THESIS

Baseline Compensation System for Underground Gravitational-wave Telescope

Koseki Miyo

Department of Physics University of Tokyo

MMM 2020

Contents

1	Bac	ground	7
	1.1	Gravitational-wave	7
		1.1.1	7
	1.2	Sources of gravitational-wave	7
		1.2.1	7
	1.3	Interferometric Gravitational-wave detection	7
		1.3.1 Introduction	7
		1.3.2 Working Principle	7
		1.3.3 The 2nd Generation Interferometers	7
	1.4	Summary of the Chapter	7
2	KA	$_{ m GRA}$	9
	2.1	Overview	9
		2.1.1	9
		2.1.2	9
	2.2	KAGRA Tunnel	9
		2.2.1 Tunnel Design	9
		2.2.2 Geological features	9
	2.3	Main Interferometer	9
		2.3.1 Overview	9
			9
	2.4		0
		v –	0
			0
	2.5	· · · · · · · · · · · · · · · · · · ·	0
3	Une	erground Seismic Noise 1	1
•	3.1		1
	0.1		1
		3.1.2 Human activity	
			2
			2
			13
		1	4
	3.2		15
	0.4	·	L5
			L5
			16

4 CONTENTS

		3.2.4	Results	17
	3.3	Differ	ential Motion Reduction	18
		3.3.1	Introduction	18
		3.3.2	Differential Motion Reduction	18
	3.4	Meası	rement of Differential Motion Reduction	20
		3.4.1	Reduction in X-arm Scale	20
		3.4.2		20
	3.5	Summ		20
4	Geo	physic	cs Interferometer (GIF)	21
	4.1	Overv	iew	21
		4.1.1	Laser Strainmeter gor Geophysics	21
		4.1.2	Motivation in GW detectors	21
	4.2	Worki	ing Principle	21
		4.2.1	Asynmetric Michelson Interferometer	21
		4.2.2	Response to the seismic strain	21
		4.2.3	Signal Detection Scheme	22
		4.2.4		22
	4.3	Optics	8	22
		4.3.1	Mode Matching Optics	
		4.3.2		23
		4.3.3	Core Optics	23
	4.4	Data	Aquisition System	23
		4.4.1		23
	4.5		nary of the Chapter	23
5	Arn	n Leng	gth Compensation System for Global Seismic Control 2	25
	5.1	Basics	s in Vibration Isolation and Control Technique	26
		5.1.1	Passive Vibration Isolation	26
		5.1.2	Active Vibration Isolation	26
		5.1.3	Sensor Belnding Control Technique	26
		5.1.4	2 Types Feedforward Control Techniques	26
		5.1.5	Toward the Global Seismic Control	26
	5.2	Difficu	ulties in the Global Seismic Control	26
		5.2.1	Overview	26
		5.2.2	Actuator Range Limit	26
		5.2.3		26
		5.2.4		26
	5.3	Arm 1	Length Compensation Using Geophysics Interferometer	26
		5.3.1		26
		5.3.2	•	26
		5.3.3		26
		5.3.4	•	26
	5.4	Summ		26

CONTENTS 5

6	Der	nonstration of Arm Length Compensation Control	27
	6.1	Experimental Arrangement	27
		6.1.1	
	6.2	Results	27
		6.2.1	27
	6.3	Discussion and Summary of the Chapter	27
		6.3.1 Discussion	27
		6.3.2 Summary	27
7	Cor	aculusion and Future Directions	29
	7.1	Conclusion	29
	7.2	Future Directions	29
\mathbf{A}	The	eory of Seismic Waves	31
	A.1	Body Wave	31
		Rayleigh 波	
		Depth Dependence	

Background

4 4	\sim	• 1	. •	1	
1.1	(ira	งบรา	t in	า ค I 🗕	wave
┸• ┸	Q I d	ινισα	.u.v.i	ıaı-	wavc

- 1.1.1 ...
- 1.2 Sources of gravitational-wave
- 1.2.1 ...
- 1.3 Interferometric Gravitational-wave detection
- 1.3.1 Introduction
- 1.3.2 Working Principle
- 1.3.3 The 2nd Generation Interferometers

Fabry-Perot Cavity

Power Recycling Cavity

Signal Recycling Cavity

1.4 Summary of the Chapter

KAGRA

2.1 Overview

- 2.1.1 ...
- 2.1.2 ...

