores the address or location of the next one
- ■Singly Linked List (SLL)
 - Each node has exactly one pointer field

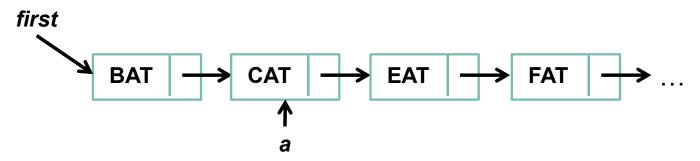


SLL Operation: Insert



- ■Steps to insert a "GAT" in between "CAT" and "EAT" nodes
 - Create a new node "a" and set data field to "GAT"
 - Set the link field of "a" to "EAT" node
 - Set the link field of "CAT" node to "a"

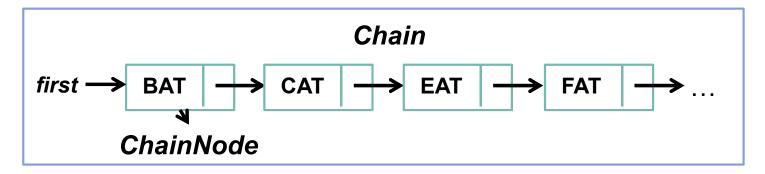
SLL Operation: Delete



- ■Steps to delete a "EAT" node from the list
 - Locate the node "a" precedes the "EAT" node
 - Set the link field of "a" to node next to "EAT" node
 - Delete the "EAT" node

Conceptual Design

- ■Defining a "ChainNode" class
 - Data field
 - Link field
- ■Designing a "Chain" class
 - Support various operation on ChainNodes



ChainNode & Chain Classes

■Composite class

```
class ChainNode
{
  friend class Chain;
  public:
    // Constructor
    ChainNode(int
    value=0, ChainNode*
    next=NULL) {
      data = value;
      link = next;

    private:
      int data;
      ChainNode *link;
};
```

```
class Chain
{
  public:
     // Create a chain with two nodes
     void Create2();

     // Insert a node with data=50
     void Insert50(ChainNode *x);

     // Delete a node
     void Delete(ChainNode *x, ChainNode *y);

private:
     ChainNode *first;
};
```

ChainNode & Chain Classes

■Nested class

```
class Chain
{
  public:
    // Create a chain with two nodes
    void Create2();

    // Insert a node with data=50
    void Insert50(ChainNode *x);

    // Delete a node
    void Delete(ChainNode *x, ChainNode *y);

private:
    class ChainNode{
       public:
          int data;
          ChainNode *link;
    }
    ChainNode *first;
};
```

Review Pointer Manipulation

■Declaration

NodeA *a1=NULL, *a2=NULL;

■ Allocate memory

- a1 = new NodeA;
- a2 = new NodeA[10];

■Delete memory

- delete a1; a1=NULL;
- delete [] a2; a2=NULL;

■Dereference

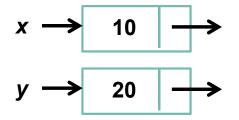
■ NodeA &a1Ref = (*a1);

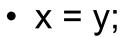
Access members

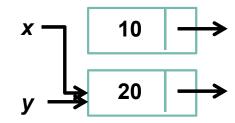
- a1->memData;
- a1->memFunc();
- (*a1).memData;
- (*a1).memFunc();

Pointer Assignment

■ChainNode *x, *y;



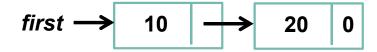




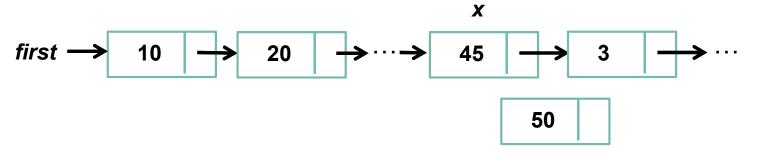
• *
$$x = *y$$
;
 $x \longrightarrow 20$
 $y \longrightarrow 20$

```
void Chain::Create2()
{
    // Create and set the fields of 2<sup>nd</sup> node
    ChainNode* second = new ChainNode(20,0);

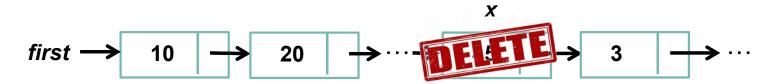
    // Create and set the fields of 1<sup>st</sup> node
    first = new ChainNode(10, second);
}
```



```
void Chain::Insert50(ChainNode *x)
{
   if(first) // Insert after x
       x→link = new ChainNode(50, x->link);
   else // Insert into empty list
      first = new ChainNode(50);
}
```



```
void Chain::Delete(ChainNode *x, ChainNode *y)
{    // x is the node to be deleted and y is the node
    // preceding x
    if(x==first) first = first->link;
    else y->link = x->link;
    delete x;
    x=NULL;
}
```



