

# Package ‘PlayerRatings’

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**Title** Dynamic Updating Methods for Player Ratings Estimation

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**Description** Implements schemes for estimating player or team skill based on dynamic updating. Implemented methods include Elo, Glicko and Stephenson. Contains pdf documentation of a reproducible analysis using approximately two million chess matches.

**LazyData** yes

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aflodds*Australian Football Game Results and Odds*

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## Description

The aflodds data frame has 675 rows and 9 variables. It shows the results and betting odds for 675 Australian football games played by 18 teams from 26th March 2009 until 24th June 2012. The data is subject to alteration and may be appended to at a later date.

## Usage

aflodds

## Format

This data frame contains the following columns:

**Date** A date object showing the date of the game.

**Week** The number of weeks since 25th March 2009.

**HomeTeam** The home team name.

**AwayTeam** The away team name.

**HomeScore** The home team score.

**AwayScore** The home team score.

**Score** A numeric vector giving the value one, zero or one half for a home win, an away win or a draw respectively.

**HomeOdds** The best decimal odds offered for the home team. This is missing for some earlier games.

**AwayOdds** The best decimal odds offered for the away team. This is missing for some earlier games.

## Source

Wikipedia and [www.oddsportal.com](http://www.oddsportal.com).

elo

*The Elo Rating System***Description**

Implements the Elo rating system for estimating the relative skill level of players in two-player games such as chess.

**Usage**

```
elo(x, status = NULL, init = 2200, gamma = 0, kfac = 27,
    history = FALSE, sort = TRUE, ...)
```

**Arguments**

x	A dataframe containing four variables: (1) a numeric vector denoting the time period in which the game took place (2) a numeric or character identifier for player one (3) a numeric or character identifier for player two and (4) the result of the game expressed as a number, typically equal to one for a player one win, zero for a player two win and one half for a draw.
status	A data frame with the current status of the system. If not NULL, this needs to be a data frame in the form of the ratings component of the returned list, containing variables named Player, Rating, and optionally Games, Win, Draw, Loss and Lag, which are set to zero if not given.
init	The rating at which to initialize a new player not appearing in status. Must be a single number. If different initializations for different players are required, this can be done using status.
gamma	A player one advantage parameter; either a single value or a numeric vector equal to the number of rows in x. Positive values favour player one, while negative values favour player two. This could represent the advantage of playing at home, or the advantage of playing white for chess. Note that this is not passed to <a href="#">predict.rating</a> , which has its own gamma parameter.
kfac	The K factor parameter. Can be a single number or a vectorized function of two arguments, the first being the ratings and the second being the number of games played. See <a href="#">kfide</a> , <a href="#">kgames</a> and <a href="#">krating</a> for examples.
history	If TRUE returns the entire history for each period in the component history of the returned list.
sort	If TRUE sort the results by rating (highest to lowest). If FALSE sort the results by player.
...	Passed to the function kfac.

## Details

The Elo rating system is a simple method for evaluating the skill of players. It has been used since around 1960 and is still employed in various settings. Although the basic form uses only the ratings, additional complexity is commonly introduced by adding a player one advantage parameter and by using different K factors. A player one advantage parameter has been added to the original definition in the reference. This is also used for prediction purposes.

This implementation has a simple initialization, and allows the K factor to depend on both the ratings and the number of games played. Default values are roughly optimized the chess data analyzed in the file `doc/ChessRatings.pdf`, using the binomial deviance criterion and considering only constant K factors. See the function `fide` for a different implementation.

## Value

A list object of class "rating" with the following components

ratings	A data frame of the results at the end of the final time period. The variables are self explanatory except for Lag, which represents the number of time periods since the player last played a game. This is equal to zero for players who played in the latest time period, and is also zero for players who have not yet played any games.
history	A three dimensional array, or NULL if history is FALSE. The row dimension is the players, the column dimension is the time periods. The third dimension gives different parameters.
gamma	The player one advantage parameter.
kfac	The K factor or K factor function.
type	The character string "Elo".

## References

Elo, Arpad (1978) The Rating of Chessplayers, Past and Present. Arco. ISBN 0-668-04721-6.

