The LUA-PHYSICAL library

$Version\ 0.1$

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Abstract

lua-physical is a pure Lua library which provides functions and object for doing computation with physical quantities. It has been written to simplify the creation problem sets. The package provides units of the SI and the imperial system. Furthermore an almost complete set of international currencies are supported, however without online exchange rates. In order to display the numbers with measurement uncertainties, the package is able to perform gaussian error propagation.

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1 Introduction

The author of this package is a teacher at the high school Kantonsschule Zug in Switzerland. The main use of this package is to write physics problem sets. LuaLATEXdoes make it possible to integrate physical calculations directly. The package has been in use since 2016. Many bugs have been found and fixed. Nevertheless it still is possible, that some were not found yet. Therefore the author recommends not to use this package industry or science. If one does so, it's the responsability of the user to check results for plausability. If the user finds some bugs, they can be reported at github.com or directly to the author (thomas.jenni(at)ksz.ch).

2 Loading

This package is a pure Lua library. Therefore one has to require it explicitly by calling require("physical"). For printing results, the siunitx package can be used. It's recommended to define a macro like \q to convert the lua quantity object to a siunitx expression.

The following Latex preambel loads the lua-physical package and creates a macro \q for printing physical quantities.

Listing 1: basic preamble

```
\usepackage{lua-physical}
     \usepackage{siunitx}
     % configure siunitx
     \sisetup{
       output-decimal-marker = {.},
       per-mode = symbol,
       separate-uncertainty = true,
       add-decimal-zero = true,
       exponent-product = \cdot,
       round-mode = off
     % load lua-physical package
     \begin{luacode*}
16
       physical = require("physical")
       N = physical.Number
     \end{luacode*}
     % print physical quantities
     \directlua{tex.print(physical.Quantity.tosiunitx(#1, "scientific-
             notation=fixed,exponent-to-prefix=false"))}%
     }
```

2.1 Dependencies

This is a standalone package. If a pretty print to LuaLATEX is wanted, the package siunitx sould be installed.

3 Usage

Given the basic preamble, units can be used in lua code directly. By convention, all units have an underscore in front of them, i.e. Meter is _m, Second is _s. All available units are listed in chapter 4. The Result of the calculation can be printed to Lual*TFX by using the macro \q{}.

Listing 2: The velocity of a car.

```
1 \begin{luacode}
2     s = 10 * _m
3     t = 2 * _s
4     v = s/t
5 \end{luacode}
6
7 A car travels $\q{s}$ in $\q{t}$. calculate its velocity.
8     $$
9     v=\frac{s}{t} = \frac{\q{s}}{\q{t}} = \q{v}
10 $$$
```

A car travels 10 m in 2 s. Calculate its velocity.

$$v = \frac{s}{t} = \frac{10 \,\mathrm{m}}{2 \,\mathrm{s}} = 5 \,\mathrm{m/s}$$

In the above listing 2, the variable s stands for displacement and has the unit meter $_m$. The variable t stands for time and is given in second $_s$. If mathematical operations are done on them, new physical quantities are created. In the problem above, the velocity v is calculated by dividing s by t. The instance v has the derived unit m/s. By using the macro q all quantities can be printed to the LualATeX code directly.

3.1 Unit conversion

Very often the result of a calculation is needed in different unit, than the given quantities are. In the following listing 3 the task is to calculate the volume of a cuboid with lengths given in different units. If the volume is calculated by multipling all three lengths, the unit of the result is cm mm m. If the unit cm³ is preferred, it has to be converted explicitly. The conversion function is called to() and is available on all physical quantitiy instances. At first this looks a bit cumbersome. The reason of this behaviour is, that the software is not able to guess the unit of the result. In many cases, like in the example here, it's not clear

what unit the result sould have. Therefore the user has always to give the target unit explicitly.

Listing 3: The volume of a cuboid.

```
1  \begin{luacode}
2    a = 12 * _cm
3    b = 150 * _mm
4    c = 1.5 * _m
5
6    V = a*b*c
7  \end{luacode}
8
9  Find the volume of a rectangular cuboid with lengths $\q{a}$,
10  $\q{b}$ and $\q{c}$.
11  $$
12    V= a \cdot b \cdot c
13    = \q{a} \cdot \q{b} \cdot \q{c}
14    = \q{V}
15    = \underset{q{V:to(_dm^3)}}
16  $$
```

Find the volume of a rectangular cuboid with lengths $12 \, \mathrm{cm}$, $150 \, \mathrm{mm}$ and $1.5 \, \mathrm{m}$.

```
V = a \cdot b \cdot c = 12 \,\mathrm{cm} \cdot 150 \,\mathrm{mm} \cdot 1.5 \,\mathrm{m} = 2700 \,\mathrm{cm} \,\mathrm{mm} \,\mathrm{m} = 27 \,\mathrm{dm}^3
```

3.1.1 Temperature Conversion

In the following problem, listing 4, the task is to convert a temperature given in the unit degree Celsius to Kelvin. As can be seen in the listing, the conversion function has two parameters.

