THESIS

Arm Length Compensation System for Underground Gravitational-wave Telescope

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Background

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1.5 Under Ground Laser Interferometer
1.5.1 ...

Summary of the Chapter

KAGRA

2.1 Overview

- 2.1.1 ...
- 2.1.2 ...

2.2 KAGRA Tunnel

2.2.1 Tunnel Design

KAGRA tunnel is excavated in the Kamioka mine in Hida, Gifu, Japan [1]. The tunnel is consisted of two floors. 干渉計を構成するほとんどの鏡は 1 階に設置された防振装置で懸架されているが、腕共振器を構成する 4 つの鏡は 1 階から 14m の高さにある 2 階から懸架されている。

The tunnel is locate under 200 m from ground surface to decrease the seismic noise effectively.

2.2.2 Geological features

Hida region to which Kamioka belongs is a ancient region in Japan island [2].

The main bedrock is the geniss.

2.3 Main Interferometer

2.3.1 Overview

KAGRA is a cryogenic intergerometric gravitational-wave detector constructed at the underground site of Kamioka mine [3].

2.3.2 Main Interferometer

Design

The design of KAGRA interferometer is dual recycled Fabry-Perot Michelson interferometer [4][5].

2.4 Vibration Isolation System

2.4.1 Overview

KAGRA has 4 types vibration isolation system.

2.4.2 Type-A Suspension System

Type-A suspensions are developed [6].

2.5 Summary of the Chapter

Underground Seismic Noise

3.1 Seismic Noise

3.1.1 Overview

...

3.1.2 Microseisms

Microseisms which power spectrum has peaks in 50–200 mHz are excitated by oceanic waves. These seismic waves can be categolized by the generating mechanism of these [7].

The primary ocean microseisms are generated only in shallow waters in coastal regions. In this regions, the water wave enery can be converted directly into seismic energy either through vertical water pressure variations, or by the impacts of surf on the shores. There are correlation between this microseismic peak and the swell at the beaches was known starting from the data sets studied by [8].

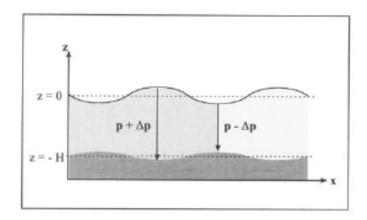
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The secondary ocean microseisms could be explained by the superposition of ocean waves of equal period traveling in opposite directions. Therefore, generating standing gravity waves of half the period [9].

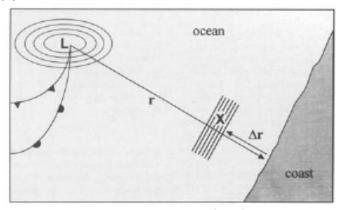
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The RMS amplitude spectral of both type of the microseisms are strongly depends on the low pressure on the ocean.

...



(a) Generating mechanism of the primary microseisms.



(b) Generating mechanism of the secondary microseisms.

Figure 3.1: Generating mechanism of the microsisms. (a) describes the mechanism of the primary microseisms. (b) describes the mechanism of the secondary microseisms.

3.1.3 Earthquakes

(Write how earthquakes disturb the large scale interferometer.)

Mechanism

遠方での大きな地震は脈動帯域以下の低周波地面振動を励起し、ロックロスの原因になる。

Early Earthquake Alert

Seismon をつかって到来時間を予測し、この低周波地面振動の RMS を抑えるための特別なフィルターに切り替えて、ロックロスをへらす工夫を行っている。しかし、このフィルターは脈動がうるさいときは再びロックロスの問題を抱えてしまう。

3.1.4 Earth Tides

3.2 Long-term Study of the seismic environment at KAGRA

3.2.1 Overview

The seismic waves are excited on the source and propagate along the surface of the Earth with amplitude decreasing with depth [10]. However, especially microseims whose peak is around 0.1 Hz are not attenuated adequately compared with higher frequencies above 1 Hz, because the wavelength is comparable to or longer than the depth. Amount of these atenuation factor is must be explaing by a complicated phenomenon, which depends on either the local geology or location of the exciting sources.

In this section, seasonal change of the RMS amplitude of the seismic noise is described.

