

Code Documentation

1. NFA to DFA conversion

I. Epsilon NFA to DFA

Step 1 – Consider $M = \{Q, \Sigma, \delta, q_0, F\}$ is NFA with ϵ . We have to convert this NFA with ϵ to equivalent DFA denoted by

$M_0 = (Q_0, \Sigma, \delta_0, q_0, F_0)$

Then obtain,

$\epsilon\text{-closure}(q_0) = \{p_1, p_2, p_3, \dots, p_n\}$

then $\{p_1, p_2, p_3, \dots, p_n\}$ becomes a start state of DFA

now $\{p_1, p_2, p_3, \dots, p_n\} \in Q_0$

```
1
2  epsilon_closures = {}
3  # Get all epsilon closure of all states
4  for state in self.transitions:
5      epsilon_closures[state] = self.epsilon_closure(state)
6  print("Epsilon closures:", epsilon_closures)
7  states = []
8  states_closures = []
9  ts = {}
10 newAlphabet = self.alphabet
11 newAlphabet.remove('eps')
12 i=0
13 # Add the epsilon closures of the first state
14 states_closures.append(list(epsilon_closures.values())[0])
15 j = len(states_closures)
16 newAcceptingStates = []
17
```

Step 2 – We will obtain δ transition on $\{p_1, p_2, p_3, \dots, p_n\}$ for each input.

$\delta_0(\{p_1, p_2, p_3, \dots, p_n\}, a) = \epsilon\text{-closure}(\delta(p_1, a) \cup \delta(p_2, a) \cup \dots \cup \delta(p_n, a))$

$= \cup_{i=1 \text{ to } n} \epsilon\text{-closure } d(p_i, a)$

Where a is input $\in \Sigma$

```

1
2 # Loop on new added states
3 while j>0:
4
5     closures = states_closures[i]
6
7     l = list(closures)
8     # If any state in accepting state is in this epsilon closures add it to the accepting states
9     if len(set(self.acceptingStates).intersection(l)):
10         newAcceptingStates.append('q'+str(i))
11
12
13     ts['q'+str(i)] = {}
14     states.append('q'+str(i))
15     print('q'+str(i))
16     print(closures)
17
18     # Loop on each alphabet
19     for alpha in newAlphabet:
20         nextState = set()
21         # Get all next states based on the input alphabet
22         for st in l:
23             nextState |= set(self.transitions[st][alpha])
24         ep = set()
25         # loop on next states of the alphabet
26         for n in nextState:
27             if len(n)>0:
28                 # Get all epsilon closures for each next state
29                 ep |= epsilon_closures[n]
30         print(alpha,ep)
31         # If this state epsilon closure in not already added then add it
32         if not(ep in states_closures) and len(ep)>0:
33             states_closures.append(ep)
34             j+=1
35         # To handle when there is no edge between states or when there is no epsilon closures
36         if len(ep)>0:
37             ts['q'+str(i)][alpha] = 'q'+str(states_closures.index(ep))
38         else:
39             ts['q'+str(i)][alpha] = []
40
41
42     print(ts)
43     # Decrement j to loop
44     j-=1
45     # Increment the new states counter
46     i+=1

```

Step 3 – The state obtained $[p_1, p_2, p_3, \dots, p_n] \in Q_0$.

The states containing final state in p_i is a final state in DFA

II. NFA to DFA without epsilon

Steps for converting NFA to DFA:

Step 1: Initially $Q' = \phi$

Step 2: Add q_0 of NFA to Q' . Then find the transitions from this start state.

```
1
2 states = [self.states[0]]
3 ts = {}
4 # Add first state
5 ts[self.states[0]] = getTransitionsOf(self.states[0],self.transitions)
6 i= len(states)
```

Step 3: In Q' , find the possible set of states for each input symbol. If this set of states is not in Q' , then add it to Q' .

```
1
2 # Loop whenever a state is added
3 while i>=0:
4     # Loop to get (To states) from the transitions dictionary
5     for a, toStates in ts[states[i- len(states)]]:
6         # If the same input alphabet goes to more than one state then name this state with '-' separated between the names of state
7         temp = '-'.join(toStates)
8         # If this state is not already added then add it
9         if not(temp in states) and temp != '':
10             newTransitions = getTransitionsOf(temp,self.transitions)
11             states.append(temp)
12             ts[temp] = newTransitions
13             i+=1
14     i-=1
```

