

Agenda.

Trees basics → use cases of trees

Terminologies:

Traversals

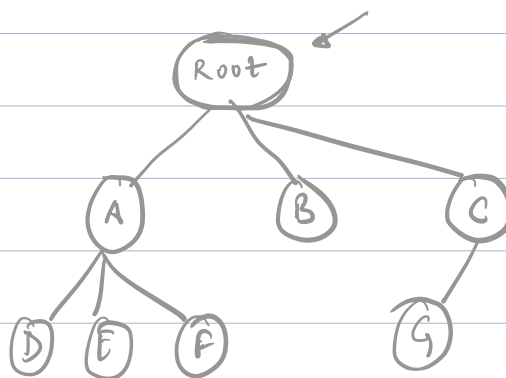
Height of tree

Size of tree.



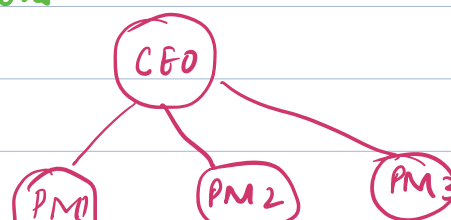
DS → Linear / Sequential.

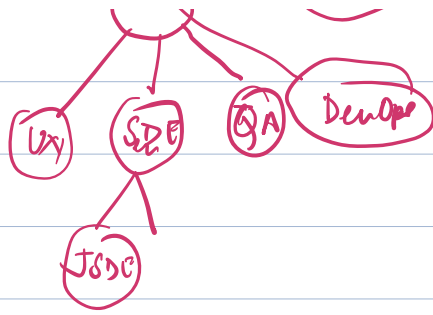
Trees → Hierarchical DS



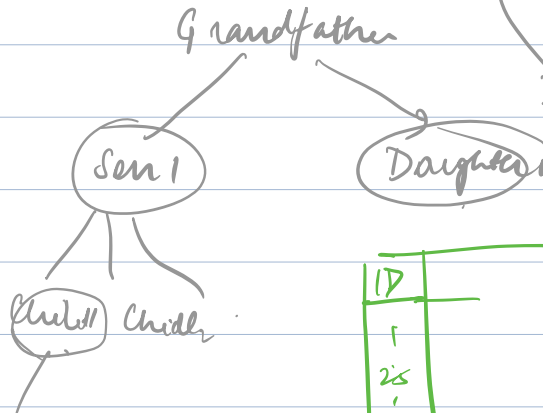
Use cases:

① Organisations



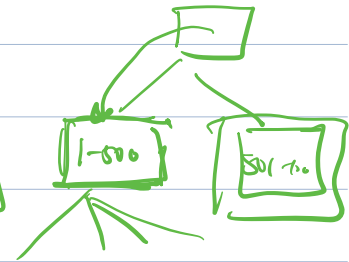


② Family Tree

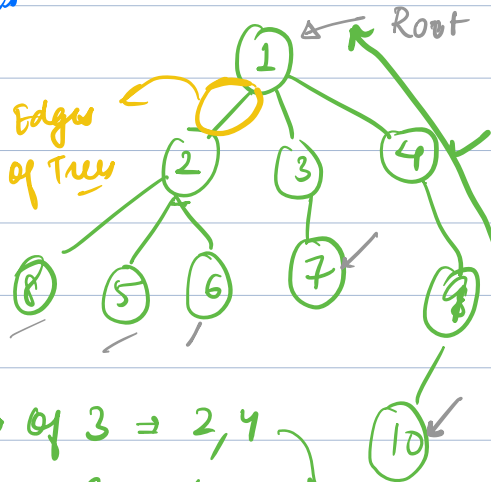


ID
1
2, 5
1000

③ Trees



Terminologies



Parent node of 7? \downarrow
3

Children of 2 \downarrow
8, 5, 6

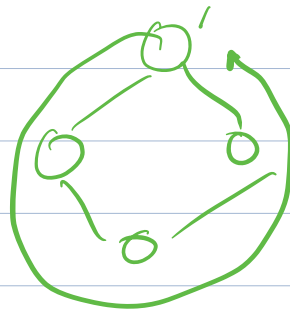
Siblings \rightarrow of 3 \Rightarrow 2, 4
ancestors \rightarrow of 9 \Rightarrow 4, 1
Successor of 4 \Rightarrow 9, 10