3.2.2 Experimental Arrangement

Seismic motion is measured by a seismometer installed on the second floor of the X-end area. This area is placed 200 m underground from the surface of the mountain. Comparison to corner area, human activity in the end area is less because the corner area has parking lots. Comparison to the Y-end area, there is no entrance connected to other mines. Therefore, the X-end area is relatively quiet in the KAGRA mine, regarding the seismic noise induced by human activity.

In this study, Trillium 120-QA which is known as three-component, very broadband, and low-noise seismometer, was used. These three outputs are proportional to the ground velocity of two horizontal and one vertical, respectively. The feature of the low-noise can resolve Peterson's new low-noise model (NLNM) and new high-noise model (NHNM) [11].



Figure 3.2: Trillium 120-QA installed on the second floor at X-end area, which is coverd by black thermal insulation cover

As shown in fig 3.2, the seismometer is housed in the black thermal insulation cover according to the installation manual [12]. Thermal insulation protects two broad categories of thermal couplings that can cause unwanted noise [12]. First is the direct coupling to the sensitivity. This coupling typically increases the noise

of the vertical channel as a periodic diurnal variation caused by the day-to-night temperature cycle, because the springs that suspended the inertial masses are temperature sensitive. The second is the coupling to tilt from the thermal fluctuation. Tilt converts the vertical acceleration of gravity into horizontal acceleration. This thermally induced tilt noise on the horizontal will be larger than the direct thermal coupling on the vertical channel. To be low sensitivity to both tilt and temperature, this model has a function to center the inertial mass after the initial installation.

The signals of the seismometer is recorded through the data aquisition system developed by LIGO [13]. The analog signal is converted to digital signal by the 16 bit analog-to-digital converters (ADC) with 16384 Hz sampling. In addition, the signal of the seismoemter is amplified with 30 db so that the ADC noise does not mask this signal.

...

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3.2.3 Data

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定常な時系列データを1年間のデータのから選んだ。
3.4.
...
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Figure 3.3: Available data from June 00 2018 to Jun 00 2019

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3.2. LONG-TERM STUDY OF THE SEISMIC ENVIRONMENT AT KAGRA 15

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... hoge ...

3.2.4 Results

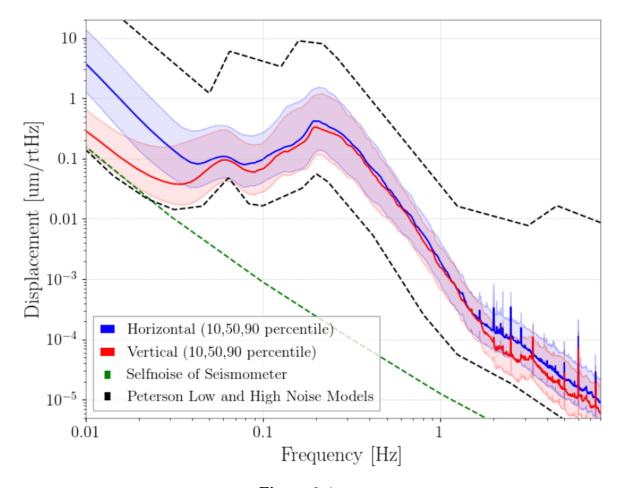


Figure 3.4

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3.3 Differential Motion Reduction

3.3.1 Introduction

The motion of two mirrors in the cavity have two modes. One is differential motion, which is the length change of that. Another one is common motion, which is the motion of the center of the cavity. In terms of the length control, it is important that the RMS amplitude of differential motion is as small as possible. Actuarlly, the amplitude of these two motions are the same each other when the mirrors moves with no coherence. However, when a coherence exists, the common motion tends to be larger than the differential one.

As discussed in this section, the coherence depends on both, the arm length and the wavelength of seismic waves. For example, if the arm length is much more smaller than the wavelength, the mirrors move together. This means that the common motion is greater than the differential motion.

The ratio of the amplitudes of the differential motion over common motion is newly defined as Common and Differential Motion Ratio (CDMR). It is usefull to know how the ground reducts the differential motion or increase the common motion.

3.3.2 Differential Motion Reduction

Differential Motion and Common Motion

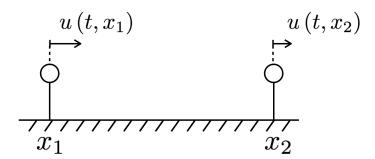


Figure 3.5: The displacements of the two points which are sparated L in X axis.

