# **Quantitative Investment Handbook**

Xinhe Liu

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# Part I

# Financial Market and Investment Tools

# Chapter 1

# **Economics and Econometrics**

#### 1.1 Macroeconomics

GDP, Inflation and Unemployment:

- $\bullet \ GDP = C + I + G + X$
- CPI, RPI, PPI, Core CPI, Nonfarm Payroll, HICP (Europe)
- Philips Curve(Inflation and Unemployment)
- Unemployment Rate(labor force), Participation Rate(total population), Quit Rate
- Unemployment: Frictional, Cyclical, Structural, Seasonal, Voluntary

Economic Indicators: Leading Indicators:

- PMI, Tanken Survey(Japan)
- Capacity Utilisation
- Retail Sales
- Consumer Sentiment/Confidence

#### Market Data Release Time Schedule:

Time	Market Data
Week 1	Employment Situation (First Friday), ISM
Week 2	Retail Sales, Consumer Sentiment
Week 3	CPI, IP
Week 4	Durable Goods, GDP, Consumer Sentiment(UoM final & Conference Board)

- PMI
- Capacity Utilisation
- Retail Sales
- Consumer Sentiment/Confidence

#### Fiscal Policy and Monetary Policy:

- General Economic Goals: Full Employment, Economic Growth, Low Inflation
- Fiscal Policy: Government Spending and Tax Policy
- Monetary Policy: Open Market Operations, Discount Rate, Reserve Requirement, Federal Fund Rate(Upper Limit for Repo Rate) (In other countries: Overnight discount rate, Refi Rate, Deposit Rate, Main Lending Rate)
- Interaction: Crowding Out: Higher Interest Rates may cause investment and consumption
- Central bank, Taylor rule

#### 1.1.1 Business Cycle and Debt Cycle

According to Ray Dailo's Opinion, business cycles are created by credit (borrowing). Growth = Productivity Growth + Debt Cycle Effect.

- Total output = Price × Quantity, while Price = Money + Credit
- Long term debt cycle: 75 to 100 years. Short term debt cycle" 5-7 years
- Key indicators Inflation, deflation, tax, government spending, unemployment (Government Action)
- "Beautify Deleveraging": The phase total debt decreases. Needs: Spending cut, Debt Restructuring, Wealth transfer, Print Money (Government Debt increases, total debt decreases, if not carefully, lead to hyper-inflation
- 2-3 years depression/deleveraging and 7-10 yeas "reflation"

**Keysian Theory** 

stagflation and non zero inflation

#### 1.2 Financial Economics

- Rationality. Utility Theroy, Indifference Curve, Risk Aversion.
   Participants are perfect optimizers with perfect Bayesian
   Information
- Efficient Market Hypothesis : 3 Forms
- Market Anomalies: Fundamental Anomalies (Factor), Technical Anomalies, Calendar Anomalies, Limits to Arbitrage

#### 1.3 Behavioral Finance

• Behavioral Finance micro: Assumes limited information, bounded rationality

**Prospect Theory** 

Neuroeconomics

• Behavioral Finance macro

Challenge Efficient Market Hypothesis(EMH): Anomalies

Fundamental Anomalies: (eg. Value Factor, Factor Models)

Technical Anomalies (Moving Average, Support and Resistance)

Calendar Anomalies

Due to other reasons such as Limits to Arbitrage

Asset Pricing: Behavioral Stochastic Discount, Sentiment Risk Premium

Behavioral Based Portfolio Theory

Adaptive Market Hypothesis

Behavioral Biases in investing

Cognitive Errors-Belief Perseverance Bias

- Conservatism (Systematically review and update new information)
- Confirmation Bias( Review screening criteria, promote diversification),
- Representativeness Bias( Review Base-rate Neglect and Sample-size Neglect, check if forecast based solely on new data, check if treat complex and simple information equally),
- Illusion of Control(excessive trading, lack of diversification, need to keep records and manage info)
- Hindsight Bias(overestimate the degree of prediction, rightness of selection (manager or investment)

Cognitive Errors-Information Processing Bias

- Anchoring and Adjustment (stick to original information)
- Mental Accounting( under-diversify, distinction of income and capital appreciation) Framing Bias(affects risk appetite)
- Availability Bias: weight according to experience, relevance, under-diversify, affected by Ad

**Emotional Bias** 

- Loss-Aversion: Disposition Effect: work together with Framing bias, Myopic loss aversion
- Overconfidence: Under-diversify, Trade Excessively
- Self-Control Bias: Not save for long-term, taking too much/little risk, asset allocation imbalance - prefer income generating assets
- Status Quo Bias: unknowingly maintain, work with Regret-Aversion and Endowment
- Endowment: hold familiar, refuse to sell certain assets
- Regret-Aversion: Herding, conservatism

## Chapter 2

# **Basic Financial Concepts**

This chapter summarizes some basic financial concepts you should know about.

