# The LUA-PHYSICAL library

### $Version\ 0.1$

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#### Abstract

lua-physical is a pure Lua library which provides functions and object for doing computation with physical quantities. It has been written to simplify the creation problem sets. The package provides units of the SI and the imperial system. Furthermore an almost complete set of international currencies are supported, however without online exchange rates. In order to display the numbers with measurement uncertainties, the package is able to perform gaussian error propagation.

# Contents

1	Introduction					
2	<b>Loa</b> 2.1	ding Dependencies	<b>3</b>			
3	Usa	${f ge}$	4			
	3.1	Unit conversion	4			
		3.1.1 Temperature Conversion	5			
		3.1.2 Uncertainty	6			
4	Sup	ported Units	9			
	4.1	Base Units	9			
	4.2	Constants	11			
	4.3	Coherent derived units in the SI	13			
	4.4	Non-SI units accepted for use with the SI	14			
	4.5	Nominal Astronomical Units	15			
	4.6	Other Non-SI units	15			
	4.7	Imperial Units	18			
	4.8	U.S. customary units	20			
	4.9	International Currencies	22			

5	Lua	Documentation	23
	5.1	physical.Quantity	23
	5.2	physical.Dimension	32
	5.3	physical.Unit	32
	5.4	physical.Number	33
Bi	bliog	raphy	36
In	$\mathbf{dex}$		37

### 1 Introduction

The author of this package is a teacher at the high school Kantonsschule Zug in Switzerland. The main use of this package is to write physics problem sets. LualATEXdoes make it possible to integrate physical calculations directly. The package has been in use since 2016. Many bugs have been found and fixed. Nevertheless it still is possible, that some were not found yet. Therefore the author recommends not to use this package industry or science. If one does so, it's the responsability of the user to check results for plausability. If the user finds some bugs, they can be reported at github.com or directly to the author (thomas.jenni (at) ksz.ch).

# 2 Loading

This package is a pure Lua library. Therefore one has to require it explicitly by calling require("physical"). For printing results, the siunitx package can be used. It's recommended to define a macro like \q to convert the lua quantity object to a siunitx expression.

The following Latex preambel loads the lua-physical package and creates a macro \q for printing physical quantities.

Listing 1: basic preamble

```
\usepackage{lua-physical}
      \usepackage{siunitx}
      % configure siunitx
      \sisetup{
        output-decimal-marker = {.},
        per-mode = symbol,
        separate-uncertainty = true,
       add-decimal-zero = true,
        exponent-product = \cdot,
       round-mode = off
      % load lua-physical package
      \begin{luacode*}
16
        physical = require("physical")
        N = physical.Number
      \end{luacode*}
      % print physical quantities
      \mbox{\ensuremath{\mbox{newcommand}}\{\q\}[1]{\%}}
        \directlua{tex.print(physical.Quantity.tosiunitx(#1, "scientific-
               notation=fixed,exponent-to-prefix=false"))}%
      }
```

### 2.1 Dependencies

This is a standalone package. If a pretty print to LuaLATEX is wanted, the package siunitx sould be installed.

# 3 Usage

Given the basic preamble, units can be used in lua code directly. By convention, all units have an underscore in front of them, i.e. Meter is \_m, Second is \_s. All available units are listed in chapter 4. The Result of the calculation can be printed to Lual\*TFX by using the macro \q{}.

Listing 2: The velocity of a car.

```
1 \begin{luacode}
2     s = 10 * _m
3     t = 2 * _s
4     v = s/t
5 \end{luacode}
6
7 A car travels $\q{s}$ in $\q{t}$. calculate its velocity.
8     $$
9     v=\frac{s}{t} = \frac{\q{s}}{\q{t}} = \q{v}
10 $$$
```

A car travels 10 m in 2 s. Calculate its velocity.

$$v = \frac{s}{t} = \frac{10 \,\mathrm{m}}{2 \,\mathrm{s}} = 5 \,\mathrm{m/s}$$

In the above listing 2, the variable s stands for displacement and has the unit meter  $_m$ . The variable t stands for time and is given in second  $_s$ . If mathematical operations are done on them, new physical quantities are created. In the problem above, the velocity v is calculated by dividing s by t. The instance v has the derived unit m/s. By using the macro q all quantities can be printed to the LualATeX code directly.

### 3.1 Unit conversion

Very often the result of a calculation is needed in different unit, than the given quantities are. In the following listing 3 the task is to calculate the volume of a cuboid with lengths given in different units. If the volume is calculated by multipling all three lengths, the unit of the result is cm mm m. If the unit cm<sup>3</sup> is preferred, it has to be converted explicitly. The conversion function is called to() and is available on all physical quantitiy instances. At first this looks a bit cumbersome. The reason of this behaviour is, that the software is not able to guess the unit of the result. In many cases, like in the example here, it's not clear

what unit the result sould have. Therefore the user has always to give the target unit explicitly.

Listing 3: The volume of a cuboid.

```
\begin{luacode}
      a = 12 * _cm
      b = 150 * _mm
      c = 1.5 * _m
      V = a*b*c
    \end{luacode}
    Find the volume of a rectangular cuboid with lengths \q{a},
10
    q{b}\ and \ q{c}\ .
11
      V= a \cdot b \cdot c
      = \q{a} \cdot \q{b} \cdot \q{c}
13
      = \q{V}
15
      = \left\{ \left( \frac{dm^3}{} \right) \right\}
```

Find the volume of a rectangular cuboid with lengths 12 cm, 150 mm and 1.5 m.

```
V = a \cdot b \cdot c = 12 \text{ cm} \cdot 150 \text{ mm} \cdot 1.5 \text{ m} = 2700 \text{ cm mm m} = \underline{27 \text{ dm}^3}
```

#### 3.1.1 Temperature Conversion

In the following problem, listing 5, the task is to convert a temperature given in the unit degree Celsius to Kelvin.