Motions of the two points can be represented as the differential motion and the common motion. Displacement of both differential motion and common motion of the two points shown in Figure (??) are defined as

$$u_{\text{diff}} \equiv \frac{u_1 - u_2}{\sqrt{2}}, \ u_{\text{comm}} \equiv \frac{u_1 + u_2}{\sqrt{2}}$$
 (3.1)

where $u_1(x,t)$ and $u_2(x,t)$ are the displacement of each points. These two motions defined in Eq.(3.1) are normalized by $\sqrt{2}$ due to conserve the total power.

Common and Differential Motion Ratio (CDMR)

CDMR is defined as the powers of common motion over the differential motion as bellow,

$$CDMR \equiv \sqrt{\frac{Common Motion}{Differential Motion}} = \sqrt{\frac{P_{comm}(\omega)}{P_{diff}(\omega)}}$$
(3.2)

where P_{comm} , P_{diff} are the power spectral densities (PSDs) of the differential motion and common motion, respectively. Each PSDs are converted from the autocorrelation function of these by the Wiener-Khinchin theorem.

First, autocorrelation function C_{diff} of the differential motion is given by its definition in Eq.(3.1)

$$C_{\text{diff}}(\tau) = \frac{1}{2} \left\langle \left[x_1(t) - x_2(t) \right] \left[x_1(t+\tau) - x_2(t+\tau) \right] \right\rangle$$
 (3.3)

$$= \frac{1}{2} \left[C_{11}(\tau) - C_{12}(\tau) - C_{21}(\tau) + C_{22}(\tau) \right], \tag{3.4}$$

,where C_{ij} are the autocorrelation functions of each point and defined as $C_{ij} \equiv \langle x_i(t)x_j(t+\tau)\rangle$, (i=1,2,j=1,2). Therefore, the power spectrum density of differential motion $P_{\text{diff}}(\omega)$ can be computed as

$$P_{\text{diff}}(\omega) = \frac{1}{2} \left[P_1(\omega) + P_2(\omega) - P_{12}(\omega) - P_{12}^*(\omega) \right]$$
 (3.5)

$$= \frac{1}{2} \left[P_1 + P_2 - \operatorname{Re}\left[\gamma\right] \times 2\sqrt{P_1 P_2} \right] \tag{3.6}$$

where $P_1(\omega)$, $P_2(\omega)$ are the power spectrum densities of each points, and $P_{12}(\omega)$ are the cross spectrum between two point. The parameter γ is the complex coherence between them defined below,

$$\gamma \equiv \frac{P_{12}}{\sqrt{P_1 P_2}}.\tag{3.7}$$

Here, assuming that seismic wave propagating each points does not decay, which means $P_1 = P_2 \equiv P$, one can compute the $P_{\text{diff}}(\omega)$ as

$$P_{\text{diff}}(\omega) = P(1 - \text{Re}\left[\gamma\right]). \tag{3.8}$$

Therefore, the PSDs of the common motion can be calculated as

$$P_{\text{comm}}(\omega) = P(1 + \text{Re}\left[\gamma\right]). \tag{3.9}$$

Finaly, CDMR defined Eq.(3.2) in case the seismic wave does not decay is represented as

$$CDMR = \sqrt{\frac{1 + \text{Re}\left[\gamma\right]}{1 - \text{Re}\left[\gamma\right]}}.$$
(3.10)

Eq.(3.10) indicate that CDMR can be expressed by only the coherence γ between of two points. For example, CDMR tends to be larger when γ close to 1. This means that the differential motion is more less than the common motion because the two points move together in the same direction.

- 3.4 Measurement of Differential Motion Reduction
- 3.4.1 Reduction in X-arm Scale
- 3.4.2 Reduction in Other Short Scale
- 3.5 Summary of the Chapter

Geophysics Interferometer (GIF)

4.1 Overview

- 4.1.1 Laser Strainmeter gor Geophysics
- 4.1.2 Motivation in GW detectors

4.2 Working Principle

4.2.1 Asymmetric Michelson Interferometer

$$\phi = 2\pi \frac{2(l_x - l_y)}{\lambda} \sim 4\pi \frac{l_x}{\lambda} \tag{4.1}$$

$$|d\phi| = 4\pi \frac{l_x}{\lambda} \left(\left| \frac{d\lambda}{\lambda} \right| + \left| \frac{dl_x}{l_x} \right| \right) \tag{4.2}$$

4.2.2 Response to the seismic strain

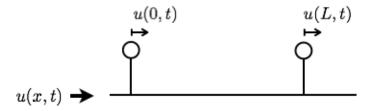


Figure 4.1: The displacements of the two points which are sparated L in X axis.

