

## 1.Find a value in a BST:

```
bool search(struct Node* root, int x)
{
    if(!root || root->data==x)return root;
    if(root->data>x)return search(root->left,x);
    if(root->data<x)return search(root->right,x);
}
```

Complexity:Time=space=O(height).

## 2.Deletion of a node in a BST:

```
int minvalue(Node* root)
{
    int min=root->data;
    while(root->left)
    {
        min=root->left->data;
        root=root->left;
    }
    return min;
}

struct Node* deleteNode(struct Node* root, int key)
{
    if(!root)return NULL;
    if(root->data>key)root->left=deleteNode(root->left,key);
    else if
    (root->data<key)root->right=deleteNode(root->right,key);
    else
```

```

{
    if(!root->left)return root->right;
    else if (!root->right)return root->left;
    else
    {
        root->data=minvalue(root->right);
        root->right=deleteNode(root->right,root->data);
    }
}
return root;
}

```

**Complexity:Time=O(height)**

### **3.Find min and max value in a BST:**

```

int minValue(struct Node *root) {
    if(!root)return -1;
    int min=root->data;
    while(root->left)
    {
        min=root->left->data;
        root=root->left;
    }
    return min;
}

```

#### 4. Find inorder successor and inorder predecessor in a BST:

Method 1:

Find inorder traversal of tree and then left and right elements of given key is pre and suc respectively.

complexity= $O(N)$

Space= $O(N)$

Method 2:

```
void findPreSuc(Node* root, Node*& pre, Node*& suc, int key)
```

```
{
    if(!root) return;
    if(root->key==key)
    {
        if(root->left)
        {
            Node* t=root->left;
            while(t->right)t=t->right;
            pre=t;
        }
        if(root->right)
        {
            Node* t=root->right;
            while(t->left)t=t->left;
            suc=t;
        }
    }
}
```

```

else if(root->key > key)
{
    suc=root;
    findPreSuc(root->left,pre,suc,key);
}
else
{
    pre=root;
    findPreSuc(root->right,pre,suc,key);
}
}

```

## 5.Check for BST:

**Method 1:**Find min from right subtree and max from left subtree.

**Complexity=Time=** $O(N^2)$

**Method 2:**

Inorder traverse the whole tree and check if  
 $prev \rightarrow data < root \rightarrow data$

```

class Solution
{
    public:
    Node* prev=NULL;
    bool isBST(Node* root)
    {

```

```

    if(root)
    {
        if(!isBST(root->left))return 0;

        if(prev && prev->data >= root->data)return 0;

        prev=root;

        return isBST(root->right);
    }
    return 1;
}
};

```

**Complexity:** $O(N)$       **Space** $=O(1)$

**Note:**if we store whole inorder traversal then space complexity will increase— $\rightarrow O(N)$

## **6.Populate Inorder successor of all nodes:**

Given a Binary Tree, write a function to populate next pointer for all nodes. The next pointer for every node should be set to point to inorder successor.

```

class Solution
{
public:
    Node* prev=NULL;
    void populateNext(Node *root)
    {

```

```

        if(!root)return;
        populateNext(root->left);
        if(prev)prev->next=root;
        prev=root;
        populateNext(root->right);
    }
};

```

## 7.Find LCA of 2 nodes in a BST:

```

Node* LCA(Node *root, int n1, int n2)
{
    if(!root)return NULL;
    if(root->data < n1 && root->data < n2)return
LCA(root->right,n1,n2);
    if(root->data > n1 && root->data > n2)return
LCA(root->left,n1,n2);

    return root;
}

```

Complexity=O(height)

## **8. Construct BST from preorder traversal:**

### **Method 1:**

**We can check one by one actual position of every element which will take  $O(N)$  for every element if tree is skewed, total complexity**

**Time =  $O(N^2)$**

### **Method 2: Using sorting**

**We can sort the pre order traversal which will become inorder traversal which can be solved easily then...**

**Complexity: Time =  $O(N \log N) + O(N)$**

### **Method 3: Using bound concept**

**Left subtree → use node → data as bound**

**Right subtree → use bound itself subtree**

**Upper bound concept**

```
Node* construct_bst(int pre[],int i,int bound,int n)
{
    if(i==n || pre[i]>bound)return NULL;
    Node* node=new Node(pre[i++]);
    node->left=construct_bst(pre,i,node->data,n);
    node->right=construct_bst(pre,i,bound,n);
    return node;
```

```

}
struct Node *constructTree(int n, int pre[], char preLN[])
{
    return construct_bst(pre,0,INT_MAX,n);
}

