

## STACKS

stack of plates

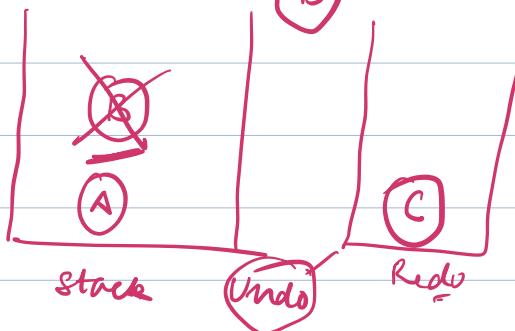
stack of chairs



\* Recursion.

\* Back and next buttons in web browser.

Open container



\* Undo and Redo functionalities in Doc

\* Parathesis Balancing.

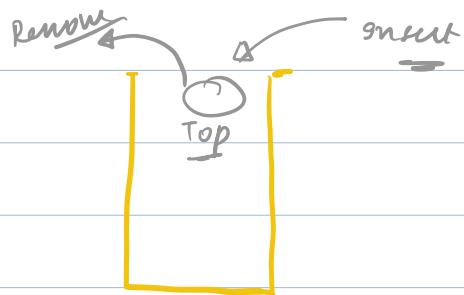
\* Expression Evaluation.

Any DS  $\rightarrow$  store Data

$\rightarrow$  insertion

$\rightarrow$  Deletion

$\rightarrow$  Access some Data



Lists  $\Rightarrow$  Dynamic Arrays

Lists are  
an alternative  
of Stack DS  
in python.

append  $\rightarrow$  insert in End  
 $O(1)$

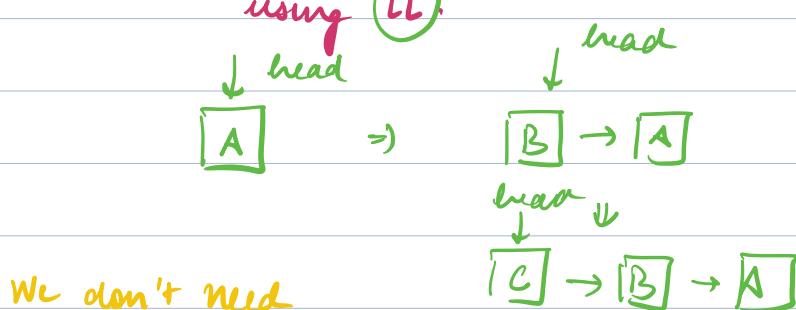
[-1]  $\rightarrow O(1)$

$l = [1, 2, 3]$        $l[-1] \rightarrow 3$        $l[-1] \leftarrow 3$        $\text{ans}[-1]$        $\text{pop}(). \rightarrow O(1)$

In LL.: Can you insert element at  
 the end of LL in  $O(1)$ ?  
 → In the beginning of list

\* Stacks can also be implemented

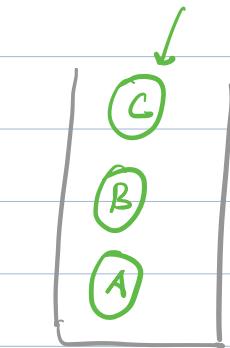
using LL.



We don't need

random access of data

$\text{head}. \text{val.}$



⇒ value of topmost

Stack ⇒ push, pop, top

append pop [-1]

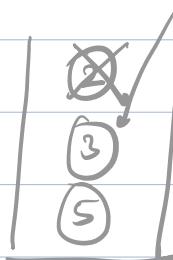
push (5)

push (3)

push (2)

pop().

top() → (3)