The response of the strainmeter to seismic waves have characteristics of the low pass filter. To calculate this response, it is assumed that the plane seismic waves which displacement u(x,t) is represented as $u(x,t) = u_0 e^{i(\omega t - kx)}$ with angular frequency of ω and wave number of k, propagate along with the direction of the

base-line of the strain meter. The length fluctuation between two mirrors sparated with L can be expressed as

$$\Delta L(t) \equiv u(0,t) - u(L,t) \tag{4.3}$$

$$= u(0,t) - u(0,t-\tau), \tag{4.4}$$

where $\tau = L/v$ is the time delay. The transfer function from the displacement to the length fluctuation is

$$H_{\rm disp}(s) \equiv \frac{\Delta L(s)}{u(s)} = 1 - \exp(-\tau s) \tag{4.5}$$

Because the strain amplitude $\epsilon(x,t)$ is defined as $\epsilon(x,t) \equiv \frac{du}{dx}$, the strain

$$\epsilon(x,t) \equiv \frac{du}{dx} = \frac{du}{dt}\frac{dt}{dx}$$
 (4.6)

$$= u(x,t)'\frac{1}{v} \tag{4.7}$$

Therefore, the response of the strainment to the seismic strain is given

$$H_{\text{strain}}(s) \equiv \frac{\Delta L(s)}{\epsilon(s)} = \frac{\Delta L(s)}{\frac{s}{v}u(s)} = (1 - \exp(-\tau s))\frac{v}{s}$$
(4.8)

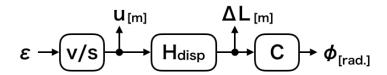


Figure 4.2

4.2.3 Signal Detection Scheme

Quadrature Phase Detection

4.2.4 Noise

どういうノイズが原理的に存在するか述べる。空気ゆらぎ、周波数雑音を述べる。

4.3 Optics

どうやって実際の干渉計を構築しているか述べる。

4.3.1 Mode Matching Optics

どういうモードマッチをして干渉計として光を干渉させているか述べる。

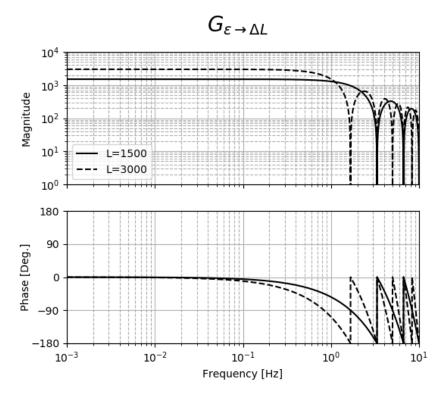


Figure 4.3

4.3.2 Frequency Stabilized Laser

どういう制御をして周波数安定をしているか述べる。

4.3.3 Core Optics

Beam Splitter

どういうミラーを使っているか述べる。

Corner Cube

どういうミラーを使っているか述べる。大きさとか表面の精度とか。

4.4 Data Aquisition System

4.4.1 ...

4.5 Summary of the Chapter

本章で述べたパラメータを表にまとめる。

Arm Length Compensation System for Global Seismic Control

5.1	Basics in Vibration Isolation and Control Tech-
	nique

5.1.1 Passive Vibration Isolation

Single Pendulum

Multi Pendulum

- 5.1.2 Active Vibration Isolation
- 5.1.3 Sensor Belnding Control Technique
- 5.1.4 2 Types Feedforward Control Techniques

Feedforward at Feedback Point

Feedforward at Error Point

5.1.5 Toward the Global Seismic Control

Overview

Suspension Point Interferometer

- 5.2 Difficulties in the Global Seismic Control
- 5.2.1 Overview
- 5.2.2 Actuator Range Limit
- 5.2.3 ...
- 5.2.4 ...
- 5.3 Arm Length Compensation Using Geophysics Interferometer
- 5.3.1 Concept
- 5.3.2 Geophysics Interferometer for Sensing the Arm Length

