

You are given a set of  $n$  intervals  $\mathcal{I} = \{I_1, \dots, I_n\}$  and  $n$  colours. Your goal is to assign each interval a colour such that any two intervals that intersect must be assigned different colours. Describe an  $O(n \log n)$  algorithm that assigns each interval a colour and uses the minimum number of colours.

**Rubric.**

- You must justify the correctness of the algorithm and argue its time complexity.
- This task will form part of the portfolio.
- Ensure that your argument is clear and keep reworking your solutions until your lab demonstrator is happy with your work.