The first argument is the target unit. The second is a boolean that tells the tofunction to call a unit specific conversion function. By default the second argument is false.

Most units do not have a conversion function. Exceptions are the unit degree Celsius <code>_degC</code> and degree Fahrenheit <code>_degF</code>. These units are ambigous and can be interpreted as temperature differences or as an absolute temperatures. In the latter case, the conversion to base units is not a linear, but an affine transformation. This is because degree Celsius and degree Fahrenheit scales have their zero points at different temperatures compared to the unit Kelvin. Therefore these units have their own conversion functions.

By default _degC and _degF units are standing for temperature differences. If one wants to have it converted absolutely, the conversion function to() should have the second argument set to true.

Listing 4: Temperature conversion.

```
1 \begin{luacode}
```

```
2  T = 20 * _degC
3  \end{luacode}
4
5  A thermometer shows $\q{T}$. Converte this quantity to Kelvin.
6  $$
7   T = \q{T:to(_K)} + \q{273.15 * _K}
8   = \q{T:to(_K,true)}
9  $$
```

A thermometer shows 20 °C. Converte this quantity to Kelvin.

$$T = 20 \,\mathrm{K} + 273.15 \,\mathrm{K} = 293.15 \,\mathrm{K}$$

3.1.2 Uncertainty

The package supports uncertainty propagation. To create a number with an uncertainty, an instance of physical.Number has to be created, see listing 5. It has to be remembered, that N is a alias for physical.Number. The first argument of the constructor N(mean, uncertainty) is the mean value and the second one the uncertainty of the measurement. If the proposed preamble is used, the uncertainty is by default seperated from the mean value by a plus-minus sign. For the uncertainty propagation the gaussian formula

$$\Delta f = \sqrt{\left(\frac{\partial f}{x_1} \cdot \Delta x_1\right)^2 + \ldots + \left(\frac{\partial f}{x_n} \cdot \Delta x_2\right)^2}$$

is used. This formula is a good estimation for the uncertainty Δf , if the quantities x_1, \ldots, x_n the function f depends on, have no correlation. Further, the function f has to behave linear, if the quantities x_i are changed in the range of their uncertainties.

Listing 5: Uncertainty in area calculation.

```
1 \begin{luacode}
2     a = N(2,0.1) * _m
3     b = N(3,0.1) * _m
4
5     A = (a*b):to(_m^2)
6 \end{luacode}
7
8     Calculate the area of a rectangle with lengths $\q{a}$ and $\q{b}$.
9     $$
10     A = a \cdot b
11     = \q{a} \cdot \q{b}
12     = \ulline{\q{A}}
13     $$$
```

Calculate the area of a rectangle with lengths $(2.00 \pm 0.10) \,\mathrm{m}$ and $(3.00 \pm 0.10) \,\mathrm{m}$.

$$A = a \cdot b = (2.00 \pm 0.10) \,\mathrm{m} \cdot (3.00 \pm 0.10) \,\mathrm{m} = (6.0 \pm 0.4) \,\mathrm{m}^2$$

Instead of printing always the uncertainties, one can use the uncertainty calculation to provide significant numbers.

In the following problem, listing 6, the task is to calculate the volume of an ideal gas. Given are pressure p in _bar, amount of substance n in _mol and temperature T in degree celsius _degC. In order to do the calculation, one has to convert T, which is given as an absolute temperature in degree celsius to the base unit Kelvin first. By setting N.omitUncertainty = true, all uncertainties are not printed.

Listing 6: Volume of an ideal gas.

```
1  \begin{luacode}
2    N.omitUncertainty = true
3    p = N(1.013,0.0001) * _bar
4    n = N(1,0.01) * _mol
5    T = N(30,0.1) * _degC
6
7    V = ( n * _R * T:to(_K,true) / p ):to(_L)
8  \end{luacode}
9
10    An ideal gas ($\q{n}$) has a pressure of $\q{p}$ and a temperature of $\q{T}$. Calculate the volume of the gas.
11    $$
12    V = \frac{ \q{n} \cdot \q{_R} \cdot \q{T:to(_K,true)} }{\q{p}} }
13    = \q{V}
14    = \unuline{\q{V}}
15    $$$
```

An ideal gas (1.0 mol) has a pressure of 1.013 bar and a temperature of $30\,^{\circ}\mathrm{C}$. Calculate the volume of the gas.

$$V = \frac{1.0\,\text{mol} \cdot 8.31\,\text{J/(mol\,K)} \cdot 303\,\text{K}}{1.013\,\text{bar}} = \underline{25\,\text{L}}$$

4 Supported Units

In this chapter, all supported units are listed. Subchapter 4.1 lists the seven base units of the International System of Units (SI) and three additional ones. In subchapter 4.2 mathematical and physical constants are defined. The subchapter 4.3 contains all derived units from the SI system. Subchapter 4.4 lists units, which are common but outside of the SI system. The subchapters 4.5 and 4.6 is dedicated to imperial and U.S. customary units. The last subchapter 4.7 containts international currencies.