Demonstration of Arm Length Compensation Control

- 6.1 Experimental Arrangement
- 6.1.1 ...
- 6.2 Results
- 6.2.1 ...
- 6.3 Discussion and Summary of the Chapter
- 6.3.1 Discussion
- 6.3.2 Summary

Conculusion and Future Directions

- 7.1 Conclusion
- 7.2 Future Directions

Appendix A

Theory of Seismic Waves

A.1 Body Wave

等方弾性体中では変位 u は以下の波動方程式に従う。

$$\rho \ddot{\boldsymbol{u}} = (\lambda + 2\mu)\nabla(\nabla \cdot \boldsymbol{u}) - \mu\nabla \times (\nabla \times \boldsymbol{u})$$
(A.1)

ここで ρ は媒質の密度、 λ , μ はラメ定数である。

この波動方程式は縦波であるP波と横波であるS波について解くことができる。 そのためにまず Helmholtz decomposition をつかって変位 u を発散成分 $u_{
m div}$ と回転 成分 $u_{\rm rot}$ で表す。つまり、

$$\mathbf{u}_{\text{div}} = \nabla \phi$$
 (A.2)

$$\mathbf{u}_{\mathrm{rot}} = \nabla \times \psi$$
 (A.3)

となるスカラーポテンシャル ϕ とベクトルポテンシャル ψ が存在し、変位uは

$$\boldsymbol{u} = \nabla \phi + \nabla \times \psi \tag{A.4}$$

と表すことができる。式 (A.1) に式 (A.4) を代入し、かつベクトル解析の公式、 $\nabla \times$ $(\nabla \times \mathbf{A}) = \nabla (\nabla \cdot \mathbf{A}) - \nabla^2 \mathbf{A}$ を使うと、

$$\ddot{\phi} = v_L^2 \nabla^2 \phi \tag{A.5}$$

$$\ddot{\phi} = v_L^2 \nabla^2 \phi \tag{A.5}$$

$$\ddot{\psi} = v_T^2 \nabla^2 \psi \tag{A.6}$$

のように2つの波動方程式を得る。ここで v_L, v_T は、

$$v_L = \sqrt{\frac{\lambda + 2\mu}{\rho}}, v_T = \sqrt{\frac{\mu}{\rho}}$$
 (A.7)

である。

 v_L, v_T らはそれぞれ縦波と横波の位相速度を表しているが、これを示す。まずス カラーポテンシャルとベクトルポテンシャルは式 (A.5)、式 (A.6) の波動方程式に従 うので、これらの一般解は

$$\phi = \phi_0(\omega t - \boldsymbol{k} \cdot \boldsymbol{x}) \tag{A.8}$$

$$\boldsymbol{\psi} = \boldsymbol{\psi}_0(\omega t - \boldsymbol{k} \cdot \boldsymbol{x}) \tag{A.9}$$

で表すことができる。ここで ω , k は各周波数と波数ベクトルである。発散成分である $u_{\rm div}$ は式 (A.2) に式 (A.8) を代入して、

$$\boldsymbol{u}_{\text{div}} = \nabla \phi_0(\omega t - \boldsymbol{k} \cdot \boldsymbol{x}) = -\boldsymbol{k}\phi \tag{A.10}$$

となるので、変位の向きは波数ベクトルと平行である。つまり縦波であり P 波に相当する。一方で回転成分である u_{rot} は式 (A.3) に式 (A.9) を代入して、

$$\mathbf{u}_{\text{rot}} = \nabla \times \mathbf{\psi}_{\mathbf{0}}(\omega t - \mathbf{k} \cdot \mathbf{x}) = -\mathbf{k} \times \mathbf{\psi}$$
(A.11)

となるので、変位の向きは波数ベクトルと直行している。つまり横波でありS波に相当する。したがって v_L, v_T はそれぞれ縦波と横波の位相速度を示していることがわかった。また λ と μ は正の定数なので、

$$v_L > v_T \tag{A.12}$$

となって、縦波のほうが横波よりも速いことがわかる。

A.2 Rayleigh 波

(レイリー波の導出。)

A.3 Depth Dependence

(レイリー波の振幅が深さに依存していることを述べる。)

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