2.2 KAGRA Tunnel

2.2.1 Tunnel Design

KAGRA tunnel is excavated in the Kamioka mine in Hida, Gifu, Japan [1]. The tunnel is consisted of two floors. 干渉計を構成するほとんどの鏡は 1 階に設置された防振装置で懸架されているが、腕共振器を構成する 4 つの鏡は 1 階から 14m の高さにある 2 階から懸架されている。

The tunnel is locate under 200 m from ground surface to decrease the seismic noise effectively.

2.2.2 Geological features

Hida region to which Kamioka belongs is a ancient region in Japan island [2].

The main bedrock is the geniss.

2.3 Main Interferometer

2.3.1 Overview

KAGRA is a cryogenic intergerometric gravitational-wave detector constructed at the underground site of Kamioka mine [3].

2.3.2 Main Interferometer

Design

The design of KAGRA interferometer is dual recycled Fabry-Perot Michelson interferometer [4][5].

2.4 Vibration Isolation System

2.4.1 Overview

KAGRA has 4 types vibration isolation system.

2.4.2 Type-A Suspension System

Type-A suspensions are developed [6].

2.5 Summary of the Chapter

Underground Seismic Noise

3.1 Seismic Noise

3.1.1 Overview

These seismic noise not only limits the sensitivity of the terrestrial gravitational-wave detector but also decreases the duty cycle of the detector. As mentioned in §1.3, because the sensitivity of the laser interferometric gravitational-wave telescope detect gravitational-waves in the differential length of the X arm and the Y arm, the fluctuations of these arm length decrease the sensitivity. Thus, we need the vibration isolation system reducing the lower seismic noise, and choose the more quiet place, in order to detect the signal in lower frequencies. On the other hands, realistically, it is difficult to reduce the seismic noise below 0.1 Hz. This difficulty means that the motions not isolated disturb the detector which only can work within the limited range. These two problems of seismic noise are resolved by constructing the detector under the ground.

It have been kwnon that places under the ground is more quiet than these on the surface of ground [7]. Especially, the seismic noise of the underground above 1 Hz is effectively reduced than the noise of the surface [8]. さらに、世界で初めて地下に建設した 20m の重力波望遠鏡 LISM はその安定性の高さを示した [9]。しかし、§3.3 で後述するとおり、長期線になるほど低周波地面振動は基線長変動に現れやすくなるため、大型化をする限り、低周波地面振動の問題は残り続ける。

Table 3.1 に、大型重力波望遠鏡で問題となる地面振動をリストアップした。The ground is vibrated by several sources. As shown in table 3.1, main sources are listed with tipical frequency band and RMS amplitude of these. The lower frequency motion tends to be originated the global environment such as ocean activity, weather, and rotation and revolution of the Earth. On the other hand, the higher one is tends to be originated the local environment such as the human activity.

Table 3.1: Baseline changes caused by several seismic sources

Sources	Frequency Band [Hz]	RMS Amplitude $[\mu m]$	Detail
Human,traffic	> 1	< 1	§3.1.2
Ocean waves (Microseisms)	0.1 – 0.3	0.1-10	$\S 3.1.3$
Large earthquakes	> 0.05	> 100	$\S 3.1.4$
Air pressure	< 0.05	> 100	$\S 3.1.5$
Moon, Sun (Earth tides)	$< 1^{-5}$	> 100	§3.1.6

In this section, these sources are described.

3.1.2 Human activity

およそ 1Hz 以上のゆれは人工的な揺れである。

3.1.3 Microseisms

Microseisms which power spectrum has peaks in 50–200 mHz are excitated by oceanic waves. These seismic waves can be categolized by the generating mechanism of these [10].

The primary ocean microseisms are generated only in shallow waters in coastal regions. In this regions, the water wave enery can be converted directly into seismic energy either through vertical water pressure variations, or by the impacts of surf on the shores. There are correlation between this microseismic peak and the swell at the beaches was known starting from the data sets studied by [11].

..