#### 2.1 Asset Management

Asset Owners(Real Money): From conservative to active: Banks, Insurance Company, Defined Contribution Plan, Pension, Endowment/Foundations

Hedge Funds(Fast Money)

Investment Purpose Statement(IPS): Consider Return, Risk, Time Horizon, Tax, Liquidity, Legal and Unique.

# 2.2 Accounting, Corporate Finance and Fundamental Analysis

Accounting:

• Balance Sheet, Income Statement, Cash flow Statement Basics

- EBIT = operating profit + non recurring expense non-recurring income, EBITDA, Operating profit, normalized net income = NI + non recurring items
- Gross Profit, Operating profit, profit before tax, net income
- Gross Margin, EBIT Margin, EBIT Margin, Net Operating Margin, Net Profit Margin
- Cash flow from Operations = NI + DA +- change in inventory/accounts payable, receivable, operating items
- CF from investing = Capital Expenditure -+ Disposal/Purchase of Assets
- CF from financing = -Dividend Share buybacks + issuance of stock/bond
- Equity: Preferred shares, authorized shares (maximum shares the board can issue), Treasury stock, buy back book value, Free float Market capitalization = share price \* ( shares outstanding shares not traded), Small free float: little share holder control, volatile share price, high premium in M&A

#### Capital Structure:

- Operating items vs financing items (cash, financial asset/liability, equity)
- Working Capital = Current Assets Current Liabilities, Operating Working Capital = Operating Assets - Operating Liabilities(exclude cash)
- Inventory COGS LIFO FIFO inventory turnover
- Payable days, receivable days, working capital cycle (payable days inventory days + receivable days)
- Leverage ratios: Debt/Equity, Total Debt/EBITDA, EBITDA/inst expense

#### Credit Scoring/Credit Analysis

#### 2.2. ACCOUNTING, CORPORATE FINANCE AND FUNDAMENTAL ANALYSIS9

- Credit Risk = Business Risk( Country, Economic Cycle, Industry Cycle, Currencies, Commodities, trends) + Financial Risk(Cash Risk)
- Creditor Cashflow Statement Net Income + D/A/non-cash items =
   FFO( Funds from Operations), FFO +- Decrease/Increase in OWC =
   Operating Cash Flow, Operating Cash Flow Capex = Free
   Operating Cash Flow(FOCF)
   FOCF + Dividends = Discretionary Cash Flow, DCF +- Acquisition,
   Asset Disposals, Net other sources/uses of cash = pre-financing
   cashflow +- Increase(Decrease) in Debt, +- Net Sale/Repurchase of
   Shares = Inc/(Dec) in Cash/Securities
- Profitability & Efficiency Ratios: EBIT/EBITDA margin, Return on Assets, Return on Invested Capital
- Coverage Ratios: EBITDA/interest(net interest), EBITDA/(interest + Principal Amortization), EBIT/interest or net interest
- Leverage Ratios: Debt/Equity, Debt/Capital, Debt/EBITDA
- Cash flow adequacy Ratios: FFO/Debt, FOCF/Debt, Free Cash flow/Debt, Retained Cash Flow/Debt
- Liquidity Ratios: maturing debt principal this year/FFO or discretionary cash flow, Quick Ratio = (Cash + Marketable Securities + Committed un-used bank credit lines)/maturing debt principal this year.