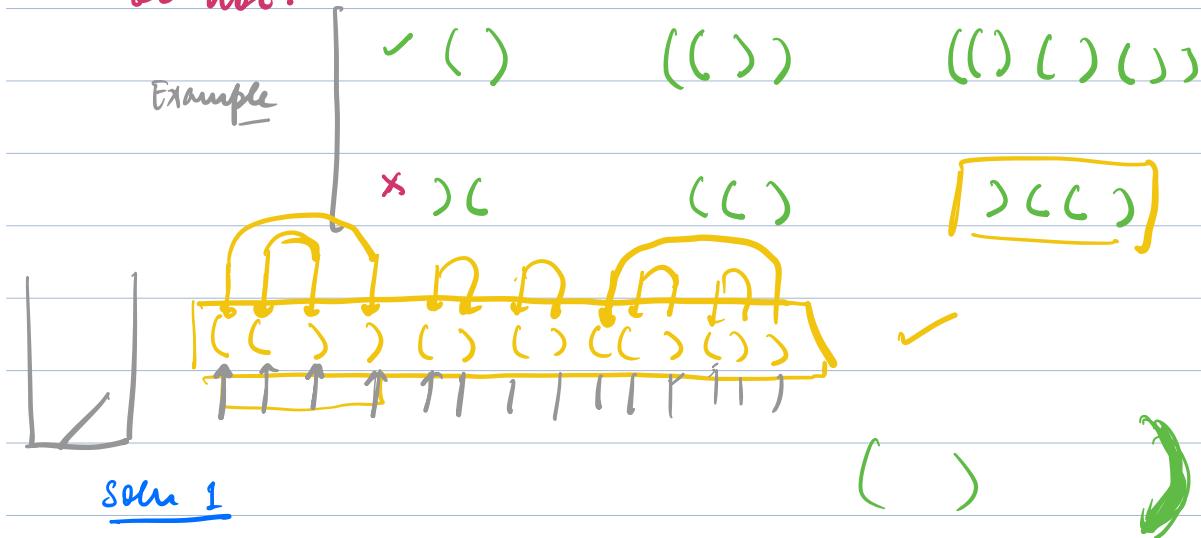
LIFO

Last in

First out

Paranthesis Balancing

you are given a sequence of brackets '()' '  
you have to tell if the sequence is balanced  
or not.



Algo:

- if opening → push '(' in stack
- if closing → ① if st. empty → False  
② pop out the '(' in the stack
- in the end → stack should be empty

```
def isBalanced(s):
    st = []
    for x in s:
        if x == '(':
            st.append('(')
        else:
            if len(st) == 0:
                return False
            else:
```

Optimized  
 $O(1)$

```
    else:
        if st[-1] == ')':
            st.pop()
        else:
            return False
    else:
```

st.pop()  
return  $\text{len(st)} = -1$

cnt = -1  
return cnt = -1

( ) ) (   
↑↑↑↑  
cnt = 0  
false

Instead of just '(' and ')'

Now we have [ ] () {} → Tell if

the string is balanced or not.

[ { } ( ) ] ) → Not balanced.

cnt 1

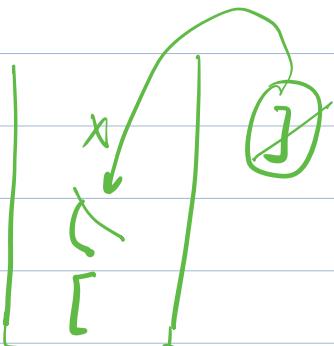
0

cnt 2

0

cnt 3

0



Failure because order is important.

'[ ' ] '  
( ) [ ] { }  
↑ ↑ ↑ ↓  
( ) [ ] { }  
↑ ↑ ↑ ↓

[ ( { ) ( ? ) ]

↑↑↑↑ X

{ } ( ) [ ]

st = []

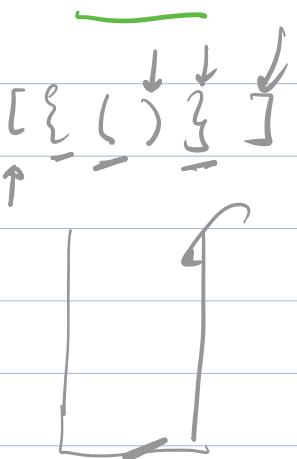
for x in s:

if x == '(' or x == '{' or x == '['

st.push(x)

else:

if x == ')' and st[-1] == '['



st.pop()

elif  $x == \{$  and  $st[-1] == \}$

st.pop()

elif  $x == )$  and  $st[-1] == ($

st.pop()

else:

return False

return len(st) == 0

Q You are given a sequence of parentheses  $\Rightarrow$  ( )