Leaf Nodes \downarrow
8, 5, 6, 7, 10

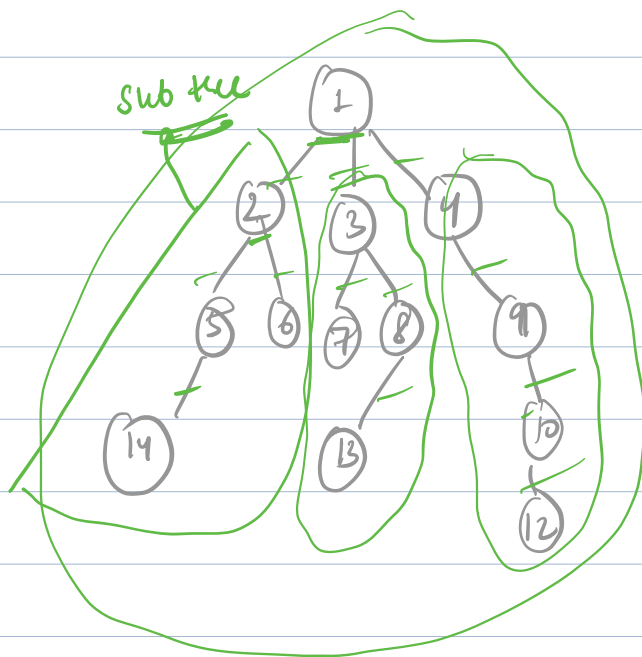
Node is combination of data, edges/connections to the children node.

h...o

- ④ 1 node can have how many parents $\Rightarrow 1$
- ⑤ No cycles



Reaching back same node without repeating any node



count of nodes = 13
Every node has 1 parent except root.

Total edges = 12

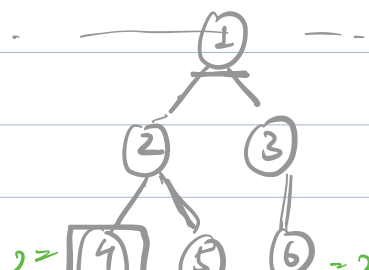
Sub trees are n nodes $\Rightarrow n-1$ edges
the reason we can seamlessly apply recursion to trees problems.

Properties of Trees:

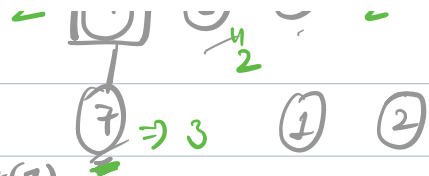
- ① Height of a node:



Distance from the farthest leaf node



in the subtree

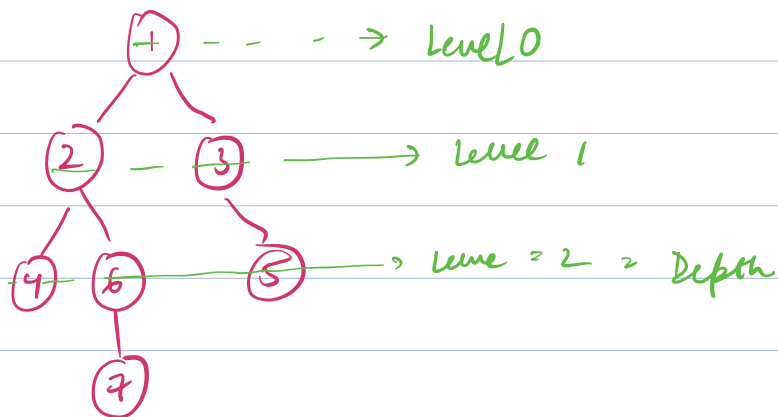


$$\begin{aligned} \text{height}(1) &= \text{height}(\text{tree}) \\ &= 3 \end{aligned}$$