## See Also

`fide`, `kfide`

## Examples

```
af1 <- aflodds[,c(2,3,4,7)]
robj <- elo(af1)
robj

robj <- elo(af1[af1$Week==1,])
for(i in 2:max(af1$Week)) robj <- elo(af1[af1$Week==i,], robj$ratings)
robj
```

fide

*The Elo Rating System Employed By The FIDE***Description**

Implements the Elo rating system for estimating the relative skill level of players in two-player games such as chess, implementing a version similar to that employed by the FIDE.

**Usage**

```
fide(x, status = NULL, init = 2200, gamma = 0, kfac = kfide,
     history = FALSE, sort = TRUE, ...)
```

**Arguments**

x	A dataframe containing four variables: (1) a numeric vector denoting the time period in which the game took place (2) a numeric or character identifier for player one (3) a numeric or character identifier for player two and (4) the result of the game expressed as a number, typically equal to one for a player one win, zero for a player two win and one half for a draw.
status	A data frame with the current status of the system. If not NULL, this needs to be a data frame in the form of the ratings component of the returned list, containing variables named Player, Rating, and optionally Games, Win, Draw, Loss Lag and Elite, which are set to zero if not given, and Opponent, which is set to the player rating if not given.
init	The rating at which to initialize a new player not appearing in status. Must be a single number. If different initializations for different players are required, this can be done using status.
gamma	A player one advantage parameter; either a single value or a numeric vector equal to the number of rows in x. Positive values favour player one, while negative values favour player two. This could represent the advantage of playing at home, or the advantage of playing white for chess. Note that this is not passed to <a href="#">predict.rating</a> , which has its own gamma parameter.
kfac	The K factor parameter. Can be a single number or a vectorized function of three arguments, the first being the ratings, the second being the number of games played, and the third being a binary indicator for whether or not a player has ever achieved a rating above 2400. See <a href="#">kfide</a> , <a href="#">kgames</a> and <a href="#">krating</a> for examples. The function <a href="#">kfide</a> is used by default.
history	If TRUE returns the entire history for each period in the component history of the returned list.
sort	If TRUE sort the results by rating (highest to lowest). If FALSE sort the results by player.
...	Passed to the function kfac.

## Details

The Elo rating system is a simple method for evaluating the skill of players. It has been used since around 1960 and is still employed in various settings. Although the basic form uses only the ratings, additional complexity is commonly introduced by adding a player one advantage parameter and by using different K factors. A player one advantage parameter has been added to the original definition in the reference. This is also used for prediction purposes.

This implementation uses default arguments that are consistent with the implementation of FIDE for rating chess players. It does not employ the initialization used by FIDE. For the chess data analyzed in the file `doc/ChessRatings.pdf`, prediction performance is poor because the default values of the K factors are too low. This can be altered using the `kv` argument which is passed to the function `kfide`.

## Value

A list object of class "rating" with the following components

<code>ratings</code>	A data frame of the results at the end of the final time period. The variables are self explanatory except for <code>Lag</code> , which represents the number of time periods since the player last played a game, <code>Elite</code> , which is a binary indicator for whether or not a player has ever reached 2400, and <code>Opponent</code> , which gives the average rating of all opponents. The <code>Lag</code> variable is equal to zero for players who played in the latest time period, and is also zero for players who have not yet played any games. The <code>Elite</code> variable is required due to the K factor dependency in the FIDE implementation. The <code>Opponent</code> variable is not currently used in the updating algorithm.
<code>history</code>	A three dimensional array, or NULL if history is FALSE. The row dimension is the players, the column dimension is the time periods. The third dimension gives different parameters.
<code>gamma</code>	The player one advantage parameter.
<code>kfac</code>	The K factor or K factor function.
<code>type</code>	The character string "Elo".

## References

Elo, Arpad (1978) The Rating of Chessplayers, Past and Present. Arco. ISBN 0-668-04721-6.

## See Also

`elo`, `kfide`

## Examples

```
afl <- aflodds[,c(2,3,4,7)]
robj <- fide(afl)
robj

robj <- fide(afl[afl$Week==1,])
for(i in 2:max(afl$Week)) robj <- fide(afl[afl$Week==i,], robj$ratings)
robj
```

## Description

Implements the Glicko rating system for estimating the relative skill level of players in two-player games such as chess. It extends the Elo method by including a deviation parameter for each player, representing uncertainty on the rating.