The secondary ocean microseisms could be explained by the superposition of ocean waves of equal period traveling in opposite directions. Therefore, generating standing gravity waves of half the period [12].

...

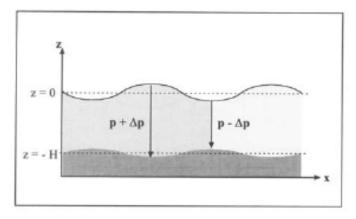
The RMS amplitude spectral of both type of the microseisms are strongly depends on the low pressure on the ocean [13].

...

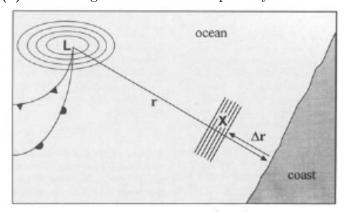
3.1.4 Large Earthquakes

hoge

Large amplitude earthquakes around the world would interrupt the operation of the gravitational wave detector and reduce their duty cycle. 実際、観測中に地震でロックが落ちたあと、復帰するまでに数時間かかる場合がある [14]。規模の大きな地震ほど、振幅がおおきいことはもちろん、長周期で減衰までにかかる時間が長い。長周期地震に対して重力波検出器が無力なのは、その防振装置が、せいぜい 100 mHz の地面振動揺れに対して最適化しているためである []。そのためこのような制



(a) Generating mechanism of the primary microseisms.



(b) Generating mechanism of the secondary microseisms.

Figure 3.1: Generating mechanism of the microsisms. (a) describes the mechanism of the primary microseisms. (b) describes the mechanism of the secondary microseisms.

御方式を使う以上、制御ノイズが増大して感度が落ちることを犠牲にしてでも、地震が来る前に、地震でロックロスしないような制御フィルターの切り替えを必要とする。この切替のために Seismon とよばれる早期地震アラートシステム [15] を用いた制御フィルターの切り替えが試みられている [16]。

hoge

• • •

...

3.1.5 Air pressure

hoge

...

•••

• • •

hoge

...

hoge

...

3.1.6 Earth Tides

 $\S 3.1.2 \text{ hoge}$

...

...

hoge

...

•••

hoge

...

• • •

3.2 Long-term Study of the seismic environment at KAGRA

3.2.1 Overview

The seismic waves are excited on the source and propagate along the surface of the Earth with amplitude decreasing with depth [7]. However, especially microseims whose peak is around 0.1 Hz are not attenuated adequately compared with higher frequencies above 1 Hz, because the wavelength is comparable to or longer than the depth. Amount of these atenuation factor is must be explaing by a complicated phenomenon, which depends on either the local geology or location of the exciting sources.

In this section, seasonal change of the RMS amplitude of the seismic noise is described.

3.2.2 Experimental Arrangement

Seismic motion is measured by a seismometer installed on the second floor of the X-end area. This area is placed 200 m underground from the surface of the mountain. Comparison to corner area, human activity in the end area is less because the corner area has parking lots. Comparison to the Y-end area, there is no entrance connected to other mines. Therefore, the X-end area is relatively quiet in the KAGRA mine, regarding the seismic noise induced by human activity.

In this study, Trillium 120-QA which is known as three-component, very broadband, and low-noise seismometer, was used. These three outputs are proportional to the ground velocity of two horizontal and one vertical, respectively. The feature of the low-noise can resolve Peterson's new low-noise model (NLNM) and new high-noise model (NHNM) [17].



Figure 3.2: Trillium 120-QA installed on the second floor at X-end area, which is coverd by black thermal insulation cover

As shown in fig 3.2, the seismometer is housed in the black thermal insulation cover according to the installation manual [18]. Thermal insulation protects two broad categories of thermal couplings that can cause unwanted noise [18]. First is the direct coupling to the sensitivity. This coupling typically increases the noise

of the vertical channel as a periodic diurnal variation caused by the day-to-night temperature cycle, because the springs that suspended the inertial masses are temperature sensitive. The second is the coupling to tilt from the thermal fluctuation. Tilt converts the vertical acceleration of gravity into horizontal acceleration. This thermally induced tilt noise on the horizontal will be larger than the direct thermal coupling on the vertical channel. To be low sensitivity to both tilt and temperature, this model has a function to center the inertial mass after the initial installation.

