

Pool Trading for Hybrid Wind-Solar Power Producers

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February 12, 2021

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1 Introduction

Renewable energies are currently advancing and gaining an increasing share of the energy production. On the one hand, this is induced by the desire to decrease the carbon footprint and on the other hand, the population is facing a decreasing availability of fossil fuels like natural gas, coal and oil. The advantage of renewable energies is that apart from not requiring fuel, which induces zero fuel costs, it is emission-free and therefore supported by the government. However, these energy sources are also non-dispatchable and have the major disadvantage of uncertainty. Conejo et al. [3] considered the case of a wind power producer. Due to the uncertainty, the wind power producer must rely on the energy traded on the balancing market. Therefore, he solved an optimisation problem to maximise the expected profits from trading on the day-ahead market and the adjustment market while also minimising the costs incurred in the balancing market caused by energy deviations.

In addition to the uncertainty, the wind power producer also faces a substantial fluctuation in production throughout the year, caused by the strong dependence on wind availability over different months in a year. Considering a wind power producer in Europe, wind availability is much higher in the winter than summer months, see, e.g. [5].

For this case study, we consider the case of an energy producer producing both wind power as well as solar energy. Several studies have been carried out to see how both resources' production variability can be decreased by exploiting the anti-correlation of wind speed and solar irradiance. Coker et al. [1] considered a region in south-west Britain to assess the variability of wind, solar and tidal current energy resources. Santos-Alamillos et al. [4] aimed at finding the optimal spatial distribution of wind and solar farms across the Southern Iberian Peninsula to minimise the resulting net variability. Bett et al. [2] analysed daily data for Great Britain and found evidence for an overall anticorrelation between wind speed and solar irradiance. As a side product, they also discovered that solar variability is significantly higher than wind variability and that

both variabilities are higher in winter than in summer. Inspired by these results, we wish to set up a pool trading model for an energy producer offering energy produced from both solar and wind power plants. This setting of a hybrid wind-solar power producer overcomes the strong fluctuation in production throughout the year due to the strong over year anti-correlation of wind speed and solar irradiance, see figure 1. In addition to the anti-correlation between wind speed and solar irradiance over the whole year, there is also an anti-correlation between both over the day, even if it is much smaller. We will exploit this anti-correlation over the day and include it into the forecast for wind and solar power production. Therefore, we will apply the forecast for wind power production for a time t in dependence on the previous times' wind speeds and previous times' solar irradiance to improve the forecast precision possibly.

To solve the decision problem, the hybrid energy producer has to face, we will solve a scenario-based multi-stage optimization problem. For generating wind and solar power scenarios, we will use a time-series-based approach.

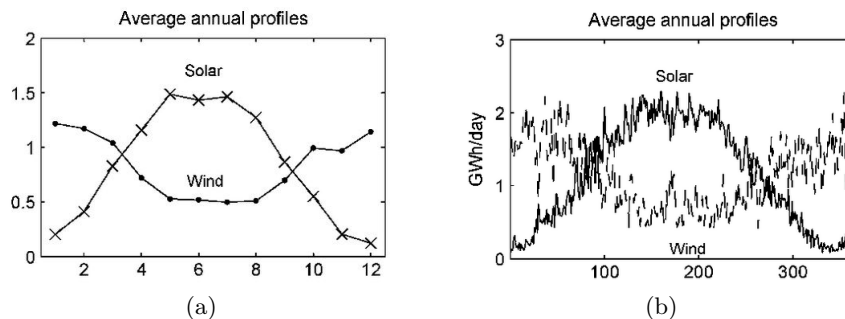


Figure 1: The average annual profiles of solar irradiance and wind speed [5]

2 Decision framework

In the introduction we mentioned the three major trading places for energy, namely the day-ahead, the adjustment and the balancing market. All three of these are cleared in a single auction process, however at different times of the day.

- The day-ahead market is cleared at a given time period t^D of day $d - 1$.
- The adjustment market is cleared at time period t^A of day $d - 1$. Please note that time period t^A takes place *after* time period t^D .
- The balancing market ensures the real-time balancing between the generation of and demand for energy by balancing out differences between the real-time operation and the last energy program settled on in the previous markets. Therefore, it is cleared just before each time period of day d .