4.1 Base Units

Quantity	Unit	Symbol	Dim.	Definition
length	meter	_m	L	The distance light travels in vacuum during $1/299792458$ second.
mass	kilogram	_kg	M	The mass of the international protoype of the kilogram.
time	second	_s	Т	Is 9 192 631 770 times the period of the radiation from the transition between the two hyperfine levels of the ground state of caesium-133.
electric current	ampere	_A	I	The constant current which, if maintained in two straight parallel conductors of infinte length, of negligible circular crosss-section, and placed 1 m apart in vacuum, would produce between these conductors a force equal to $2 \cdot 10^{-7}$ N/m.
thermody- namic temperature	kelvin	_K	Θ	Is the fraction $1/273.16$ of the thermodynamic temperature of the triple point of water.
amount of substance	mole	_mol	N	Amount of substance that contains as many particles as there are atoms in 0.012 kg of carbon-12.
luminous intensity	candela	_cd	J	The luminous intensity, in a given direction, of a source that emits monochromatic radiation of frequenc $540 \cdot 10^{12} \mathrm{Hz}$ and has a radiant intensity in that direction of $(1/683) \mathrm{W/sr}$

Quantity	entity Unit Symbol Dim.		Dim.	Definition			
number	_	_1	1	The dimensionless number one.			
information	bit	_bit	В	The smallest amount of information.			
currency	euro	_EUR	\mathbf{C}	The value of the currency Euro.			

Table 1: Base units of the International System of Units (SI), information, currency and the dimensionless number one.

4.2 Constants

Name	Symbol	Dim.	Definition
pi	_Pi	1	$3.1415926535897932384626433832795028841971 * _1$
eulersnumber	щ	1	2.7182818284590452353602874713526624977572 * _1
speedoflight	o _l	$ m L^1 T^{-1}$	299792458 * _m/_s
gravitationalconstant	၁၅၂	$L^{3} M^{-1} T^{-2}$	$N(6.67408e-11,3.1e-15) * _m^3/(_kg*_s^2)$
planckconstant	_h_P	$ m L^2~M^1~T^{-1}$	$N(6.626070040e-34, 8.1e-42) * _J*_s$
${\tt reducedplanckconstant}$	_h_Pbar	$ m L^2~M^1~T^{-1}$	_h_P/(2*Pi)
elementarycharge	Φ	$\mathrm{T}^1\mathrm{I}^1$	N(1.6021766208e-19, 9.8e-28) * _C
vacuumpermeability	0 ⁻ n-	$L^1 \mathrm{M}^1 \mathrm{T}^{-2} \mathrm{I}^{-2}$	$4e-7*Pi * _N/_A^2$
vacuumpermitivity	0 - 0	$L^{-3} \mathrm{M}^{-1} \mathrm{T}^4 \mathrm{I}^2$	1/(_u_0*_c^2)
atomicmassunit	n_	M^1	N(1.66053904e-27, 2e-35) * _kg
electronmass	e E	M^1	N(9.10938356e-31, 1.1e-38) * _kg
protonmass	ď-m-	M^1	N(1.672621898e-27, 2.1e-35) * _kg
neutronmass	u-m-	M^1	N(1.674927471e-27, 2.1e-35) * _kg
bohrmagneton	_u_B	$\mathrm{L}^2\mathrm{I}^1$	_e*_h_Pbar/(2*_m_e)
nuclearmagneton	N-n-	$\mathrm{L}^2\mathrm{I}^1$	_e*_h_Pbar/(2*_m_p)

