## سنتر فيوتشر

Subject: Sols Zie

Chapter: PUN 2 Vii VI

Mob: 0112 3333 122

0109 3508 204

math matical induction ig 218= 81 ال ندن محدالعلاقة عنوا ﴿ فَعْرَضُ مِحْدَ الْعَالُوتَ عَمْرًا n=k @ خاول رشان محد العلاج n = k+1 = Prove that Prove that by using mathmatical induction show that  $1+2+3+4----+n=\frac{n(n+1)}{2}$  $\frac{n=1}{2}$  R-H-S  $\frac{1}{2}(2)=1$ العلان م معید فنوا ۱ = ۱ ۱ م 1+2+3+----+ k = k(|c+1) requied to prove relation is true at

$$1 + 2 + 3 + - - - - + k + (k+1) = (k+1)(k+2)$$

$$1 + 2 + 3 + - - - + k + (k+1)$$

$$= k(k+1) + (k+1) = (k+1)(\frac{k}{2} + 1)$$

$$= (k+1)(k+2) = R \cdot H \cdot S$$

$$n = (k+1)(k+2) = R \cdot H \cdot S$$

$$n = (k+1)(k+2) = R \cdot H \cdot S$$

Prove 
$$\frac{1}{4}$$
 $\frac{1^{2}+2^{2}+3^{2}+\cdots+n^{2}}{5} = \frac{n(n+1)(2n+1)}{6}$ 
 $\frac{n=1}{5}$ 
 $\frac{1}{5}$ 
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$$\begin{array}{lll}
n_{2} k & = y \times 1 & = y \times 2 \\
1^{2} + 2^{2} + 3^{2} - - - + k^{2} & = k \cdot (k+1)/2k+1) \\
n_{2} k & = y \times 1 & = y \times 1 & = y \times 1 \\
1^{2} + 2^{2} + 3^{2} - - - + k^{2} + (k+1)^{2} & = (k+1)(k+2)/2k+3) \\
1^{2} + 2^{2} + 3^{2} - - - + k^{2} + (k+1)^{2} & = (k+1)(k+2)/2k+3) \\
1 & = k \cdot (k+1)/2k+1) + (k+1)^{2} \\
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Prove that

1.3 + 
$$\frac{1}{3.5}$$
 +  $\frac{1}{5.7}$  -  $\frac{1}{(2n-1)/2n+1}$ 
 $\frac{n}{2n+1}$ 
 $\frac{n$ 

$$\frac{1}{1 \cdot 3} + \frac{1}{3 \cdot 5} + \frac{1}{5 \cdot 7} - \cdots + \frac{1}{(2k-1)(2k+1)} (2k+1)$$

$$= \frac{k}{2k+1} + \frac{1}{(2k+3)(2k+3)}$$

$$= \frac{k(2k+3)+1}{(2k+3)(2k+3)} = \frac{2k^2+3k+1}{(2k+1)(2k+3)}$$

$$= \frac{(2k+1)(k+1)}{(2k+3)} = R \cdot H \cdot S$$

$$= \frac{(2k+1)(2k+3)}{(2k+3)}$$

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$$= \frac{n^2(n+1)^2}{4}$$

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$$\frac{N=1}{k+1} = \frac{1^{2}(2)^{2}}{4} = 1$$

$$\frac{1}{k+1} = \frac{1^{2}(k+1)^{2}}{4} = \frac{1}{k^{2}(k+1)^{2}} = \frac{1}{k^{2}(k+1)$$

$$= (k+1)^{2} (k^{2} + 4k + 4)$$

$$= (k+1)^{2} (k+2)^{2} = R \cdot H \cdot S$$

$$= (n+1)! -1$$

$$\begin{array}{lll}
n = k+1 & \text{siz} & \text{siz} & \text{siz} & \text{siz} & \text{siz} & \text{siz} \\
k+1 & \text{c.} & = (|c+2|! - |\\
- & |c+1|| & \text{c.} & |c+1|| & |c+1|$$

$$\frac{1}{c=1} = 1 - \frac{1}{(n+1)!}$$

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$$\frac{1}{c=1} = \frac{1}{(n+1)!}$$

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L. H. 
$$S = 1 - \frac{1}{(k+1)!} + \frac{1}{(k+2)!}$$

=  $1 + \frac{1}{(k+2)!} = 1 - \frac{1}{(k+2)!}$ 

=  $1 + \frac{1}{(k+2)!} = 1 - \frac{1}{($ 

required to grove (Cos Q + i Sin Q) = Cos (k+1) Q+ i Sin (k+1)0 L. H. S = (Cos Q + isin 0) = (Cosa+isino) (cosa+isino) = (Coska+isinka) | Cosa+isinol = Coska Cosa - Sinka Sina +i Coska Sino +i Sinka as o = cos (ka+0) + i sin(ka+0) = Cos(k+1)0+; Sin(k+1)0 : العلانة صعيد لحمه فم ١

Sin(x±y) = Sinx COSY ± COSX Siny COS(x±y) = COSX COSY = Sinx Siny

Prove that

$$(1+i) = 2$$
 $OS(\frac{n\pi}{4}) + iSin(\frac{n\pi}{4})$ 
 $OS(\frac{n$ 

L.H.S. 
$$(1+1)$$
  $\frac{k^{2}}{2^{2}} \left( \frac{\cos k\pi}{4} + i \frac{\sin k\pi}{4} \right)$ 

$$= 2^{\frac{1}{2}} \left( \frac{\cos k\pi}{4} - \frac{\sin k\pi}{4} \right)$$

$$+ i \frac{\sin k\pi}{4} + i \frac{\cos k\pi}{4}$$

$$+ i \frac{\sin k\pi}{4} + i \frac{\cos k\pi}{4} \right)$$

$$= 2^{\frac{1}{2}} \left( \frac{\cos k\pi}{4} - \frac{\sin k\pi}{4} \right)$$

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Prove 
$$\begin{pmatrix} 1 & x \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & x \\ 0 & 1 \end{pmatrix}$$
 $R \cdot H \cdot S = \begin{pmatrix} 1 & x \\ 0 & 1 \end{pmatrix}$ 
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L. H. S = 
$$\begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & (k+1)x \\ 0 & 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & (k+1)x \\ 0 & 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & kx \\ 0 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & kx \\ 0 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & kx \\ 0 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & kx \\ 0 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & kx + x \\ 0 & 1 & 1 \end{bmatrix}$$

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