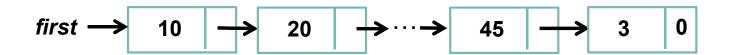
Template Chain Class

```
Template < class T > class Chain; // Forward declaration
template < class T >
class ChainNode {
friend class Chain <T>;
private:
       T data;
       ChainNode<T>* link;
};
template <class T>
class Chain {
public:
       // Constructor
       Chain(void) {first = last = NULL;}
       // Chain operations...
private:
      ChainNode<T> *first;
      ChainNode<T> *last;
};
```

```
template < class T >
void Chain<T>::InsertBack(const T& e)
{
   if(first) {// Non-empty chain
      last->link = new ChainNode<T>(e);
      last = last->link;
   }
   else // Insert into an empty chain
      first = last = new ChainNode<T>(e);
}
```

```
template < class T >
void Chain<T>::Concatenate(Chain<T>& b)
{    // b is concatenated to the end of *this
    if ( first ) { last->link = b.first; last = b.last; }
    else { first = b.first; last = b.last; }
    b. first = b.last = 0;
}
```

■ Reverse a chain, such that (a^1, a^2, \dots, a^n) turns into $(a^n, a^{n-1}, \dots, a^1)$



first

3

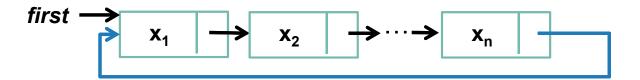
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10

Circular Lists

- A singly-linked circular list
- ■The link field of the last node points to the first node



- ■Check for the last node
 - if(current->link == first)
- ■You could visit a node from any position

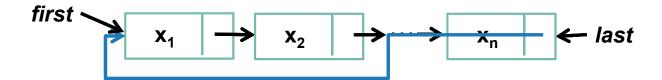
Circular Lists: Insert

- ■Suppose we want to insert a new node at the front of list
- ■Set link field of new node to *first* and set *first* to new node
- ■Go to the last node and set the link field to new node



Circular Lists

- ■Computation complexity for finding the last one?
 - O(N)
- ■Computation complexity for finding the first one?
 - We could away access the first node via [last->link]
 - O(1)
- ■It is more convenient to store the last node of a circular list



Circular Lists: Insert at Front

```
Template<class T>
void CircularList<T>::InsertFront(const T& e)
{
    ChainNode<T>* newNode = new ChainNode<T>(e);

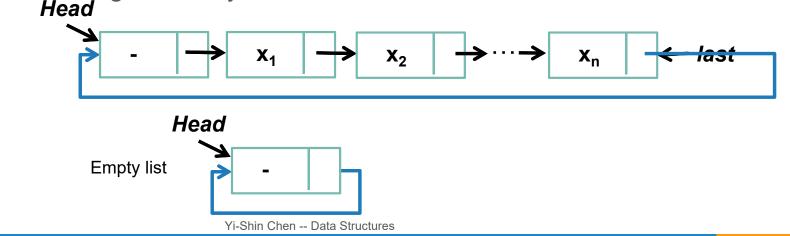
    if(last) { // nonempty list
        newNode->link = last->link;
        last->link = newNode;
    }
    else{ // empty list
        last = newNode;
        newNode->link = newNode;
    }
}
```

Circular Lists

■How to represent an "empty" list?



■Introducing a dummy node "Header" *Head*



Sparse Matrix

$$a[6][6] = \begin{pmatrix} 15 & 0 & 0 & 22 & 0 & -15 \\ 0 & 11 & 3 & 0 & 0 & 0 \\ 0 & 0 & 0 & -6 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 91 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 28 & 0 & 0 & 0 \end{pmatrix}$$

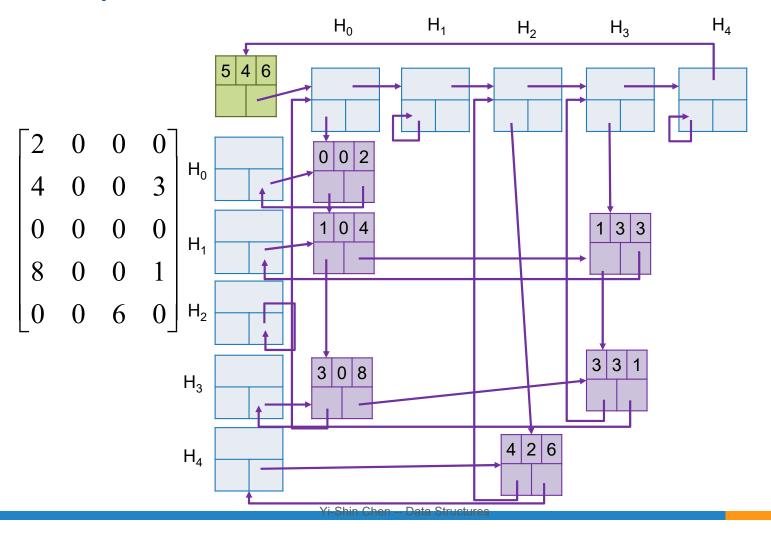
- A matrix has many zero elements
- Devise a sequential array
 - store **non-zero** elements
 - **row-major** order
- Access specific column is difficult
- Using circular lists representation