Most of the units transform linearly to base units. Exceptions are the unit degree Celsius <code>\_degC</code> and degree Fahrenheit <code>\_degF</code>. These units are ambigous and can be interpreted as temperature differences or as an absolute temperatures. In the latter case, the conversion to base units is not a linear, but an affine transformation. This is because degree Celsius and degree Fahrenheit scales have their zero points at different temperatures compared to the unit Kelvin.

By default <code>\_degC</code> and <code>\_degF</code> units are standing for temperature differences. If one wants to have it converted absolutely, it has to be done adding / subtracting the quantities <code>\_degC\_0</code> and <code>\_degF\_0</code>.

Listing 4: Temperature conversion.

```
1 \begin{luacode}
2 theta_1 = 110 * _degC
3 T_1 = ( theta_1 + _degC_0 ):to(_K)
4 theta_1 = T_1:to(_degC) - _degC_0
5
6 theta_2 = 212 * _degF
7 T_2 = ( theta_2 + _degF_0 ):to(_K)
8 theta_2 = T_2:to(_degF) - _degF_0
```

```
\end{luacode}
    \begin{align*}
      \vartheta_1 &= \q{theta_1} \\
13
      \vartheta_2 &= \q{theta_2} \\
     T_2 \&= q{T_2} \
```

```
\vartheta_1=110\,{}^{\circ}\mathrm{C}
T_1 = 383.15 \,\mathrm{K}
\vartheta_2 = 212\,{}^{\circ}\mathrm{F}
T_2 = 373.15 \,\mathrm{K}
```

Listing 5: Temperature conversion.

```
\begin{luacode}
 theta = 20 * _degC
T = ( theta + _degC_0 ):to(_K)
A thermometer shows \q{\theta}. Convert this quantity to Kelvin
  T = q{theta} + q{_degC_0:to()}
```

A thermometer shows. Converte this quantity to Kelvin.

$$T = 20 \,\mathrm{K} + 273.15 \,\mathrm{K} = 293.15 \,\mathrm{K}$$

#### 3.1.2 Uncertainty

The package supports uncertainty propagation. To create a number with an uncertainty, an instance of physical. Number has to be created, see listing 6. It has to be remembered, that N is a alias for physical.Number. The first argument of the constructor N(mean, uncertainty) is the mean value and the second one the uncertainty of the measurement. If the proposed preamble is used, the uncertainty is by default seperated from the mean value by a plus-minus sign.

For the uncertainty propagation the gaussian formula

$$\Delta f = \sqrt{\left(\frac{\partial f}{x_1} \cdot \Delta x_1\right)^2 + \dots + \left(\frac{\partial f}{x_n} \cdot \Delta x_2\right)^2}$$

is used. This formula is a good estimation for the uncertainty  $\Delta f$ , if the quantities  $x_1, \ldots, x_n$  the function f depends on, have no correlation. Further, the function f has to behave linear, if the quantities  $x_i$  are changed in the range of their uncertainties.

Listing 6: Uncertainty in area calculation.

```
1 \begin{luacode}
2    a = N(2,0.1) * _m
3    b = N(3,0.1) * _m
4
5    A = (a*b):to(_m^2)
6 \end{luacode}
7
8 Calculate the area of a rectangle with lengths $\q{a}$ and $\q{b}$.
9 $$
10    A = a \cdot b
11    = \q{a} \cdot \q{b}
12    = \uuline{\q{A}}
13 $$$
```

Calculate the area of a rectangle with lengths  $(2.00 \pm 0.10) \,\mathrm{m}$  and  $(3.00 \pm 0.10) \,\mathrm{m}$ .

$$A = a \cdot b = (2.00 \pm 0.10) \,\mathrm{m} \cdot (3.00 \pm 0.10) \,\mathrm{m} = \underline{(6.0 \pm 0.4) \,\mathrm{m}^2}$$

Instead of printing always the uncertainties, one can use the uncertainty calculation to provide significant numbers.

In the following problem, listing 7, the task is to calculate the volume of an ideal gas. Given are pressure p in \_bar, amount of substance n in \_mol and temperature T in degree celsius \_degC. In order to do the calculation, one has to convert T, which is given as an absolute temperature in degree celsius to the base unit Kelvin first. By setting N.omitUncertainty = true, all uncertainties are not printed.

Listing 7: Volume of an ideal gas.

```
13 = \q{V}
14 = \uuline{\q{V}}
15 $$
```

An ideal gas (1.0 mol) has a pressure of 1.013 bar and a temperature of 30  $^{\circ}\mathrm{C}.$  Calculate the volume of the gas.

$$V = \frac{1.0\,\text{mol} \cdot 8.31\,\text{J/(mol\,K)} \cdot 303\,\text{K}}{1.013\,\text{bar}} = \underline{25\,\text{L}}$$

# 4 Supported Units

All supported units are listed in this chapter. Subchapter 4.1 lists the seven base units of the International System of Units (SI). In subchapter 4.2 mathematical and physical constants are defined. The subchapter ?? contains all derived units from the SI system. Subchapter ?? lists units, which are common but outside of the SI system. The subchapters 4.7 and 4.8 are dedicated to imperial and U.S. customary units. The last subchapter 4.9 containts international currencies.

