

1. Parameters used, for tuning 5 runs I set num_children (lambda) = 100 but it took 10h to run both cells, and I tried to use num_children = 100 for 30 runs (EA), but it took 16 hours running and it never finished so I had to speed the running time by change num_children from 100 to 400, I tried 250 it kept running for 6h and It never finished so I had to make it higher to speed thing up.

a. For with crowding - green_Crowdin_config.txt

```
1 [[ea]
2 mu = 1000
3 num_children = 400
4 mutation_rate = 0.05
5 parent_selection = k_tournament_with_replacement
6 survival_selection = k_tournament_without_replacement
7 # Don't touch this
8 individual_class = LinearGenotype
9
10 [recombination_kwargs]
11 method = uniform
12
13 [parent_selection_kwargs]
14 k = 2
15
16 [survival_selection_kwargs]
17 k = 3
18
19 [fitness_kwargs]
20 crowding = True
21 yellow = False
22 # Don't touch this
23 failure_fitness = ${problem:failure_fitness}
24
25 [mutation_kwargs]
26 bonus = False
27 # Don't touch this
28 bounds = ${problem:bounds}
29
30 # Don't touch any of these
31 [problem]
32 visible_margin = 3
33 failure_fitness = -1
34 minimize_area = False
35 bounds = ((0, 50), (0, 15))
36 shapes = [[(-2, 1), (-2, 0), (-1, 0), (-2, -1), (0, 0), (1, 0), (2, 0), (0, 1), (1, 1), (0, 2), (3, 0),
(-1), (0, 0), (1, -1), (0, 1), (0, 2), (2, -1), (-1, -1), (-1, 1)], [(1, 0), (0, 0), (0, 1), (1, -1),
(1, 1), (0, 2), (0, -2), (0, 3), (0, -3), (1, -2), (1, 3), (1, -3), (1, 2)], [(0, -1), (0, 0), (0, 1)
```

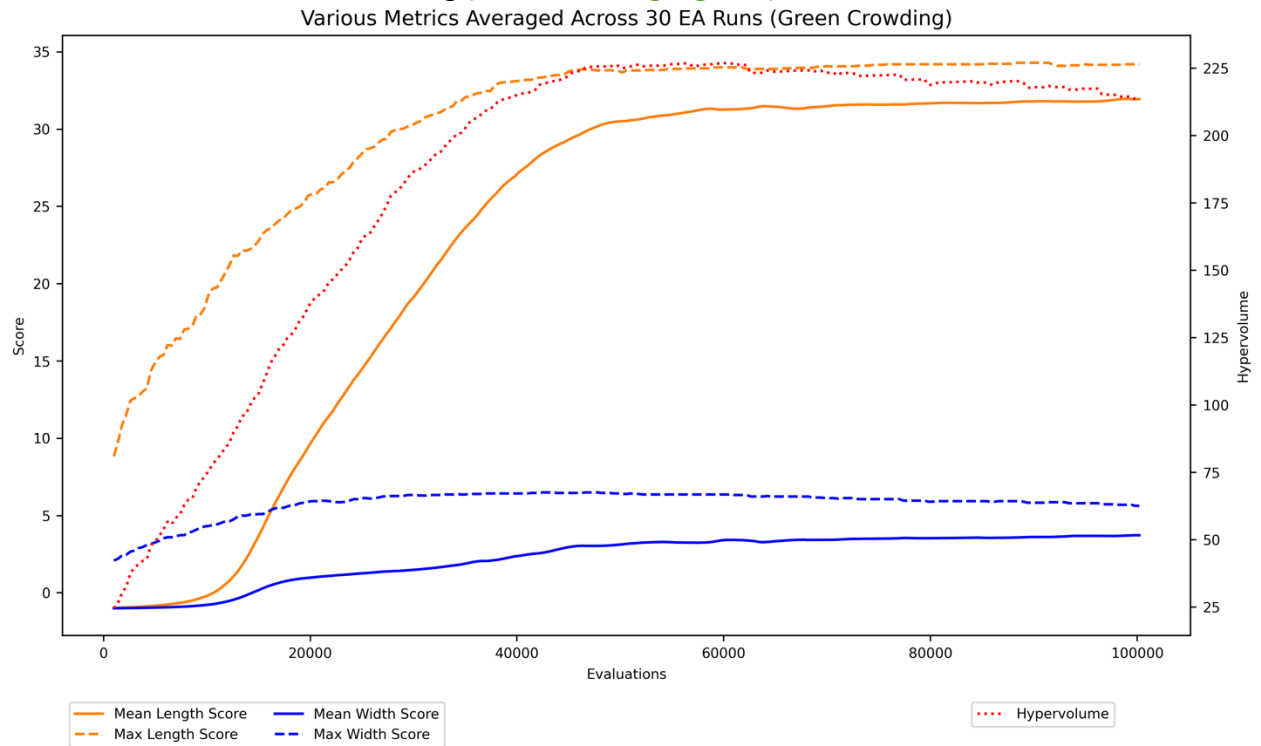
b. for with no crowding – green_no_crowding_config.txt

```
1 [[ea]]
2 mu = 1000
3 num_children = 400
4 mutation_rate = 0.05
5 parent_selection = k_tournament_with_replacement
6 survival_selection = k_tournament_without_replacement
7 # Don't touch this
8 individual_class = LinearGenotype
9
10 [recombination_kwargs]
11 method = uniform
12
13 [parent_selection_kwargs]
14 k = 2
15
16 [survival_selection_kwargs]
17 k = 3
18
19 [fitness_kwargs]
20 crowding = False
21 yellow = False
22 # Don't touch this
23 failure_fitness = ${problem:failure_fitness}
24
25 [mutation_kwargs]
26 bonus = False
27 # Don't touch this
28 bounds = ${problem:bounds}
29
30 # Don't touch any of these
31 [problem]
32 visible_margin = 3
33 failure_fitness = -1
34 minimize_area = False
35 bounds = ((0, 50), (0, 15))
36 shapes = [[(-2, 1), (-2, 0), (-1, 0), (-2, -1), (0, 0), (1, 0), (2, 0), (0, 1), (1, 1), (0, 2), (3, 0),
(-1), (0, 0), (1, -1), (0, 1), (0, 2), (2, -1), (-1, -1), (-1, 1)], [(1, 0), (0, 0), (0, 1), (1, -1),
(1, 1), (0, 2), (0, -2), (0, 3), (0, -3), (1, -2), (1, 3), (1, -3), (1, 2)], [(0, -1), (0, 0), (0, 1)
```

