

Supporting information for: Reproducing Relative Alchemical Free Energies of Hydration

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1 Softcore Functions

We describe here the softcore functions^{S1,S2} as implemented in the MD packages AMBER, CHARMM, Gromacs and Sire. Both the van der Waals, V_{LJ} (Lennard–Jones potential) and the electrostatic interactions, V_{Coul} (Coulomb potential) as a function of the order parameter λ are given for the disappearing atoms only. For the appearing atoms replace λ with $1 - \lambda$ and *vice versa*. Eq. (1) is the generalized form for all codes while the specific distance dependent

functions are outlined in eq. (2) for Sire, eq. (3) for AMBER, eq. (4) for Gromacs and eq. (5) for CHARMM.

$$V = V_{\text{LJ}} + V_{\text{Coul}} = 4\epsilon_{\text{ij}}(1 - \lambda) \left[\left(\frac{\sigma_{ij}}{r_{\text{LJ}}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{\text{LJ}}} \right)^6 \right] + (1 - \lambda)^n \frac{q_i q_j}{4\pi\epsilon_0 r_{\text{Coul}}} \quad (1)$$

For Sire

$$\begin{aligned} r_{\text{LJ}} &= (\alpha\sigma_{ij}\lambda + r_{ij}^2)^{\frac{1}{2}} \\ r_{\text{Coul}} &= (\lambda + r_{ij}^2)^{\frac{1}{2}} \end{aligned} \quad (2)$$

For AMBER

$$\begin{aligned} r_{\text{LJ}} &= (\alpha\sigma_{ij}^6\lambda + r_{ij}^6)^{\frac{1}{6}} \\ r_{\text{Coul}} &= (\beta\lambda + r_{ij}^p)^{\frac{1}{p}} \\ n &= 1 \end{aligned} \quad (3)$$

For Gromacs

$$\begin{aligned} r_{\text{LJ}} &= (\alpha\sigma_{ij}^w\lambda^p + r_{ij}^w)^{\frac{1}{w}} \\ p &= 1, 2; w = 6, 48; \\ r_{\text{Coul}} &= r_{\text{LJ}} \\ \alpha_{\text{Coul}} &= 0, \alpha_{\text{LJ}} \\ n &= 1 \end{aligned} \quad (4)$$

For CHARMM (PSSP), applied to all “reactant” and all “product” atoms

$$\begin{aligned} r_{\text{LJ}} &= (\alpha\lambda + r_{ij}^2)^{\frac{1}{2}} \\ r_{\text{Coul}} &= (\beta\lambda + r_{ij}^2)^{\frac{1}{2}} \\ n &= 1 \end{aligned} \quad (5)$$

r_{vdW} , r_{Coul} and r_{Coul} (all in red) are the distance dependent functions, ϵ_{ij} and σ_{ij} are the Lennard-Jones parameters, q_i and q_j are the charges and ϵ_0 is the vacuum permittivity, α and β are the softcore tuning parameters determining the softness of the potential, and r_{ij} the distance between atoms i and j .

The exponent n is only used in the Coulomb softcore function of Sire. Gromacs allows additional exponents for λ ($p = 1$ or 2) and w for the distance dependency with values of either 6 or 48. The Coulomb softcore parameter α_{Coul} in Gromacs is the same as for the Lennard-Jones parameter α_{LJ} unless the Coulomb softcore function is requested not to be used and thus $\alpha_{\text{Coul}} = 0$. The CHARMM softcore function (PSSP) is applied to *all* atoms in the perturbed group and not only to dummy atoms as in the other codes. The perturbed group comprises of all atoms that need to be transformed, i.e. any atom that differs in at least one force field parameter in the other end state. “Dummy” atom is used here as a shorthand notation for any atom that appears or disappears during the course of the transformation.

2 Separated Protocols

When the AFE (alchemical free energy) simulation is separated into van der Waals and Coulomb steps it must be ensured that charges of vanishing atoms are switched off before the vdW radius is scaled to zero. This is to avoid that other atoms e.g. from solvent come in close contact to a charged atom without the associated excluded volume from the van der Waals term.