## Usage

```
glicko(x, status = NULL, init = c(2200,300), gamma = 0, cval = 15,
      history = FALSE, sort = TRUE, ...)
```

## Arguments

x	A dataframe containing four variables: (1) a numeric vector denoting the time period in which the game took place (2) a numeric or character identifier for player one (3) a numeric or character identifier for player two and (4) the result of the game expressed as a number, typically equal to one for a player one win, zero for a player two win and one half for a draw.
status	A data frame with the current status of the system. If not NULL, this needs to be a data frame in the form of the ratings component of the returned list, containing variables named Player, Rating, Deviation, and optionally Games, Win, Draw, Loss and Lag, which are set to zero if not given.
init	The rating vector at which to initialize a new player not appearing in status. Must be a vector of length two giving the initial rating and initial deviation respectively. If different initializations for different players are required, this can be done using status.
gamma	A player one advantage parameter; either a single value or a numeric vector equal to the number of rows in x. Positive values favour player one, while negative values favour player two. This could represent the advantage of playing at home, or the advantage of playing white for chess. Note that this is not passed to <code>predict.rating</code> , which has its own gamma parameter.
cval	The c parameter, which controls the increase in the player deviations across time. Must be a single non-negative number.
history	If TRUE returns the entire history for each period in the component history of the returned list.
sort	If TRUE sort the results by rating (highest to lowest). If FALSE sort the results by player.
...	Not used.

## Details

The Glicko rating system is a method for evaluating the skill of players. It is more complex than Elo but typically yields better predictions. Default values are roughly optimized for the chess data analyzed in the file `doc/ChessRatings.pdf`, using the binomial deviance criterion. A player one advantage parameter has been added to the original definition in the reference. This is also be used for prediction purposes.

## Value

A list object of class "rating" with the following components

ratings	A data frame of the results at the end of the final time period. The variables are self explanatory except for Lag, which represents the number of time periods since the player last played a game. This is equal to zero for players who played in the latest time period, and is also zero for players who have not yet played any games.
history	A three dimensional array, or NULL if history is FALSE. The row dimension is the players, the column dimension is the time periods. The third dimension gives different parameters.
gamma	The player one advantage parameter.
cval	The c parameter.
type	The character string "Glicko".

## References

Glickman, M.E. (2001) Dynamic paired comparison models with stochastic variances. *Journal of Applied Statistics*, 28, 673-689.

## See Also

[elo](#), [steph](#)

## Examples

```
afl <- aflodds[,c(2,3,4,7)]
robj <- glicko(afl)
robj

robj <- glicko(afl[afl$Week==1,])
for(i in 2:max(afl$Week)) robj <- glicko(afl[afl$Week==i,], robj$ratings)
robj
```



hist.rating

*Histogram Plotting for a Rating Object***Description**

Plot histograms of estimated ratings or other features, including full history progressions.

**Usage**

```
## S3 method for class 'rating'
hist(x, which = "Rating", tng=15, history = FALSE, log = FALSE,
     xlab = which, main = paste(x$type," Ratings System"), density = FALSE,
     add = FALSE, ...)
```

**Arguments**

x	An object of class "rating".
which	The variable to be plotted.
tng	A single value. If the number of games played by the player is below this value, the player is not depicted on the plot.
history	If TRUE, a histogram is plotted for every single time point. Only available if the history was retained in x.
log	The log(x+1) transform. May be useful if plotting e.g. the number of games.
xlab,main	Graphical parameters.
density	If TRUE, plot a density estimate rather than a histogram.
add	Add to an existing plot? Only relevant for density estimates.
...	Other parameters to be passed through to plotting functions.

**See Also**

[plot.rating](#)

**Examples**

```
af1 <- aflodds[,c(2,3,4,7)]
robj <- steph(af1)
hist(robj, xlim = c(1900,2500), density=TRUE)

af1 <- aflodds[,c(2,3,4,7)]
robj <- steph(af1, history=TRUE)
hist(robj, history=TRUE, xlim = c(1900,2500), density=TRUE)
```

---

kfide*The K Factor Function Used By FIDE*

---

## Description

Calculates the K factor for the Elo rating system based on player rating, number of games played, and optionally a binary elite player identifier.

