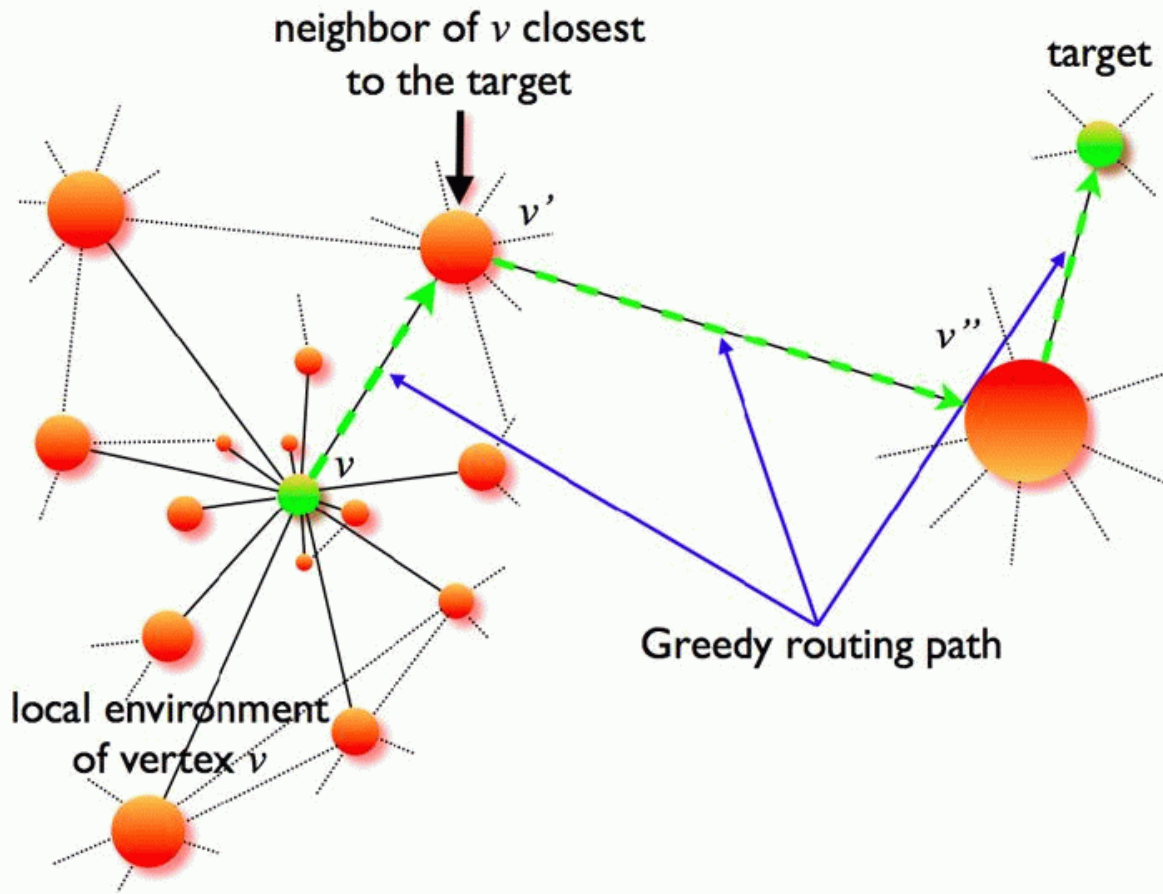


* Map Routing *



Team Members :-

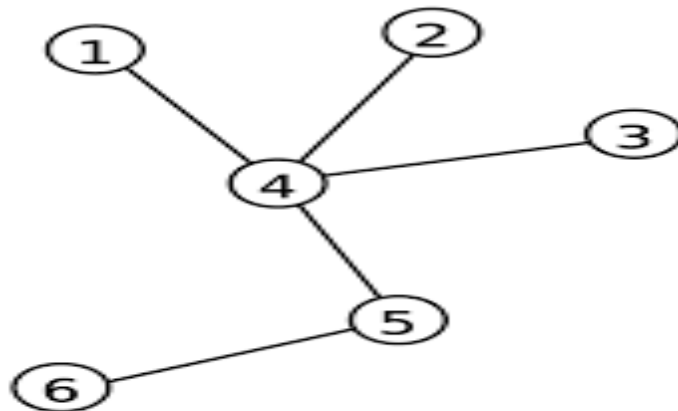
1. Mohamed Hassen Mohamed Radwan (Sec 14).
2. Mohamed Khaled Gomaa (Sec 14).
3. Ahmed Saad Eldeen Abdul Ghani (Sec 1).

-3rd Year 2018-2019

* Map construction *

- **Map** was represented as Undirected Weighted Graph:-

Each Point represented as node and each road represented
As edge and each weight represented as time to reach from
Point to another point.



