Block diagram manipulation 4.2.2

There are occasions when there is interaction between the control loops and, for the purpose of analysis, it becomes necessary to re-arrange the block diagram configuration. This can be undertaken using Block Diagram Transformation Theorems.

Table 4.1 Block Diagram Transformation Theorems

Transformation	Equation	Block diagram	Equivalent block diagram
Combining blocks in cascade	$Y = (G_1 G_2)X$	$X \longrightarrow G_1 \longrightarrow G_2 \longrightarrow $	$X \longrightarrow G_1G_2 \longrightarrow Y$
2. Combining blocks in parallel; or eliminating a forward loop	$Y = G_1 X \pm G_2 X$	X G_1 G_2 Y G_2	$X \longrightarrow G_1 \pm G_2 \longrightarrow Y$
3. Removing a block from a forward path	$Y = G_1 X \pm G_2 X$		G_2 G_2 G_2 G_2 G_2 G_2 G_2
4. Eliminating a feedback loop	$Y=G_1(X\pm G_2Y)$	$X \stackrel{+}{\Longrightarrow} G_1$	$X \longrightarrow G_1 \longrightarrow Y$ $1 \pm G_1 G_2 \longrightarrow Y$
5. Removing a block from a feedback loop	$Y = G_1(X \pm G_2Y)$	G ₂	$\begin{array}{c c} X & \hline \\ \hline$
6. Rearranging summing points	$Z = W \pm X \pm Y$	W → ± Z → ± Z	<i>W</i> → ± <i>X</i> → ± <i>Z</i>
7. Moving a summing point ahead of a block	$Z = GX \pm Y$	$X \longrightarrow G \longrightarrow X \longrightarrow $	$X + \bigcirc G$ Y Y
8. Moving a summing point beyond a block	$Z=G(X\pm Y)$	$\begin{array}{c c} X + & & & \\ X + & & & \\ X + & & & \\ Y & & & \\ \end{array}$	$\begin{array}{c c} X & G & \downarrow \\ Y & G & \downarrow \\ \end{array}$
9. Moving a take-off point ahead of a block	Y=GX	$X \longrightarrow G$	$X \longrightarrow G \longrightarrow Y$
10. Moving a take-off point beyond a block	Y=GX	$X \longrightarrow G \longrightarrow Y$	$X \longrightarrow G \longrightarrow Y$ $X \longrightarrow \frac{1}{G} \longrightarrow Y$