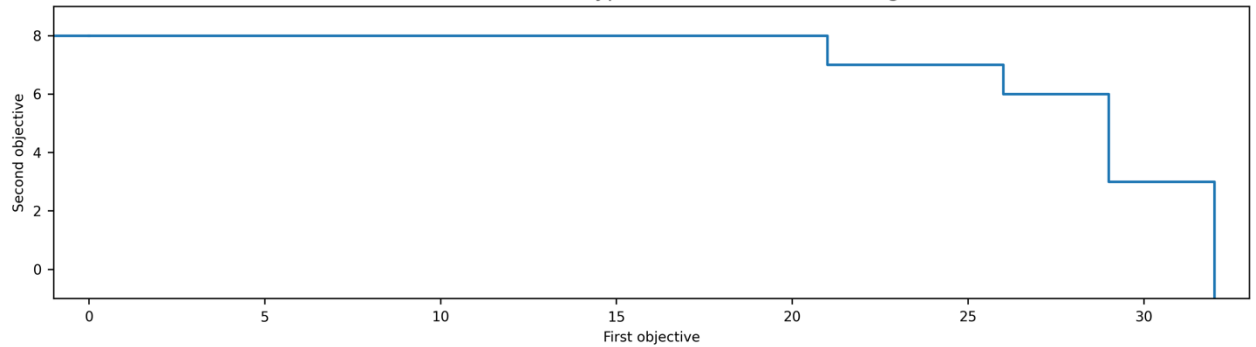
2- plots and combined Pareto front for green trial

For With crowding

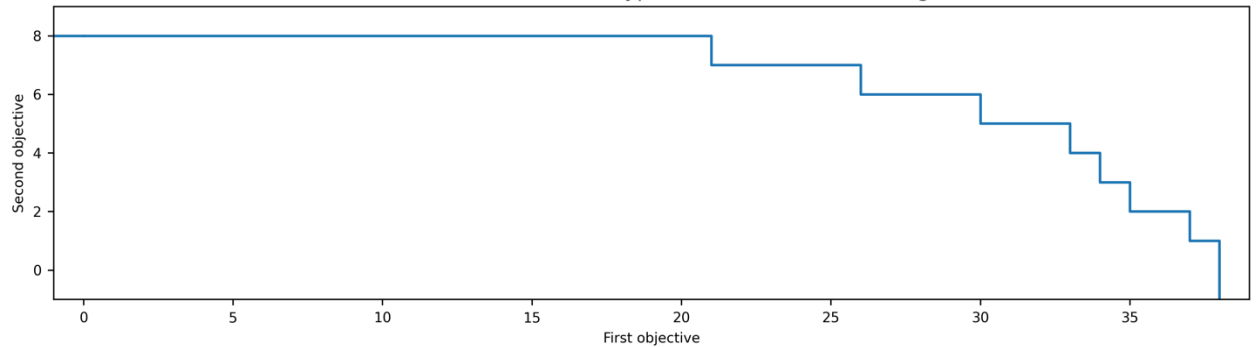
a.1 Plots for 30 runs with crowding (with Crowding – green)



Best Pareto Front Hypervolume (Green Crowding)

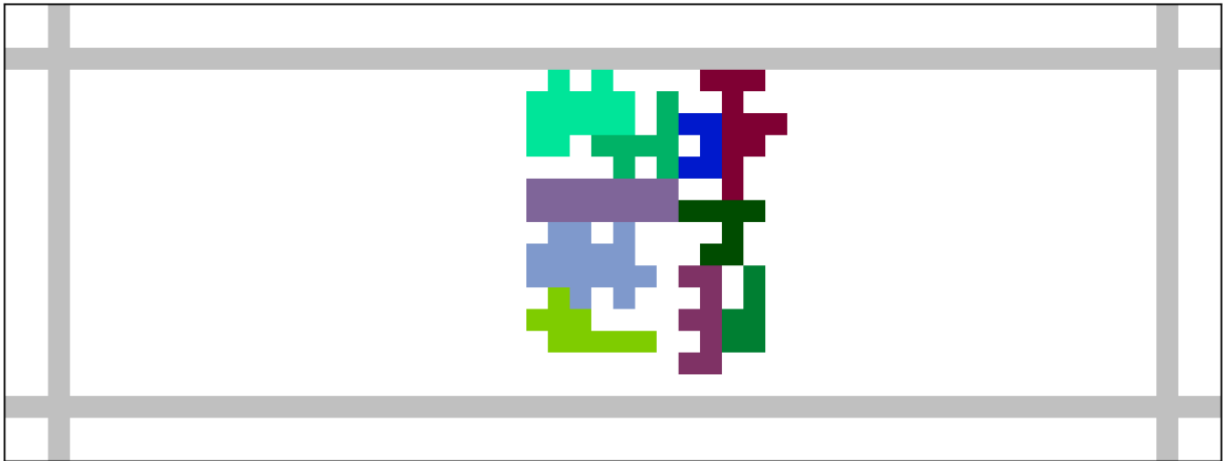


Combined Pareto Front Hypervolume (Green Crowding)

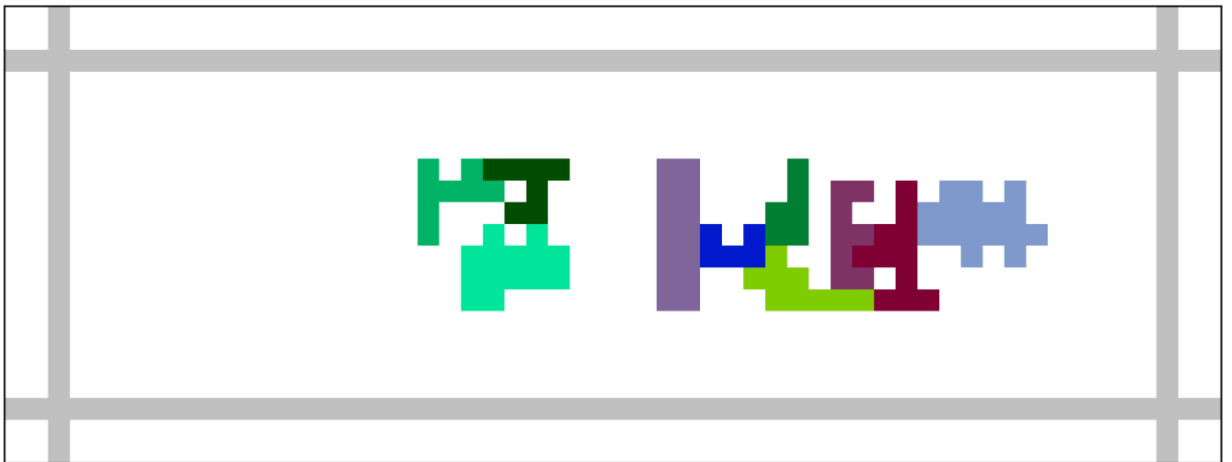


a.2 Combined Pareto Front (with crowding green)