There are three major decisions the hybrid energy producer has to face. First, he has to submit an offering curve to the day-ahead market for day d . **The day-ahead market for day d is closed at 10 am of day $d - 1$.** Then, he has to modify the submitted energy offers in the adjustment market depending on how the wind and solar power forecast updates change. **The adjustment market for day d is closed at 11.45 pm of day $d - 1$.** Finally, he needs to balance out his energy deviations by trading in the balancing market for each time period of day d . From now on, we assume hourly periods. This means that the balancing market for the time period 6.00-7.00 am of day d closes at 5.50 am of day d .

The producer faces several factors that influence his short-term decision making process. It is inevitable to account for the imbalance costs, i.e. the costs entailed by deviations in the energy production. Apart from that, he is influenced by all sorts of mechanisms through which energy deviations are priced in the balancing market and the beneficial impact of an adjustment market clearing after the clearance of the day-ahead market. Energy deviations are not unusual for producers of non-dispatchable energy sources as windspeed and solar irradiance exert a high variability. As soon as a producer deviates from his agreed-upon amount of energy he has traded on the market before, he has to sell its surplus or buy his generation deficit at an *imbalance price*. We denote the price for positive energy deviations, i.e. higher production than planned, by λ_t^+ , and the price for negative energy deviations by λ_t^- . We denote the price for positive energy deviations, i.e. higher production than planned, by λ_t^+ , and the price for negative energy deviations by λ_t^- .

Let δ_t be the system imbalance for time t , that means if $\delta_t < 0$ there is an negative system imbalance and otherwise a generation excess or balance ($\delta_t = 0$) in the power system. Then λ_t^+ and λ_t^- are given by

$$\lambda_t^+ = \begin{cases} \lambda_t^D & \text{if } \delta_t < 0 \\ \min(\lambda_t^D, \lambda_t^{DN}) & \text{if } \delta_t \geq 0. \end{cases} \quad \lambda_t^- = \begin{cases} \max(\lambda_t^D, \lambda_t^{UP}) & \text{if } \delta_t < 0 \\ \lambda_t^D & \text{if } \delta_t \geq 0. \end{cases}$$

where we write λ_t^D for the day-ahead market price, λ_t^{UP} for the price of the upward energy that may needs to be added and λ_t^{DN} for the price of the downward energy that may have to be discharged from the system.

The producer offers an amount E_t^D of energy at the day-ahead market, while his plant produces an amount E_t , which is most probably not equal to the amount offered at the day-ahead market. We denote the total deviation by

$$\Delta_t = E_t - E_t^D = d_t (P_t - P_t^D)$$

indicating the timespan by d_t and the actual resp. offered amount of power by P_t resp. P_t^D . Here, the total power produced in time t is given by the sum of the produced solar power P_t^S and wind power P_t^W , i.e.

$$P_t = P_t^S + P_t^W.$$

In this decision framework, we assume that the hybrid power producer can only offer a total energy amount and cannot offer price differences between the produced solar and wind energy.

We define the imbalances price ratios by

$$r_t^+ = \frac{\lambda_t^+}{\lambda_t^D} \quad \text{and} \quad r_t^- = \frac{\lambda_t^-}{\lambda_t^D}.$$

Given these ratios, we can define the imbalance cost C_t for time t as

$$C_t = \begin{cases} \lambda_t^D (1 - r_t^+) \Delta_t & \text{if } \Delta_t \geq 0 \\ -\lambda_t^D (r_t^- - 1) \Delta_t & \text{if } \Delta_t < 0. \end{cases}$$

Then we can formulate the revenue R_t in terms of the maximum level of revenue, which could be realised in a situation free of wind and irradiance uncertainty, and the imbalance cost, i.e.

$$R_t = \lambda_t^D E_t - C_t.$$

Given this formulatuion, it is easy to deduce that maximising the revenue is equivalent to minimising the imbalance costs.

2.1 Uncertainty Characterization

We face four major sources of uncertainty. The most essential source of uncertainty is the weather, which influences both the wind and solar power generation. Apart from that, we have uncertainty concerning the market characteristics like day-ahead market price, adjustment market price and the prices for imbalance.