### 4.1 Base Units

Quantity	Unit	Symbol	Dim.	Definition
time	second	_s	Τ	The SI unit of time. It is defined by taking the fixed numerical value of the caesium frequency $\Delta\nu_{Cs}$ , the unperturbed ground-state hyperfine transition frequency of the caesium 133 atom, to be 9192631770 when expressed in the unit 1/s.
length	meter	_m	L	The SI unit of length. It is defined by taking the fixed numercial value of the speed of light in vacuum $c$ to be 299 792 458 when expressed in the unit of 1 m/s.
mass	kilogram	_kg	M	The SI unit of mass. It is defined by taking the fixed numerical value of the Planck constant $h$ to be $6.62607015\cdot10^{-34}$ when expressed in m <sup>2</sup> kg/s.
electric current	ampere	_A	I	The SI unit of electric current. It is defined by taking the fixed numerical value of the elementary charge $e$ to be $1.602176634\cdot10^{-19}$ when expressed in As.
thermody- namic temperature	kelvin	_K	Θ	The SI unit of the thermodynamic temperature. It is defineed by taking the fixed numerical value of the Boltzmann constant $k_B$ to be $1.380649\cdot10^{-23}$ when expressed in $1\mathrm{kg}\mathrm{m}^2/(\mathrm{s}^2\mathrm{K})$

Quantity	$\operatorname{Unit}$	Symbol	Dim.	Definition
amount of substance	mole	_mol	N	The SI unit of amount of substance. One mole contains exactly $6.02214076\cdot10^{23}$ elementary entities. This number is the fixed numerical value of the Avogadro constant $N_A$ when expressed in $1/\text{mol}$ .
luminous intensity	candela	_cd	J	The SI unit of luminous intensity in a given direction. It is defined by taking the fixed numerical value of the luminous efficacy of monochromatic radiation of frequency $5.4 \cdot 10^{14} \mathrm{Hz}$ , $K_{cd}$ , to be 683 when expressed in the unit $\mathrm{cd}  \mathrm{sr}  \mathrm{s}^3 / (\mathrm{kg}  \mathrm{m}^2)$ .
number	_	_1	1	The dimensionless number one.
information	bit	_bit	В	The smallest amount of information. $$
currency	euro	_EUR	С	The value of the currency Euro.

Table 1: Base units of the International System of Units (SI) [3], information, currency and the dimensionless number one.

# 4.2 Constants

All physical constants are taken from the NIST webpage [1].

Name	Symbol	Definition
pi	_Pi	3.1415926535897932384626433832795028841971 * _1
eulersnumber	_E	2.7182818284590452353602874713526624977572 * _1
speedoflight	_c	299792458 * _m/_s
${\it gravitational} constant$	_Gc	N(6.67408e-11,3.1e-15) * _m^3/(_kg*_s^2)
planckconstant	_h_P	6.62607015e-34 * _J*_s
${\it reduced planck constant}$	_h_Pbar	_h_P/(2*_Pi)
elementarycharge	_e	1.602176634e-19 * _C
vacuumpermeability	_u_0	4e-7*Pi * _N/_A^2
vacuumpermitivity	_e_0	1/(_u_0*_c^2)
atomicmassunit	_u	N(1.66053904e-27, 2e-35) * _kg
electronmass	_m_e	N(9.10938356e-31, 1.1e-38) * _kg
protonmass	_m_p	N(1.672621898e-27, 2.1e-35) * _kg
neutronmass	_m_n	N(1.674927471e-27, 2.1e-35) * _kg
bohrmagneton	_u_B	_e*_h_Pbar/(2*_m_e)
nuclearmagneton	_u_N	_e*_h_Pbar/(2*_m_p)
electronmagneticmoment	_u_e	N(-928.4764620e-26,5.7e-32) * _J/_T
protonmagneticmoment	_u_p	N(1.4106067873e-26,9.7e-35) * _J/_T
neutronmagneticmoment	_u_n	N(-0.96623650e-26,2.3e-26) * _J/_T
finestructureconstant	_alpha	_u_0*_e^2*_c/(2*_h_P)
rydbergconstant	_Ry	_alpha^2*_m_e*_c/(2*_h_P)

Name	Symbol	Definition
avogadronumber	_N_A	6.02214076e23/_mol
boltzmannconstant	_k_B	1.380649e-23 * _J/_K
molargasconstant	_R	N(8.3144598, 4.8e-6) * _J/(_K*_mol)
${\it stefanboltz} mann constant$	_sigma	_Pi^2*_k_B^4/(60*_h_Pbar^3*_c^2)
standardgravity	_g_0	9.80665 * _m/_s^2

### 4.3 Coherent derived units in the SI

All units in this section are coherent derived units from the SI base units with special names, [2, 118].

Quantity	Unit	Symbol	Definition
Plane Angle <sup>1</sup>	radian	_rad	_1
Solid $Angle^2$	steradian	_sr	_rad^2
Frequency	hertz	_Hz	1/_s
Force	newton	_N	_kg*_m/_s^2
Pressure	pascal	_Pa	_N/_m^2
Energy	joule	_J	_N*_m
Power	watt	_W	_J/_s
Electric Charge	$\operatorname{coulomb}$	_C	_A*_s
Electric Potential	volt	_V	_J/_C
Electric Capacitance	farad	_F	_C/_V
Electric Resistance	ohm	_Ohm	_V/_A
Electric Conductance $^3$	siemens	_S	_A/_V
Magnetic Flux	weber	_Wb	_V*_s
Magnetic Flux Density	tesla	_T	_Wb/_m^2
Inductance	henry	_H	_Wb/_A
Celsius Temperature <sup>4</sup>	celsius	_degC	_K
Luminous Flux	lumen	_lm	_cd*_sr
Illuminance	lux	_lx	_lm/_m^2

<sup>&</sup>lt;sup>1</sup>In the SI system, the quantity Plane Angle has the dimension of a number.

