

1. 采用Recursion-Tree方法求解递推式

$$T(n) = T(n/4) + T(n/2) + n^2.$$

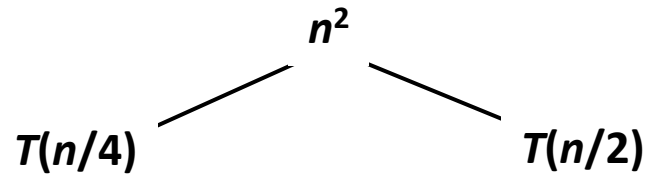
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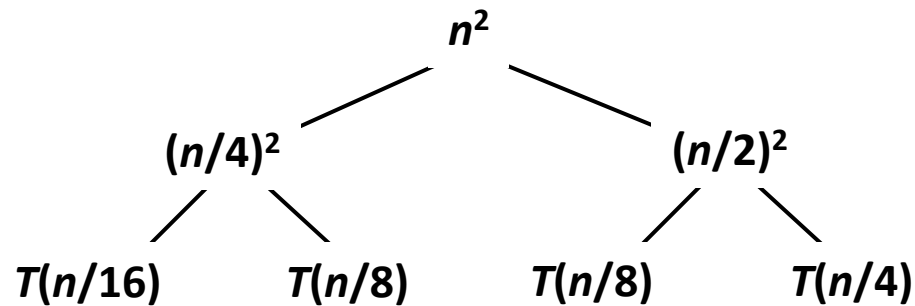
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