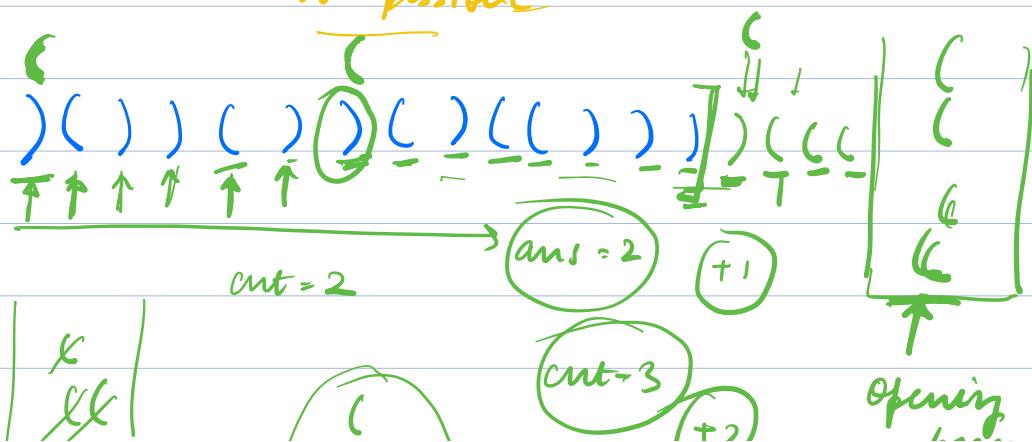
You can reverse any parentheses. How many minimum parentheses would you have to reverse to balance the string. Return -1 if not possible.