Name	Symbol	Dim.	Definition
electronmagneticmoment	e n -	$\mathrm{L}^2\mathrm{I}^1$	$N(-928.4764620e-26,5.7e-32) * _J/_T$
protonmagneticmoment	d-n-	$\mathrm{L}^2\mathrm{I}^1$	$N(1.4106067873e-26,9.7e-35) * _J/_T$
neutronmagneticmoment	u-n-	$\mathrm{L}^2\mathrm{I}^1$	$N(-0.96623650e-26,2.3e-26) * _J/_T$
finestructureconstant	_alpha	1	_u_0*_e^2*_c/(2*_h_P)
rydbergconstant	_Ry	L^{-1}	_alpha^2*_m_e*_c/(2*_h_P)
avogadronumber	_N_A	N^{-1}	N(6.022140857e23, 7.4e23)/_mol
boltzmannconstant	_k_B	$\rm L^2 M^1 T^{-2} \Theta^{-1}$	$N(1.38064852e-23, 7.9e-23) * _J/_K$
molargasconstant	ж _.	$\rm L^2 M^1 T^{-2} \Theta^{-1} N^{-1}$	N(8.3144598, 4.8e-6) * _J/(_K*_mol)
stefanboltzmannconstant	_sigma_	$\rm L^2 M^1 T^{-2} \Theta^{-1} N^{-1}$	Pi^2*_k_B^4/(60*_h_Pbar^3*_c^2)
standardgravity	-g-0	$ m L^1T^{-2}$	9.80665 * _m/_s^2
nominalsolarradius	_R_Sun	L^1	6.957e8 * _m
nominalsolarirradiance	_S_Sun	$ m M^{1}T^{-3}$	1361 * _W/_m^2
nominalsolarluminosity	_L_Sun	$\mathrm{L}^2\mathrm{M}^1\mathrm{T}^{-3}$	3.828e26 * _W
nominalsolareffectivetemperature	_T_Sun	Θ^1	5772 * _K
nominalsolarmassparameter	_GM_Sun	$ m L^3T^{-2}$	1.3271244e20 * _m^3 * _s^-2
nominalterrestrialequatorialradius	_Re_E	L^1	6.3781e6 * _m
${\tt nominalterrestrialpolarradius}$	_Rp_E	L^1	6.3568e6 * _m
nominalterrestrialmassparameter	_GM_E	$ m L^3T^{-2}$	3.986004e14 * _m^3 * _s^-2
nominaljovianequatorialradius	_Re_J	L^1	7.1492e7 * _m
nominaljovianpolarradius	_Rp_J	L^1	6.6854e7 * _m
nominaljovianmassparameter	_GM_J	$ m L^3T^{-2}$	1.2668653e17 * _m^3*_s^-2

Table 2: Physical constants.

4.3 Derived Units of the International System of Units (SI)

All units in this section are derived from the SI base units, $[1,\,123\text{-}129].$

Quantity	Unit	Symbol	Dimension	Definition
plane angle	radian	_rad	1	_1
solid angle	steradian	_sr	1	_rad^2
frequency	hertz	_Hz	T^{-1}	1/_s
force	newton	_N	$ m M~L~T^{-2}$	_kg*_m/_s^2
pressure	pascal	_Pa	${ m M}{ m L}^{-1}{ m T}^{-2}$	_N/_m^2
energy	joule	_J	${ m M}{ m L}^2{ m T}^{-2}$	_N*_m
power	watt	_W	${ m M}{ m L}^2{ m T}^{-3}$	_J/_s
electric charge	coulomb	_C	ΤΙ	_A*_s
electric potential difference	volt	_V	${ m M}{ m L}^2{ m T}^{-3}{ m I}^{-1}$	_J/_C
capacitance	farad	_F	$L^{-2} M^{-1} T^4 I^2$	_C/_V
electric resistance	ohm	_Ohm	$L^2 M T^{-3} I^{-2}$	_V/_A
electric conductance	siemens	_S	$L^{-2} M^{-1} T^3 I^2$	_A/_V
magnetic flux	weber	_Wb	$L^2 \mathrm{M} \mathrm{T}^{-2} \mathrm{I}^{-1}$	_V*_s
magnetic flux density	tesla	_T	${ m M}~{ m T}^{-2}{ m I}^{-1}$	_V*_s
inductance	henry	_H	$L^2 M T^{-2} I^{-2}$	_Wb/_A
Celsius temperature	degree Celsius	_degC	Θ	_K
luminous flux	lumen	_lm	J	_cd*_sr
illuminance	lux	_lux	$\mathrm{L}^{-2}\mathrm{J}$	_lm/_m^2

Quantity	Unit	Symbol	Dimension	Definition
activity	becquerel	_Bq	T^{-1}	1/_s
absorbed dose	gray	_Gy	$L^2 T^{-2}$	_J/_kg
dose equivalent	sievert	_Sv	$L^2 T^{-2}$	_J/_kg
catalytic activity	katal	_kat	$\mathrm{T}^{-1}\mathrm{N}$	_mol/_s

Table 3: Derived units of the International System of Units (SI)

4.4 Units outside of the International System of Units (SI)

There are a few units with dimension 1. The unit Bel is only available with prefix decibel, because $_B$ is the unit byte.