## Usage

```
kfide(rating, games, elite = NULL, kv = c(10,15,30))
```

## Arguments

rating	A numeric vector of player ratings.
games	A numeric vector with the number of games played by each player.
elite	If not NULL, then a binary identifier for elite players.
kv	The three different K factors that the function can produce.

## Details

This function is designed to be used for the `kfac` argument of either [fide](#) or [elo](#). It returns `kv[1]` for elite players, `kv[2]` for non-elite players with 30 games or more, and `kv[3]` for non-elite players with less than 30 games. The default is the current FIDE implementation which uses the K factors 10, 15 and 30. The K factor of 30 was changed from 25 in the year 2011. In this context, elite players are defined by FIDE as being those who have reached the rating 2400 or more at any time in the past.

## Value

A numeric vector of K factors.

## See Also

[fide](#)

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kgames

---

*A K Factor Function With Dependence On Number Of Games*

---

## Description

Calculates the K factor for the Elo rating system based on number of games played.

## Usage

```
kgames(rating, games, elite = NULL, gv = 30, kv = c(32,26))
```

## Arguments

rating	A numeric vector of player ratings. The K factor does not depend on this quantity.
games	A numeric vector with the number of games played by each player.
elite	Not used.
gv	A numeric vector of length one less than kv giving the thresholds for the number of games played.
kv	A numeric vector of length one more than gv giving the different K factors that the function can produce.

## Details

This function is designed to be used for the `kfac` argument of either [fide](#) or [elo](#). It returns `kv[i]` for players who have played a total number of games within the intervals defined by `gv` (closed on the right).

## Value

A numeric vector of K factors.

## See Also

[elo](#), [fide](#)

---

krating

*A K Factor Function With Dependence On Rating*


---

**Description**

Calculates the K factor for the Elo rating system based on the player rating.

**Usage**

```
krating(rating, games, elite = NULL, rv = 2300, kv = c(32,26))
```

**Arguments**

rating	A numeric vector of player ratings.
games	A numeric vector with the number of games played by each player. The K factor does not depend on this quantity.
elite	Not used.
rv	A numeric vector of length one less than kv giving the thresholds for the ratings.
kv	A numeric vector of length one more than gv giving the different K factors that the function can produce.

**Details**

This function is designed to be used for the kfac argument of either [fide](#) or [elo](#). It returns kv[i] for players who have a rating within the intervals defined by rv (closed on the right).

**Value**

A numeric vector of K factors.

**See Also**

[elo](#), [fide](#)

---

metrics

*Prediction Evaluation*


---

**Description**

Returns measures that assess prediction performance.

**Usage**

```
metrics(act, pred, cap = c(0.01,0.99), which = 1:3, na.rm = TRUE,
        sort = TRUE, digits = 3, scale = TRUE)
```

**Arguments**

<code>act</code>	A numeric vector of actual values. Typically equal to one for a player one win, zero for a player two win, and one half for a draw.
<code>pred</code>	A numeric vector of predictions, typically values between zero and one. A matrix can also be given, in which case the <i>j</i> th column contains the predictions for model <i>j</i> .
<code>cap</code>	A numeric vector of length two giving values at which to cap the binomial deviance.
<code>which</code>	Select metrics using any subset of 1 : 3. All are produced by default.
<code>na.rm</code>	Remove missing values in predictions. The default is to remove missing values because the default predict method will predict missing values for games with new players.
<code>sort</code>	By default output is ordered from best to worst using the first metric specified.
<code>digits</code>	Round to this number of digits.
<code>scale</code>	If TRUE (the default), all metrics are scaled so that a value of 100 corresponds to predicting 0.5 for every game.

**Details**

The preferred metric for assessing predictions in chess is the capped binomial deviance. Mean squared error and mean absolute error metrics are also produced. By default all metrics are scaled so that the value 100 represents the zero information case. If not scaled, then all metrics are multiplied by 100.

**Value**

A numeric vector.

