Model

Objective

**Dataset** 

Issues

## Alternative Idea 1

Brief other

url

Here is some text<sup>1</sup>

Idea:

$$\begin{split} \mathbf{v} &= \mathrm{MLP}(\mathbf{z_e}) & \text{(Reaction embeddings to flux vector)} \\ &\mathrm{fitness} = \mathbf{w}^\top \mathbf{v} & \text{(Predicted fitness from flux vector)} \\ &\mathcal{L}_{\mathrm{null}} = \| \mathbf{S} \mathbf{v} \|_2^2 & \text{(Null-space constraint loss)} \\ &\mathcal{L}_{\mathrm{pFBA}} = \| \mathbf{v} \|_1 & \text{(Parsimonious flux balance objective)} \\ &\mathcal{L}_{\mathrm{fitness}} = (\mathbf{w}^\top \mathbf{v} - \mathrm{fitness})^2 & \text{(Fitness constraint loss)} \\ &\mathcal{L}_{\mathrm{total}} = \mathcal{L}_{\mathrm{pFBA}} + \lambda_{\mathrm{null}} \mathcal{L}_{\mathrm{null}} + \lambda_{\mathrm{fitness}} \mathcal{L}_{\mathrm{fitness}} & \text{(Total PINN loss)} \end{split}$$

- $\mathbf{z_e}$  is the reaction embedding vector mapped via MLP to the flux vector  $\mathbf{v}.$
- w is a binary vector indicating the biomass pseudoreaction.
- fitness is the experimentally measured fitness (growth ratio mutant/wildtype).
- S is the stoichiometric matrix enforcing the null-space constraint.

## **Brief of Other Attempts**

If you think that these directions are interesting I can will expand on them. For brevity I just highlight my findings.

## References

1. Corso, G., Stark, H., Jegelka, S., Jaakkola, T. & Barzilay, R. Graph neural networks. *Nat Rev Methods Primers* 4, 1–13 (2024).