1-Best Length

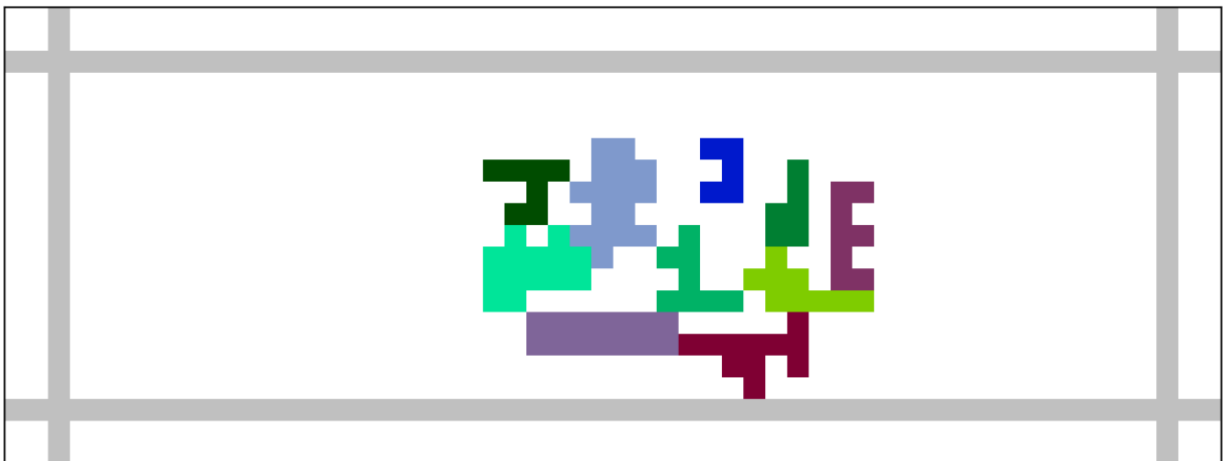


2-Best width

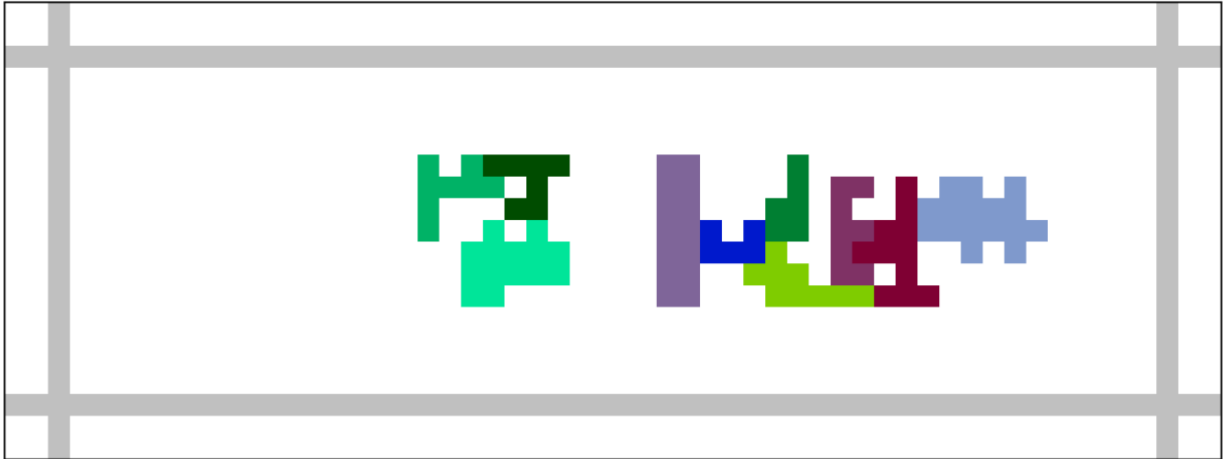


a.3 Best Front (with crowding-green)