② Depth of a node:

Distance from the root node

③ Levels



Binary Trees

↳ Every node can have a max of 2 children

Ternary Trees \Rightarrow At max(3) children

K-ary Trees \Rightarrow At max(K) children

①

①
②

Left child

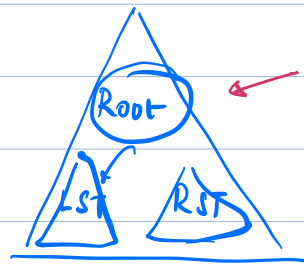
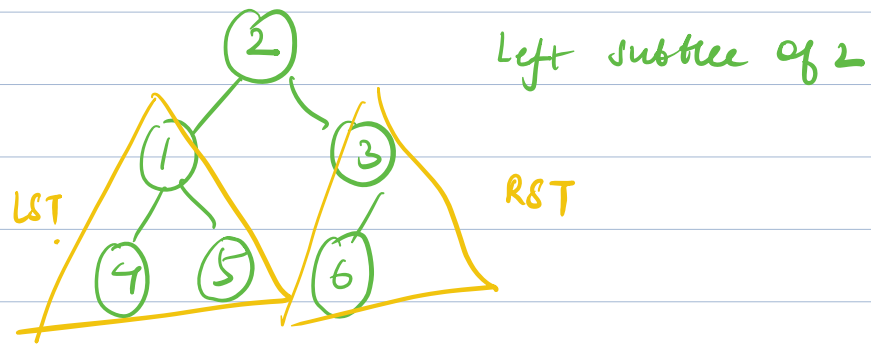
①
② ③

Right child

①
②
③

Left subtree

Right subtree



Implementation (Binary Trees)

class TreeNode:

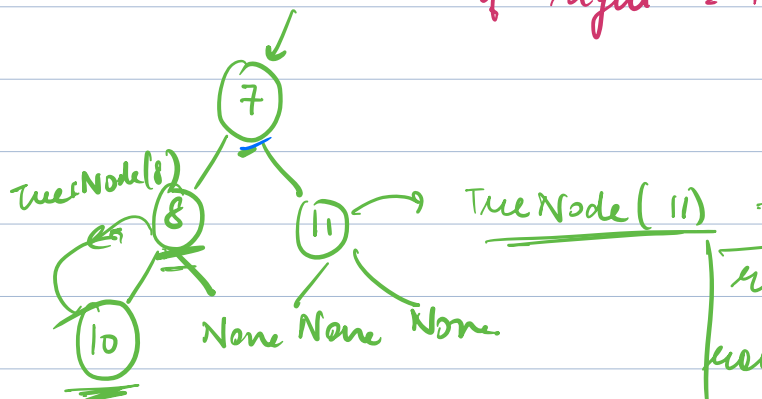
def __init__(self, data):

self.data = data.

self.left = None \Rightarrow

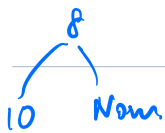
self.right = None. \Rightarrow

References
to the root
node of
LST, RST



root.data = 7
root.left = TreeNode(8)
root.right = TreeNode(11)

x = TreeNode(10)