<sup>&</sup>lt;sup>2</sup>In the SI system, the quantity Solid Angle has the dimension of a number.

<sup>&</sup>lt;sup>3</sup>The unit \_PS stands for peta siemens and is in conflict with the german version of the unit horsepower (Pferdestärke). Since the latter is more common than peta siemens, \_PS is defined as the german version of horsepower.

<sup>&</sup>lt;sup>3</sup>The unit \_degC is by default interpreted as a temperature difference.

Quantity	Unit	Symbol	Definition
Activity	becquerel	_Bq	1/_s
Absorbed Dose	gray	_Gy	_J/_kg
Dose Equivalent	sievert	_Sv	_J/_kg
Catalytic Activity	katal	_kat	_mol/_s

Table 2: Coherent derived units of the SI

# 4.4 Non-SI units accepted for use with the SI

There are a few units with dimension 1.

Quantity	Unit	Symbol	Definition
Time	minute	_min	60*_s
	hour	_h	60*_min
	day	_d	24*_h
Plane Angle	degree	_deg	(_Pi/180)*_rad
	arcminute	_arcmin	_deg/60
	arcsecond	_arcsec	_arcmin/60
Area	hectare	_hectare	1e4*_m^2
Volume	liter	_L	1e-3*_m^3
Mass	tonne	_t	1e3*_kg

Table 3: Units outside of the International System of Units (SI)

### 4.5 Nominal Astronomical Units

The nominal values of solar, terrestrial and jovial quantities are taken from IAU Resolution B3 [4].

Quantity	Unit	Symbol	Definition
Length	nomsolradius	_R_S_nom	6.957e8 * _m
Irradiance	nomsolirradiance	_S_S_nom	1361 * _W/_m^2
Radiant Flux	nomsolluminosity	_L_S_nom	3.828e26 * _W
Temperature	nom so leff temperature	_T_S_nom	5772 * _K
Mass Parameter	nomsolmassparam	_GM_S_nom	1.3271244e20 * _m^3*_s^-2
Length	nomterrequadius	_Re_E_nom	6.3781e6 * _m
Length	nomterrpolradius	_Rp_E_nom	6.3568e6 * _m
Mass Parameter	nomterrmassparam	_GM_E_nom	3.986004e14 * _m^3*_s^-2
Length	nomjovianeqradius	_Re_J_nom	7.1492e7 * _m
Length	nomjovianpolradius	_Rp_J_nom	6.6854e7 * _m
Mass Parameter	nomjovianmassparam	_GM_J_nom	1.2668653e17 * _m^3*_s^-2

# 4.6 Other Non-SI units

The unit Bel is only available with prefix decibel, because  $\_{\tt B}$  is the unit byte.

Quantity	Unit	Symbol	Definition
Time	svedberg	_svedberg	1e-13*_s
	week	_wk	7*_d
	year	_a	365.25*_d
Length	angstrom	_angstrom	1e-10*_m
	fermi	_fermi	1e-15*_m
	astronomical unit	_au	149597870700*_m
	lightsecond	_ls	_c*_s
	lightyear	_ly	_c*_a
	parsec	_pc	(648000/_Pi)*_au
Area	barn	_barn	1e-28*_m^2
	are	_are	1e2*_m^2
Volume	metricteaspoon	_tsp	5e-3*_L
	metric table spoon	_Tbsp	3*_tsp
Plane Angle	gradian	_gon	(Pi/200)*_rad
	turn	_tr	2*Pi*_rad
Solid Angle	spat	_sp	4*Pi*_sr

Quantity	Unit	Symbol	Definition
Pressure	bar	_bar	1e5*_Pa
	standardatmosphere	_atm	101325*_Pa
	technicalatmosphere	_at	_kp/_cm^2
	millimeterofmercury	_mmHg	133.322387415*_Pa
	torr	_Torr	(101325/760)*_Pa
Force	kilopond	_kp	_kg*_g_0
Energy	thermochemical calorie	_cal	4.184*_J
	international calorie	_cal_IT	4.1868*_J
	gramoftnt	_g_TNT	1e3*_cal
	tonoftnt	_t_TNT	1e9*_cal
	electronvolt	_eV	_e*_V
	wattsecond	_Ws	_W*_s
	watthour	_Wh	_W*_h
Power	voltampere	_VA	_V*_A
Electric Charge	amperesecond	_As	_A*_s
	amperehour	_Ah	_A*_h
Information	nibble	_nibble	4*_bit
	byte	_B	8*_bit
Information Transfer Rate	bitpersecond	_bps	_bit/_s
Number	percent	_percent	1e-2*_1
	permille	_permille	1e-3*_1
	partspermillion	_ppm	1e-6*_1
	partsperbillion	_ppb	1e-9*_1
	partspertrillion	_ppt	1e-12*_1
	partsperquadrillion	_ppq	1e-15*_1
	decibel	_dB	_1