1-Best Length

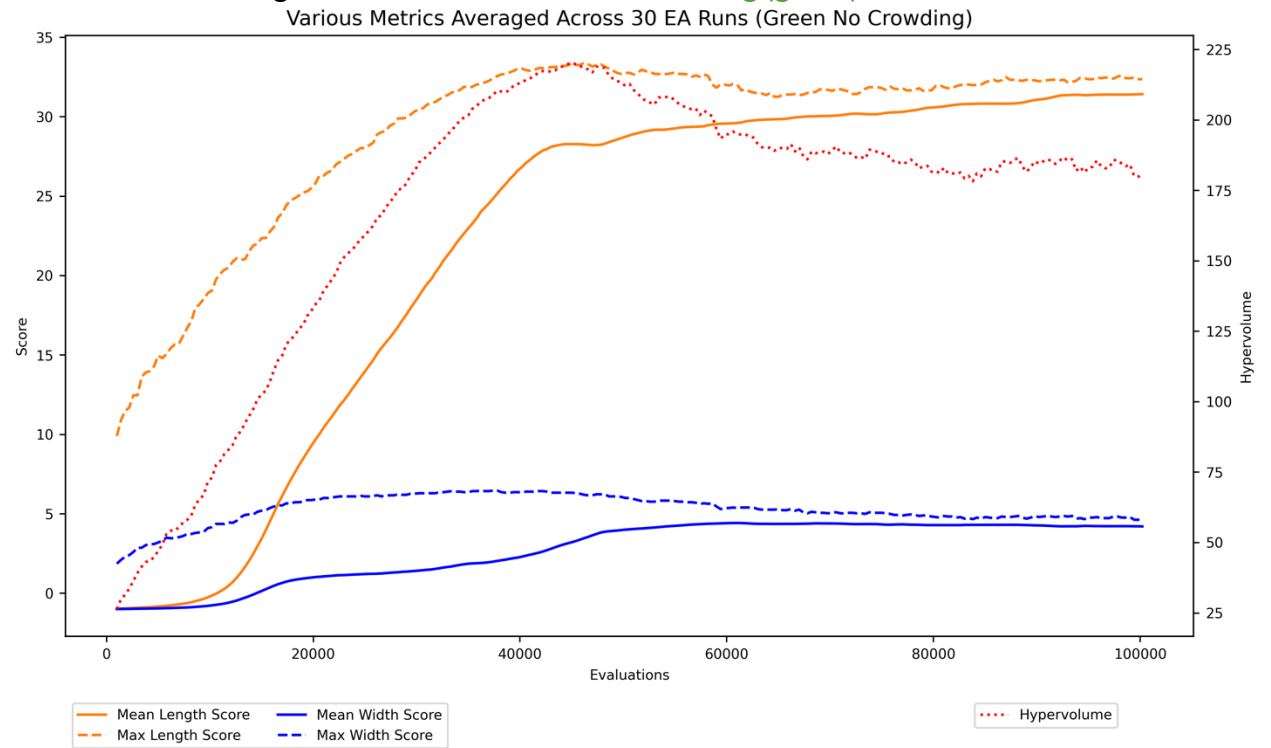


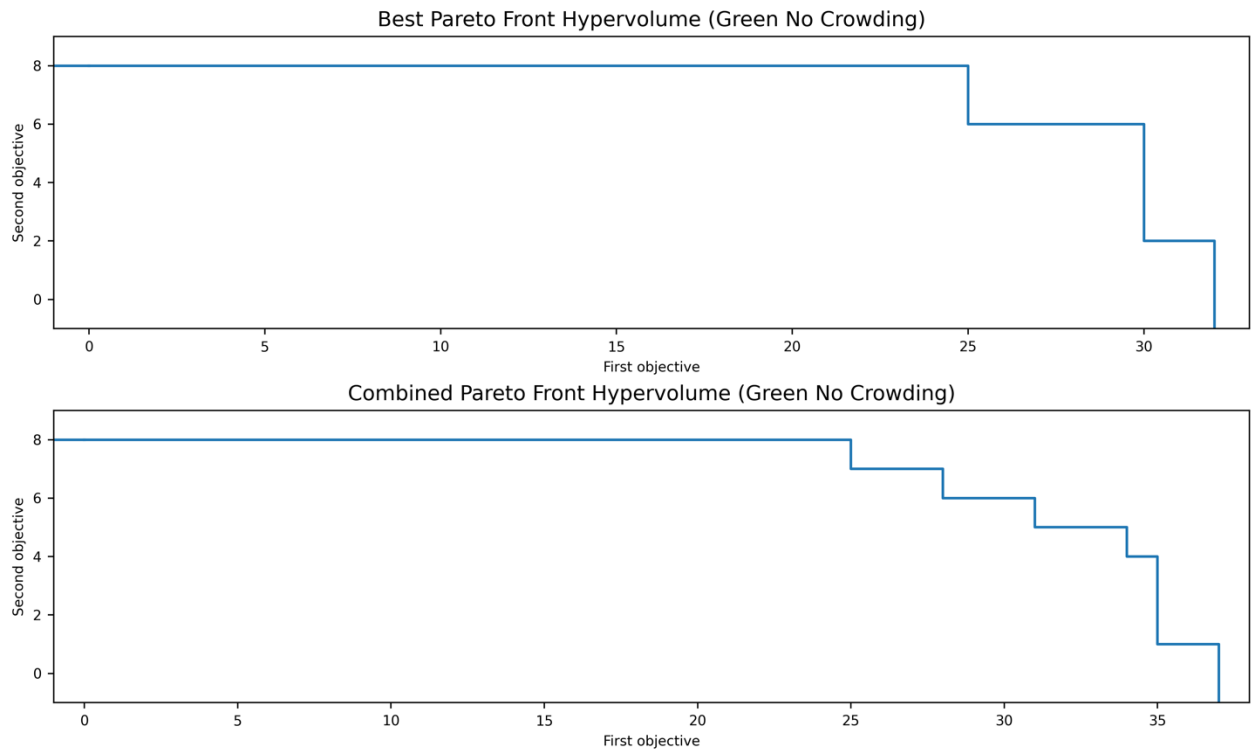
2-Best Width



For without crowding – green

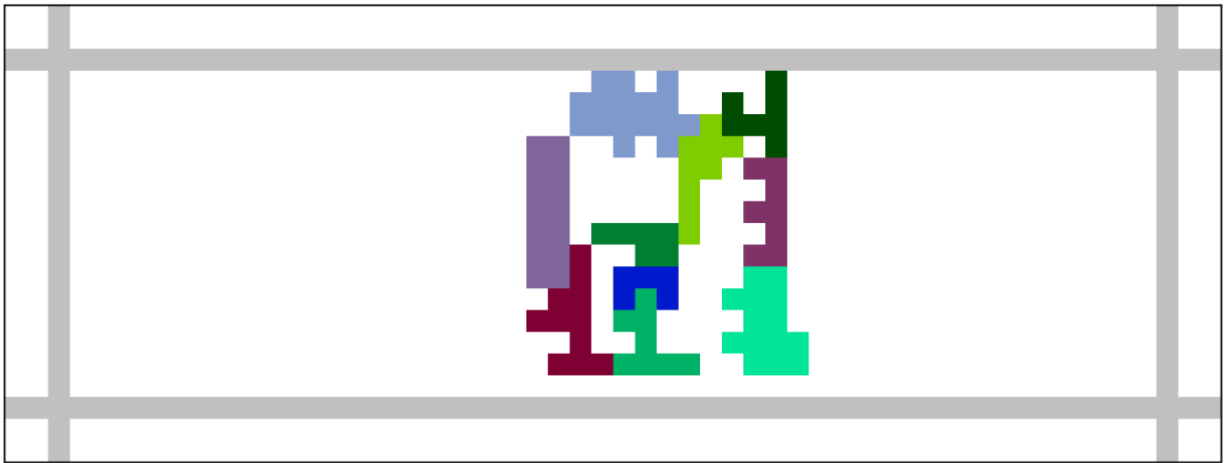
B. For without crowding - Plots for 30 runs with no crowding (green)





Combined Front (without crowding -- green)

1- Best Length

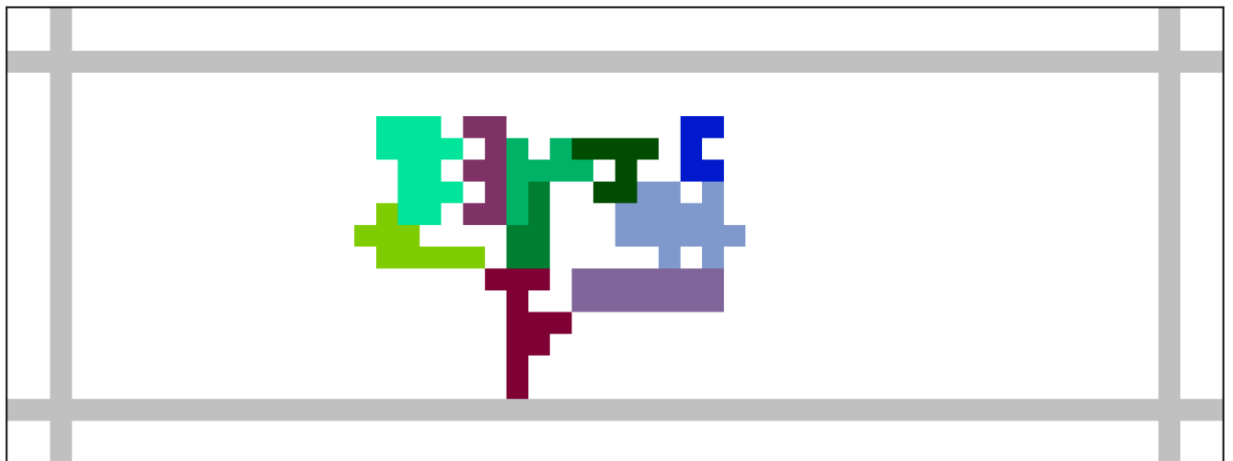


2- Best Width



Best Front (Without Crowding - green)