Quantity	Unit	Symbol	Dimension	Definition
	percent %	_percent	1	1e-2*_1
	permille $\%$	_permille	1	1e-3*_1
	parts-per-million	_ppm	1	1e-6*_1
	parts-per-billion	_ppb	1	1e-9*_1
	parts-per-trillion	_ppt	1	1e-12*_1
	parts-per-quadrillion	_ppq	1	1e-15*_1
	decibel	_dB	1	_1
plane angle	degree	_deg	1	(Pi/180)*_rad
	arc minute	_arcmin	1	_deg/60
	arc second	_arcsec	1	_arcmin/60
	gradian	_gon	1	(Pi/200)*_rad
	turn	_tr	1	2*Pi*_rad
solid angle	spat	_sp	1	4*Pi*_sr
length	astronomical unit	_au	L	149597870700*_m
	lightyear	_ly	L	_c*_a
	parsec	_pc	L	(648000/Pi)*_au
	angstrom	_angstrom	L	1e-10*_m
	fermi	_fermi	L	1e-15*_m
area	are	_ar	L^2	1e2*_m^2
	hectare	_hectare	L^2	1e4*_m^2
	barn	_barn	L^2	1e-28*_m^2
volume	liter	_L	L^3	0.001*_m^3
	metric teaspoon	_tsp	L^3	0.005*_L
	metric tablespoon	_Tbsp	L^3	3*_tsp

Quantity	Unit	Symbol	Dimension	Definition
time	minute	_min	Т	_60*_s
	hour	_h	Τ	_60*_min
	day	_d	Τ	_24*_h
	week	_wk	Τ	_7*_d
	year	_a	Τ	365.25*_d
	svedberg	_svedberg	Τ	1e-13*_s
mass	tonne	_t	M	1000*_kg

Table 4: Units outside of the International System of Units (SI)

4.5 Imperial Units

Quantity	Unit	Symbol	Dimension	Definition
length	inch	_in	L	0.0254*_m
	thou	_th	L	0.001*_in
	pica	_pica	L	_in/6
	point	_pt	L	_in/72
	hand	_hh	L	4*_in
	foot	_ft	L	12*_in
	yard	_yd	L	3*_ft
	rod	_rd	L	5.5*_yd
	chain	_ch	L	4*_rd
	furlong	_fur	L	10*_ch
	mile	_mi	L	8*_fur
	league	_lea	L	3*_mi
	nautical mile	_nmi	L	1852 * _m
	nautical league	_nlea	L	3*_nmi
	cable	_cbl	L	_nmi/10
	fathom	_ftm	L	6*_ft
velocity	knot	_kn	$\mathrm{L}^1\mathrm{T}^{-1}$	_nmi/_h
area	acre	_ac	L^2	43560*_ft^2
volume	gallon	_gal	L^3	4.54609*_L
	quart	_qt	L^3	_gal/4
	pint	_pint	L^3	_qt/2
	cup	_cup	L^3	_pint/2
	gill	_gi	L^3	_pint/4
	fluid ounce	_fl_oz	L^3	_gi/5
	fluid dram	_fl_dr	L^3	_fl_oz/8

Quantity	Unit	Symbol	Dimension	Definition
mass	grain	_gr	M	64.79891*_mg
	pound	_lb	M	7000*_gr
	ounce	_oz	M	_lb/16
	dram	_dr	M	_1b/256
	stone	_st	M	14*_lb
	quarter	_qtr	M	2*_st
	${\bf hundred weight}$	_cwt	M	4*_qtr
	long ton	_ton	M	20*_cwt

Table 5: Imperial units

4.6 U.S. customary units

In the U.S., the length units are bound to the meter differently than in the imperial system. The followin definitions are taken from https://en.wikipedia.org/wiki/United_States_customary_units.

Quantity	Unit	Symbol	Dimension	Definition
length	U.S. survey inch	_in_US	L	_m/39.37
	U.S. survey hand	_hh_US	L	4*_in_US
	U.S. survey foot	_ft_US	L	3*_hh_US
	U.S. survey link	_li_US	L	0.66*_ft_US
	U.S. survey yard	_yd_US	L	3*_ft_US
	U.S. survey rod	_rd_US	L	5.5*_yd_US
	U.S. survey chain	_ch_US	L	4*_rd_US
	U.S. survey furlong	_fur_US	L	10*_ch_US
	U.S. survey mile	_mi_US	L	8*_fur_US
	U.S. survey league	_lea_US	L	3*_mi_US
	U.S. survey fathom	_ftm_US	L	72*_in_US
	U.S. survey cable	_cbl_US	L	120*_ftm_US
area	U.S. acre	_ac_US	L^2	_ch_US*_fur_US
volume	U.S. gallon	_gal_US	L^3	231*_in^3
	U.S. quart	_qt_US	L^3	_gal_US/4
	U.S. pint	_pint_US	L^3	_qt_US/2
	U.S. cup	_pint_US	L^3	_pint_US/2
	U.S. gill	_gi_US	L^3	_pint_US/4
	U.S. fluid ounce	_fl_oz_US	L^3	_gi_US/4
	U.S. table spoon	_Tbsp_US	L^3	_fl_oz_US/2
	U.S. tea spoon	_tsp_US	L^3	_Tbsp_US/3
	U.S. fluid dram	_fl_dr_US	L^3	_fl_oz_US/8