Figure S1 depicts how force field parameters vary for a transformation carried out in the direction of disappearing atoms. The mutation is shown with the charge step first followed by the vdW step but each step can really be run independently. Please note that both charge and vdW step would be simulated at a range of individual λ s. Typically the charge transfer is done with linear scaling while the vdW mutation is done with softcores (see above). The transformation is fully symmetrical that is the parameters must be switched on in opposite

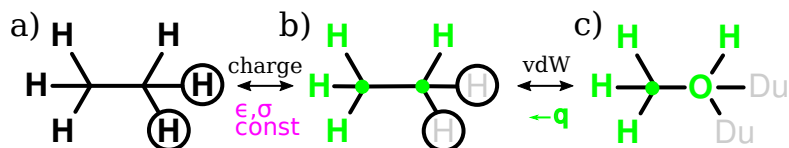


Figure S1: The mutation of ethane into methanol and explicit topologies for three states. a) The two circles denote atoms that have both vdW and Coulomb terms switched on with parameters for the respective hydrogen atom type. b) The two hydrogen atoms have their charges switched to zero (gray symbols in black circle). All other charges are the ones from the methanol end state c (green) to ensures charge neutrality at each step. VdW parameters are constant in the charge transfer step (see annotations in magenta). c) vdW and Coulomb parameters as for methanol while dummy atoms (gray Du) have those parameters all set to zero.

order if atoms are to be “created”. The intermediate state b has the vdW parameters from state a but the charges from state c.

Figure S1 shows how topology files may be created in cases where the MD software does not allow independent λ s for electrostatic and vdW mutations. With Gromacs, for instance, the transformation only requires a single topology file with both A and B states (in single topology fashion, see main text) and a single simulation control file with separate λ vectors for charge and vdW transformations. Any intermediate state from Figure S1 is thus created “on-the-fly” i.e. implicitly during the simulation run. With AMBER (up to version 16 as of this writing), however, three explicit topology files (with sander, two with pmemd) and two control files would need to be created. The state b in Figure S1 would be created from state a with the charges from state c. The bonded terms can be combined with either mutation step or run separately. For AMBER the easiest way is to combine vdW with bonded terms because charges are independent of atom types.

Figure S2 illustrates explicit topologies for transformations with both appearing and disappearing atoms in one simulation. The principle is essentially the same as in Figure S1: charges of dummy atoms must be switched off before vdW parameters are set to zero to avoid interactions of “naked” charge sites with other atoms possibly leading to very close contact, large energies and forces, and thus to unstable simulations and/or noisy statistics. However, charge neutrality at every λ step is not supported in most MD codes i.e. the total system

charge varies with λ unless the charges of *all* atoms are switched off. Possible strategies would be to explicitly create topology files for each intermediate λ state and distribute the diminished charges from the dummy atoms over to the non-dummy atoms. MD software like CHARMM allows to do this through scripting although this would be just as extensive as scripting the aforementioned strategy.

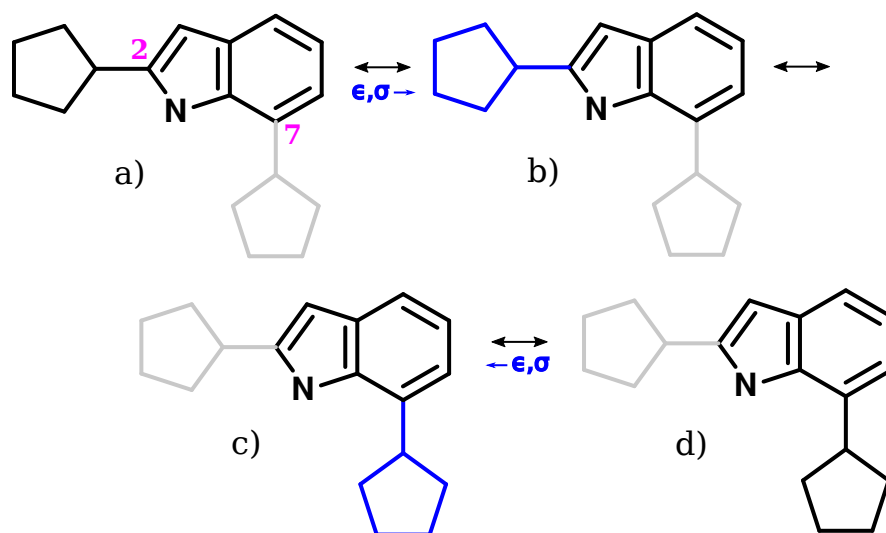


Figure S2: Explicit topologies involved in a mutation with both appearing and disappearing atoms by example of the cyclopentanyl transfer from the 2 position in indole to the 7 position. Blue lines denote atoms which have their charges switched off but with vdW parameters from the left (state b) or right (state c). Gray lines are dummy atoms with Coulomb and vdW parameters all zero. Note, the hydrogen bound to the 2 (state d) and 7 positions (state a) can be directly mutated from the respective carbon atom type without ring breaking.^{S3}