1- Best Length



2- Best Width



Statical analysis (green)

Number of samples: 30

data/1d/green_crowding/hypervolume_per_run.txt mean: 213.6

data/1d/green_crowding/hypervolume_per_run.txt stdv: 31.05012632546905

data/1d/green_no_crowding/hypervolume_per_run.txt mean: 178.96666666666667

data/1d/green_no_crowding/hypervolume_per_run.txt stdv: 48.09292967846179

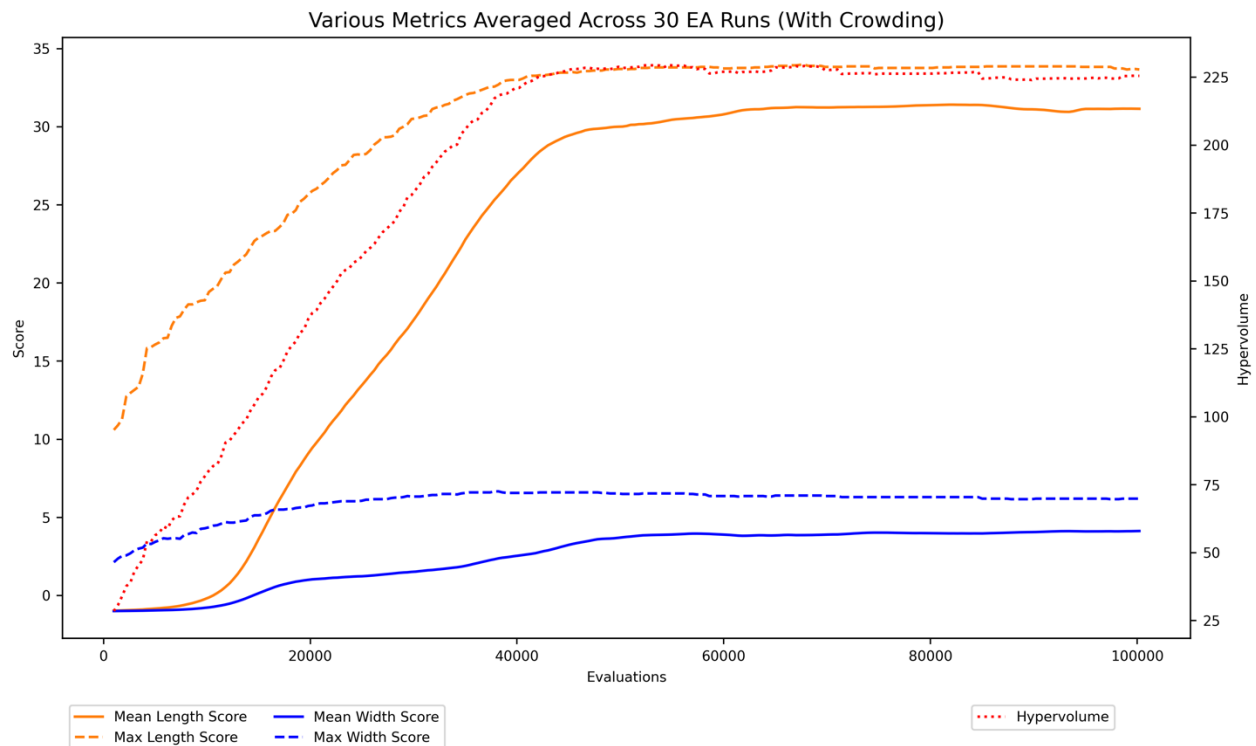
p-value: 0.001724954543288306

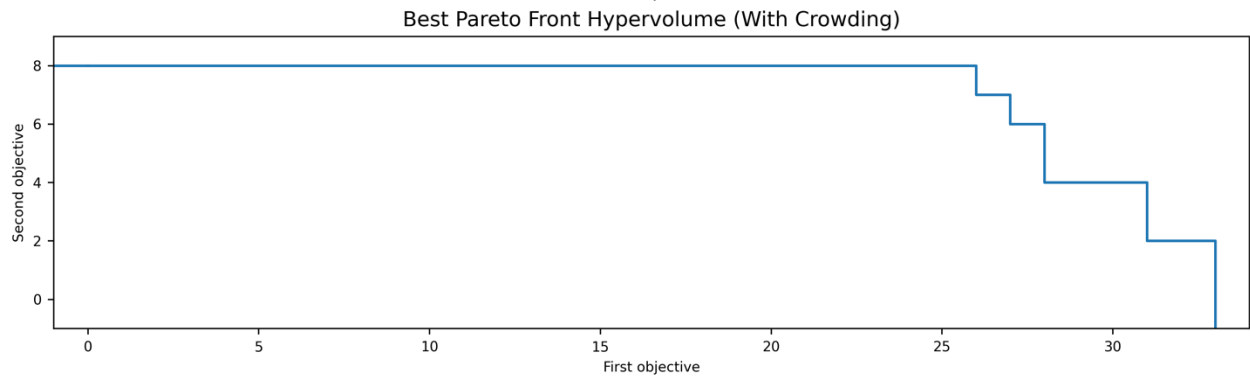
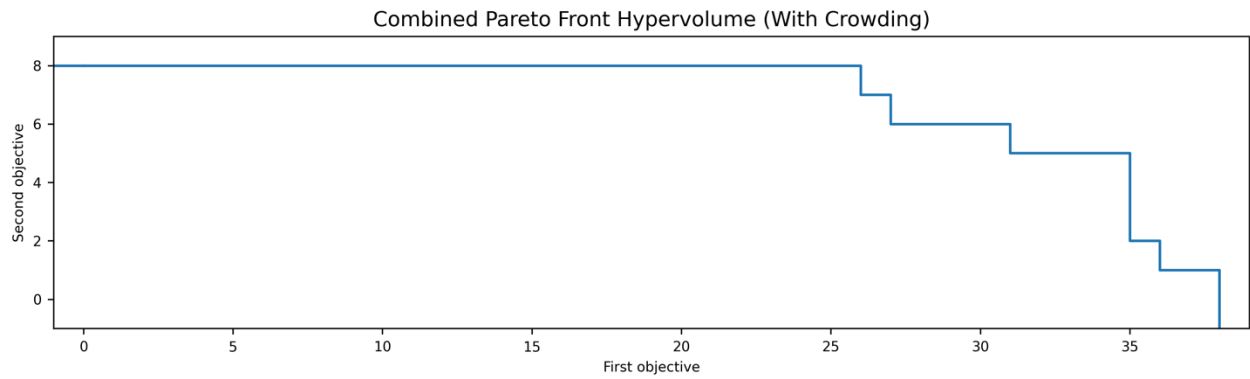
The analysis indicates that enabling crowding in the algorithm led to much better results than no crowding, since the average Hypervolume for with crowding is 213.6 and for no crowding is 178.96, that tell us that the experiment with crowding performed better than with no crowding. P-value = 0.0017249 which is much lower than the cutoff value alpha of 0.005 and that means that the difference between the two experiment is statistically significant.