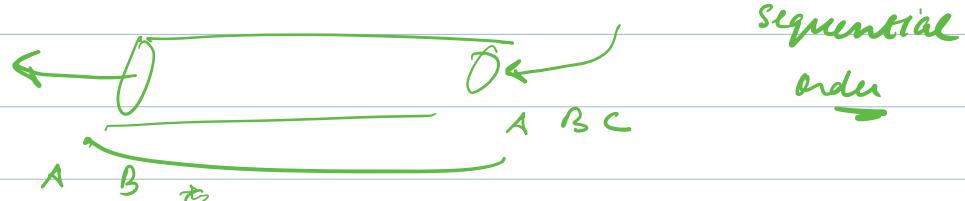
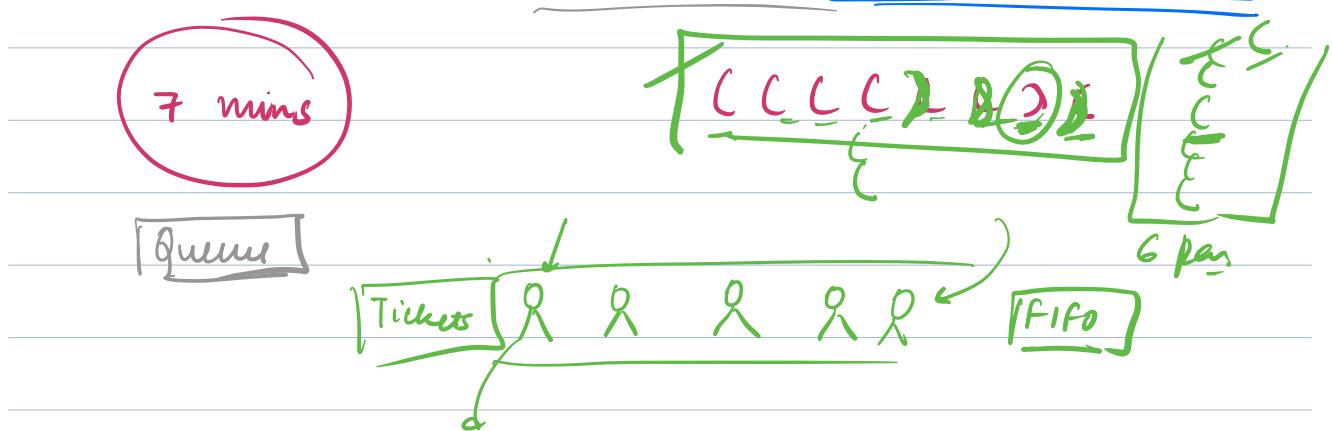
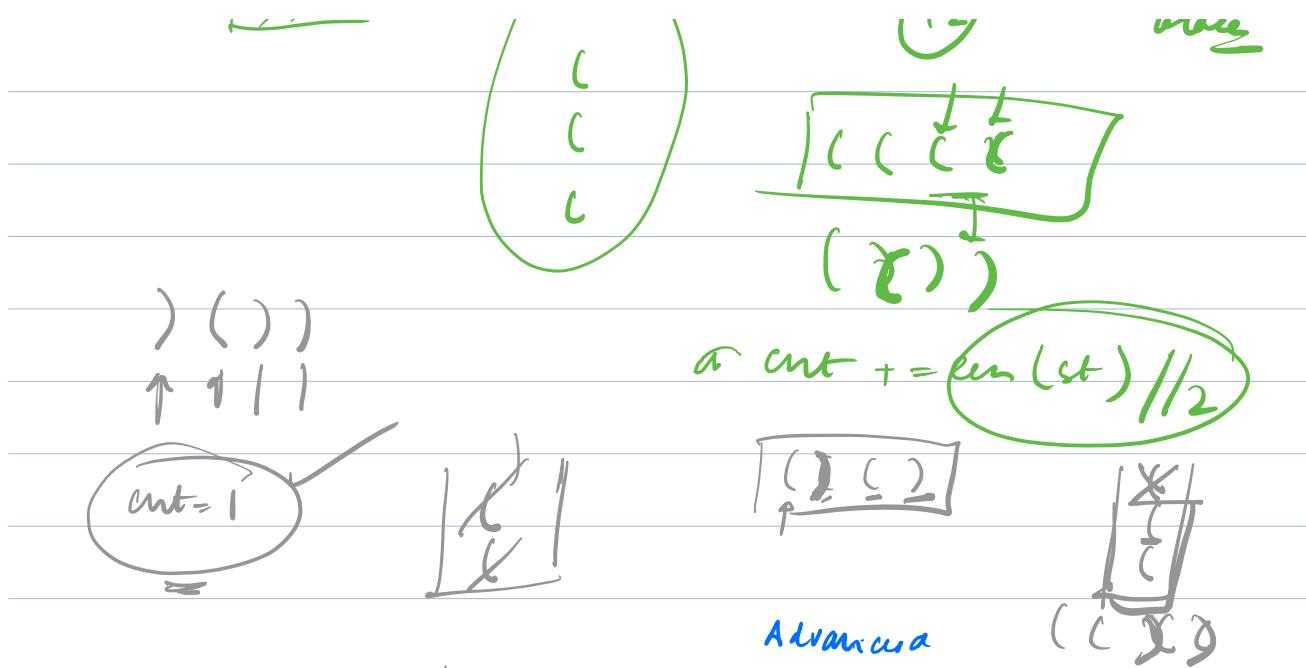
$$")(" \Rightarrow 2 \checkmark$$

$$((((( )))))( )() \Rightarrow 2$$

If length is odd  $\Rightarrow$

not possible

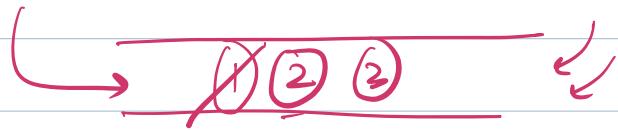




**push()**  
**pop()**  
**front()**

**push(1)**  
**push(2)**  
**push(3)**  
**pop()**  
**front() - 1**

**Application**  
**MQ**



import collections

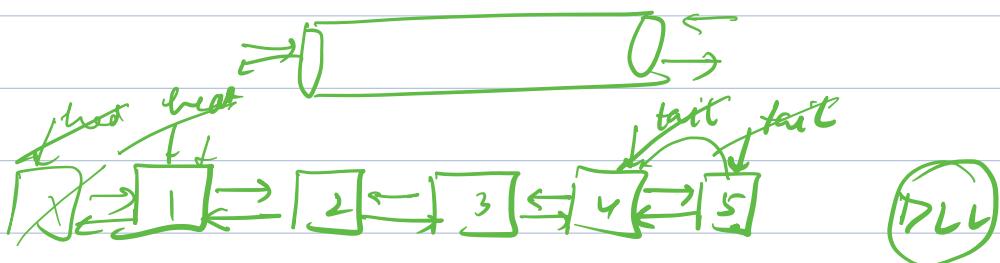
collections.deque.