Quantity	Unit	Symbol	Dimension	Definition
mass	U.S. quarter	_qtr_US	L^3	25*_1b
	U.S. hundredweight	_qtr_US	L^3	4*_qtr_US
	U.S. short ton	_ton_US	L^3	20*_cwt_US

Table 6: U.S. customary units

4.7 International Currencies

Quantity	Unit	Symbol	Dimension	Definition
currency	Afghan afghani	_AFN	С	0.012*_EUR
	Albanian lek	_ALL	C	0.008*_EUR
	Armenian Dram	_AMD	C	0.0018*_EUR
	Angolan Kwanza	_AOA	C	0.0028*_EUR
	Argentine Peso	_ARS	C	0.021*_EUR
	Australian dollar	_AUD	C	0.63*_EUR
	Azerbaijani Manat	_AZN	C	0.63*_EUR
	Bosnian Mark	_BAM	C	0.51*_EUR
	Bangladeshi Taka	_BDT	C	0.011*_EUR
	Burundian Franc	_BIF	C	0.00049*_EUR
	U.S. dollar	_USD	C	0.89*_EUR
	Japanese yen	_JPY	C	0.008*_EUR
	British pound	_GBP	C	1.17*_EUR
	Canadian dollar	_CAD	C	0.66*_EUR
	Swiss franc	_CHF	C	0.88*_EUR
	Chinese yuan	_CNY	\mathbf{C}	0.13*_EUR
	Swedish krona	_SEK	\mathbf{C}	0.094*_EUR
	New Zealand dollar	_NZD	C	0.60*_EUR

Table 7: Currency units based on exchange rates from 7.3.2019, 21:00 UTC.

5 Lua Documentation

In this chapter, the following shortcuts will be used.

```
1 local D = physical.Dimension
2 local U = physical.Unit
3 local N = physical.Number
4 local Q = physical.Quantity
```

The term number refers to a lua integer or a lua float number. By string a lua string is meant and by bool a lua boolean.

5.1 physical.Quantity

The quantity class is the main part of the library. Each physical Quantity and all units are represented by an instance of this class.

Q.new(q=nil)

Copy Constuctor

Parameters

```
    q: Q or number, optional
        Optional argument is either Q, a number or nil.
    return: Q
    The created Q instance
```

Note

As an argument it takes Q, number or nil. If Q is given, a copy of it is made and returned. If a number is given, the function creates a dimeensionless quantity with that value. In the case nil is given, the quantity _1 is returned.

Example

```
1 myOne = Q()
2 myNumber = Q(42)
3 myLength = Q(73*_m)
```

Q.defineBase(symbol,name,dimension)

This function is used to declare the base units. Units are represented as Q instances.

Parameters

symbol: string

symbol of the base quantity

name: string

name of the base quantity

dimension: D

Instance of the ${\tt D}$ class, which represents the dimension of the

 $\begin{array}{c} \text{quantity.} \\ \text{return}: \textbf{Q} \end{array}$

The created Q instance.

Note

The function creates a global variable, an underscore concatenated with the symbol argument, e. g. m becomes the global variable _m.

The name is used for example in the siunitx conversion function, e.g meter will be converted to \meter.

Each quantity has a dimension associated with it. The argument dimension allows any dimension to be associated to base quantities. By default, the SI convention is used.

Example

```
1 Q.defineBase("m", "meter", L)
2 Q.defineBase("kg", "kilogram", M)
```

Quantity.define(symbol, name, q, tobase=nil, frombase=nil)

Creates a new derived unit from an expression of other units. For affine quantities like the temperature in celcius, one can give convertion functions to and from base units.

Parameters

symbol : string

Symbol of the base quantity

name: string

Name of the base quantity

q: physical.Quantity
Definition of the unit

tobase: function, optional

to convert a quantity to base units

frombase: function, optional

to convert a quantity from the base units

```
return: Quantity
The defined quantity
```

Examples

```
1  Q.define("L", "liter", _dm^3)
2  Q.define("Pa", "pascal", _N/_m^2)
3  Q.define("C", "coulomb", _A*_s)
4
5  Q.define(
6    "degC",
7    "celsius",
8     _K,
9    function(q)
10      q.value = q.value + 273.15
11      return q
12    end,
13    function(q)
14      q.value = q.value - 273.15
15    return q
16    end
17 )
```

Quantity.definePrefix(symbol,name,factor)

Defines a new prefix.

```
symbol : string, Symbol of the base quantity
name : string, Name of the base quantity
factor : number, the factor which corresponds to the prefix
```

```
1 Q.definePrefix("c", "centi", 1e-2)
2 Q.definePrefix("a", "atto", 1e-18)
```