To deal with these uncertainties in order to solve the decision problem the hybrid power producer has to solve, we consider a scenario-based multi-stage optimization problem. For this purpose, we consider N_T periods of the market horizon, N_D scenarios for day-ahead prices, and N_A scenarios for the adjustment market prices. Thus, we have several realisations of day-ahead and adjustment market prices, which we summarise in

$$\begin{aligned} \lambda^D &= \left\{ \lambda_t^D \mid t \in \{1, \dots, N_T\} \right\} \\ \lambda^A &= \left\{ \lambda_t^A \mid t \in \{1, \dots, N_A\} \right\}. \end{aligned}$$

The hybrid power producer has to adhere the following sequence of decisions. First, he designs an offer strategy for the day-ahead market and submits his selling offers for each period of the market horizon. Second, once the day-ahead market price is known for each time period, he has to decide on the amount of energy that he wishes to sell or buy from the adjustment market. As soon as the adjustment market prices are known as well as the imbalance prices and the generated wind and solar power, the producer knows his level of imbalance and can compute the resulting costs for the latter.

2.2 A Hybrid Wind Solar Pool Trading Model Formulation

We set up a maximisation model for the hybrid wind-solar power producer. As already discussed previously, the producer has to decide on the amount of energy offered on the day-ahead resp. adjustment market for each timeperiod t and each scenario ω , denoted by $P_{t\omega}^D$ resp. $P_{t\omega}^A$. We split up the total deviation Δ_t into a positive and a negative deviation Δ_t^+ resp. Δ_t^- such that

$$\Delta_t = \Delta_t^+ - \Delta_t^-,$$

which we also have to include as one of the constraints. Thus, we wish to maximise the profit given by the sum of the revenues on the respective markets and possible imbalance costs. As we also aspire to consider the risk aversion of the producer, we include a conditional-value-at-risk term. For this, we need a weighting factor, denoted by β , the confidence level α , an auxiliary variable ζ and the continuous non-negative variable η , which is defined as the maximum of the auxiliary variable minus the revenue. We also have to include this definition as a constraint in our maximisation model.

The first block of constraints restricts the amount of energy we offer on both markets. First, we cannot offer more energy on the day-ahead market than the maximum amount of energy we can produce in both plants, denoted by P_{\max} . In each scenario and for every timeperiod, the total amount of energy offered, $P_{t\omega}^O$, comprises the amount of energy we offer on the day-ahead and the adjustment market and can, again, not exceed the maximum amount of energy we can produce. The latter comprises the maximum amount of solar energy we can produce, expressed by the parameter P_{\max}^S , and the maximum amount of wind energy we can produce, denoted by P_{\max}^W . Moreover, in any scenario, each source's amount of energy cannot exceed the respective maximum production amount.

The second block of constraints considers possible deviations. First, we define the total deviation as the difference between the actually produced and the initially offered amount of energy, multiplied by the duration of the time period. Apart from that, we split up the total deviation in terms of the positive, i.e. excess energy, and negative, i.e. energy deficit, deviation. On the one hand, the positive deviation cannot exceed what was actually produced in that scenario. This would happen if the producer didn't offer anything on either market, but then produced something non-zero. On the other hand, the negative deviation cannot be larger than P_{\max} , in which case the producer would offer all its capacity on the market, but actually produces nothing.

The offering curve conditions induce the third block of constraints. The first constraint ensures that offering curves are non-decreasing, which is a realistic and valid assumption to make on the energy market. Herefore we define the matrix O to sort the day-ahead prices associated with each period in an increasing manner for each scenario ω . Therefore, element $O(t, \omega)$ represents the position of the day-ahead price $\lambda_{t\omega}^D$ over all scenarios $\omega \in \Omega$. Moreover, the producer can only submit one offering curve no matter which imbalance price realises. We call this assumption the "non-anticipativity" constraint. This condition has to hold for the offering curve on the day-ahead market and the adjustment market. However, the amount of energy offered on the adjustment

market might change with the day-ahead market price realisation and the wind and solar power forecasts, which are more precise the closer you get to the point of energy delivery. Conejo et al. refer to this as the "certainty gain effect", cf. [3]. When formulating the mathematical model, one has to differ between the time periods between the closure of the day-ahead market and the adjustment market and the time periods between the adjustment market's closure and delivery. This is only of relevance for the constraints concerning the non-anticipativity constraints. Therefore, we use the t as the overall timeperiod index and τ for the timeperiods between the closure of the day-ahead and the adjustment market.