The signals of the seismometer is recorded through the data aquisition system developed by LIGO [19]. The analog signal is converted to digital signal by the 16 bit analog-to-digital converters (ADC) with 16384 Hz sampling. In addition, the signal of the seismoemter is amplified with 30 db so that the ADC noise does not mask this signal.

...

...

3.2.3 Data

```
定常な時系列データを1年間のデータのから選んだ。
3.4.
...
```



Figure 3.3: Available data from June 00 2018 to Jun 00 2019

```
\mathrm{hoge}\ \dots
```

٠.

3.2. LONG-TERM STUDY OF THE SEISMIC ENVIRONMENT AT KAGRA17

hoge ...
..
hoge ...
..

3.2.4 Results

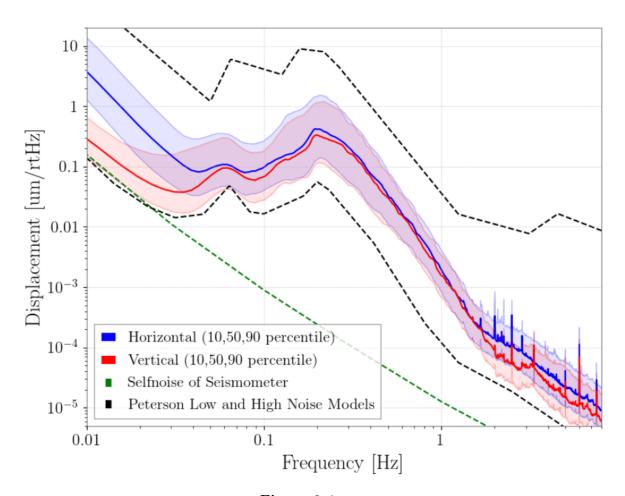


Figure 3.4

huge ...

. . .

...

3.3 Differential Motion Reduction

3.3.1 Introduction

The motion of two mirrors in the cavity have two modes. One is differential motion, which is the length change of that. Another one is common motion, which is the motion of the center of the cavity. In terms of the length control, it is important that the RMS amplitude of differential motion is as small as possible. Actuarly, the amplitude of these two motions are the same each other when the mirrors moves with no coherence. However, when a coherence exists, the common motion tends to be larger than the differential one.

As discussed in this section, the coherence depends on both, the arm length and the wavelength of seismic waves. For example, if the arm length is much more smaller than the wavelength, the mirrors move together. This means that the common motion is greater than the differential motion.

The ratio of the amplitudes of the differential motion over common motion is newly defined as Common and Differential Motion Ratio (CDMR). It is usefull to know how the ground reducts the differential motion or increase the common motion.

3.3.2 Differential Motion Reduction

Differential Motion and Common Motion

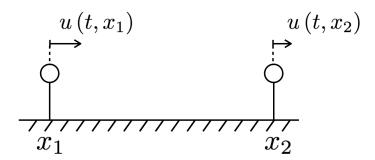


Figure 3.5: The displacements of the two points which are sparated L in X axis.

Motions of the two points can be represented as the differential motion and the common motion. Displacement of both differential motion and common motion of the two points shown in Figure (??) are defined as

$$u_{\text{diff}} \equiv \frac{u_1 - u_2}{\sqrt{2}}, \ u_{\text{comm}} \equiv \frac{u_1 + u_2}{\sqrt{2}}$$
 (3.1)

where $u_1(x,t)$ and $u_2(x,t)$ are the displacement of each points. These two motions defined in Eq.(3.1) are normalized by $\sqrt{2}$ due to conserve the total power.

Common and Differential Motion Ratio (CDMR)

CDMR is defined as the powers of common motion over the differential motion as bellow,

$$CDMR \equiv \sqrt{\frac{Common Motion}{Differential Motion}} = \sqrt{\frac{P_{comm}(\omega)}{P_{diff}(\omega)}}$$
(3.2)

where P_{comm} , P_{diff} are the power spectral densities (PSDs) of the differential motion and common motion, respectively. Each PSDs are converted from the autocorrelation function of these by the Wiener-Khinchin theorem.