Quantity.addPrefix(prefixes, units)

Create several units with prefixes from a given unit.

```
prefixes: string, list of unit symbols
units: Quantity, list of quantities

1  Q.addPrefix({"n","u","m","k","M","G"},{_m,_s,_A})
```

Quantity.to(self,q,usefunction=false)

Converts the quantity self to the unit of the quantity q. If the boolean usefunction is true, the convertion function is used for conversion.

```
q: Quantity
usefunction: Bool

1    s = 1.9 * _km
2    print( s:to(_m) )
3    1900 * _m
4
5    T = 10 * _degC
6    print( T:to(_K) )
7    10 * _K
8    print( T:to(_K,true) )
9    283.15 * _K
```

self: Quantity

self: Quantity

Quantity.tosiunitx(self,param,mode)

Converts the quantity into a siunitx string.

Quantity.isclose(self,q,r)

Checks if this quantity is close to another one. The argument ${\tt r}$ is the maximal relative deviation.

```
self : Quantity
q : Quantity, Number
r : Number
```

```
1  s_1 = 1.9 * _m
2  s_2 = 2.0 * _m
3  print( s_1:isclose(s_2,0.1) )
4  true
5  print( s_1:isclose(s_2,0.01) )
6  false
```

Quantity.min(q1, q2, ...)

Returns the smallest quantity of several given ones. The function returns q1 if the Quantities are equal.

```
{\tt q1:Quantity,Number}, {\tt first\ argument}
```

 ${\tt q2}: {\tt Quantity, Number}, {\tt second} \ {\tt argument}$

```
1 s_1 = 15 * _m
2 s_2 = 5 * _m
3 print(s_1:min(s_2))
4 5 * m
```

Quantity.max(q1, q2, ...)

Returns the biggest quantity of several given ones. The function returns **q1** if the Quantities are equal.

```
{\tt q1:Quantity,Number}, \ {\tt first\ argument}
```

q2: Quantity, Number, second argument

```
1 s_1 = 15 * _m
2 s_2 = 5 * _m
3 print(s_1:max(s_2))
4 15 * _m
```

Quantity.abs(q)

Returns the absolute value of the given quantity q.

q: Quantity, Number, argument

```
1 U = -5 * _V
2 print(U)
3 -5 * _V
4 print(U:abs())
5 5 * _V
```

Quantity.sqrt(q)

Returns the square root of the given quantity.

q: Quantity, Number argument

```
1 A = 25 * _m^2
2 s = sqrt(A)
3 print(s)
```

Quantity.log(q, base)

Returns the logarithm of the given quantitiy. If no base is given, the natural logarithm is calculated.

 ${\tt q}:{\tt Quantity}, {\tt Number} \ {\tt dimensionless} \ {\tt argument}$

base: Quantity, Number dimensionless argument

```
1 I = 1 * _W/_m^2
2 I_0 = 1e-12 * _W/_m^2
3 print(10 * (I/I_0):log(10) * _dB)
4 120 * _dB
```

Quantity.exp(q)

Returns the value of the exponential function of the given quantitiy.

 ${\tt q}: {\tt Quantity}, {\tt Number} \ {\tt dimensionless} \ {\tt argument}$

```
1 x = 2 * _1
2 print( x:exp() )
3 7.3890560989307
```

Quantity.sin(q)

Returns the value of the sinus function of the given quantitiy.

 ${\tt q}: {\tt Quantity}, {\tt Number} \ {\tt dimensionless} \ {\tt argument}$

```
1 alpha = 30 * _deg
2 print( alpha:sin() )
3 0.5
```

Quantity.cos(q)

Returns the value of the cosinus function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1 alpha = 60 * _deg
2 print( alpha:cos() )
3 0.5
```

Quantity.tan(q)

Returns the value of the tangent function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1 alpha = 45 * _deg
2 print( alpha:tan() )
3 1
```

Quantity.asin(q)

Returns the value of the arcus sinus function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1 x = 0.5 * _1
2 print( x:asin():to(_deg) )
3 30 * _deg
```

Quantity.acos(q)

Returns the value of the arcus cosinus function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1  x = 0.5 * _1
2  print( x:acos():to(_deg) )
3  60 * _deg
```

Quantity.atan(q)

Returns the value of the arcus tangent function of the given quantity. The quantity has to be dimensionless.