Α	row	col	value
smArray[0]	0	0	15
smArray[1]	0	3	22
smArray[2]	0	5	-15
smArray[3]	1	1	11
smArray[4]	1	2	3
smArray[5]	2	3	-6
smArray[6]	4	0	91
smArray[7]	5	2	28

Linked Structure

- Header node: for each row or column
 - **Down**: link to the 1st non-zero term in the column
 - **Right**: link to the 1st non-zero term in the row
 - Next: link to the next head node
 - The header node for row *i* is also the header node for column *i*
- Element node, each non-zero term that stores
 - Data of row, col, and value
 - A down field to link to the next non-zero term in the same column
 - A right field to link to the next non-zero term in the same row
- The header of header nodes (a circular list)
 - Store dimension of the matrix

Sparse Matrix in Linked Structure



Create a Sparse Matrix

- ■Given a nxm sparse matrix with r non-zero terms
 - the total number of required nodes are max{n, m} + r + 1
- ■Input format
 - The 1st line gives the dimension of matric and # of non-zero terms
 - Each subsequent input line is a triple of the form (i, j, a_{ii})
 - Triples are ordered by rows and within rows by columns

_	$\mathbf{\alpha}$	$\mathbf{\alpha}$	A	
2	0	0	0	
4	0	0	3	
Λ	Λ	Λ		
0	0	0	0	
8	0	0	1	
•	0			
_0	O	6	O	

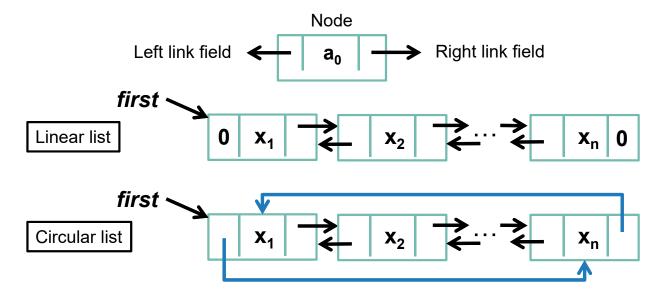
Input

Create a Sparse Matrix

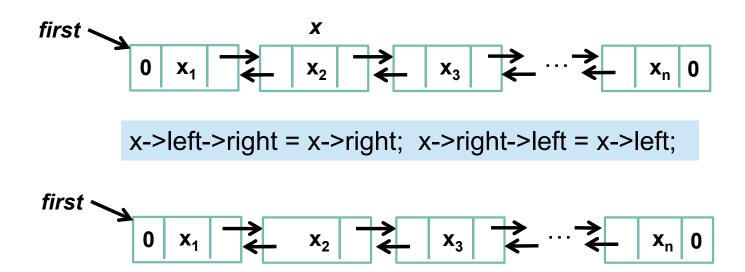
- ■Performance analysis
 - Set up header nodes, O(max{n,m})
 - Set up non-zero nodes, O(r)
 - Close column lists, O(max{n,m})
 - Link header nodes, O(max{n,m})
- ■Total complexity: O(max{n,m}+r) = O(n+m+r)