First, autocorrelation function C_{diff} of the differential motion is given by its definition in Eq.(3.1)

$$C_{\text{diff}}(\tau) = \frac{1}{2} \left\langle \left[x_1(t) - x_2(t) \right] \left[x_1(t+\tau) - x_2(t+\tau) \right] \right\rangle$$
 (3.3)

$$= \frac{1}{2} \left[C_{11}(\tau) - C_{12}(\tau) - C_{21}(\tau) + C_{22}(\tau) \right], \tag{3.4}$$

,where C_{ij} are the autocorrelation functions of each point and defined as $C_{ij} \equiv \langle x_i(t)x_j(t+\tau)\rangle$, (i=1,2,j=1,2). Therefore, the power spectrum density of differential motion $P_{\text{diff}}(\omega)$ can be computed as

$$P_{\text{diff}}(\omega) = \frac{1}{2} \left[P_1(\omega) + P_2(\omega) - P_{12}(\omega) - P_{12}^*(\omega) \right]$$
 (3.5)

$$= \frac{1}{2} \left[P_1 + P_2 - \operatorname{Re}\left[\gamma\right] \times 2\sqrt{P_1 P_2} \right] \tag{3.6}$$

where $P_1(\omega)$, $P_2(\omega)$ are the power spectrum densities of each points, and $P_{12}(\omega)$ are the cross spectrum between two point. The parameter γ is the complex coherence between them defined below,

$$\gamma \equiv \frac{P_{12}}{\sqrt{P_1 P_2}}.\tag{3.7}$$

Here, assuming that seismic wave propagating each points does not decay, which means $P_1 = P_2 \equiv P$, one can compute the $P_{\text{diff}}(\omega)$ as

$$P_{\text{diff}}(\omega) = P(1 - \text{Re}\left[\gamma\right]). \tag{3.8}$$

Therefore, the PSDs of the common motion can be calculated as

$$P_{\text{comm}}(\omega) = P(1 + \text{Re}\left[\gamma\right]). \tag{3.9}$$

Finaly, CDMR defined Eq.(3.2) in case the seismic wave does not decay is represented as

$$CDMR = \sqrt{\frac{1 + \text{Re}\left[\gamma\right]}{1 - \text{Re}\left[\gamma\right]}}.$$
(3.10)

Eq.(3.10) indicate that CDMR can be expressed by only the coherence γ between of two points. For example, CDMR tends to be larger when γ close to 1. This means that the differential motion is more less than the common motion because the two points move together in the same direction.

- 3.4 Measurement of Differential Motion Reduction
- 3.4.1 Reduction in X-arm Scale
- 3.4.2 Reduction in Other Short Scale
- 3.5 Summary of the Chapter

Geophysics Interferometer (GIF)

4.1 Overview

- 4.1.1 Laser Strainmeter gor Geophysics
- 4.1.2 Motivation in GW detectors

4.2 Working Principle

4.2.1 Asymmetric Michelson Interferometer

$$\phi = 2\pi \frac{2(l_x - l_y)}{\lambda} \sim 4\pi \frac{l_x}{\lambda} \tag{4.1}$$

$$|d\phi| = 4\pi \frac{l_x}{\lambda} \left(\left| \frac{d\lambda}{\lambda} \right| + \left| \frac{dl_x}{l_x} \right| \right) \tag{4.2}$$

4.2.2 Response to the seismic strain

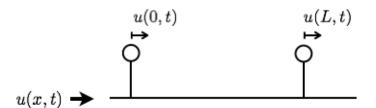


Figure 4.1: The displacements of the two points which are sparated L in X axis.