With the MD packages tested in this study the number of input files are as follows. With Gromacs this can be done with only two topology and two control files where one charge transfer can be combined with a vdW on/off step. Gromacs' λ vectors only apply to the perturbed group as a whole and so it is not possible to define a λ vector for only a subset. AMBER requires two such files with sander and three topology/two control files with pmemd for the three steps charge off, vdw on/off and charge on. This is possible because with AMBER a subset of the perturbed group can be chosen to have zero charges (but AMBER does not have λ vectors). CHARMM has scripting facilities that let the user manipulate force field parameters of any arbitrary subset of the system such that intermediate states

can be defined “on-the-fly” with only one control script and one topology file. The tool FESetup^{S4} automates most of these setup steps for all these MD packages.

3 Detailed Results

3.1 AMBER

Table S1 compares the separated protocol with the 1-step protocol. The separated protocol transforms Coulomb force field parameters separately from the Lennard-Jones and all bonded parameters. The 1-step protocol transforms all force field parameters simultaneously and thus invokes both Coulomb and vdW softcore functions.

Table S1: Comparison between separated and 1-step protocol in AMBER. The data for the 1-step protocol highlights problems in the code in red. ΔG_{sol} has been computed with pmemd. ΔG_{vac} has been computed with sander.

transformation		separated protocol			1-step		
		ΔG_{sol}	ΔG_{vac}	$\Delta\Delta G$	ΔG_{sol}	ΔG_{vac}	$\Delta\Delta G$
ethane	methane	1.794	1.773	0.021	2.784	2.855	-0.071
methane	ethane	-1.800	-1.801	0.001	-2.866	-2.862	-0.004
methanol	methane	2.746	-3.443	6.189	7.102	0.871	6.231
methane	methanol	-2.747	3.448	-6.195	-7.176	-0.857	-6.319
ethane	methanol	-2.838	3.362	-6.200	-2.250	3.996	-6.246
methanol	ethane	2.836	-3.361	6.196	2.199	-3.998	6.197
toluene	methane	9.222	5.982	3.240	6.090	0.450	5.640
methane	toluene	-9.286	-5.863	-3.422	-6.155	-0.539	-5.616
neopentane ^a	methane	70.163	69.848	0.315	65.763	58.495	7.267
methane ^a	neopentane	-70.171	-69.921	-0.250	-65.824	-58.779	-7.045
neopentane ^b	methane	11.411	11.544	-0.132	4.424	3.480	0.944
methane ^b	neopentane	-11.426	-11.550	0.125	-4.447	-3.485	-0.962
2-methylfuran	methane	14.622	11.533	3.089	2.205	-0.943	3.148
methane	2-methylfuran	-14.604	-11.504	-3.100	-2.216	-0.063	-2.153
2-methylindole	methane	24.251	15.473	8.778	7.113	-4.021	11.135
methane	2-methylindole	-24.312	-15.174	-9.138	-7.128	1.858	-8.986

^acentral mapping.

^bterminal mapping.

The separated protocol produces consistent results in both solution and in vacuum. The

values are in line with the free energies obtained with the other MD packages (see main text). Each ΔG is the sum of the charge and vdW plus bonded contributions. The 1-step protocol on the other hand displays various problems. While the smaller systems with only a few dummy atoms show ΔG and $\Delta\Delta G$ consistent with the separated protocol, the larger transformations show, in part, striking differences and even inconsistencies in forward and backward vacuum simulations. It is not clear, however, if the inconsistencies can be attributed to the vacuum transformations only.

Figure S3 shows a problem with end point geometries. This is demonstrated with the average distance between the carbon atom and the four attached hydrogens atoms in the neopentane to methane case. The methane carbon atom is mapped here to the central atom of neopentane. The distances are recorded for the vdW plus bonded transformation i.e. the charges correspond to the methane end state.