# 4.7 Imperial Units

Quantity	Unit	Symbol	Definition
Length	inch	_in	0.0254*_m
	thou	_th	0.001*_in
	pica	_pica	_in/6
	point	_pt	_in/72
	hand	_hh	4*_in
	foot	_ft	12*_in
	yard	_yd	3*_ft
	$\operatorname{rod}$	_rd	5.5*_yd
	chain	_ch	4*_rd
	furlong	_fur	10*_ch
	mile	_mi	8*_fur
	league	_lea	3*_mi
	${\it nautical mile}$	_nmi	1852 * _m
	nauticalleague	_nlea	3*_nmi
	cable	_cbl	_nmi/10
	fathom	_ftm	6*_ft
Velocity	knot	_kn	_nmi/_h
Area	acre	_ac	43560*_ft^2
Volume	gallon	_gal	4.54609*_L
	quart	_qt	_gal/4
	$\operatorname{pint}$	_pint	_qt/2
	cup	_cup	_pint/2
	gill	_gi	_pint/4
	fluidounce	_fl_oz	_gi/5
	fluiddram	_fl_dr	_fl_oz/8

Quantity	Unit	Symbol	Definition
Mass	grain	_gr	64.79891*_mg
	pound	_lb	7000*_gr
	ounce	_oz	_lb/16
	$\operatorname{dram}$	_dr	_1b/256
	stone	_st	14*_lb
	quarter	_qtr	2*_st
	${\bf hundred weight}$	_cwt	4*_qtr
	longton	_ton	20*_cwt

Table 4: Imperial units

# 4.8 U.S. customary units

In the U.S., the length units are bound to the meter differently than in the imperial system. The followin definitions are taken from https://en.wikipedia.org/wiki/United\_States\_customary\_units.

Quantity	Unit	Symbol	Definition
Length	ussurveyinch	_in_US	_m/39.37
	ussurveyhand	_hh_US	4*_in_US
	ussurveyfoot	_ft_US	3*_hh_US
	ussurveylink	_li_US	0.66*_ft_US
	ussurveyyard	_yd_US	3*_ft_US
	ussurveyrod	_rd_US	5.5*_yd_US
	ussurveychain	_ch_US	4*_rd_US
	ussurveyfurlong	_fur_US	10*_ch_US
	ussurveymile	_mi_US	8*_fur_US
	ussurveyleague	_lea_US	3*_mi_US
	us survey fathom	_ftm_US	72*_in_US
	ussurveycable	_cbl_US	120*_ftm_US
Area	ussurveyacre	_ac_US	_ch_US*_fur_US
Volume	usgallon	_gal_US	231*_in^3
	usquart	_qt_US	_gal_US/4
	uspint	_pint_US	_qt_US/2
	uscup	_cup_US	_pint_US/2
	usgill	_gi_US	_pint_US/4
	usfluidounce	_fl_oz_US	_gi_US/4
	ustablespoon	_Tbsp_US	_fl_oz_US/2
	usteaspoon	_tsp_US	_Tbsp_US/3
	usfluiddram	_fl_dr_US	_fl_oz_US/8

Quantity	Unit	Symbol	Definition
Mass	usquarter	_qtr_US	25*_1b
Mass	ushund redweight	_cwt_US	4*_qtr_US
Mass	uston	_ton_US	20*_cwt_US

Table 5: U.S. customary units

# 4.9 International Currencies

Currency	Symbol	Definition
AfghanAfghani	_AFN	0.012*_EUR
AlbanianLek	_ALL	0.008*_EUR
ArmenianDram	_AMD	0.0018*_EUR
AngolanKwanza	_AOA	0.0028*_EUR
ArgentinePeso	_ARS	0.021*_EUR
AustralianDollar	_AUD	0.63*_EUR
AzerbaijaniManat	_AZN	0.63*_EUR
BosnianMark	_BAM	0.51*_EUR
BangladeshiTaka	_BDT	0.011*_EUR
BurundianFranc	_BIF	0.00049*_EUR
BolivianBoliviano	_BOB	0.13*_EUR
BrazilianReal	_BRL	0.23*_EUR
BotswanaPula	_BWP	0.083*_EUR
BelarusianRuble	_BYN	0.42*_EUR
CanadianDollar	_CAD	0.66*_EUR
USDollar	_USD	0.89*_EUR
JapaneseYen	_JPY	0.008*_EUR
PoundSterling	_GBP	1.16*_EUR
ChineseRenminbiYuan	_CNY	0.13*_EUR
SwedishKrona	_SEK	0.094*_EUR
New Zeal and Dollar	_NZD	0.61*_EUR

Table 6: International currency units based on exchange rates from 7.3.2019, 21:00 UTC.

### 5 Lua Documentation

In this chapter, the following shortcuts will be used.

```
1 local D = physical.Dimension
2 local U = physical.Unit
3 local N = physical.Number
4 local Q = physical.Quantity
```

The term number refers to a lua integer or a lua float number. By string a lua string is meant and by bool a lua boolean.

### 5.1 physical.Quantity

The quantity class is the main part of the library. Each physical Quantity and all units are represented by an instance of this class.

### Q.new(q=nil)

Copy Constuctor

```
q: Q or number, optional
Optional argument is either Q, a number or nil.
return: Q
The created Q instance
```

As an argument it takes Q, number or nil. If Q is given, a copy of it is made and returned. If a number is given, the function creates a dimensionless quantity with that value. In the case nil is given, the quantity \_1 is returned.

#### Example

```
1 myOne = Q()
2 myNumber = Q(42)
3 myLength = Q(73*_m)
```

### Q.defineBase(symbol,name,dimension)

This function is used to declare base quantities from which all other quantities are derived from.

```
symbol : string
    The symbol of the base quantity.
name : string
    The name of the base quantity.
dimension : D
    An instance of the D class, which represents the dimension of the quantity.
```

```
return : Q
```

The created  ${\tt Q}$  instance.