The response of the strainmeter to seismic waves have characteristics of the low pass filter. To calculate this response, it is assumed that the plane seismic waves which displacement u(x,t) is represented as $u(x,t) = u_0 e^{i(\omega t - kx)}$ with angular frequency of ω and wave number of k, propagate along with the direction of the

base-line of the strain meter. The length fluctuation between two mirrors sparated with L can be expressed as

$$\Delta L(t) \equiv u(0,t) - u(L,t) \tag{4.3}$$

$$= u(0,t) - u(0,t-\tau), \tag{4.4}$$

where $\tau = L/v$ is the time delay. The transfer function from the displacement to the length fluctuation is

$$H_{\rm disp}(s) \equiv \frac{\Delta L(s)}{u(s)} = 1 - \exp(-\tau s) \tag{4.5}$$

Because the strain amplitude $\epsilon(x,t)$ is defined as $\epsilon(x,t) \equiv \frac{du}{dx}$, the strain

$$\epsilon(x,t) \equiv \frac{du}{dx} = \frac{du}{dt}\frac{dt}{dx}$$
 (4.6)

$$= u(x,t)'\frac{1}{v} \tag{4.7}$$

Therefore, the response of the strainment to the seismic strain is given

$$H_{\text{strain}}(s) \equiv \frac{\Delta L(s)}{\epsilon(s)} = \frac{\Delta L(s)}{\frac{s}{v}u(s)} = (1 - \exp(-\tau s))\frac{v}{s}$$
(4.8)

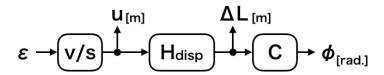


Figure 4.2

4.2.3 Signal Detection Scheme

Quadrature Phase Detection

4.2.4 Noise

どういうノイズが原理的に存在するか述べる。空気ゆらぎ、周波数雑音を述べる。

4.3 Optics

どうやって実際の干渉計を構築しているか述べる。

4.3.1 Mode Matching Optics

どういうモードマッチをして干渉計として光を干渉させているか述べる。

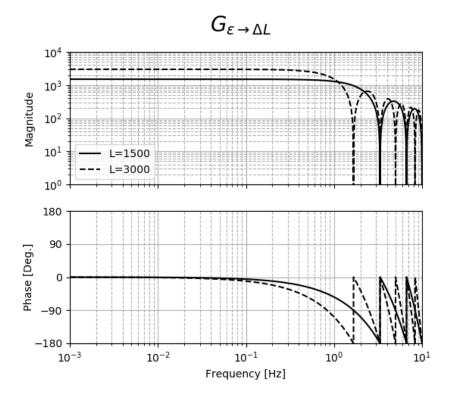


Figure 4.3

4.3.2 Frequency Stabilized Laser

どういう制御をして周波数安定をしているか述べる。

4.3.3 Core Optics

Beam Splitter

どういうミラーを使っているか述べる。

Corner Cube

どういうミラーを使っているか述べる。大きさとか表面の精度とか。

4.4 Data Aquisition System

4.4.1 ...

4.5 Summary of the Chapter

本章で述べたパラメータを表にまとめる。

Arm Length Compensation System for Global Seismic Control

- 5.1 Basics in Vibration Isolation and Control Technique
- 5.1.1 Passive Vibration Isolation

Single Pendulum

Multi Pendulum

- 5.1.2 Active Vibration Isolation
- 5.1.3 Sensor Belnding Control Technique
- 5.1.4 2 Types Feedforward Control Techniques

Feedforward at Feedback Point

Feedforward at Error Point

5.1.5 Toward the Global Seismic Control

Overview

Suspension Point Interferometer

- 5.2 Difficulties in the Global Seismic Control
- 5.2.1 Overview
- 5.2.2 Actuator Range Limit
- 5.2.3 ...
- 5.2.4 ...
- 5.3 Arm Length Compensation Using Geophysics Interferometer
- 5.3.1 Concept
- 5.3.2 Geophysics Interferometer for Sensing the Arm Length

Demonstration of Arm Length Compensation Control

- 6.1 Experimental Arrangement
- 6.1.1 ...
- 6.2 Results
- 6.2.1 ...
- 6.3 Discussion and Summary of the Chapter
- 6.3.1 Discussion
- 6.3.2 Summary

Conculusion and Future Directions

- 7.1 Conclusion
- 7.2 Future Directions

Appendix A

Theory of Seismic Waves

A.1 Body Wave

等方弾性体中では変位 u は以下の波動方程式に従う。

$$\rho \ddot{\boldsymbol{u}} = (\lambda + 2\mu)\nabla(\nabla \cdot \boldsymbol{u}) - \mu\nabla \times (\nabla \times \boldsymbol{u})$$
(A.1)