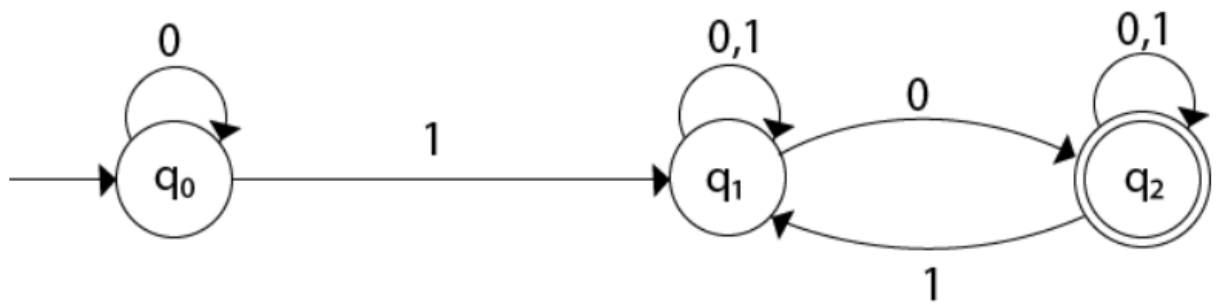
Step 4: In DFA, the final state will be all the states which contain F(final states of NFA)

```
# Function to get Accepting states
acceptingStates = self.getAcceptingStates(self.acceptingStates,states)

def getAcceptingStates(self,oldStates,newStates):
    states = []
    for s in newStates:
        if s in oldStates or len(set(oldStates).intersection(set(s.split('-'))))>0:
            states.append(s)
    return states
```

Screenshots:

For example:



python

Alphabets:(separated by ','), for ϵ add eps

0,1

States:(separated by ',')

q0,q1,q2

Start State

q0

Accepting States:(separated by ',')

q2

Next

Input transition table:

	0	1
->q0	q0	q1
q1	q1,q2	q1
*q2	q2	q1,q2

Enter the transition in the table

To enter multiple destination states (separate by ',')

Convert to DFA

Output:

	0	1
->q0	q0	q1
q1	q1-q2	q1
*q1-q2	q1-q2	q1-q2

2. CFG to PDA conversion

Step 1: The code defines a PDA (Pushdown Automaton) class, which simulates a context-free grammar (CFG) using a pushdown automaton.

Initialize the PDA instance: The `__init__` method initializes a new PDA instance with the following parameters:

variables: A set of variables (non-terminal symbols) in the CFG.

terminals: A set of terminal symbols in the CFG.

start_variable: The start variable for the CFG.

production_rules: A dictionary containing the production rules for each variable.

```
class PDA:
    def __init__(self, variables, terminals, start_variable, production_rules):
        self.states = ['q_start', 'q_push_start_var', 'q_loop', 'q_final']
        self.variables = variables
        self.terminals = terminals
        self.start_variable = start_variable
        self.production_rules = production_rules
        self.transitions = self.create_transitions()
```

Step 2: The `create_transitions` method generates the transition rules for the PDA, based on the given CFG. The transitions are created for the following scenarios:

- Transition from `q_start` to `q_push_start_var`, pushing the stack symbol \$.
- Transition from `q_push_start_var` to `q_loop`, pushing the start variable.
- Transitions for production rules, in the `q_loop` state. If a variable `A` produces a string `w`, the PDA pushes the symbols of `w` in reverse order onto the stack.
- Transitions for terminal symbols, in the `q_loop` state, reading the terminal symbol from the input and popping it from the stack.
- Transition from `q_loop` to `q_final`, popping the stack symbol \$.

```
def create_transitions(self):
    transitions = {}

    # Transition from q_start to q_push_start_var, pushing the stack symbol $
    transitions[('q_start', '', '')] = [('q_push_start_var', '$')]

    # Transition from q_push_start_var to q_loop, pushing the start variable
    transitions[('q_push_start_var', '', '')] = [('q_loop', self.start_variable)]

    # Transitions for production rules, in q_loop state
    state_counter = 1

    # Loop through the production rules for each variable
    for variable in self.variables:
        for prod_rule in self.production_rules[variable]:
            previous_state = 'q_loop'

            # Loop through the symbols in the production rule, in reverse order
            for symbol in enumerate(prod_rule[::-1]):
                new_state = f'q_alt_{state_counter}'
                state_counter += 1
                transitions[(previous_state, '', variable)] = [(new_state, symbol)]
                previous_state = new_state
                variable = '' # Clear the variable after the first iteration

            # Transition back to q_loop after pushing all symbols
            transitions[(previous_state, '', '')] = [('q_loop', '')]
```

```

# Transitions for terminal symbols, in q_loop state
for terminal in self.terminals:
    # For each terminal symbol a, with input a and pop a, push ε
    transitions[('q_loop', terminal, terminal)] = [('q_loop', '')]

# Transition from q_loop to q_final, popping the stack symbol $
transitions[('q_loop', '', '$')] = [('q_final', '')]

return transitions