The function creates a global variable of the created base quantity. The name consist of an underscore concatenated with the <code>symbol</code> argument, i.e. the symbol m becomes the global variable \_m.

The name is used for example in the siunitx conversion function, e.g meter will be converted to \meter.

Each quantity has a dimension associated with it. The argument dimension allows any dimension to be associated to base quantities.

#### Example

```
1 Q.defineBase("m", "meter", L)
2 Q.defineBase("kg", "kilogram", M)
```

### Quantity.define(symbol, name, q)

Creates a new derived quantity from an expression of other quantities. Affine quantities like the absolute temperature in celsius are not supported.

```
symbol : string
    Symbol of the base quantity
name : string
    The Name of the derived quantity.
q : physical.Quantity
    The definition of the derived quantity.
return : Quantity
    The created quantity.
```

The function creates a global variable of the created base quantity. The name consist of an underscore concatenated with the symbol argument, i.e. the symbol N becomes the global variable \_N.

The name is used for example in the siunitx conversion function, e.g newton will be converted to \newton.

#### Example

```
1 Q.define("L", "liter", _dm^3)
2 Q.define("Pa", "pascal", _N/_m^2)
3 Q.define("C", "coulomb", _A*_s)
4
5 Q.define("degC", "celsius", _K)
```

### Quantity.defineAlias(symbol, q)

Creates an alias of a quantity.

```
symbol : string
```

The name of the alias.

q: Quantity

The aliased quantity.

```
1 Q.defineAlias("degC_0", 273.15*_degC)
```

## Quantity.definePrefix(symbol,name,factor)

Defines a new prefix.

```
symbol : string
```

Symbol of the base quantity

name: string

Name of the base quantity

factor : number

The factor which corresponds to the prefix

```
1 Q.definePrefix("c", "centi", 1e-2)
2 Q.definePrefix("a", "atto", 1e-18)
```

### Quantity.addPrefix(prefixes, units)

Create several units with prefixes from a given unit.

```
prefixes: string
```

A list of unit symbols.

units: Quantity

A list of quantities.

```
1 Q.addPrefix({"n","u","m","k","M","G"},{_m,_s,_A})
```

### Quantity.to(self,q)

Converts the quantity self to the unit of the quantity q.

```
self: Quantity A quantity.
```

q: Quantity The quantity to wich self will be converted to.

```
1  s = 1.9 * _km
2  print( s:to(_m) )
3  1900 * _m
4
5  T = 10 * _degC
6  print( T:to(_K) )
7  10 * _K
8  print( T:to(_K) )
9  10 * _K
```

### Quantity.tosiunitx(self,param,mode)

Converts the quantity into a siunity string.

### Quantity.isclose(self,q,r)

Checks if this quantity is close to another one. The argument  ${\tt r}$  is the maximal relative deviation.

```
self : Quantity
q : Quantity, Number
r : Number
```

```
1  s_1 = 1.9 * _m
2  s_2 = 2.0 * _m
3  print( s_1:isclose(s_2,0.1) )
4  true
5  print( s_1:isclose(s_2,0.01) )
6  false
```

# Quantity.min(q1, q2, ...)

Returns the smallest quantity of several given ones. The function returns q1 if the Quantities are equal.

```
q1: Quantity, Number, first argument
```

 ${\tt q2}: {\tt Quantity, Number}, {\tt second} \ {\tt argument}$ 

```
1 s_1 = 15 * _m
2 s_2 = 5 * _m
3 print(s_1:min(s_2))
4 5 * m
```

## Quantity.max(q1, q2, ...)

Returns the biggest quantity of several given ones. The function returns  ${\tt q1}$  if the Quantities are equal.

```
q1: Quantity, Number, first argumentq2: Quantity, Number, second argument
```

```
1 s_1 = 15 * _m
2 s_2 = 5 * _m
3 print(s_1:max(s_2))
4 15 * _m
```

### Quantity.abs(q)

Returns the absolute value of the given quantity q.

q: Quantity, Number, argument

```
1 U = -5 * _V
2 print(U)
3 -5 * _V
4 print(U:abs())
5 5 * _V
```

### Quantity.sqrt(q)

Returns the square root of the given quantity.

q: Quantity, Number argument

```
1 A = 25 * _m^2
2 s = sqrt(A)
3 print(s)
```

## Quantity.log(q, base)

Returns the logarithm of the given quantitiy. If no base is given, the natural logarithm is calculated.

 ${\tt q}: {\tt Quantity}, {\tt Number} \ {\tt dimensionless} \ {\tt argument}$ 

base: Quantity, Number dimensionless argument

```
1 I = 1 * _W/_m^2

2 I_0 = 1e-12 * _W/_m^2

3 print(10 * (I/I_0):log(10) * _dB)

4 120 * _dB
```

### Quantity.exp(q)

Returns the value of the exponential function of the given quantitiy.

q: Quantity, Number dimensionless argument

```
1 x = 2 * _1
2 print( x:exp() )
3 7.3890560989307
```

# Quantity.sin(q)

Returns the value of the sinus function of the given quantitiy.