The clear difference in hypervolumes (with a p-value of 0.00172) shows that using crowding in the algorithm helps improve the diversity and quality of the solutions.

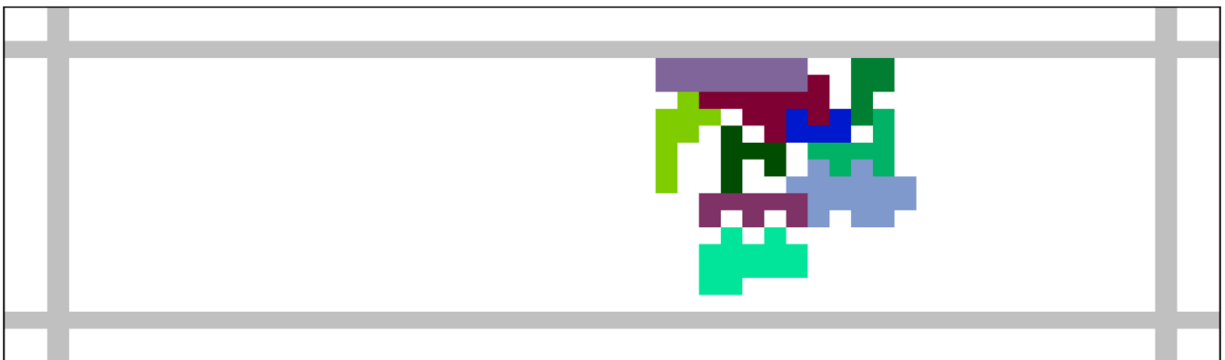
Also, From the Plots and the Picture above we can tell that with crowding experiment better than without crowding.

Plots With Crowding (Yellow)