$y = \text{TreeNode}(8)$

$y.\text{left} = x$

$\text{root} = \text{TreeNode}(7)$

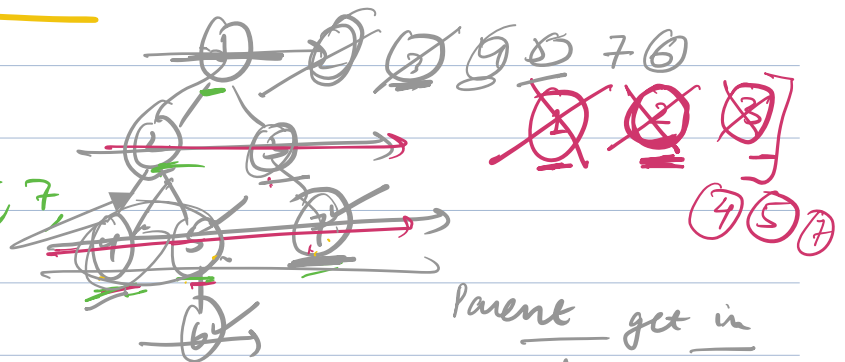
$\text{root}.\text{left} = y$

$\text{root}.\text{right} = \text{TreeNode}(11)$

Level Order Traversal

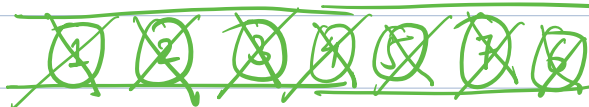
LOT order \rightarrow

1, 2, 3, 4, 5, 7, 6



Parent get in

first
children get in
first



1

```
def printLevelOrder (TreeNode root):
```

```
    qu = collections.deque([root])
```

```
    while not qu.empty():
```

```
        x = qu.popleft()
```

```
        if x.left:
```

```
            qu.append(x.left)
```

```
        if x.right:
```

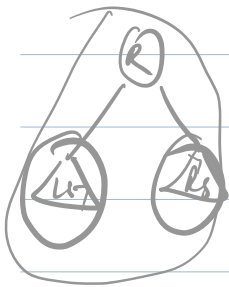
```
            qu.append(x.right)
```

```
        print(x.data)
```

~~1 2 3 4 5 6 7 8~~

✓ 1 2 3 4 5 7 6

Q Given the root node of a ^{Binary} tree.
Find the total number of nodes in the tree?



```
def size ( root: ):
```

Assumption: This fn returns me

size of tree rooted at root node

```
if root == None:  ✓ BC  
    return 0
```

```
return 1 + size ( root.left ) + size ( root.right )
```

```
def size ( root ):
```

BC \Rightarrow if a leaf Node

```
if !root.left and !root.right:  
    return 1
```

\Rightarrow cnt = 1

if root.left:

cnt += size (root.left) (2)

if root.right

cnt += size (root.right)

return cnt.

$$1+2+1 = \boxed{4}$$

Break - 10 min.

Traversal :

- ↳ Preorder Traversal \Rightarrow Root Left Right
- ↳ Inorder Traversal
- ↳ Post Order Traversal



Root Left Right

① ② 4 7 5 8 3 6

def preorder(root):

 print (root.data)

 if root.left :

 preorder (root.left)

 if root.right :

 preorder (root.right)

def preorder (root)

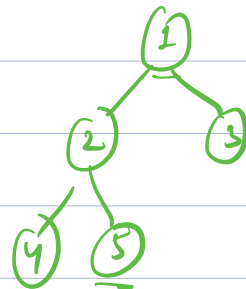
1 if root == None:

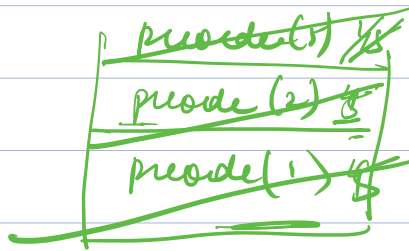
2 return .

3 print (root.data)

4 preorder (root.left)

5 preorder (root.right)

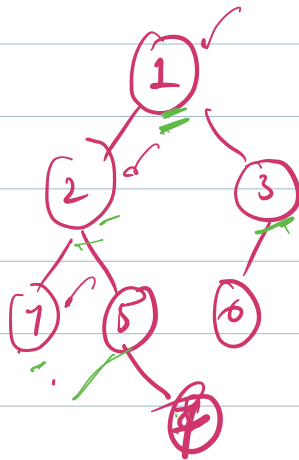




① ② ④ ⑤

Post Order

Left Right Root



4 7 5 2 6 3 ①

postorder (left
postorder (right
print root

Inorder

Left Root Right



4 2 5 7 6 3

inorder (left
print root
inorder (right

h-w find height of tree

def height (root) :
pass