

إعدادي 2020









## ww.CollegeTanta.cf Partial fractions Dif: The function Pm (x) = am x m + am - x m - 1 + .... + a, x + a. is called a plonomial of degree M, as am + 0 The function $Q(x) = \frac{P_m(x)}{q_m(x)}$ rational function denominator $\frac{2}{X+1} = \frac{3}{X+2} = \frac{2(X+2)-3(X+1)}{(X+1)(X+2)} = \frac{1-X}{(X+1)(X+2)}$ To put any fraction inthe form of partial follow these steps, 1- Make sure that the degree of the mnumerator is higher then the degree of the denominator 2- Analize 9n(x). Theroots of "q"are one of four cases Casel: Simple roots of 1st degree. $Q(x) = \frac{P_m(x)}{(x-a)} = \frac{\alpha_i}{x-a}$ $\alpha_1 = \lim_{x \to a} (x - a) Q(x) = \frac{P_m(x)}{(\dots)}$ Ex: factorize x2+1 (x+2)(x-1) x2+x=2 x3+1 x2+x-2 $Q(x) = 1 + \frac{3-x}{x^2 + x - 2} = 1 + \frac{3-x}{(x+1)(x+1)} = 1 + \frac{a}{x+1}$

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$$\alpha = \lim_{X \to \infty} \frac{3-x}{x+z} = \frac{2}{3}$$

$$b = \lim_{x \to -2} \frac{3-x}{x-1} = \frac{5}{-3}$$

$$Q(x) = 1 + \frac{2}{3(x-1)} + \frac{5}{3(x+2)}$$

\*

Case 2: Rebeated real roots.

$$Q(x) = P_m(x) = a_k a_{k-1} a_k$$
 $(x-a)^{K} (x-a)^{K-1} (x-a)$ 

where ax > By direct method

ax-1 ... a, > By one of two methods

1- By assuming different values for x in both sides.

2- Compairing the cooffeicients of bouth sides.

Ex. factorize 
$$f(x) = \frac{x+1}{(x+z)(x-1)^3}$$

$$f(x) = \frac{\alpha}{(x+z)} + \frac{b}{(x-1)^2} + \frac{c}{(x-1)^2} + \frac{d}{x-1}$$

$$\frac{x+1}{(x+2)(x-1)^3} = \frac{\alpha(x-1)^3 + b(x+2) + (x+2)(x+1) + d(x+2)(x+1)^2}{(x+2)(x-1)^3}$$

Otacisco 
$$a = \lim_{x \to -2} \frac{x+1}{(x-1)^3} = \frac{-1}{-27} = \frac{1}{27}$$

$$b = \lim_{x \to 1} \frac{x+1}{x+2} = \frac{2}{3}$$

## www.CollegeTanta.cf Put X = -1 0=-8x1 +2 -2 -2 +40 0 = -8 + 2 - 2 c + 4 d -> 0 Put x=0 $1 = -\frac{1}{27} - \frac{2}{3} - 2C - 2d \implies 2$ Case 3: Distencet complex root. $Q(x) = \frac{P_n(x)}{\alpha x^2 + bx + c} = \frac{\alpha x + b_0}{\alpha x^2 + bx + c}$ Case 4: Repeated complex voot. $Q(x) = \frac{p_n(x)}{(\alpha x^2 + bx + c)^K} = \frac{a_1 \xi x + b_1 x}{(\alpha x^2 + bx + c)^K}$ $E_{x}$ : $f(x) = \frac{x+2}{(x-1)(x-2)^2(x^2+4)}$ $f(x) = \frac{x+2}{(x-1)(x-2)^2(x^2+4)}$ = ce + b < dx + e b = 4 $\alpha = \frac{3}{5}$ x+2= a(x-2) (x+4)+b(x-1)(x2+4)+c(x-1)(x-2) (x2+4) + &(x-1)(x-2)2 (dx+e) Put: x2+4=0 x+2=(dx+e)(16+4x) = 16dx + 16e - 16d + 4ex

## www.CollegeTanta.cf 16e-16d 0 0 • • f(x) = (x2+1) (x2+2) (x2+3) (x2+4) ··· a