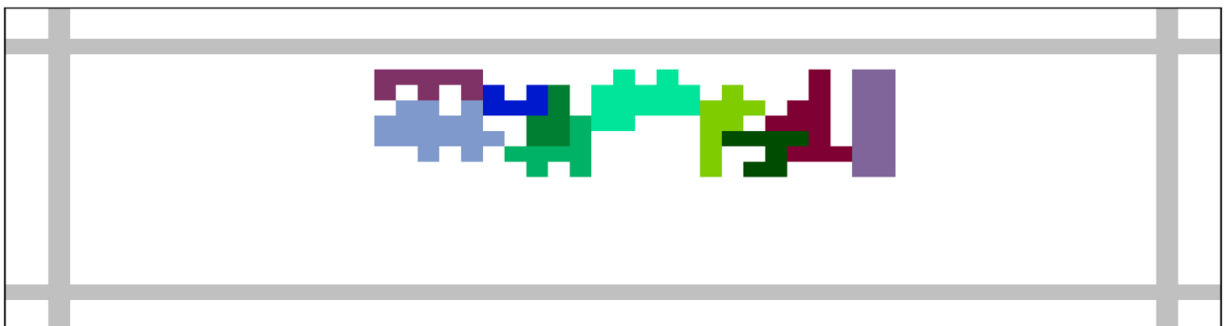




Combined Front
1- Best Length

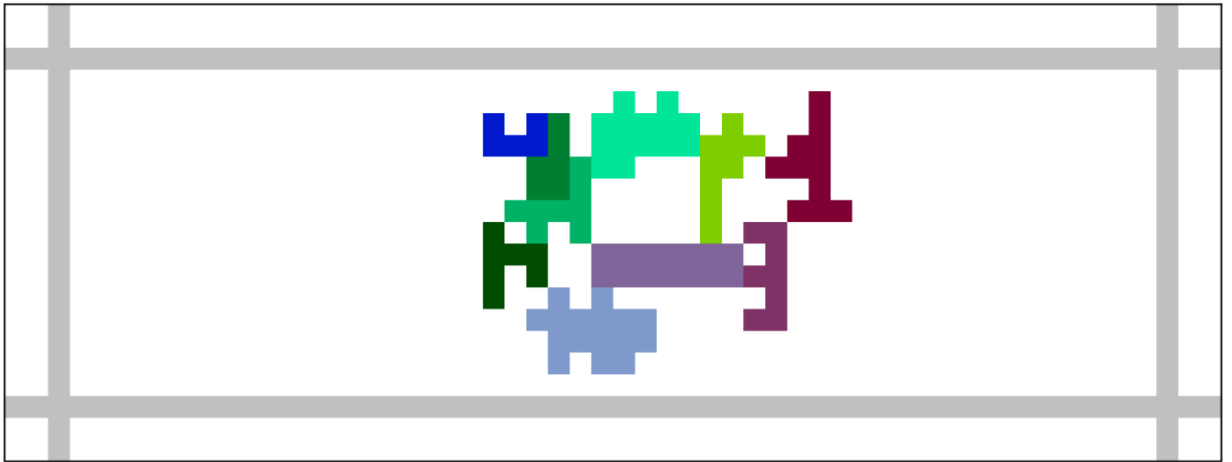


2- best Width

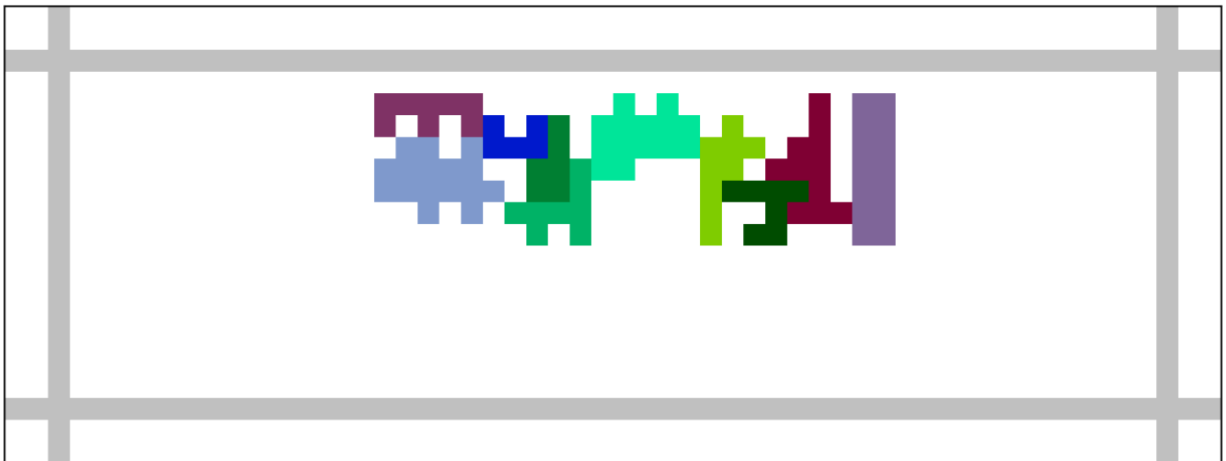


Pareto Front

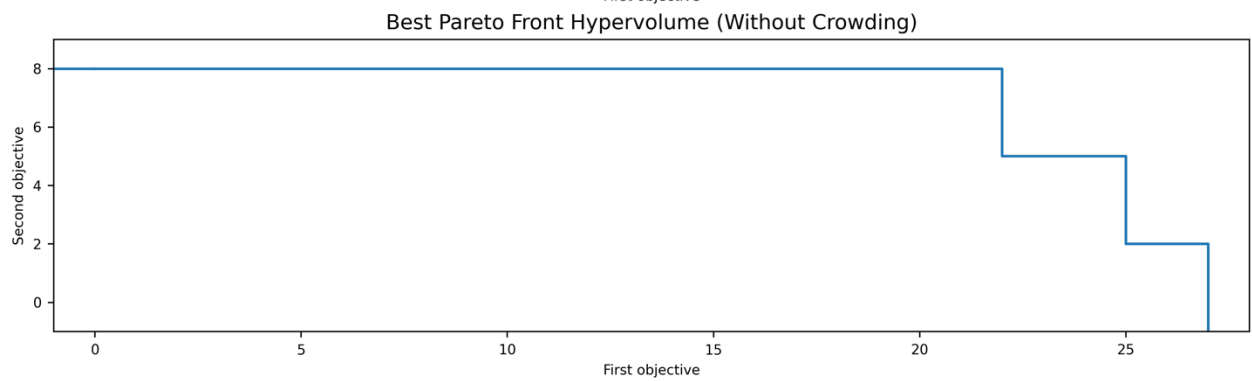
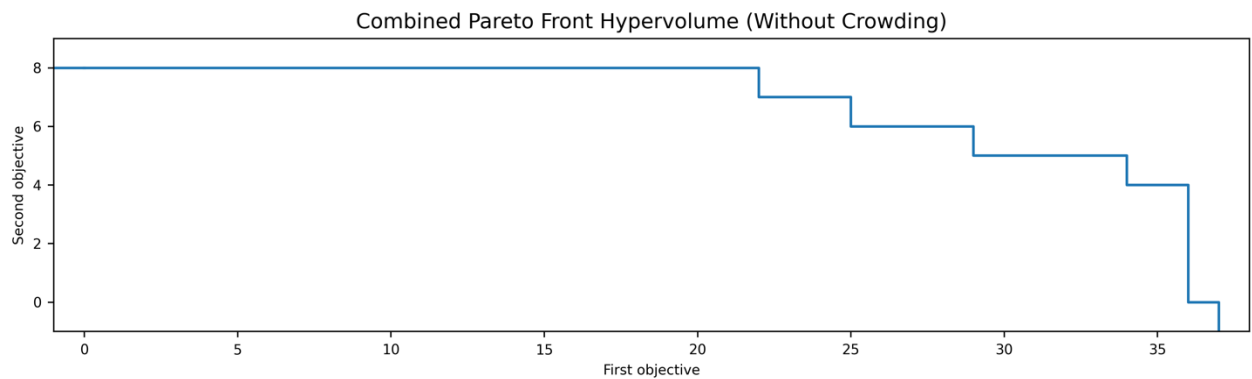
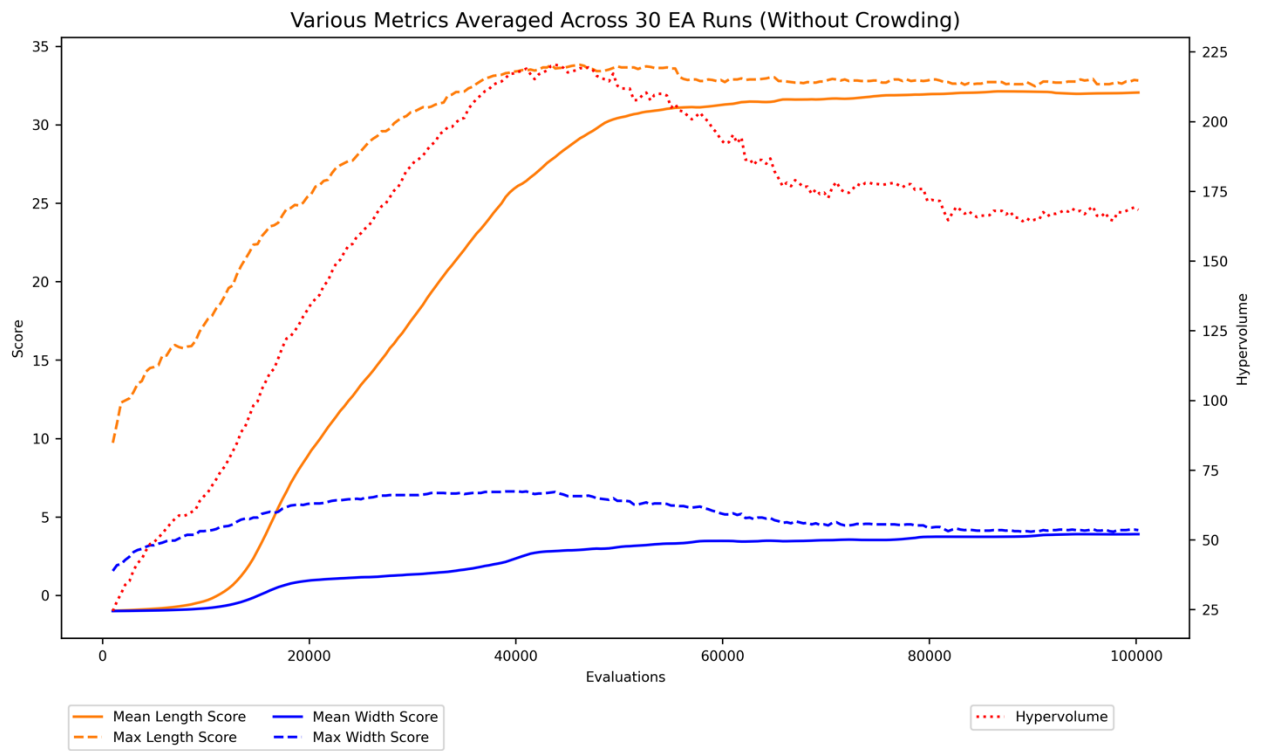
1- Best Length