ここで ρ は媒質の密度、 λ , μ はラメ定数である。

この波動方程式は縦波であるP波と横波であるS波について解くことができる。 そのためにまず Helmholtz decomposition をつかって変位 u を発散成分 $u_{
m div}$ と回転 成分 $u_{\rm rot}$ で表す。つまり、

$$\mathbf{u}_{\text{div}} = \nabla \phi$$
 (A.2)

$$\mathbf{u}_{\text{rot}} = \nabla \times \psi$$
 (A.3)

となるスカラーポテンシャル ϕ とベクトルポテンシャル ψ が存在し、変位uは

$$\boldsymbol{u} = \nabla \phi + \nabla \times \psi \tag{A.4}$$

と表すことができる。式 (A.1) に式 (A.4) を代入し、かつベクトル解析の公式、 $\nabla \times$ $(\nabla \times \mathbf{A}) = \nabla(\nabla \cdot \mathbf{A}) - \nabla^2 \mathbf{A}$ を使うと、

$$\ddot{\phi} = v_L^2 \nabla^2 \phi \tag{A.5}$$

$$\ddot{\phi} = v_L^2 \nabla^2 \phi \tag{A.5}$$

$$\ddot{\psi} = v_T^2 \nabla^2 \psi \tag{A.6}$$

のように2つの波動方程式を得る。ここで v_L, v_T は、

$$v_L = \sqrt{\frac{\lambda + 2\mu}{\rho}}, v_T = \sqrt{\frac{\mu}{\rho}}$$
 (A.7)

である。

 v_L, v_T らはそれぞれ縦波と横波の位相速度を表しているが、これを示す。まずス カラーポテンシャルとベクトルポテンシャルは式 (A.5)、式 (A.6) の波動方程式に従 うので、これらの一般解は

$$\phi = \phi_0(\omega t - \boldsymbol{k} \cdot \boldsymbol{x}) \tag{A.8}$$

$$\boldsymbol{\psi} = \boldsymbol{\psi}_0(\omega t - \boldsymbol{k} \cdot \boldsymbol{x}) \tag{A.9}$$

で表すことができる。ここで ω , k は各周波数と波数ベクトルである。発散成分である $u_{\rm div}$ は式 (A.2) に式 (A.8) を代入して、

$$\boldsymbol{u}_{\text{div}} = \nabla \phi_0(\omega t - \boldsymbol{k} \cdot \boldsymbol{x}) = -\boldsymbol{k}\phi \tag{A.10}$$

となるので、変位の向きは波数ベクトルと平行である。つまり縦波であり P 波に相当する。一方で回転成分である u_{rot} は式 (A.3) に式 (A.9) を代入して、

$$\mathbf{u}_{\text{rot}} = \nabla \times \mathbf{\psi}_{\mathbf{0}}(\omega t - \mathbf{k} \cdot \mathbf{x}) = -\mathbf{k} \times \mathbf{\psi}$$
(A.11)

となるので、変位の向きは波数ベクトルと直行している。つまり横波でありS波に相当する。したがって v_L, v_T はそれぞれ縦波と横波の位相速度を示していることがわかった。また λ と μ は正の定数なので、

$$v_L > v_T \tag{A.12}$$

となって、縦波のほうが横波よりも速いことがわかる。

A.2 Rayleigh 波

(レイリー波の導出。)

A.3 Depth Dependence

(レイリー波の振幅が深さに依存していることを述べる。)