The geometrical variation along λ for the data in the main text is shown in the black and red graphs. The initial distance is slightly smaller than what is expected from a C–H distance for the particular atom types at $\lambda = 0$. The final distance is about 1.23 Å which is in contrast to the 1.09 Å of the c3–hc bond of the GAFF force field. The crosses in violet mark the geometries of the “pure” (non-perturbed) end points and are connected with a straight line. The other crosses denote test cases which successively replace the methyls on neopentane with hydrogens. The C–H distance decreases in correlation with the number of the methyl groups i.e. tert-butane, propane, ethane. This seems to suggest that a “crowding” of dummy atoms around a central atom compounds the problem of a too long C–H distance. Neither of these three test cases, however, displays the expected end point distance.

To further test this hypothesis methyl and ethyl groups are added to all terminal methyl groups of neopentane, see cyan and green lines in Figure S3. In both cases the end point distance is about 1.12 Å with a slightly lower value for the ethyl substitution but which are still too high.

As Gromacs conveniently allows us to use a separate λ for bonded terms we tested this on

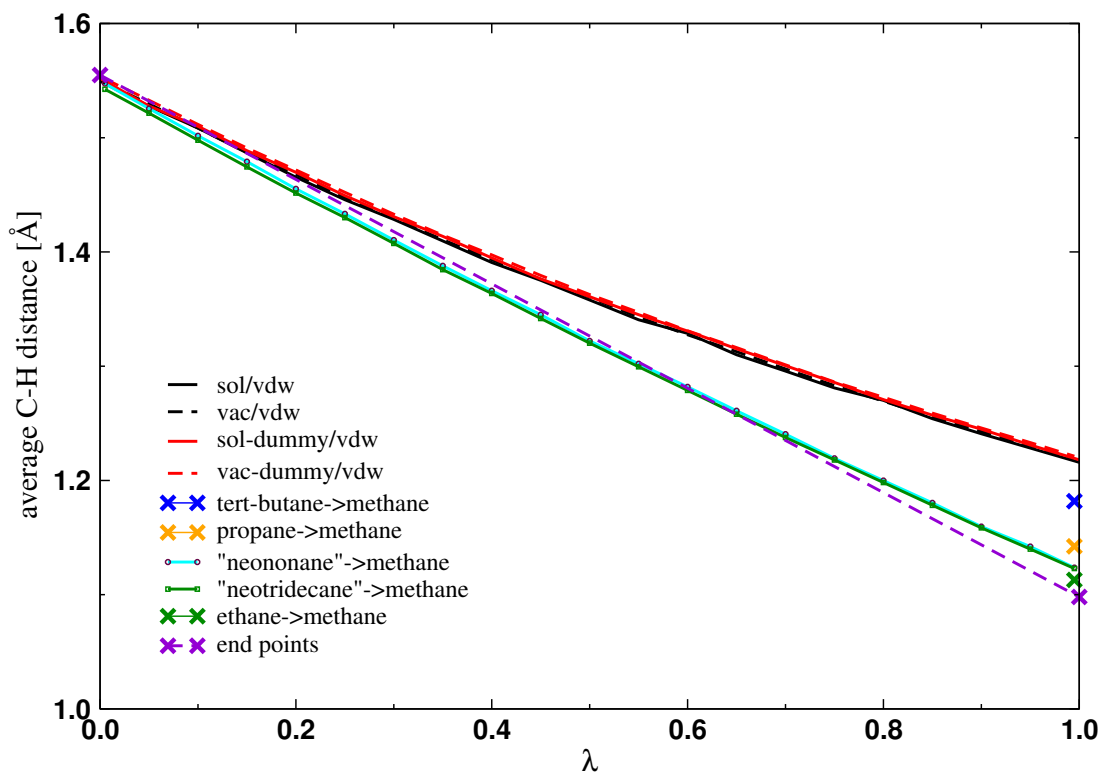


Figure S3: The average C–H distance shown as a function of λ for the neopentane to methane and related cases. The black and red lines display how the distance changes in solution and the vacuum phase, and with and without explicit dummy atoms. The other test systems are designed to reduce the number of dummy atoms that surround the central carbon atom to show whether “crowding” is the cause of the issue. The crosses denote end points only, in particular the violet crosses represent the non-perturbed end point distances. For details see the text.

the neopentane case. After the charges were transformed to the methane end state (dummy atoms have zero charges), the bonded terms were mutated from neopentane to methane while the vdW parameters were kept constant at the neopentane initial state. The observed end distance was about 1.23 Å which is to be expected given that the symmetrically arranged methyl groups will repel each other and thus not allow to reach the final distance. Only after the final vdW (only) mutation had been carried out, were the final distances of 1.09 Å reached.