2- Best Width



Plots With No Crowding (Yellow)

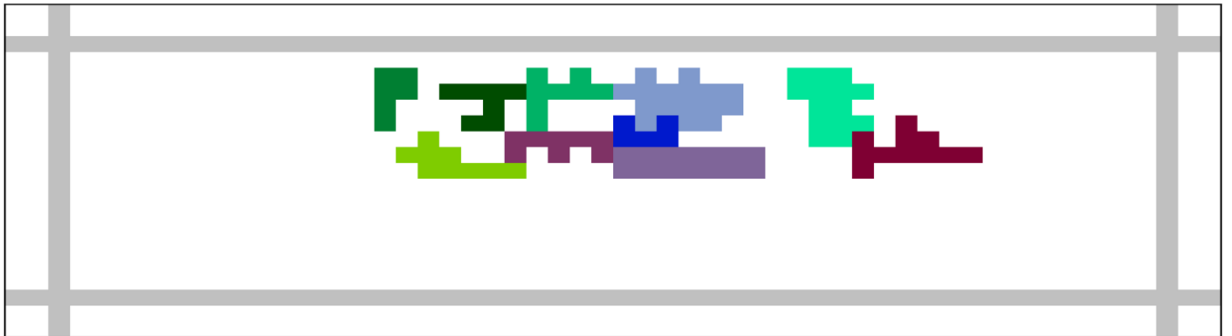


Combined Front

1- Best length

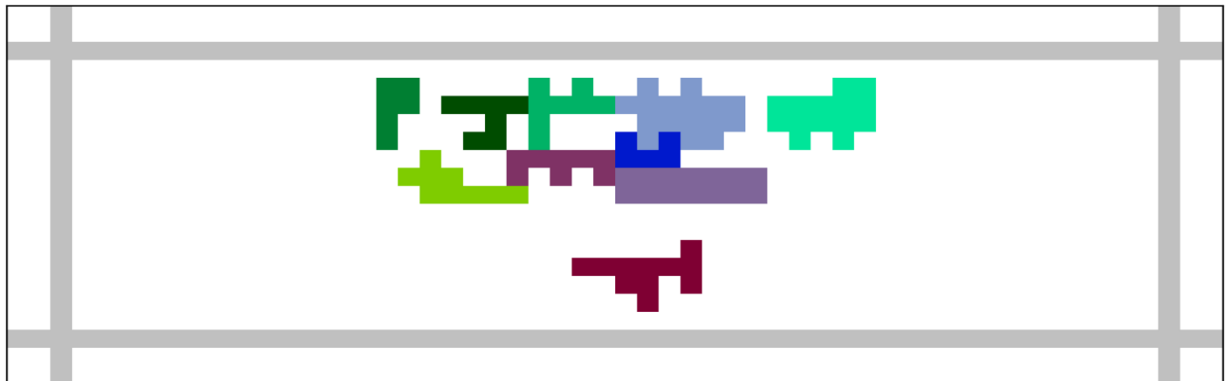


2- Best Width

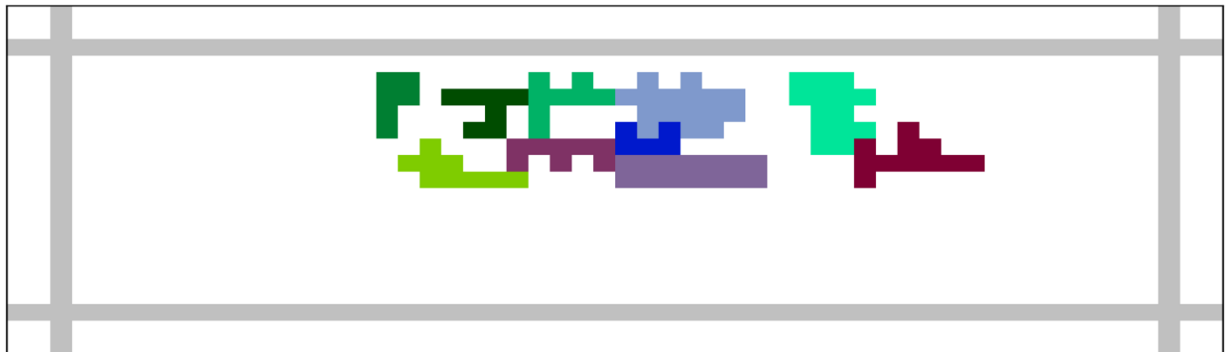


Best Front

1- Best Length



2- Best width



From the Picture above we can tell that the experiment with crowding is better than without crowding, now let's look at the statistical analysis.

```
Number of samples: 30
data/1d/yellow/with_crowding/hypervolume_per_run.txt mean: 225.53333333333333
data/1d/yellow/with_crowding/hypervolume_per_run.txt stdv: 34.48911205836869
data/1d/yellow/without_crowding/hypervolume_per_run.txt mean: 168.4
data/1d/yellow/without_crowding/hypervolume_per_run.txt stdv: 42.0997174206259
p-value: 3.895366856148652e-07
```

The analysis indicates that enabling crowding in the algorithm led to much better results than no crowding, since the average Hypervolume for with crowding is 225.53 and for no crowding is 168.4, that tells us that the experiment with crowding performed better than with no crowding. P-value = 3.895×10^{-7} which is much lower than the cutoff value alpha of 0.005 and that means that the difference between the two experiments is statistically significant.

The clear difference in hypervolumes shows that using crowding in the algorithm helps improve the diversity and quality of the solutions.

Now if we compare between yellow with and green with crowding, we can tell that yellow with crowding has performed better since the average hypervolume for yellow is 225.5. And between yellow and green with no crowding, Green has performed better since it has an average hypervolume of 178.96.

We can also tell by looking at the plots that yellow with crowding has performed better than green.

And green without crowding has performed better than yellow.