1, 2, 3

q = collections.deque([1, 2, 3])

q.append(4) → L append left() → L

q.pop() → R pop() → R



class Node:

def:

self.next

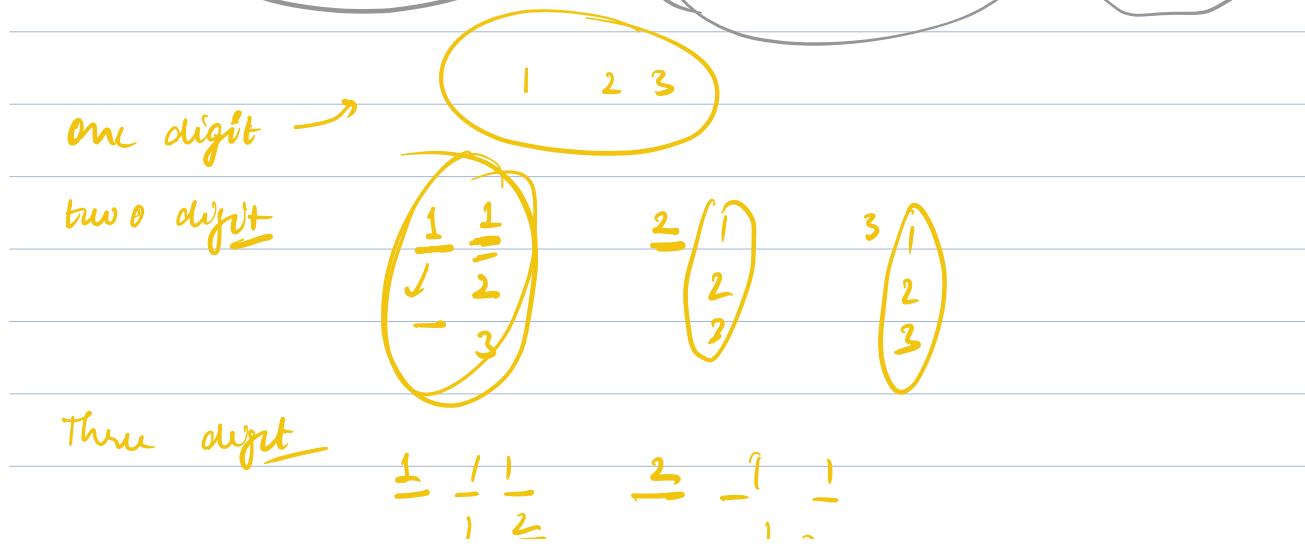
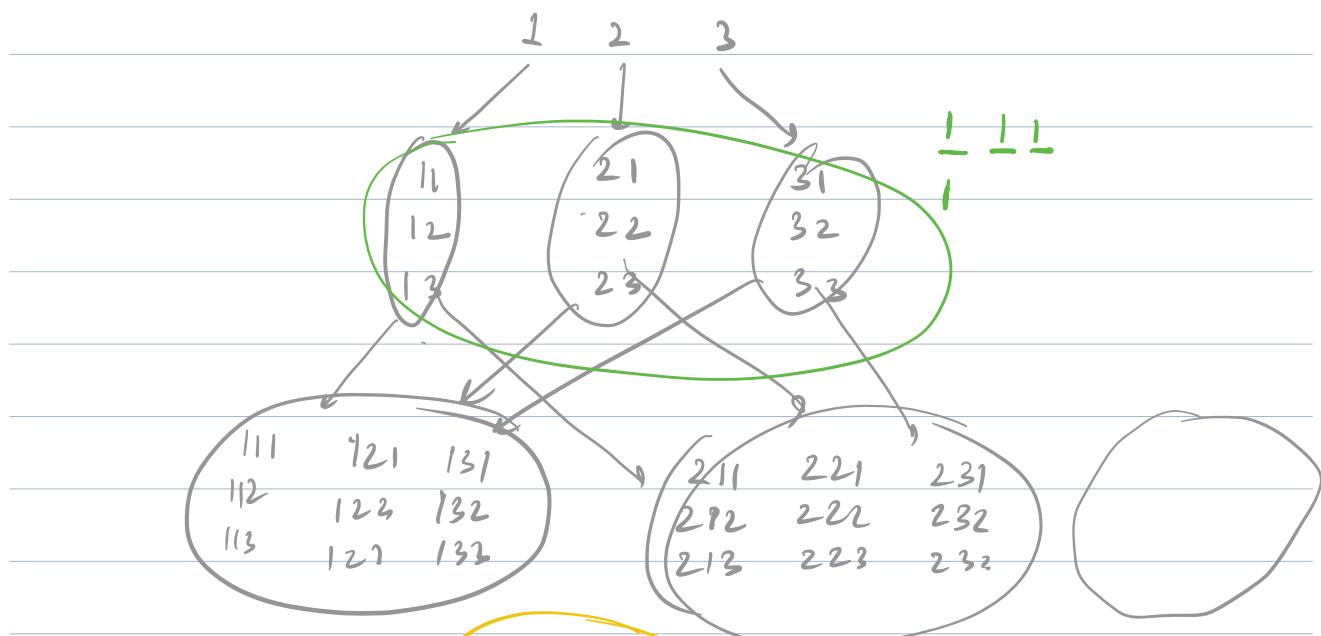
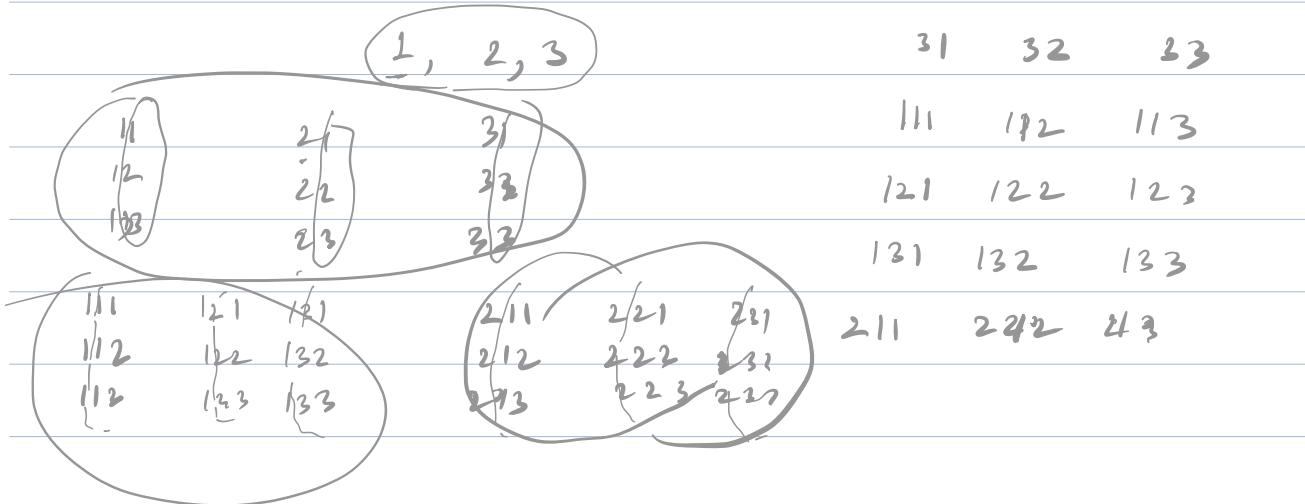
self.prev