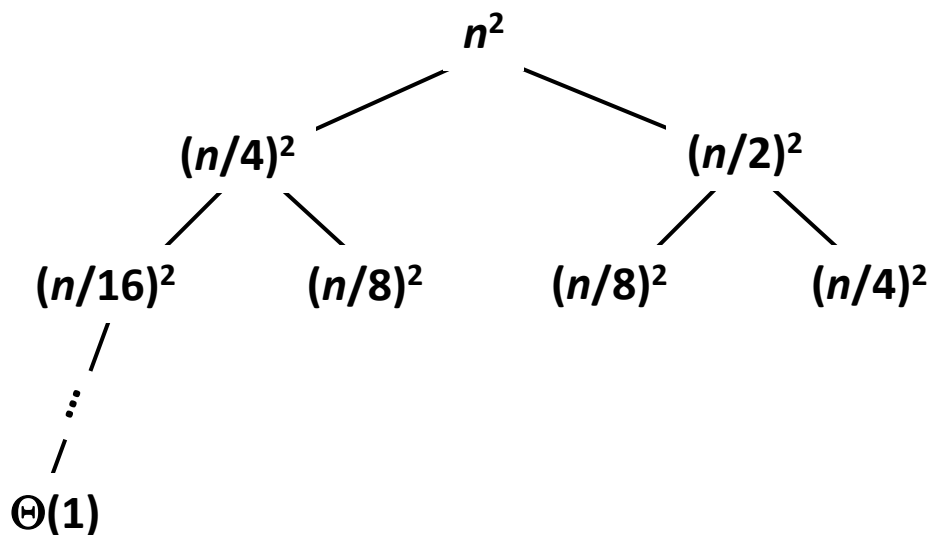
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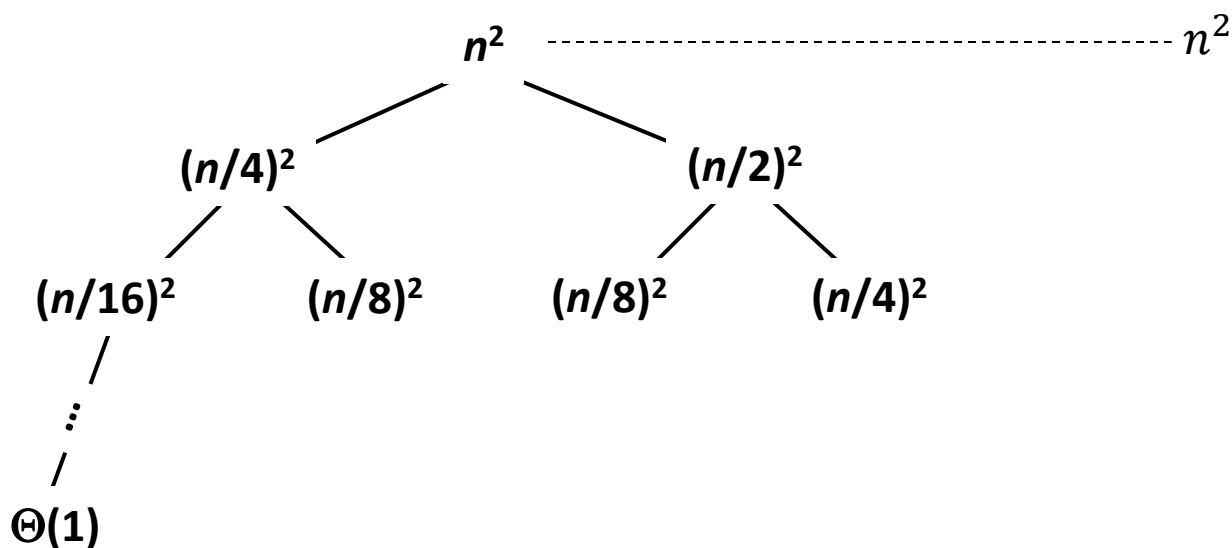
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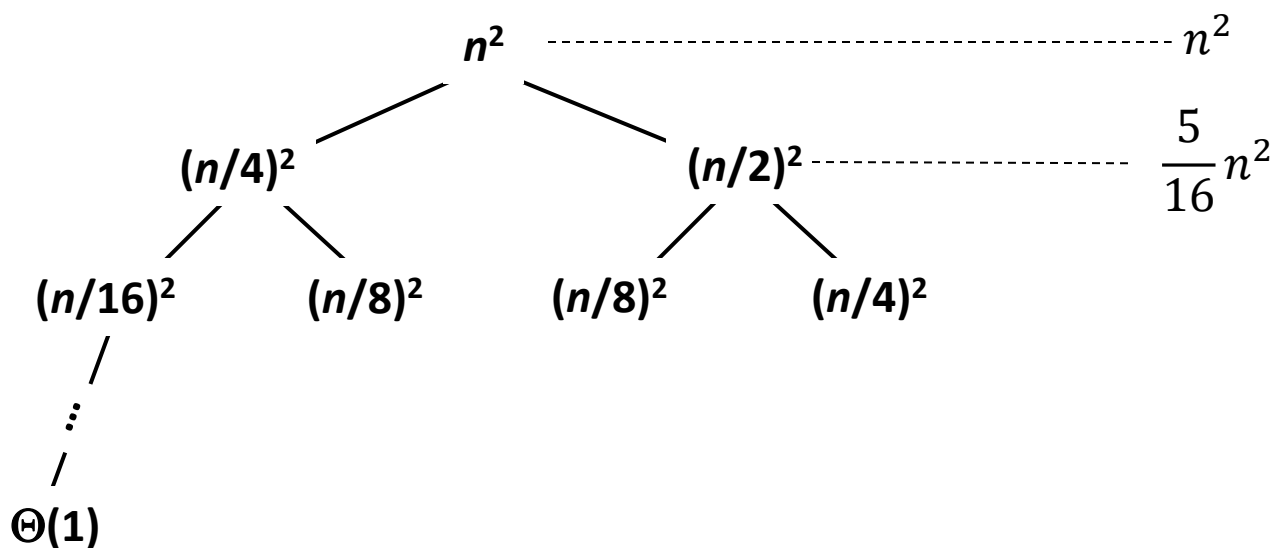