Tax: Effective Tax Rate, Loss Harvesting and Tax-Aware investment Valutaion fundamentals:

- Intrinsic Value and two approaches absolute valuation and relative valuation
- Enterprise Value = Debt + Equity Value Cash/Cash Equivalent = Net Debt Value + Equity Value
- Equity Value (affected by performance (operating), investing and financing (leverage)) = Price x Shares Outstanding

- Asset = Enterprise Value + Non-core assets(not valued by Multiples/DCF models, like cash)
- Free Cash Flow Calculation: EBIT tax on EBIT (LT tax rate x EBIT)
   NOPAT (net operating profit after tax )/EBIAT, Free Cash flow =
   NOPAT + D&A capex increase in OWC + decrease in OWC Increase in Other net operating assets + Decrease in other net operating assets -+ change in Long term tax liabilities
- FCFF, FCFE
- Discount Rate- Weighted Average Cost of Capital (WACC) CAPM / required rate of return, WACC = D/(D+E) cost of net debt x (1-t) +  $(rf + (r_m r_f) \times beta) \times E/(D+E)$ , D is net debt
- Equity Market Expectaion: Gordon Growth Model

$$\mathbb{E}(R_e) = \frac{D_0(1+g)}{P_0}$$

Grinold-Kroner Model

$$\mathbb{E}(R_e) \; \frac{D}{P} - \Delta S + i + g + \Delta P E$$

• EV multipliers : EV/Sales, EV/EBITEV/EBITDA

Fundamental Analysis, Company Analysis and Value Investing

Management/Strategic Analysis(SWOT, Five forces etc), Industry/Region/ Sector Analysis + competitor Analysis

### 2.3 Real-life trading

- Shorting a Stock: achieved by a stock-loan process of broker/dealer: broker need to borrow and put colleteral, during borrow agreement, any dividend is passed (synthetically) from the borrower to the beneficial owner. Corporate actions: borrower vote as in lender's proxy.
- SHOrt squeeze: Stock with high short interest trended upwards, short side cover their shorts.

- Naked short: short (t+2) before borrow, can borrow/buy later.
- Short interest thredhold: 8% of market cap or free float.
- Prime-brokerage: Agency only brokerage does not own books

## Chapter 3

# Major Asset Classes and Asset Valuation Theories

#### 3.1 Money Market

- Overnight (O/N) reference ratesL SONIA(Sterling Overnight Index Average), EONIA, SOFR ALl has different day count convention
- LIBOR Rate, STIR Futures (Cash Settlement by 100 expected interest), IMM Dates (Exchange for interest rate and currency futures)
- T-bill(1,3,6,12 Month), T-note, T-bond
- Commercial Paper( Issued by best quality companies)
- Day Count Conventions
- Repo Market: Repo(seller, needs cash), Reverse Repo(buyer, owns collateral for a while)
- Fed Funds Rate:
  - The Upper Bound: Interest on Excess Reserves: interest rate paid by the Fed on Excess reserves held by banks at the Fed. (many money market participants are not reserve account holders so they do not have access to the IOER).

3.2. FX

 Lower Bound: Overnight RRP: Non-reserve account holder can earn interest by entering into an overnight reserve repo(overnight RRP)- offer each day.

#### 3.2 FX

#### **Basic Concepts:**

- FX Market is Extremely liquid (smaller bid ask spread on equity)
- Market Size High to Low: USD, EUR, Cheap Currencies: JPY(safe currency), CHF, GBP, Rich(high rate) currencies: ZAR, MXN, AUD
- Uncovered Interest Rate Parity and Covered IRP
- Interest Rate Forward/Futures, Non-deliverable forwards(NDF)
- FX Drivers: Interest rate differential, inflation rate differential, Global M&A/Capital Flows, Technical Drivers(Indicators), Central Bank Policies, Risk Appetite
- Purchasing Power Parity

#### 3.3 Equity

#### Sell Side Services

- Traditionally, Sales and Trading Service build around research (content stream)
- New Model -automation: Algo-trading, Dark pools, MiFID
- ETF Market: Market Maker/Specialist who issue ETF Shares to investors, buy underlying stocks with ETF or money from fund and stock exchange.

Physical ETF: generate return from holding all, or samples of underlying shares like index funds. Kept safe by a custodian.

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Synthetic ETF: Entering into total return swaps with counterparty issuer.

ETFs fo pay dividends monthly, quarterly, half-yearly or annual. Based on funds income net of expense and distribute to share holders on the register on record date. Paid via brokerage account.

Tracking error: Annual fees are deducted Reflecting daily NAVs.