```

Step 3: The main function processes the given CFG by creating a PDA instance and printing the generated transition rules.

```

# Main function for testing the PDA class
def main():
    # Define variables, terminals, start variable, and production rules
    variables = {'S', 'B'}
    terminals = {'a', 'b', 'c'}
    start_variable = 'S'
    production_rules = {
        'S': ['aBc', 'ab'],
        'B': ['SB', '']
    }

    # Create a PDA object with the given parameters
    pda = PDA(variables, terminals, start_variable, production_rules)

    # Print the transitions in a human-readable format
    for key, values in pda.transitions.items():
        for value in values:
            print(f"From {key[0]} with input '{key[1]}' and pop '{key[2]}' to {value[0]} and push '{value[1]}'")

    print(f"")
    print(f"another format\n")

    # Print the transitions in another format
    for key, values in pda.transitions.items():
        for value in values:
            print(f"{key[0]}, '{key[1]}', '{key[2]}' --> {value[0]}, '{value[1]}'")

```

past cfg

```

variables = {'S', 'B'}
terminals = {'a', 'b', 'c'}
start_variable = 'S'
production_rules = {
    'S': ['aBc', 'ab'],
    'B': ['SB', '']
}

# Create a PDA object with the given parameters
pda = PDA(variables, terminals, start_variable, production_rules)

```

```
PROBLEMS OUTPUT DEBUG CONSOLE TERMINAL

PS C:\Users\ziada> & C:/Users/ziada/AppData/Local/Programs/Python/Python311/python.exe "c:/Users/ziada/OneDrive
From q_start with input '' and pop '': to q_push_start_var and push '$'
From q_push_start_var with input '' and pop '': to q_loop and push 'S'
From q_loop with input '' and pop 'S': to q_alt_1 and push '(0, 'c')'
From q_alt_1 with input '' and pop '': to q_alt_2 and push '(1, 'B')'
From q_alt_2 with input '' and pop '': to q_alt_3 and push '(2, 'a')'
From q_alt_3 with input '' and pop '': to q_loop and push ''
From q_loop with input '' and pop '': to q_loop and push ''
From q_alt_4 with input '' and pop '': to q_alt_5 and push '(1, 'a')'
From q_alt_5 with input '' and pop '': to q_loop and push ''
From q_loop with input '' and pop 'B': to q_alt_6 and push '(0, 'B')'
From q_alt_6 with input '' and pop '': to q_alt_7 and push '(1, 'S')'
From q_alt_7 with input '' and pop '': to q_loop and push ''
From q_loop with input 'c' and pop 'c': to q_loop and push ''
From q_loop with input 'b' and pop 'b': to q_loop and push ''
From q_loop with input 'a' and pop 'a': to q_loop and push ''
From q_loop with input '' and pop '$': to q_final and push ''
```

Another Format

```
PROBLEMS OUTPUT DEBUG CONSOLE TERMINAL

From q_loop with input '' and pop '$': to q_final and push

another format

q_start, '', '': --> q_push_start_var, '$'
q_push_start_var, '', '': --> q_loop, 'S'
q_loop, '', 'S': --> q_alt_1, '(0, 'c')'
q_alt_1, '', '': --> q_alt_2, '(1, 'B')'
q_alt_2, '', '': --> q_alt_3, '(2, 'a')'
q_alt_3, '', '': --> q_loop, ''
q_loop, '', '': --> q_loop, ''
q_alt_4, '', '': --> q_alt_5, '(1, 'a')'
q_alt_5, '', '': --> q_loop, ''
q_loop, '', 'B': --> q_alt_6, '(0, 'B')'
q_alt_6, '', '': --> q_alt_7, '(1, 'S')'
q_alt_7, '', '': --> q_loop, ''
q_loop, 'c', 'c': --> q_loop, ''
q_loop, 'b', 'b': --> q_loop, ''
q_loop, 'a', 'a': --> q_loop, ''
q_loop, '', '$': --> q_final, ''
```