Q I have given you 3 digits → 1, 2, 3

I want you to tell me the  $k^{\text{th}}$  smallest number that you can form using 3 digits only.



① ② ③ ⑪ ⑫ ⑬ (K=5)  
 21 22 23



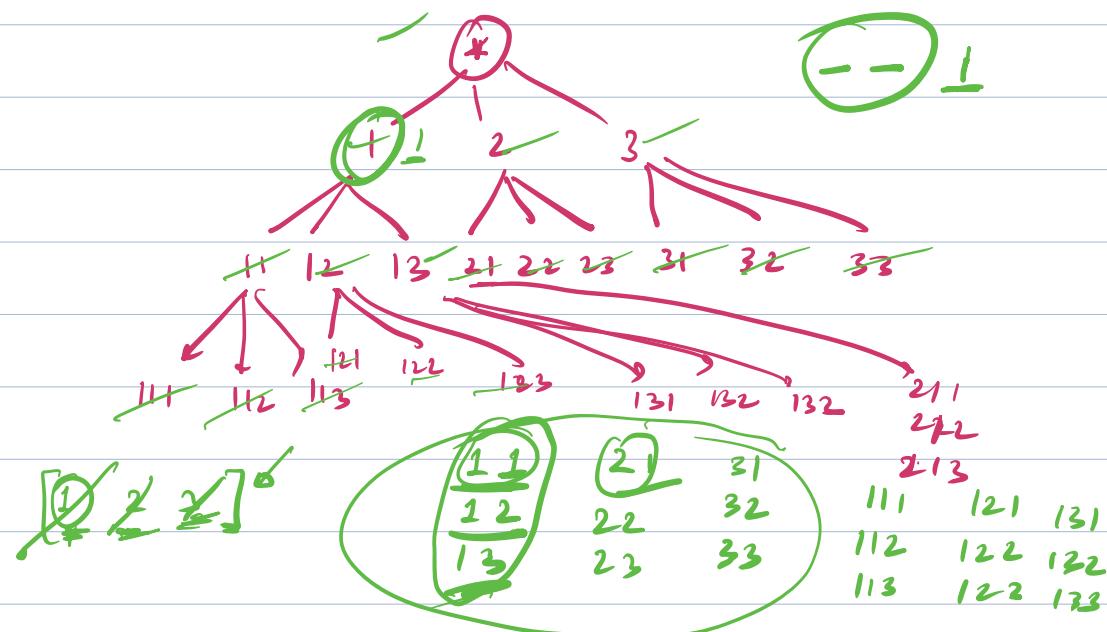
	1	3
2	1	
2	2	
2	3	
3	1	
3	2	
3	1	

	1	2
1	2	

2	1
---	---

2	3
---	---

2	.
---	---



(1) 2 3

--- 1

111	121	131
112	122	132
113	123	133

X 1 2 3 11 12 13 21 22 23 31 32 33

num \* 10 + 1

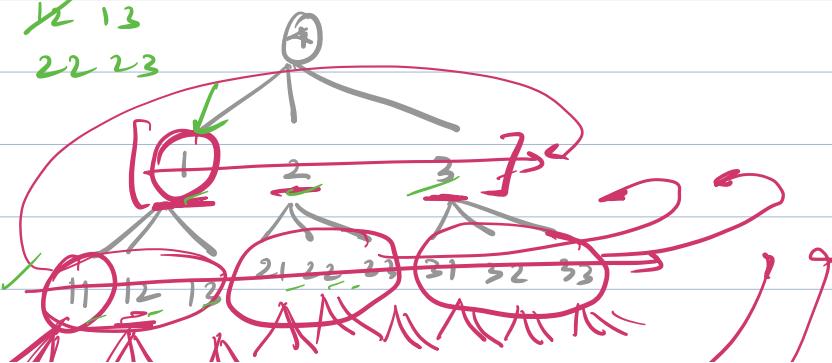
3

BFS

LVT

[X, Y, Z]  
11 12 13  
21 22 23

BFS & LVT  
Post order



9

Level order traversal

$\Rightarrow$  Queue

$k^{\text{th}}$  smaller

import collections

[1, 2, 3]

$$[2, 3]$$

۲۷

~~X~~ ~~2, 3, 11, 122, 1)~~  
~~21 22 23~~  
~~31 32 33~~  
20.2 111 112 113  
~~x = 2~~

2. 2

$$x=11$$

2012 ✓

✓

10

$$\underline{K=3}$$

K21

3 /

*white*

$$k > 0$$

$x = \text{qu.popleft}()$

qu. append ( $10^k x + 1$ )

gu.append(10\*x+2)

qu · append ( $10^x x + 3$ )

return x

$\{x, \lambda, \beta\}$   $\mu_1$

$k_{2y}$   $k_{23}$   $k_{22}$   $k_{21}$   $k_{20}$

00

11

00

00

(B)  $\rightarrow$  Base 3

$\begin{array}{|c|c|c|} \hline 1 & 2 \\ \hline 0 & 1 & 2^3 \\ \hline \end{array}$

10 20

11 21  
12 22

100

101