



Figure 1.6 Plots of polynomials having various orders M , shown as red curves, fitted to the data set shown in Figure 1.4 by minimizing the error function (1.2).

passes exactly through each data point and $E(\mathbf{w}^*) = 0$. However, the fitted curve oscillates wildly and gives a very poor representation of the function $\sin(2\pi x)$. This latter behaviour is known as *over-fitting*.

Our goal is to achieve good generalization by making accurate predictions for new data. We can obtain some quantitative insight into the dependence of the generalization performance on M by considering a separate set of data known as a *test set*, comprising 100 data points generated using the same procedure as used to generate the training set points. For each value of M , we can evaluate the residual value of $E(\mathbf{w}^*)$ given by (1.2) for the training data, and we can also evaluate $E(\mathbf{w}^*)$ for the test data set. Instead of evaluating the error function $E(\mathbf{w})$, it is sometimes more convenient to use the root-mean-square (RMS) error defined by

$$E_{\text{RMS}} = \sqrt{\frac{1}{N} \sum_{n=1}^N \{y(x_n, \mathbf{w}) - t_n\}^2} \quad (1.3)$$

in which the division by N allows us to compare different sizes of data sets on an equal footing, and the square root ensures that E_{RMS} is measured on the same scale (and in the same units) as the target variable t . Graphs of the training-set and test-set