- Construct _Graph_Source_Code:- Complexity:- O(E).

```
Console.WriteLine("Enter Number of Intersection Points ?!..");
int number_of_intersection = int.Parse(Console.ReadLine());
for (int i = 0; i < number_of_intersection; i++)
{
    Line = Console.ReadLine();
    splitter = Line.Split(' ');

    ID1 = int.Parse(splitter[0]);
    x1 = double.Parse(splitter[1]);
    y1 = double.Parse(splitter[2]);

    try { ID_getter[x1][y1] = ID1; }
    catch (Exception e){ ID_getter[x1] = new Dictionary<double, int>(); ID_getter[x1][y1]
= ID1; }

    Tuple<double, double> coordinate = new Tuple<double, double>(x1, y1);
    Coordinate_getter[ID1] = coordinate;

    all_nodes.Add(ID1);
}
Console.WriteLine("Enter Number of Road ?!..");
int number_of_roads = int.Parse(Console.ReadLine());
for (int i = 0; i < number_of_roads; i++)
{
    Line = Console.ReadLine();
    splitter = Line.Split(' ');

    ID1 = int.Parse(splitter[0]);
    ID2 = int.Parse(splitter[1]);
    length = double.Parse(splitter[2]);
    volocity = double.Parse(splitter[3]);

    try { adj[ID1].Add(ID2); }
    catch(Exception e) { adj[ID1] = new List<int>(); adj[ID1].Add(ID2); }
    try { adj[ID2].Add(ID1); }
    catch (Exception e) { adj[ID2] = new List<int>(); adj[ID2].Add(ID1); }

    try { speed[ID1][ID2] = volocity; }
    catch(Exception e) { speed[ID1] = new Dictionary<int, double>(); speed[ID1][ID2] =
volocity; }

    try { speed[ID2][ID1] = volocity; }
    catch (Exception e) { speed[ID2] = new Dictionary<int, double>(); speed[ID2][ID1] =
volocity; }

    try { distance[ID1][ID2] = length; }
    catch (Exception e) { distance[ID1] = new Dictionary<int, double>();
distance[ID1][ID2] = length; }
    try { distance[ID2][ID1] = length; }
    catch (Exception e) { distance[ID2] = new Dictionary<int, double>();
distance[ID2][ID1] = length; }

}
```

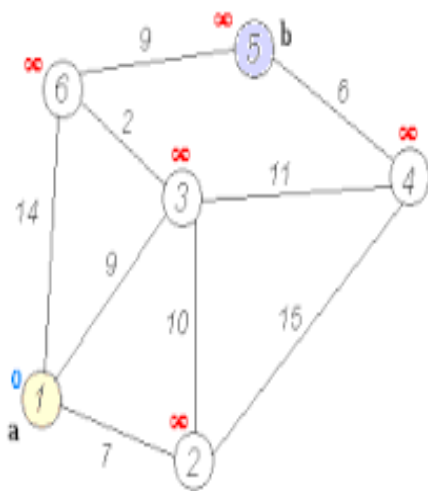
1. Read all Intersection Point that exists in a Map.
2. Read all Roads data and make for each intersection point adjacent list for all its neighbors and save both speed and length for each road in some dictionary.

* Dijkstra Algorithm *

- **Dijkstra Algorithm** is an Algorithm for finding Shortest Path Between -

1. One Source to Only One Destination.
2. One Source to all Destination Can Reached by This Node.

USING PRIORITY_QUEUES.



Complexity for Algorithm: - **$O(S E \log V)$.**

- S: number of starting nodes
- V: # of intersection points that are checked until reaching the destinations
- E: # of roads that are checked until reaching the destinations

- But we can minimize this complexity by decreasing its constant factor not its dominant factor.
i.e. (**Minimizing # of Starting Nodes in our Algorithm**).

Ex: - When Source is not Intersection Point and Destination is also not Intersection Point (HOW TO MINIMIZE COMPLEXITY)-?!

Solution: - Make # of starting nodes = min (# of intersection can i reach from Source on foot, # of intersection that from it can I reach to destination on foot).

-Sure I Can Reach form Node to Node On foot if Distance between this Nodes is Less than or Equal Radius that given.

- Dijkstra_Source_Code:-

```
static void dijkstra(int source)
{
    shortest_path.Clear();
    parent.Clear();
    shortest_path[source] = 0;

    PriorityQueue pq = new PriorityQueue();
    Tuple<double, int> start = new Tuple<double, int>(0, source);
    pq.push(start);
    while(!pq.empty())
    {
        int cur = pq.top();
        pq.pop();
        for (int i = 0; i < adj[cur].Count; i++)
        {
            int child = adj[cur][i];
            double LocalMin;

            if (child == source) continue;
            try { LocalMin = shortest_path[child]; }
            catch(Exception e) { shortest_path[child] = -1; }

            double time = (double)distance[cur][child] / speed[cur][child];
            if (shortest_path[child] == -1 || time +
shortest_path[cur]<shortest_path[child])
            {
                shortest_path[child] = time + shortest_path[cur];
                parent[child] = cur;
                Tuple<double, int> temp = new Tuple<double, int>(time +
shortest_path[cur], child);
                pq.push(temp);
            }
        }
    }
}
```

- Greedy Solution.

➤ **Greedy Choice:-**For each step find Shortest Time to pass from it.

- **Handling Cases.**

1. IF Source is intersection and destination is not.

(Dijkstra on Source and find node that from it can I reach to destination on foot with max R meters and with min time from Source.)

2. IF Source is not intersection and destination is intersection.

(Dijkstra on Destination and find node that I can reach to it from Source on foot with max R meters and with min time to destination.)

3. IF Source is intersection and destination is intersection.

(Dijkstra on Destination or Source and find shortest time directly.)

4. IF Source is not intersection and destination is not intersection.

(Make # of starting nodes on Dijkstra algorithm = min (# of intersection can I reach from Source on foot, # of intersection that from it can I reach to destination on foot) and find shortest time from source to destination).

- **Printing Path:-**

To print path we need to Backtrack for each node to its Parent.

Complexity: - $O(V)$.

- **Source Code:-**

```
for (int j = 0; j < path.Count; j++)  
{  
    Console.Write(path[j]);  
    Console.Write(" ");  
}  
Console.WriteLine();
```