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print( x:atan():to(_deg) )
3 45 * _deg
```

Quantity.sinh(q)

Returns the value of the hyperbolic sine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$\sinh(x) = 0.5 \cdot e^x - 0.5/e^x \quad .$$

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print( x:sinh() )
3 1.1752011936438
```

Quantity.cosh(q)

Returns the value of the hyperbolic cosine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$\cosh(x) = 0.5 \cdot e^x + 0.5/e^x \quad .$$

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print(x:cosh())
3 1.5430806348152
```

Quantity.tanh(q)

Returns the value of the hyperbolic tangent function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$
.

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print( x:tanh() )
3 0.76159415595576
```

Quantity.asinh(q)

Returns the value of the inverse hyperbolic sine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$asinh(x) = \ln\left(x + \sqrt{x^2 + 1}\right) \quad .$$

q: Quantity, Number dimensionless argument

```
1 x = 1 * _1
2 print(x:asinh())
3 0.88137358701954
```

Quantity.acosh(q)

Returns the value of the inverse hyperbolic cosine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$a\cosh(x) = \ln\left(x + \sqrt{x^2 - 1}\right) \quad , x > 1 \quad .$$

q: Quantity, Number dimensionless argument bigger than or equal to one

```
1 x = 2 * _1
2 print(x:acosh())
3 1.3169578969248
```

Quantity.atanh(q)

Returns the value of the inverse hyperbolic cosine function of the given quantity. The quantity has to be dimensionless. Since lua doesn't implement the hyperbolic functions the following formula is used

$$\operatorname{atanh}(x) = \ln\left(\frac{1+x}{1-x}\right) \quad , -1 < x < 1 \quad .$$

 ${\tt q}: {\tt Quantity}, {\tt Number} \ {\rm dimensionless} \ {\rm argument} \ {\rm with} \ {\rm magnitude} \ {\rm smaller} \ {\rm than} \ {\rm one}.$

```
1 x = 0.5 * _1
2 print( x:atanh() )
3 0.54930614433405
```

5.2 physical.Dimension

All physical quantities do have a physical dimension. For example the quantity Area has the dimension L^2 (length to the power of two). In the SI-System there are seven base dimensions, from which all other dimensions are derived. Each dimension is represented by an n-tuple, where n is the number of base dimensions. Each physical quantity has an associated dimension object. It is used two check if two quantities can be added or subtraced and if they are equal.

Dimension.new(q=nil)

Constructor of the Dimension class.

Parameters

 ${\bf q}$: Dimension or string, ${\rm optional}$

The name or symbol of the dimension. If q is a dimension, a copy of it is made. If no argument ist given, a dimension *zero* is created.

return: Dimension

The created Quantity object

Notes

_

Examples

```
1  V_1 = D("Velocity")
2  L = D("L")
3  V_2 = D(L/T)
```

5.3 physical.Unit

The task of this class is keeping track of the unit term. The unit term is a fraction of units. The units in the enumerator and denominator can have an exponent.

Unit.new(u=nil)

Copy Constructor. It copies a given unit object. If nothing is given, an empty unit is created.

Parameters

u: Unit

The unit object which will be copied.

return : Unit

The created Unit object

Unit.new(symbol, name, prefixsymbol=nil, prefixname=nil)

Constructor. A new Unit object with symbol is created. The prefixsymbol and prefixname are optional.

Parameters

symbol: String

The symbol of the unit.

name: String

The name of the unit.

prefixsymbol : String

The optional symbol of the prefix.

prefixname : String

The optional name of the prefix.

return : Unit

The created Unit object

Unit.tosiunitx(self)

The unit term will be compiled into a string, which the LaTeX package siunitx can understand.

Parameters

return: String

The siunitx representation of the unit term.

5.4 physical.Number

It does arithmetics with gaussian error propagation. A number instance has a mean value called ${\bf x}$ and an uncertainty called ${\bf dx}$.

Number.new(n=nil)

This is the copy Constructor. It copies a given number object. If n is nil, an instance representing number zero with uncertainty zero is created.

Parameters

n: Number

The number object to be copied.

return: Number

The created Number instance.

Number.new(x, dx)

This constructor, creates a new instance with mean value x and uncertainty dx.

Parameters

x: number

mean value

dx: number

uncertainty value

return : Number

The created Number instance.

Examples

```
1 n = N(12,0.1)
2 print(n)
```

Number.new(str)

This constructor creates a new instance from a string. It can parse strings of the form 3.4, 3.4e-3, 5.4e-3 +/- 2.4e-6, 5.45(7)e-23.

Parameters / Return

str: string

The number as a string.

return : Number

The created Number object

Examples

```
1     n_1 = N("12.3e-6")
2     print(n_1)
3
4     n_2 = N("12 +/- 0.1")
5     print(n_2)
6
7     n_3 = N("12.0(1)")
8     print(n_3)
```

Number.mean(n)

Returns the mean value

Parameters / Return

return: number
The mean value

Number.uncertainty(n)

Returns the uncertainty value

Parameters / Return

return : number

The uncertainty value

Number.abs(n)

Returns the absolute value of the number.

Parameters / Return

return: number
The absolute value

Number.sqrt(n)

Returns the square root of the number.

Parameters / Return

return: number
The square root

References

[1] Bureau International des Poids et Mesures. The international system of units (si), 2006.