The final block of constraints evolves around the conditional-value-at-risk measures, which are introduced in a more detailed way in Chapter 4 of [3].

Combining the explained objective with all these constraints gives the mathematical model below, which we shall translate into Julia as found in the provided notebook.

$$\begin{aligned} \text{Maximize } & P_{t\omega}^D, \forall t, \forall \omega; P_{t\omega}^A, \forall t, \forall \omega; \Delta_{t\omega}^+, \forall t, \forall \omega; \Delta_{t\omega}^-, \forall t, \forall \omega; \eta_\omega, \forall \omega; \zeta \\ \sum_{\omega=1}^{N_\Omega} \sum_{t=1}^{N_T} \pi_\omega & \left[\lambda_{t\omega}^D P_{t\omega}^D d_t + \lambda_{t\omega}^A P_{t\omega}^A d_t + \lambda_{t\omega}^D r_{t\omega}^+ \Delta_{t\omega}^+ - \lambda_{t\omega}^D r_{t\omega}^- \Delta_{t\omega}^- \right] \\ & + \beta \left(\zeta - \frac{1}{1-\alpha} \sum_{\omega=1}^{N_\Omega} \pi_\omega \eta_\omega \right) \end{aligned} \quad (1)$$

$$0 \leq P_{t\omega}^D \leq P_{\max}, \quad \forall t, \forall \omega \quad (2)$$

$$P_{t\omega}^O = P_{t\omega}^D + P_{t\omega}^A, \quad \forall t, \forall \omega \quad (3)$$

$$0 \leq P_{t\omega}^O \leq P_{\max}, \quad \forall t, \forall \omega \quad (4)$$

$$P_{t\omega} = P_{t\omega}^S + P_{t\omega}^W, \quad \forall t, \forall \omega \quad (5)$$

$$P_{\max} = P_{\max}^S + P_{\max}^W, \quad (6)$$

$$\Delta_{t\omega} = d_t (P_{t\omega} - P_{t\omega}^O), \quad \forall t, \forall \omega \quad (7)$$

$$\Delta_{t\omega} = \Delta_{t\omega}^+ - \Delta_{t\omega}^-, \quad \forall t, \forall \omega \quad (8)$$

$$0 \leq \Delta_{t\omega}^+ \leq P_{t\omega} d_t, \quad \forall t, \forall \omega \quad (9)$$

$$0 \leq \Delta_{t\omega}^- \leq P_{\max} d_t, \quad \forall t, \forall \omega \quad (10)$$

$$P_{t\omega}^D - P_{t\omega'}^D \leq 0, \quad \forall t, \forall \omega, \omega' : O(\lambda_{t\omega}^D) + 1 = O(\lambda_{t\omega'}^D) \quad (11)$$

$$P_{t\omega}^D = P_{t\omega'}^D, \quad \forall t, \forall \omega, \omega' : \lambda_{t\omega'}^D = \lambda_{t\omega}^D \quad (12)$$

$$\begin{aligned} P_{t\omega}^A &= P_{t\omega'}^A, \quad \forall t, \forall \omega, \omega' : (\lambda_{t\omega'}^D = \lambda_{t\omega}^D \forall t) \\ &\text{and } (P_{\tau\omega'} = P_{\tau\omega}, \forall \tau = 1, 2, \dots, N_{T_1}) \end{aligned} \quad (13)$$

$$- \sum_{t=1}^{N_T} \left[\lambda_{t\omega}^D P_{t\omega}^D d_t + \lambda_{t\omega}^A P_{t\omega}^A d_t + \lambda_{t\omega}^D (r_{t\omega}^+ \Delta_{t\omega}^+ - r_{t\omega}^- \Delta_{t\omega}^-) \right] + \zeta - \eta_\omega \leq 0, \forall \omega \quad (14)$$

$$\eta_\omega \geq 0, \quad \forall \omega \quad (15)$$

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