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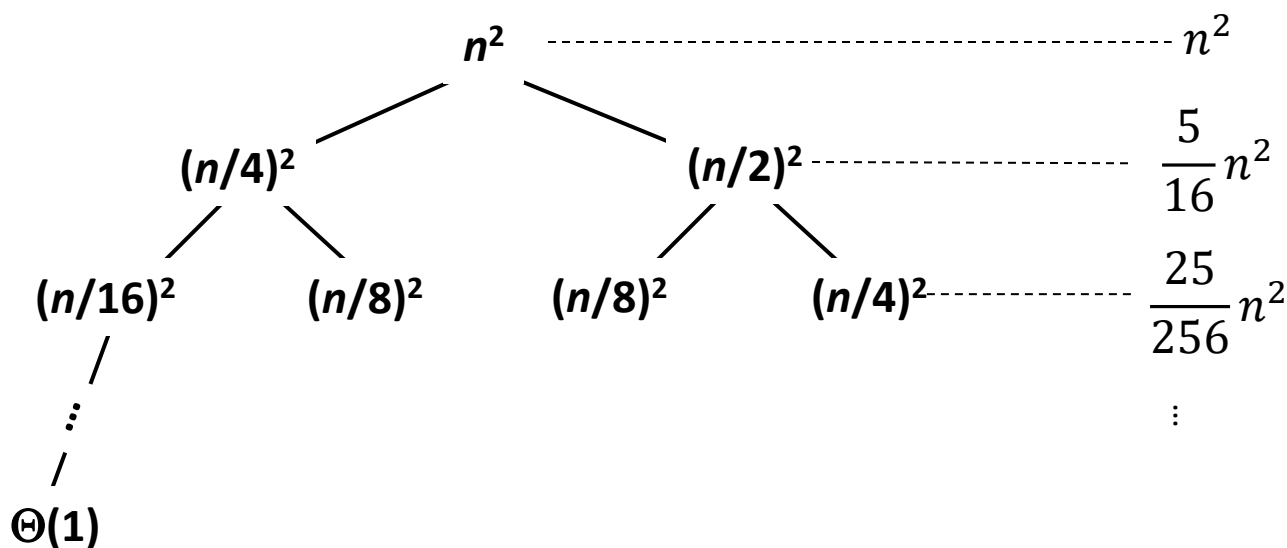
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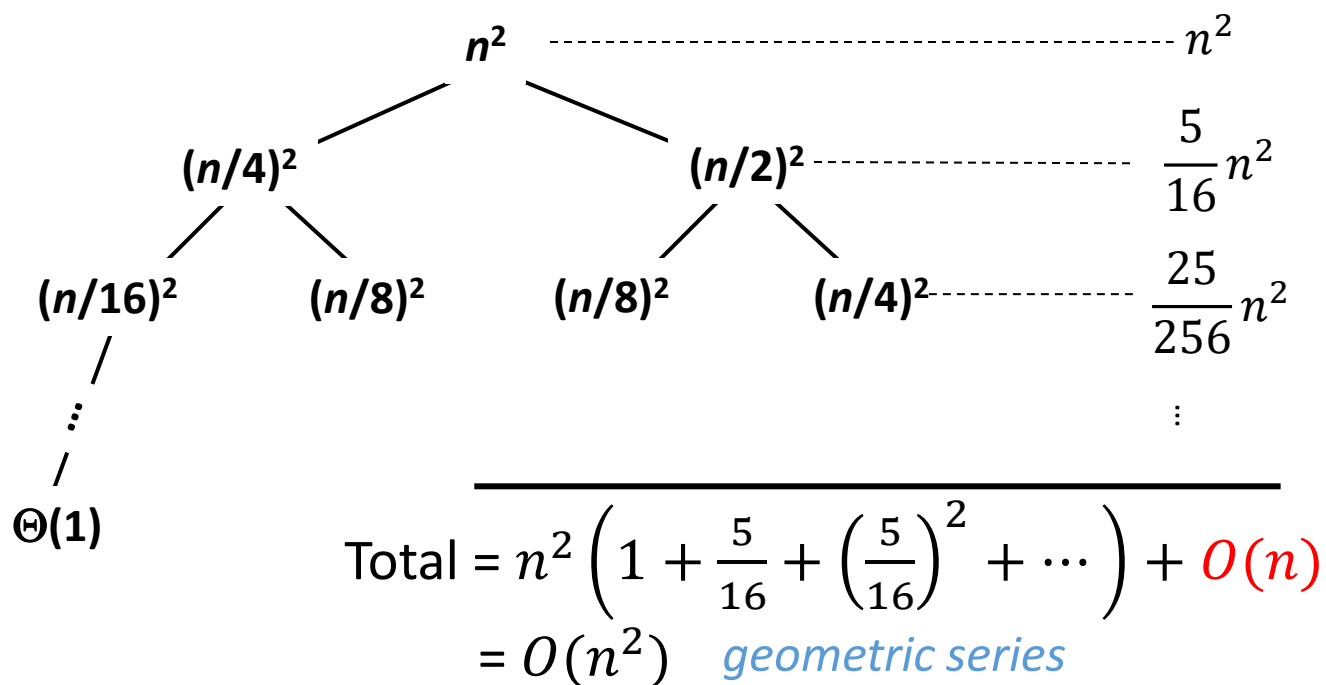
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2. 采用Master Theorem求解下列递推式.