 ${\tt q}: {\tt Quantity}, {\tt Number} \ {\tt dimensionless} \ {\tt argument}$ 

```
1 alpha = 30 * _deg
2 print( alpha:sin() )
3 0.5
```

# Quantity.cos(q)

Returns the value of the cosinus function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1 alpha = 60 * _deg
2 print( alpha:cos() )
3 0.5
```

### Quantity.tan(q)

Returns the value of the tangent function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1 alpha = 45 * _deg
2 print( alpha:tan() )
3 1
```

### Quantity.asin(q)

Returns the value of the arcus sinus function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1 x = 0.5 * _1
2 print( x:asin():to(_deg) )
3 30 * _deg
```

## Quantity.acos(q)

Returns the value of the arcus cosinus function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1  x = 0.5 * _1
2  print( x:acos():to(_deg) )
3  60 * _deg
```

### Quantity.atan(q)

Returns the value of the arcus tangent function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print( x:atan():to(_deg) )
3 45 * _deg
```

## Quantity.sinh(q)

Returns the value of the hyperbolic sine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$\sinh(x) = 0.5 \cdot e^x - 0.5/e^x \quad .$$

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print( x:sinh() )
3 1.1752011936438
```

### Quantity.cosh(q)

Returns the value of the hyperbolic cosine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$\cosh(x) = 0.5 \cdot e^x + 0.5/e^x \quad .$$

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print(x:cosh())
3 1.5430806348152
```

### Quantity.tanh(q)

Returns the value of the hyperbolic tangent function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$
.

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print( x:tanh() )
3 0.76159415595576
```

### Quantity.asinh(q)

Returns the value of the inverse hyperbolic sine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$asinh(x) = \ln\left(x + \sqrt{x^2 + 1}\right) \quad .$$

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print(x:asinh())
3 0.88137358701954
```

### Quantity.acosh(q)

Returns the value of the inverse hyperbolic cosine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$a\cosh(x) = \ln\left(x + \sqrt{x^2 - 1}\right) \quad , x > 1 \quad .$$

 ${\tt q}: {\tt Quantity}, {\tt Number} \ {\rm dimensionless} \ {\rm argument} \ {\rm bigger} \ {\rm than} \ {\rm or} \ {\rm equal} \ {\rm to} \ {\rm one}.$ 

```
1 x = 2 * _1
2 print(x:acosh())
3 1.3169578969248
```

### Quantity.atanh(q)

Returns the value of the inverse hyperbolic cosine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$\operatorname{atanh}(x) = \ln \left( \frac{1+x}{1-x} \right) \quad , -1 < x < 1 \quad .$$

 ${\tt q}: {\tt Quantity}, {\tt Number} \ {\rm dimensionless} \ {\rm argument} \ {\rm with} \ {\rm magnitude} \ {\rm smaller} \ {\rm than} \ {\rm one}.$ 

```
1 x = 0.5 * _1
2 print( x:atanh() )
3 0.54930614433405
```

### 5.2 physical.Dimension

All physical quantities do have a physical dimension. For example the quantity Area has the dimension  $L^2$  (length to the power of two). In the SI-System there are seven base dimensions, from which all other dimensions are derived. Each dimension is represented by an n-tuple, where n is the number of base dimensions. Each physical quantity has an associated dimension object. It is used to check equality and if addition or substraction is allowed.

### Dimension.new(q=nil)

Constructor of the Dimension class.

q: Dimension or string, optional

The name or symbol of the dimension. If q is a dimension, a copy of it is made. If no argument ist given, a dimension zero is created.

return: Dimension
The created Quantity object

#### Example

### 5.3 physical.Unit

The task of this class is keeping track of the unit term. The unit term is a fraction of units. The units in the enumerator and denominator can have an exponent.

#### Unit.new(u=nil)

Copy Constructor. It copies a given unit object. If nothing is given, an empty unit is created.

u: Unit

The unit object which will be copied.

return : Unit

The created Unit object

### Unit.new(symbol, name, prefixsymbol=nil, prefixname=nil)

Constructor. A new Unit object with symbol is created. The prefixsymbol and prefixname are optional.

symbol: String

The symbol of the unit.

name: String

The name of the unit.

prefixsymbol : String

The optional symbol of the prefix.

prefixname : String

The optional name of the prefix.

return: Unit

The created Unit object

### Unit.tosiunitx(self)

The unit term will be compiled into a string, which the LaTeX package siunitx can understand.

return: String

The siunity representation of the unit term.

### 5.4 physical.Number

It does arithmetics with gaussian error propagation. A number instance has a mean value called  ${\tt x}$  and an uncertainty called  ${\tt dx}$ .

### Number.new(n=nil)

This is the copy Constructor. It copies a given number object. If n is nil, an instance representing number zero with uncertainty zero is created.

#### n: Number

The number object to be copied.

return : Number

The created Number instance.

### Number.new(x, dx)

This constructor, creates a new instance with mean value  ${\tt x}$  and uncertainty  ${\tt dx}.$ 

x: number

mean value

dx : number

uncertainty value

return : Number

The created Number instance.

#### Example

```
1 n = N(12,0.1)
2 print(n)
```

### Number.new(str)

This constructor creates a new instance from a string. It can parse strings of the form 3.4, 3.4e-3, 5.4e-3 +/- 2.4e-6, 5.45(7)e-23.

### Parameters / Return

 ${\tt str}: {\tt string}$ 

The number as a string.

return : Number

The created Number object

### Example