Table S2 summarizes the free energy components for the 2-methylindole to methane case for both forward and backward transformations. The electrostatic contributions display a very small SEM and the averages from both directions agree with each other up to the

second digit after the comma. The van der Waals contributions show a higher SEM and the averages from the solution simulations agree well with each other. However, the van der Waals contributions from the vacuum transformation are apart by $0.3 \text{ kcal mol}^{-1}$ (highlighted in red).

Table S2: Free energy components for 2-methylindole computed from implicit dummy RAFF simulations. The data are averages over three runs.

transformation		$\Delta G_{\text{sol}}^{\text{vdW}}$	SEM	$\Delta G_{\text{vac}}^{\text{vdW}}$	SEM	$\Delta G_{\text{sol}}^{\text{elec}}$	SEM	$\Delta G_{\text{vac}}^{\text{elec}}$	SEM
2-methylindole	methane	4.832	0.022	3.484	0.009	19.419	0.007	11.989	0.001
methane	2-methylindole	-4.900	0.017	-3.185	0.011	-19.412	0.009	-11.989	0.001

In sum, this indicates a problem of the RAFF code in AMBER. Whether that is a bug or a conceptual issue with the particular implementation can not be explained at the moment.

Table S3 summarizes the free energies obtained from forward and backward simulations of the cyclopentanyl transfer from position 2 to position 7 on indole and *vice versa*. Results from three different protocols are shown: 1) implicit dummy atoms and partial re/discharge of the 5-ring only; 2) implicit dummy atoms and full re/discharge of all atoms; 3) explicit dummy atoms and partial re/discharge. The free energies from the implicit dummy simulations agree very well with each other while the explicit dummy atom results are about $0.2 \text{ kcal mol}^{-1}$ higher and forward and backward simulations have a larger hysteresis of $0.1 \text{ kcal mol}^{-1}$.

3.2 Sire/SOMD

Table S4 shows relative free energy of hydration $\Delta\Delta G$ compared to $\Delta\Delta G$ values extracted from absolute free energy calculations, depicted in Fig ?? in the paper.

Initially, Sire/SOMD RAFF protocols used all bonds constraint algorithm. In this way all the solute bonds are constrained, which results in a systematic offset for each RAFF predictions, compared to the RAFF from absolute free energy calculations. Figure S4 show the discrepancy between RAFF computed with all bond constraints and RAFF from absolute free energy calculations.

Table S3: Free energies of hydration for the 2-cyclopentanylindole to 7-cyclopentanylindole case with three different protocols. The data are averages over three runs.

transformation		ΔG_{sol}	SEM	ΔG_{vac}	SEM	$\Delta\Delta G_{\text{hydr}}$	SEM
implicit, partial							
2-cyclopentanylindole	7-cyclopentanylindole	4.194	0.032	3.833	0.014	0.361	0.032
7-cyclopentanylindole	2-cyclopentanylindole	-4.300	0.044	-3.964	0.011	-0.335	0.045
implicit, full							
2-cyclopentanylindole	7-cyclopentanylindole	4.286	0.063	3.921	0.028	0.365	0.069
7-cyclopentanylindole	2-cyclopentanylindole	-4.418	0.033	-4.098	0.014	-0.320	0.036
explicit, partial							
2-cyclopentanylindole	7-cyclopentanylindole	4.145	0.041	3.517	0.043	0.628	0.059
7-cyclopentanylindole	2-cyclopentanylindole	-4.256	0.030	-3.759	0.009	-0.497	0.032

Table S4: Final relative free energy of hydration $\Delta\Delta G$ estimations and standard error SEM with Sire/SOMD unperturbed hydrogen bonds protocol, RAFF, compared with relative free energy of hydration computed from absolute free energy simulations, RAFF-absolute