Bibliography

- [1] T Uchiyama, K Furuta, M Ohashi, S Miyoki, O Miyakawa, and Y Saito. Excavation of an underground site for a km-scale laser interferometric gravitational-wave detector. *Classical and Quantum Gravity*, 31(22):224005, 2014. Link.
- [2] Yukio Isozaki, Kazumasa Aoki, Takaaki Nakama, and Shuichi Yanai. New insight into a subduction-related orogen: a reappraisal of the geotectonic framework and evolution of the japanese islands. *Gondwana Research*, 18(1):82–105, 2010. Link.
- [3] T Akutsu and et. al. Construction of kagra: an underground gravitational-wave observatory. *Progress of Theoretical and Experimental Physics*, 2018(1), 01 2018. Link.
- [4] Yoichi Aso, Yuta Michimura, Kentaro Somiya, Masaki Ando, Osamu Miyakawa, Takanori Sekiguchi, Daisuke Tatsumi, and Hiroaki Yamamoto. Interferometer design of the kagra gravitational wave detector. *PHYSICAL REVIEW D Phys Rev D*, 88:043007, 2013. Link.
- [5] Kentaro Somiya. Detector configuration of kagra the japanese cryogenic gravitational-wave detector. Classical and Quantum Gravity, 29(12):124007, jun 2012. Link.
- [6] Okutomi Koki. Development of 13.5-meter-tall Vibration Isolation System for the Main Mirrors in KAGRA. PhD thesis, SOKENDAI, The Graduate University for Advanced Studies, 2019. Link.
- [7] Jerry A Carter, Noel Barstow, Paul W Pomeroy, Eric P Chael, and Patrick J Leahy. High-frequency seismic noise as a function of depth. *Bulletin of the Seismological Society of America*, 81(4):1101–1114, 1991.
- [8] LCGT collaboration. Lcgt design document version 3.0. Technical Report JGW-T0400030-v4, Institute for Cosmic Ray Research, University of Tokyo, JGW document, 11 2009.
- [9] Shuichi Sato, Shinji Miyoki, Souichi Telada, Daisuke Tatsumi, Akito Araya, Masatake Ohashi, Yoji Totsuka, Mitsuhiro Fukushima, Masa-Katsu Fujimoto, LISM Collaboration, et al. Ultrastable performance of an underground-based laser interferometer observatory for gravitational waves. *Physical Review D*, 69(10):102005, 2004.
- [10] P Bormann. New manual of seismological observatory practice. *GFZ German Research Centre for Geosciences*, 2012. Link.

34 BIBLIOGRAPHY

[11] RA Haubrich, WH Munk, and FE Snodgrass. Comparative spectra of microseisms and swell. *Bulletin of the Seismological Society of America*, 53(1):27–37, 1963. Link.

- [12] Michael Selwyn Longuet-Higgins. A theory of the origin of microseisms. *Philosophical Transactions of the Royal Society of London. Series A, Mathematical and Physical Sciences*, 243(857):1–35, 1950. Link.
- [13] L Naticchioni, M Perciballi, F Ricci, E Coccia, V Malvezzi, F Acernese, F Barone, G Giordano, R Romano, M Punturo, R De Rosa, P Calia, and G Loddo. Microseismic studies of an underground site for a new interferometric gravitational wave detector. Classical and Quantum Gravity, 31(10):105016, may 2014.
- [14] Michael Coughlin, Christopher Stubbs, Sergio Barrientos, Chuck Claver, Jan Harms, R. Chris Smith, and Michael Warner. Real-time earthquake warning for astronomical observatories. *Experimental Astronomy*, 39(2):387–404, Jun 2015.
- [15] Michael Coughlin, Paul Earle, Jan Harms, Sebastien Biscans, Christopher Buchanan, Eric Coughlin, Fred Donovan, Jeremy Fee, Hunter Gabbard, Michelle Guy, Nikhil Mukund, and Matthew Perry. Limiting the effects of earth-quakes on gravitational-wave interferometers. *Classical and Quantum Gravity*, 34(4):044004, feb 2017.
- [16] S Biscans, J Warner, R Mittleman, C Buchanan, M Coughlin, M Evans, H Gabbard, J Harms, B Lantz, N Mukund, A Pele, C Pezerat, P Picart, H Radkins, and T Shaffer. Control strategy to limit duty cycle impact of earthquakes on the LIGO gravitational-wave detectors. *Classical and Quantum Gravity*, 35(5):055004, jan 2018.
- [17] Jon R Peterson. Observations and modeling of seismic background noise. Technical report, US Geological Survey, 1993.
- [18] Nanometrics Inc., 250 Herzberg Road Kanata, Ontario, Canada K2K 2A1. Trillium 120Q/QA User Guide, 04 2017.
- [19] Rolf Bork, R Abbott, D Barker, and J Heefner. An overview of the ligo control and data acquisition system. arXiv preprint physics/0111077, 2001.