a) $T(n) = 4T(n/2) + n$

b) $T(n) = 4T(n/2) + n^2$

c) $T(n) = 4T(n/2) + n^3$

d) $T(n) = 3T(n/4) + n \log n$

Master Theorem. Suppose that $T(n)$ is a function on the non-negative integers that satisfies the recurrence:

$$T(n) = aT(n/b) + f(n)$$

with $T(0) = 0$ and $T(1) = \Theta(1)$, where n/b means either $\lfloor n/b \rfloor$ or $\lceil n/b \rceil$.

Case 1. If $f(n) = O(n^k)$ for some constant $k < \log_b a$, then $T(n) = \Theta(n^{\log_b a})$.

Case 2. If $f(n) = \Theta(n^k \log^p n)$ for $p \geq 0$ and $k = \log_b a$, then $T(n) = \Theta(n^k \log^{p+1} n)$.

Case 3. If $f(n) = \Omega(n^k)$ for some constant $k > \log_b a$, and if $af(n/b) \leq cf(n)$ for some constant $c < 1$ and all sufficiently large n , then $T(n) = \Theta(f(n))$.

2. 采用Master Theorem求解下列递推式.

$$a) T(n) = 4T(n/2) + n$$

$$a = 4, b = 2,$$

$$n^{\log_b a} = n^2; \text{ and}$$

$$f(n) = n = O(n^1).$$

*Case 1: $k < \log_b a$,
then $T(n) = \Theta(n^2)$.*

Master Theorem. Suppose that $T(n)$ is a function on the non-negative integers that satisfies the recurrence:

$$T(n) = aT(n/b) + f(n)$$

with $T(0) = 0$ and $T(1) = \Theta(1)$, where n/b means either $\lfloor n/b \rfloor$ or $\lceil n/b \rceil$.

Case 1. If $f(n) = O(n^k)$ for some constant $k < \log_b a$, then $T(n) = \Theta(n^{\log_b a})$.

Case 2. If $f(n) = \Theta(n^k \log^p n)$ for $p \geq 0$ and $k = \log_b a$, then $T(n) = \Theta(n^k \log^{p+1} n)$.

Case 3. If $f(n) = \Omega(n^k)$ for some constant $k > \log_b a$, and if $af(n/b) \leq cf(n)$ for some constant $c < 1$ and all sufficiently large n , then $T(n) = \Theta(f(n))$.

2. 采用Master Theorem求解下列递推式.

$$b) \quad T(n) = 4T(n/2) + n^2$$

$$a = 4, b = 2,$$

$$n^{\log_b a} = n^2; \text{ and}$$

$$f(n) = n^2.$$

Case 2: $f(n) = (n^2 \log^0 n)$,
and $k = 2$,

then $T(n) = \Theta(n^2 \log n)$.

Master Theorem. Suppose that $T(n)$ is a function on the non-negative integers that satisfies the recurrence:

$$T(n) = aT(n/b) + f(n)$$

with $T(0) = 0$ and $T(1) = \Theta(1)$, where n/b means either $\lfloor n/b \rfloor$ or $\lceil n/b \rceil$.

Case 1. If $f(n) = O(n^k)$ for some constant $k < \log_b a$, then $T(n) = \Theta(n^{\log_b a})$.

Case 2. If $f(n) = \Theta(n^k \log^p n)$ for $p \geq 0$ and $k = \log_b a$, then $T(n) = \Theta(n^k \log^{p+1} n)$.

Case 3. If $f(n) = \Omega(n^k)$ for some constant $k > \log_b a$, and if $af(n/b) \leq cf(n)$ for some constant $c < 1$ and all sufficiently large n , then $T(n) = \Theta(f(n))$.

2. 采用Master Theorem求解下列递推式.

$$c) \quad T(n) = 4T(n/2) + n^3$$

$$a = 4, b = 2,$$
$$n^{\log_b a} = n^2; \text{ and}$$
$$f(n) = n^3.$$

*Case 3: $f(n) = \Omega(n^3)$,
and $4(n/2)^3 \leq cn^3$ (reg.
cond.) for $c = 1/2$,
then $T(n) = \Theta(n^3)$.*

Master Theorem. Suppose that $T(n)$ is a function on the non-negative integers that satisfies the recurrence:

$$T(n) = aT(n/b) + f(n)$$

with $T(0) = 0$ and $T(1) = \Theta(1)$, where n/b means either $\lfloor n/b \rfloor$ or $\lceil n/b \rceil$.

Case 1. If $f(n) = O(n^k)$ for some constant $k < \log_b a$, then $T(n) = \Theta(n^{\log_b a})$.

Case 2. If $f(n) = \Theta(n^k \log^p n)$ for $p \geq 0$ and $k = \log_b a$, then $T(n) = \Theta(n^k \log^{p+1} n)$.

Case 3. If $f(n) = \Omega(n^k)$ for some constant $k > \log_b a$, and if $af(n/b) \leq cf(n)$ for some constant $c < 1$ and all sufficiently large n , then $T(n) = \Theta(f(n))$.

2. 采用Master Theorem求解下列递推式.

$$d) \quad T(n)=3T(n/4)+n\log n$$

$$a = 3, \quad b = 4,$$

$$n^{\log_b a} = n^{0.793}; \text{ and}$$

$$f(n) = n\log n.$$

Case 3: $f(n) = \Omega(n^1)$,
and $3(n/4)\log(n/4) \leq$
 $cn\log n$ (reg. cond.) for
 $c = 3/4$,
then $T(n) = \Theta(n\log n)$.

Master Theorem. Suppose that $T(n)$ is a function on the non-negative integers that satisfies the recurrence:

$$T(n) = aT(n/b) + f(n)$$

with $T(0) = 0$ and $T(1) = \Theta(1)$, where n/b means either $\lfloor n/b \rfloor$ or $\lceil n/b \rceil$.

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