```

Complexity;Time= $O(N)$

## 9.Binary Tree to BST:

```

class Solution{
public:
    void inorder(Node* root,vector<int>& v)
    {
        if(!root)return;
        inorder(root->left,v);
        v.push_back(root->data);
        inorder(root->right,v);
    }
    void inorder_bst(Node* root,vector<int>& v,int &i)
    {
        if(!root) return ;
        inorder_bst(root->left,v,i);
        root->data=v[i++];
        inorder_bst(root->right,v,i);
    }
    Node *binaryTreeToBST (Node *root)
    {
        vector<int> v;

```



```

        inorder(root,v);
        sort(v.begin(),v.end());
        int i=0;
        inorder_bst(root,v,i);
        return root;
    }
};

```

**Complexity:  $O(N \log N)$**

## **10.Convert a normal BST into a Balanced BST:**

**Method 1:**

**A Simple Solution is to traverse nodes in Inorder and one by one insert into a self-balancing BST like AVL tree. Time complexity of this solution is  $O(n \log n)$  and this solution doesn't guarantee.**

**Method 2:**

**1.Traverse given BST in inorder and store result in an array. This step takes  $O(n)$  time. Note that this array would be sorted as inorder traversal of BST always produces sorted sequence.**

**2.Build a balanced BST from the above created sorted array using the recursive approach discussed here. This step also takes  $O(n)$  time as we traverse every element exactly once and processing an element takes  $O(1)$  time.**

```

Node* get_BBST(vector<int>& in,int st,int ed)
{

```

```

    if(st>ed)return NULL;
    int mid=(st+ed)/2;
    Node* node=new Node(in[mid]);

    node->left=get_BBST(in,st,mid-1);
    node->right=get_BBST(in,mid+1,ed);

    return node;

}
void inorder(Node* root,vector<int>& in)
{
    if(!root)return;
    inorder(root->left,in);
    in.push_back(root->data);
    inorder(root->right,in);
}
Node* buildBalancedTree(Node* root)
{
    vector<int> in;
    inorder(root,in);
    return get_BBST(in,0,in.size()-1);
}

```

## **11.Merge two BST [ V.V.V>IMP ]:**

**Method 1: (Insert elements of the first tree to second):**

Take all elements of first BST one by one, and insert them into the second BST. Inserting an element to a self balancing BST takes  $\text{Log}n$  time (See this) where  $n$  is size of the BST. So time complexity of this method is  $\text{Log}(n) + \text{Log}(n+1) \dots \text{Log}(m+n-1)$ . The value of this expression will be between  $m\text{Log}n$  and  $m\text{Log}(m+n-1)$ . As an optimization, we can pick the smaller tree as first tree.

**Method 2 (Merge Inorder Traversals):**

- 1.Do inorder traversal of first tree and store the traversal in one temp array arr1[]. This step takes  $O(m)$  time.**
- 2.Do inorder traversal of second tree and store the traversal in another temp array arr2[]. This step takes  $O(n)$  time.**
- 3.The arrays created in step 1 and 2 are sorted arrays. Merge the two sorted arrays into one array of size  $m + n$ . This step takes  $O(m+n)$  time.**
- 4.Construct a balanced tree from the merged array using the technique discussed in this post. This step takes  $O(m+n)$  time.**

Time complexity of this method is  $O(m+n)$  which is better than method 1. This method takes  $O(m+n)$  time even if the input BSTs are not balanced.

## 12.Find Kth largest element in a BST:

**Method 1:**

We can store inorder traversal of tree in an array then return `arr[n-k]`;

**Complexity:**Time= $O(N)$       Space= $O(n)$

**Method 2:**By using a index variable and when it becomes `index==k` then return `root->data`

**class Solution**

```
{
    public:
    int ans=-1;
    void get_kthLargest(Node* root,int k,int &idx)
    {
        if(!root)return ;
        get_kthLargest(root->right,k,idx);
        if(idx==k)
        {
            ans=root->data;
            idx++;
            return;
        }
        else idx++;
        get_kthLargest(root->left,k,idx);
    }
    int kthLargest(Node *root, int K)
    {
```

```

        int idx=1;
        get_kthLargest(root,K,idx);
        return ans;
    }
};