**See Also**

[predict.rating](#)

**Examples**

```
af1 <- aflodds[,c(2,3,4,7)]
train <- af1[af1$Week <= 80,]
test <- af1[af1$Week > 80,]
robj <- elo(train)
metrics(test$Score, predict(robj, test))
metrics(test$Score, predict(robj, test), scale = FALSE)
```

plot.rating

*Plot Player Features Across Time for a Rating Object***Description**

Plot line traces of estimated ratings or other features for selected players. This function can only be used if the full history is retained in the object `x`.

**Usage**

```
## S3 method for class 'rating'
plot(x, which = "Rating", players = NULL, t0 = 1, tv = NULL,
     npl = 10, random = FALSE, xlab = "Time Period", ylab = paste(x$type, " Ratings"),
     main = paste(x$type, " Ratings System"), inflation = FALSE, add=FALSE, ...)
```

**Arguments**

<code>x</code>	An object of class "rating".
<code>which</code>	The variable to be plotted.
<code>players</code>	If not NULL, should be a vector of player identifiers to explicitly select players to be plotted.
<code>t0</code>	The time at which to begin. Note that unless players are specified explicitly, players who do not play at time <code>t0</code> will not be selected for the plot. Can also be a vector of length two, in which case the second value is the time at which to end.
<code>tv</code>	If not NULL, then a vector of values to be used on the x-axis instead of the time index.
<code>npl</code>	The number of players to select.
<code>random</code>	If TRUE, <code>npl</code> players are selected at random from those who played at time <code>t0</code> . If FALSE (the default), the <code>npl</code> players who played most games at <code>t0</code> are selected. Ignored if <code>players</code> is not NULL.
<code>xlab,ylab,main</code>	Graphical parameters.
<code>inflation</code>	If TRUE, plot the average rating of the best <code>npl</code> players at each time point. This is designed to investigate ratings inflation.
<code>add</code>	Add to an existing plot.
<code>...</code>	Other parameters to be passed through to plotting functions.

**Details**

Note that the argument `random` is not used by default, since it can produce flat profiles from randomly selected players who play few games. The default selection is non-random and selects more active players, however they may be more likely to improve over time than the general population.

**See Also**[hist.rating](#)**Examples**

```

afl <- aflodds[,c(2,3,4,7)]
robj <- steph(afl, history=TRUE)
plot(robj)

```

predict.rating

*Predict Result Of Games Based On Player Ratings***Description**

Predict the result of two-player games as a number between zero and one, given the estimated ratings for each player.

**Usage**

```

## S3 method for class 'rating'
predict(object, newdata, tng=15, trat=NULL, gamma=30,
        thresh, ...)

```

**Arguments**

object	An object of class "rating".
newdata	A dataframe containing three variables: (1) a numeric vector denoting the time period in which the game is taking place (2) a numeric or character identifier for player one (3) a numeric or character identifier for player two. The time period can contain missing values as it is not used for the prediction. Note that this argument cannot be missing; if predictions on the original dataset are required, then this dataset must be passed to the prediction function.
tng	A single value. If the number of games played by either player is below this value, then either the prediction will be a missing value, or the prediction will be based on trat.
trat	Either a single number or a vector of length two, giving the rating and deviation parameters to be used for players who have played less than tng games. If NULL then these predictions will be missing.
gamma	A player one advantage parameter; either a single value or a numeric vector equal to the number of rows in newdata. Positive values favour player one, while negative values favour player two. This could represent the advantage of playing at home, or the advantage of playing white for chess. The default value is roughly optimal for chess ratings.
thresh	A single value. If given, a binary vector is returned indicating whether the prediction is greater than this value.
...	Not used.

**Details**

The function predicts the expectation of the game result. If the value of one is a win for player one, and the value of zero is a win for player two, and there are no other possibilities, then the prediction is the probability of a win for player one. This is not the case when draws are a possibility.

**Value**

A numeric vector of predictions, which may contain missing values.

**See Also**

[metrics](#)

**Examples**

```
af1 <- aflodds[,c(2,3,4,7)]
train <- af1[af1$Week <= 80,]
test <- af1[af1$Week > 80,]
robj <- elo(train)
pvals <- predict(robj, test)
```

---

steph

*The Stephenson Rating System*


---

**Description**

Implements the Stephenson rating system for estimating the relative skill level of players in two-player games such as chess. It extends the Glicko method by including a second parameter controlling player deviation across time, a bonus parameter, and a neighbourhood parameter.