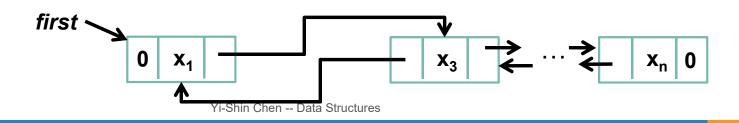
Double Linked Lists

- ■Each node has two link fields
- ■Could move in two directions to visit nodes

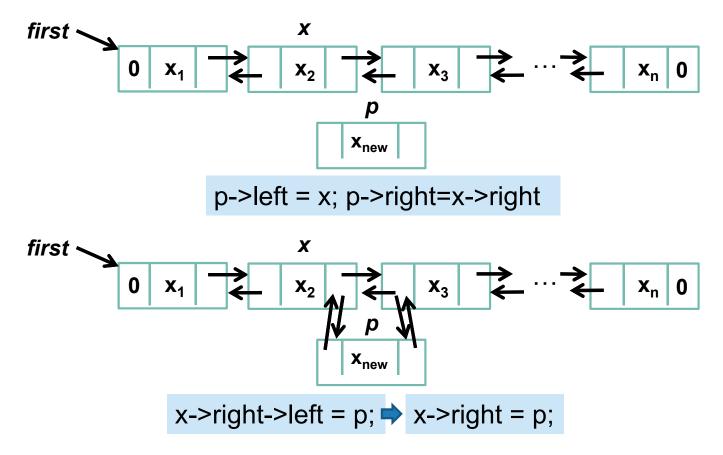


Double Linked Lists: Delete





Double Linked Lists: Insert



Self-Study Topics

- ■Polynomial using linked lists
- Linked stacks and queues



Visit Elements in a Container

- ■Suppose we have a chain C of datatype Chain<int>.
 - Output all integers in C
 - Obtain the maximum, minimum or mean of all integers in C
 - Obtain the sum, product, or sum of squares of all integers in C
- ■All operations require to visit every element in the chain C

How to Visit a Container?

```
For each item in C
{
    currentItem = current item in C;
    //do something with currentItem;
}
```

■In an array representation

```
for (int i = 0; i < n; i++)
{
   int currentItem = a[i];
   // do something with currentItem;
}</pre>
```

How to Visit a Container?

```
For each item in C
{
    currentItem = current item in C;
    // do something with currentItem;
}
```

■In a linked list representation

```
for (ChainNode<int> *ptr=first; ptr!=0; ptr=ptr->link)
{
   int currentItem = ptr->data;
   // do something with currentItem;
}
```

Visiting a Container using Iterator

- A powerful mechanism to visit a container with arbitrary data type
- Guarantee runtime range safety
- Applicable to all STL algorithms
- ■Suitable for team development
- Might scarify some amount of performance

```
// Possible implementation of STL copy algorithm
template < class Iterator >
void copy(Iterator start, Iterator end, Iterator to)
{ // copy from src[start, end) to dst[to, to+end-start)
   while (start != end)
   { *to = *start; start++; to++; }
}
```

What is an Iterator?

```
void main()
{
  int x [3] = {0,1,2};
  for (int* y = x; y != x+3; y++)
     cout << *y << endl;
}</pre>
```

- ■An *iterator* is a pointer to an element in a container
- ■Using dereferencing operator (*) to access an element
- ■Support pre- or post- increment operator (++)

```
void main()
{
   for (Iterator y = start; y != end; y++)
      cout << *y << endl;
}</pre>
```

C++ Iterators

- **■Input** iterator
 - Read access, pre- and post- "++" operators.
- **■Output** iterator
 - Write access, pre- and post- "++" operators.
- **■Forward** iterator
 - pre- and post- "++" operators.
- **■Bidirectional** iterator
 - pre- and post- "++" and "--" operators.
- ■Random access iterator
 - Permit pointer jumps by arbitrary amounts.
- ■All iterators supports "==", "!=" and "*" operators

Forward Iterator for Chain

```
template <class T>
class Chain {
public:
       // Constructor
      Chain(void) {first = last = NULL;}
       // Chain operations...
       class ChainIterator{...};
       // Get the first element
       ChainIterator begin() {return ChainIterator(first);}
       // Get the end of the list
       ChainIterator end() {return ChainIterator(0);}
private:
      ChainNode<T> *first;
      ChainNode<T> *last;
};
```

Forward Iterator for Chain

■General usage

```
void main()
{
    Chain<int> myChain;
    // do operations on myChain here...

// print out every element in myChain
    Chain<int>::ChainIterator my_it;
    for (my_it = myChain.begin(); myChain!=myChain.end(); ++m_it)
        cout << *m_it << endl;

// Use STL algorithm to calculate the sum of myChain
    int sum = std::accumulate(myChain.begin(), myChain.end(),0);
}</pre>
```

```
Class ChainIterator{ // A nested class within Chain
public:
 // Constructor
  ChainIterator(ChainNode<T>* startNode = 0)
               {current = startNode;}
  // Dereferencing operator
  T& operator*() const {return current->data;}
  T* operator->() const {return &current->data;}
  // Increment operator
  ChainIterator& operator++() // pre-"++"
  { current = current->link ; return *this; }
  ChainIterator operator++(int)// post- "++"
    ChainIterator old = *this;
    current = current->link;
    return old;
  // Equality operators
 bool operator!=(const ChainIterator right) const
  { return current != right.current; }
 bool operator==(const ChainIterator right) const
  { return current == right.current;}
private:
   ChainNode<T>* current;
};
                     Vi Shin Chen Data Structures
```