```

**Complexity: Time=O(K+H)      Space=O(H)**

### **13.Find Kth smallest element in a BST;**

**Method 1:**

**Same like above**

**Method 2:**

```

class Solution
{
    public:
    int ans=-1;
    void get_kthLargest(Node* root,int k,int &idx)
    {
        if(!root)return ;
        get_kthLargest(root->left,k,idx);
        if(idx==k)
        {
            ans=root->data;
            idx++;
            return;
        }
    }
}

```

```

    }
    else idx++;
    get_kthLargest(root->right,k,idx);
}
int KthSmallestElement(Node *root, int K)
{
    int idx=1;
    get_kthLargest(root,K,idx);
    return ans;
}

```

**Complexity:Time=O(K+height)      Space=O(1)**

**14.Count pairs from 2 BST whose sum is equal to given value "X":**

**Method 1:**

**For every element in BST\_1,we will search an element in BST\_2 and if found then increment counter otherwise continue:**

**Complexity:Time=O(N\*height)                      Space=O(1)**

**Method 2:Using Maps**

```

class Solution
{
public:
    int c=0;

```

```

void get_pair(Node* root,unordered_map<int,int>& m,int k)
{
    if(!root)return;
    get_pair(root->left,m,k);
    if(m.find(k-root->data)!=m.end())c++;
    //else m[root->data]++;
    get_pair(root->right,m,k);

}
void inorder(Node* root,unordered_map<int,int>& m)
{
    if(!root)return;
    inorder(root->left,m);
    m[root->data]++;
    inorder(root->right,m);
}
int countPairs(Node* root1, Node* root2, int x)
{
    unordered_map<int,int> m;
    inorder(root2,m);
    get_pair(root1,m,x);
    return c;
}
};

```

**Complexity:Time=O(N)      space=O(n)**

## 15.Find the median of BST :

### Method 1:

Traverse the entire tree in orderly and store elements in an array and return median accordingly.

For even number elements—return  $((array[n/2] + array[n/2 - 1]) / 2)$ ;

For odd—return  $array[n/2]$ ;

Complexity: Time =  $O(N)$    Space =  $O(N)$

### Method 2: Space = $O(1)$

```
void count_nodes(Node* root, int &c){
    if(!root) return;
    count_nodes(root->left, c);
    c++;
    count_nodes(root->right, c);
}
```

```
void func(Node* root, Node* &cur, Node* &prev, int &c, int k, int &f){
    if(!root) return;
    func(root->left, cur, prev, c, k, f);
    if(prev == NULL){
        prev = root;
        c++;
    }
    else if(c == k){
        c++;
    }
}
```



```

        cur = root;
        f = 1;
        return;
    }
    else if(f==0){
        c++;
        prev = root;
    }
    func(root->right,cur,prev,c,k,f);
}

```

**float findMedian(struct Node \*root)**

```

{
    //Code here
    int n = 0;
    count_nodes(root,n);
    Node* cur = NULL;
    Node* prev = NULL;
    int c = 1;
    int x = (n/2)+1;
    int f = 0;
    func(root,cur,prev,c,x,f);
    if(n&1){
        float ans = (cur->data)*1.0;
        return ans;
    }
    else {
        float ans = ((cur->data+prev->data)*1.0)/(2*1.0);
        return ans;
    }
}

```

```
}
```

Time=O(n)

BUT

Space=O(1)

## 16.Count BST nodes that lie in a given range:

Method 1:

Use inorder traversal and check one by one.

Complexity ,time=O(N)

```
void inorder(Node* root,int l,int h,int &c)
{
    if(!root)return;
    inorder(root->left,l,h,c);
    if(root->data>=l && root->data<=h )c++;
    inorder(root->right,l,h,c);
}
int getCount(Node *root, int l, int h)
{
    int c=0;
    inorder(root,l,h,c);
    return c;
}
```

Method 2:

```
int getCount(Node *root, int l, int h)
{
```

```

    if(!root)return 0;
    if(root->data==l && root->data==h)return 1;
    if(root->data>=l && root->data<=h)
    return
1+getCount(root->left,l,h)+getCount(root->right,l,h);
    if(root->data < l)return getCount(root->right,l,h);
    else return getCount(root->left,l,h);
}

```

**Complexity:**

Time complexity of the above program is  $O(h + k)$  where  $h$  is height of BST and  $k$  is number of nodes in given range.