transformation		RAFF		RAFF-absolute	
		$\Delta\Delta G$	SEM	$\Delta\Delta G$	SEM
ethane	methane	-0.014	0.056	0.046	0.021
methane	ethane	0.049	0.023	-0.046	0.021
methanol	methane	5.993	0.054	6.214	0.055
methane	methanol	-5.969	0.042	-6.214	0.055
ethane	methanol	-6.091	0.035	-6.260	0.051
methanol	ethane	6.090	0.022	6.260	0.051
toluene	methane	2.891	0.093	3.065	0.031
methane	toluene	-3.069	0.022	-3.065	0.031
neopentane ^a	methane	-0.200	0.054	-0.190	0.060
methane ^a	neopentane	0.139	0.055	0.190	0.060
neopentane ^b	methane	-0.111	0.006	-0.190	0.060
methane ^b	neopentane	0.104	0.063	0.190	0.060
2-methylfuran	methane	2.923	0.055	2.903	0.029
methane	2-methylfuran	-2.834	0.037	-2.903	0.029
2-methylindole	methane	8.643	0.063	8.571	0.029
methane	2-methylindole	-8.674	0.083	-8.571	0.029
2-cyclopentanylindole	7-cyclopentanylindole	-0.116	0.077	0.080	0.142
7-cyclopentanylindole	2-cyclopentanylindole	0.018	0.081	-0.080	0.142

^acentral mapping.

^bterminal mapping.

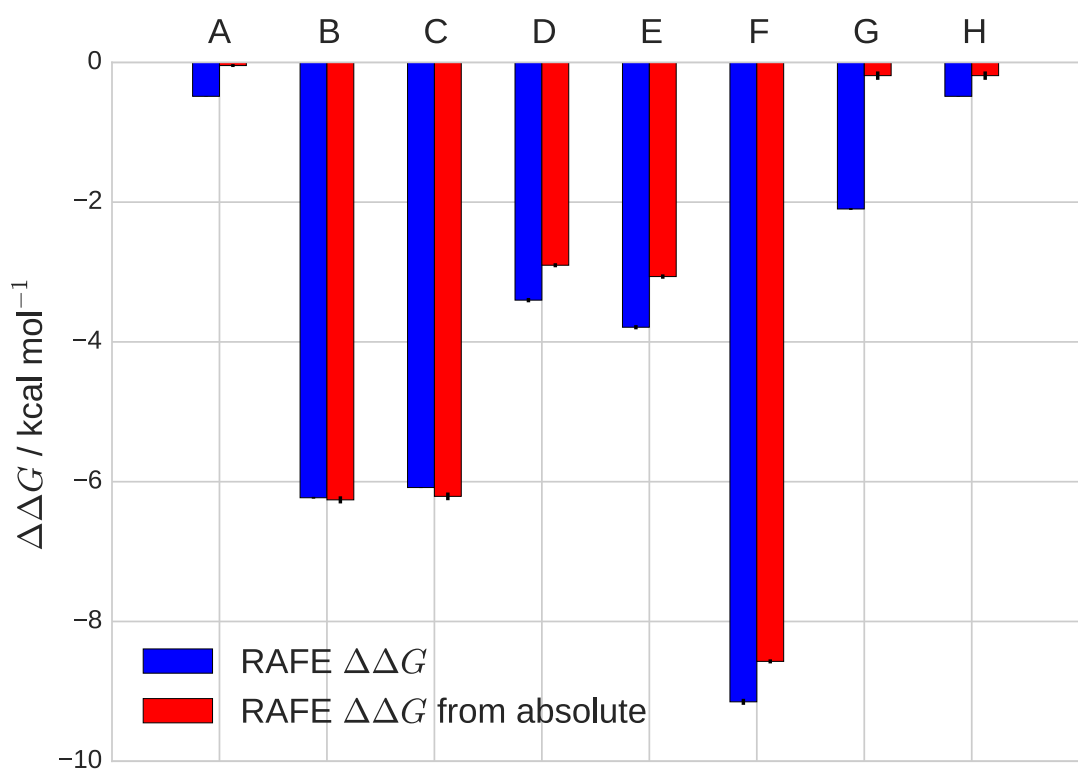


Figure S4: Comparison between RAFE of hydration computed with all bond constraints and RAFE computed from absolute free energy calculations

Finally, figure S5 and tab. S5 compare relative free energy of hydration $\Delta\Delta G$ estimated with RAFE using all bonds constraints, no constraints and unperturbed hydrogen bond constraints.