```
1    n_1 = N("12.3e-6")
2    print(n_1)
3
4    n_2 = N("12 +/- 0.1")
5    print(n_2)
6
7    n_3 = N("12.0(1)")
8    print(n_3)
```

### Number.mean(n)

Returns the mean value

### Parameters / Return

return: number
The mean value

# Number.uncertainty(n)

Returns the uncertainty value

### Parameters / Return

return : number

The uncertainty value

### Number.abs(n)

Returns the absolute value of the number.

### Parameters / Return

return: number

The absolute value

### Number.sqrt(n)

Returns the square root of the number.

### Parameters / Return

return: number
The square root

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# Index

acre _ac, 18	furlong _fur, 18
amperehour _Ah, 17	
amperesecond _As, 17	gallon _gal, 18
angstrom _angstrom, 16	gill <b>_gi</b> , 18
arcminute _arcmin, 14	gradian _gon, 16
arcsecond _arcsec, 14	grain _gr, 19
are _are, 16	gramoftnt _g_TNT, 17
astronomicalunit _au, 16	gravitationalconstant _Gc, 11
atomicmassunit _u, 11	gray _Gy, 14
avogadronumber _N_A, 12	
/	hand _hh, 18
bar _bar, 17	hectare _hectare, 14
barn _barn, 16	henry _H, 13
becquerel _Bq, 14	hertz _Hz, 13
bitpersecond _bps, 17	hour _h, 14
bohrmagneton _u_B, 11	hundredweight _cwt, 19
boltzmannconstant _k_B, 12	& <b>=</b> ,
byte _B, 17	inch _in, 18
	international calorie _cal_IT, 17
cable _cbl, 18	,
celsius _degC, 13	joule _J, 13
chain _ch, 18	
coulomb _C, 13	katal _kat, 14
cup _cup, 18	kilopond _kp, 17
1 - 1/	knot _kn, 18
day _d, 14	
decibel _dB, 17	league _lea, 18
degree _deg, 14	lightsecond _ls, 16
dram _dr, 19	lightyear _ly, 16
	liter _L, 14
electronmagneticmoment _u_e, 11	longton _ton, 19
electronmass _m_e, 11	lumen _lm, 13
electronvolt _eV, 17	lux _lx, 13
elementarycharge _e, 11	
eulersnumber _E, 11	metrictablespoon _Tbsp, 16
	metricteaspoon _tsp, 16
farad _F, 13	mile _mi, 18
fathom _ftm, 18	millimeterofmercury _mmHg, 17
fermi_fermi, 16	minute _min, 14
finestructureconstant _alpha, 11	molargasconstant _R, 12
fluiddram _fl_dr, 18	
fluidounce _fl_oz, 18	nauticalleague _nlea, 18
foot _ft, 18	nauticalmile _nmi, 18

neutronmagneticmoment _u_n, 11	sievert _Sv, 14
neutronmass _m_n, 11	spat _sp, 16
newton _N, 13	speedoflight _c, 11
nibble _nibble, 17	standardatmosphere _atm, 17
nomjovianeqradius _Re_J_nom, 15	standardgravity _g_0, 12
nomjovianmassparam _GM_J_nom,	stefanboltzmannconstant _sigma, 12
15	steradian _sr, 13
nomjovianpolradius _Rp_J_nom, 15	stone _st, 19
nomsolefftemperature _T_S_nom, 15	svedberg _svedberg, 16
nomsolirradiance _S_S_nom, 15	svedberg _svedberg, 10
	technicalatmosphere _at, 17
nomsolluminosity _L_S_nom, 15	
nomsolmassparam _GM_S_nom, 15	tesla _T, 13
nomsolradius _R_S_nom, 15	thermochemicalcalorie _cal, 17
nomterreqradius _Re_E_nom, 15	thou _th, 18
nomterrmassparam _GM_E_nom, 15	tonne_t, 14
nomterroolradius _Rp_E_nom, 15	tonoftnt _t_TNT, 17
nuclearmagneton _u_N, 11	torr _Torr, 17
1 0 10	turn _tr, 16
ohm _Ohm, 13	
ounce _oz, 19	uscup _cup_US, 20
pargos no 16	usfluiddram _fl_dr_US, 20
parsec_pc, 16	usfluidounce _fl_oz_US, 20
partsperbillion _ppb, 17	usgallon _gal_US, 20
partspermillion _ppm, 17	usgill _gi_US, 20
partsperquadrillion _ppq, 17	ushundredweight _cwt_US, 21
partspertrillion _ppt, 17	uspint _pint_US, 20
pascal Pa, 13	usquart _qt_US, 20
percent _percent, 17	usquarter _qtr_US, 21
permille _permille, 17	ussurveyacre _ac_US, 20
pi _Pi, 11	ussurveycable _cbl_US, 20
pica _pica, 18	ussurveychain _ch_US, 20
pint _pint, 18	ussurveyfathom _ftm_US, 20
planckconstant _h_P, 11	ussurveyfoot _ft_US, 20
point _pt, 18	ussurveyfurlong _fur_US, 20
pound _1b, 19	9 :
protonmagneticmoment _u_p, 11	ussurveyhand hh_US, 20
protonmass _m_p, 11	ussurveyinch _in_US, 20
	ussurveyleague _lea_US, 20
quart _qt, 18	ussurveylink _li_US, 20
quarter _qtr, 19	ussurveymile _mi_US, 20
	ussurveyrod _rd_US, 20
radian _rad, 13	ussurveyyard _yd_US, 20
reducedplanckconstant _h_Pbar, 11	ustablespoon _Tbsp_US, 20
rod _rd, 18	usteaspoon _tsp_US, 20
rydbergconstant Ry, 11	uston _ton_US, 21
•	
siemens _S, 13	vacuumpermeability _u_0, 11

vacuum permitivity \_e\_0, 11 volt \_V, 13 voltampere \_VA, 17

 $\begin{array}{c} \text{watt $\_$W, $13$} \\ \text{watthour $\_$Wh, $17$} \end{array}$ 

 $\begin{array}{l} {\rm wattsecond\ \_Ws,\ 17} \\ {\rm weber\ \_Wb,\ 13} \\ {\rm week\ \_wk,\ 16} \end{array}$ 

yard \_yd, 18 year \_a, 16