**Usage**

```
steph(x, status = NULL, init = c(2200,300), gamma = 0, cval = 10,
      hval = 10, bval = 0, lambda = 2, history = FALSE, sort = TRUE, ...)
```

**Arguments**

- |        |   |
|--------|---|
| x      | A dataframe containing four variables: (1) a numeric vector denoting the time period in which the game took place (2) a numeric or character identifier for player one (3) a numeric or character identifier for player two and (4) the result of the game expressed as a number, typically equal to one for a player one win, zero for a player two win and one half for a draw. |
| status | A data frame with the current status of the system. If not NULL, this needs to be a data frame in the form of the ratings component of the returned list, containing variables named Player, Rating, Deviation, and optionally Games, Win, Draw, Loss and Lag, which are set to zero if not given.  |



<code>init</code>	The rating vector at which to initialize a new player not appearing in status. Must be a vector of length two giving the initial rating and initial deviation respectively. If different initializations for different players are required, this can be done using status.
<code>gamma</code>	A player one advantage parameter; either a single value or a numeric vector equal to the number of rows in <code>x</code> . Positive values favour player one, while negative values favour player two. This could represent the advantage of playing at home, or the advantage of playing white for chess. Note that this is not passed to <code>predict.rating</code> , which has its own gamma parameter.
<code>cval</code>	The <code>c</code> parameter, which controls the increase in the player deviations across time. Must be a single non-negative number. Note that both <code>cval</code> and <code>hval</code> increase player deviations, so if <code>hval</code> is not zero then <code>cval</code> should typically be lower than the corresponding parameter in <code>glicko</code> .
<code>hval</code>	The <code>h</code> parameter, which also controls the increase in the player deviations across time. Must be a single non-negative number.
<code>bval</code>	The bonus parameter, which gives a per game bonus to each player on the basis that players who play more often may improve irrespective of whether they win or lose. A single non-negative number. Note that this will create ratings inflation (i.e. ratings will increase over time).
<code>lambda</code>	The neighbourhood parameter, which shrinks player ratings towards their opponents. A single non-negative number.
<code>history</code>	If TRUE returns the entire history for each period in the component history of the returned list.
<code>sort</code>	If TRUE sort the results by rating (highest to lowest). If FALSE sort the results by player.
<code>...</code>	Not used.

## Details

The Stephenson rating system is a method for evaluating the skill of players. It was developed by Alec Stephenson in 2012 as a variant of his winning entry in a competition to find the most useful practical chess rating system, organized by Jeff Sonas on Kaggle, a platform for data prediction competitions. The precise details are given in the file `doc/ChessRatings.pdf`.

This implementation is written so that Glicko is obtained as a special case upon setting all of the parameters `hval`, `bval` and `lambda` to zero. Default values are roughly optimized for the chess data analyzed in the file `doc/ChessRatings.pdf`, using the binomial deviance criterion.

## Value

A list object of class "rating" with the following components

<code>ratings</code>	A data frame of the results at the end of the final time period. The variables are self explanatory except for <code>Lag</code> , which represents the number of time periods since the player last played a game. This is equal to zero for players who played in the latest time period, and is also zero for players who have not yet played any games.
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history	A three dimensional array, or NULL if history is FALSE. The row dimension is the players, the column dimension is the time periods. The third dimension gives different parameters.
gamma	The player one advantage parameter.
cval	The c parameter.
hval	The h parameter.
bval	The bonus parameter.
lambda	The neighbourhood parameter.
type	The character string "Stephenson".

## References

Glickman, M.E. (2001) Dynamic paired comparison models with stochastic variances. *Journal of Applied Statistics*, 28, 673-689.

## See Also

[glicko](#)

## Examples

```
af1 <- aflodds[,c(2,3,4,7)]
robj <- steph(af1)
robj

robj <- steph(af1[af1$Week==1,])
for(i in 2:max(af1$Week)) robj <- steph(af1[af1$Week==i,], robj$ratings)
robj
```

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