References

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Table S5: Relative free energy of hydration $\Delta\Delta G$ computed with all bond constraints, *All bonds*, no constraints, *None*, and unperturbed hydrogen bond constraint, *unpert H bonds*

transformation		All bonds		None		unpert H bonds	
		$\Delta\Delta G$	SEM	$\Delta\Delta G$	SEM	$\Delta\Delta G$	SEM
ethane	methane	-0.486	0.003	-0.186	0.041	-0.014	0.056
methane	ethane	0.493	0.005	0.008	0.021	0.0485	0.022
methanol	methane	6.069	0.006	6.498	0.008	5.993	0.054
methane	methanol	-6.083	0.007	-6.153	0.017	-5.969	0.042
ethane	methanol	-6.229	0.012	-6.147	0.031	-6.091	0.035
methanol	ethane	6.235	0.011	6.099	0.004	6.090	0.022
toluene	methane	3.730	0.276	3.096	0.063	2.891	0.093
methane	toluene	-3.790	0.030	-3.071	0.063	-3.069	0.022
neopentane ^a	methane	-2.098	0.013	-0.142	0.142	-0.200	0.054
methane ^a	neopentane	2.041	0.012	0.0187	0.0618	0.139	0.055
neopentane ^b	methane	-0.486	0.003	-0.147	0.060	-0.111	0.006
methane ^b	neopentane	0.593	0.021	-0.147	0.0608	0.104	0.063
2-methylfuran	methane	3.381	0.022	2.817	0.035	2.923	0.055
methane	2-methylfuran	-3.402	0.031	-2.895	0.063	-2.834	0.037
2-methylindole	methane	9.297	0.063	8.721	0.056	8.643	0.063
methane	2-methylindole	-9.150	0.043	-8.615	0.041	-8.674	0.083

^acentral mapping.

^bterminal mapping.

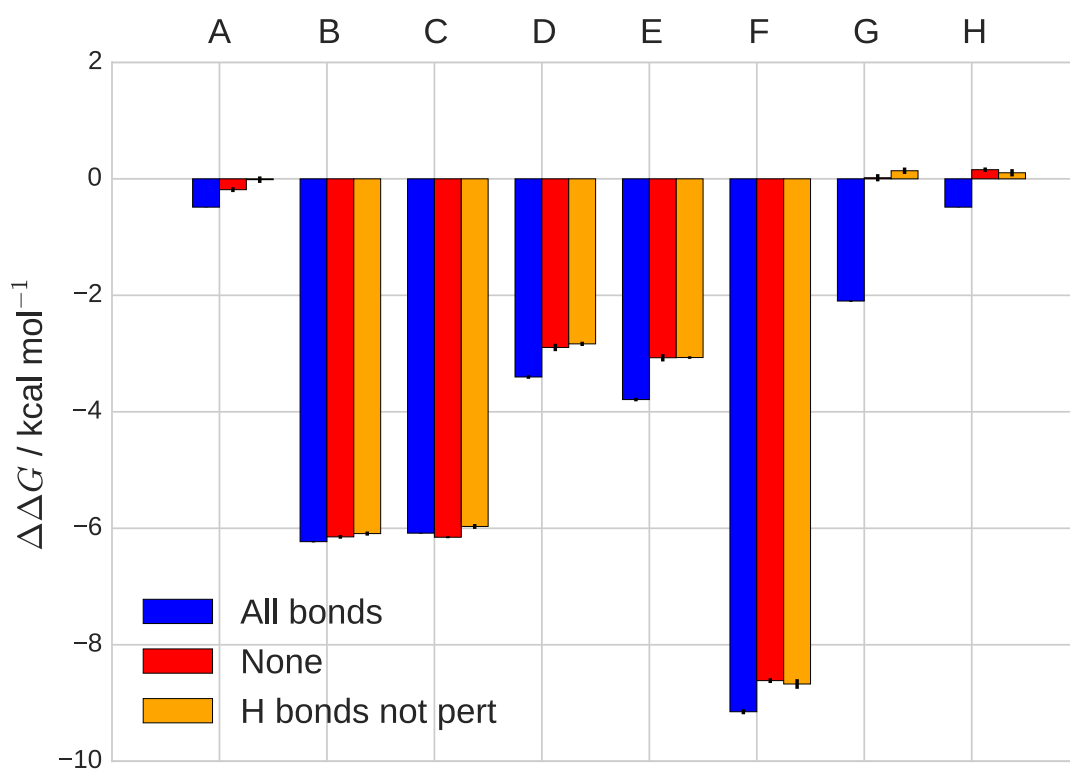


Figure S5: Comparison between RAfE of hydration computed with all bond constraints, no constraints and unperturbed hydrogen bonds constraint

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