## **17.Replace every element with the least greater element on its right:**

**Method 1:**

For every element we will find least element on right hand side it will take  $O(N^2)$  time complexity.

**Method 2:**

We will build a BST by iterating the array from left to right

```

struct Node{
    int data;
    Node* left;
    Node* right;
    Node(int val)
    {

```

```

        data=val;
        left=right=NULL;
    }

};

class Solution{
public:
    Node* insert(Node* root,Node* &suc,int val)
    {
        if(!root)return root=new Node(val);
        if(val<root->data)
        {
            suc=root;
            root->left=insert(root->left,suc,val);
        }
        else
            if(val>=root->data)root->right=insert(root->right,suc,val);

        return root;
    }
    vector<int> findLeastGreater(vector<int>& arr, int n) {
        // int n=arr.size();

        Node* root=NULL;
        for(int i=n-1;i>=0;i--)
        {
            Node* suc=NULL;
            root=insert(root,suc,arr[i]);
            if(suc)arr[i]=suc->data;
            else arr[i]=-1;
        }
    }
};

```

```

    }
    return arr;
}
};

```

**Expected Time Complexity:  $O(N \log N)$**

**Expected Auxiliary Space:  $O(N)$**

## 18.Preorder to Postorder :

Given an array `arr[]` of `N` nodes representing preorder traversal of BST.  
The task is to print its postorder traversal.

```

class Solution{
public:
    //Function that constructs BST from its preorder traversal.
    struct Node* insert(Node* root,int val)
    {
        if(!root)return root=newNode(val);
        if(root->data>val)root->left=insert(root->left,val);
        else if(root->data<=val)root->right=insert(root->right,val);
        return root;
    }
    Node* post_order(int pre[], int size)
    {
        Node* root=NULL;
        for(int i=0;i<size;i++)
        {
            root=insert(root,pre[i]);
        }
        return root;
    }
};

```

**Expected Time Complexity:  $O(N)$ .  
Expected Auxiliary Space:  $O(N)$ .**

## **19.Check whether BST contains Dead end:**

**Here Dead End means, we are not able to insert any element after that node.**

**Method 1:**

**For every element check if  $ele-1$  &  $ele+1$  exists in BST,then return true.**

**Complexity:Time= $O(N \cdot \text{height})$     Space= $O(1)$**

**Method 2:Using maps**

**We can store all elements in the map and then check for all BST elements whether  $ele-1$  &  $ele+1$  exists the return true.**

**Complexity:Time= $O(N)$     space= $O(N)$**

**Method 3:Using upper bound and lower bound**

```
bool deadend(Node* root,int lo,int up)
{
    if(!root)return 0;
    if(lo==up)return 1;
    return deadend(root->left,lo,root->data-1) or
    deadend(root->right,root->data+1,up);
```

```

}
bool isDeadEnd(Node *root)
{
    return deadend(root,1,INT_MAX);
}

```

## 20.Largest BST in a Binary Tree [ V.V.V.V.V IMP ]:

We will create a vector for every node which contain four values (BST,count,lower bound,upper bound).

```

class Solution{
public:
    vector<int> get_largestBST(Node* root)
    {
        if(!root)return {1,0,INT_MAX,INT_MIN};
        if(!root->left &&
!root->right)return{1,1,root->data,root->data};

        vector<int> l=get_largestBST(root->left);
        vector<int> r=get_largestBST(root->right);
        if(l[0] && r[0])
        {
            if(root->data > l[3] && root->data < r[2])
            {
                int x=l[2];
                int y=r[3];
                if(x==INT_MAX)x=root->data;
                if(y==INT_MIN)y=root->data;
                return {1,l[1]+r[1]+1,x,y};
            }
        }
    }
}

```

```

        }
        else return {0,max(l[1],r[1]),0,0};
    }
    else return {0,max(l[1],r[1]),0,0};
}
int largestBst(Node *root)
{
    vector<int> v=get_largestBST(root);
    return v[1];
}
};

```

For confusion refer:

 [Largest BST in a Binary Tree | BST | Love Babbar DSA She...](#)

Expected Time Complexity:  $O(N)$ .