#### 3.4 Currency/Foreign Exchange

#### 3.5 Fixed-Income

**Basic Concepts:** 

- Day Count Convention, Dirty Price
- Macaulay Duration, Modified Duration, DVo1, Dollar Duration, Effective Duration
- Maturity Effect, Coupon Effect, Yield Effect, Coupon Frequency Effect on Duration
- Term Structure of Yield Curve, Expectation Theory, Liquidity Preference Hypothesis, Segmented Markets/Preferred Habitat Theory. Bond Markets: ¡ 1 y (money market) 1-3, 3-10 (bellwehter of market movements, the major contributor for beta in the fixed-income portfolio) 10(long end, relatively illiquid and sensitive)
- long end risks: liquidity, credit( sovereign credit), inflation, growth
- Carry(difference between coupon-like cash-flow and funding cost) and Roll Down: Both assumes no yield curve shift
- yield curve trading/fly trading, steepner, flatener, positive/negative butterfly, Barbell and Bullet
- Inflation Linked bonds(Linkers) UK Index-Linked Gilts, French OATi, US TIPS, JGBi. Breakeven Inflation: The difference in linker

yields and nominal bond yields (linker coupon is always lower under positive inflation)

• Treasury Strips, UK Gilt Strips

#### Calculations

• Spot yield, par yield, forward rate, Bootstrapping

#### 3.6 Commodities

- Much more volatile than other major asset classes.(volatility from both supply/demand side)
- Low correlation with traditional asset classes
- Market drivers
  - Fear: Reduced risk appetite/ fight to real assets. Geopolitics shuts down supply chains
  - Currencies; Gold-USD, Oil-USD
  - OPEC, Freak weather, earthquake
- Commodity Currencies: IMF found 22 commodity currencies ( CHF-copper, AUD-Iron Ore,uranium)
- Stocks-to-Use Ratio, Reverse-to-Production Ratio
- Oil: Brent
- Physical Trade vs Derivatives(liquidity and leverage, low cost, less exotic)
- BSCOM, GSCI
- Commodity Futures, Convenience Yield, Contango(normal), Backwardation(Reversed)

#### Calculations

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- Yield = Collateral Yield + Roll Yield/Cost + Spot Return
- 1. NPV and IRR
- 2. Discounted Cash Flow Model
  - Free Cashflow
  - Required Rate of Return = Cost of Capital = Risk-adjusted discount rate: Usually from the CAPM
- 3. Valuation using Multiples P/E, P/B

#### 3.7 Derivatives

#### Swap

- Interest Rate Swap fixed bond + floating bond (received swap position: long fixed bond, short floating/FRA, duration/DVo1 is the difference of these two)
- Asset swap: Asset manager pay fixed, receive float, subject to credit risk

#### **Futures**

- long futures/ long cash = "funded beta"
- Used in asset-management: Tactical Asset Allocation, Beta management, Volatility Management
- Mark-to-market: "A martingale", variation margin changes everyday, fixed on EDSP -Exchange Delivery Settlement Price at the last day, cash settlement
- Open interest(# of net short contracts) vs volume(activity)
- Basis and Basis Risk: divergence of futures and underlying

#### CDS(Derivative)

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- Reference entity(borrower or obligor), reference obligation, obligations(trigger to credit event), deliverable obligations(usually pari-passu or senior in priority of payment to the reference entity), portfolio(deliverable obligations the protection buyer elects to deliver, execute accrued interest), conditions to payment(Entity party must have deliveredL Credit Event Notice, Notice to Public Info, Physical Settlement, etc)
- Fixed Coupon CDS: standardized (not "par spred") CDS: 100, 500bp(High Yield): To payment moves
- CDS pricing: probability of default x exposure of default x Loss
   Given Default driven by time, rates, spread

Credit Value Adjustment(CVA)

- pricing according to credit worthness of the counter-party
- Volatility market volatility, probability of counterparty default
- Funding Value Adjustement(FVA): uncollatteralised position hedge with collateralised

#### 3.7.1 Option

Credit Value Adjustment(CVA)

- Black-Scholes Model, Black's Model, Black-Scholes Equation (Heat Equation)
- Pricing factors and Greeks  $\Delta$ ,  $\Gamma$ ,  $\theta$ ,  $\nu$ (vega), vanna,  $\rho$ ,  $\epsilon$
- Pricing American Option

$$\frac{\partial V}{\partial t} + \frac{\sigma^2 S^2}{2} \frac{\partial^2 V}{\partial S^2} + rS \frac{\partial V}{\partial S} - rV < 0$$

Option Trading Strategies

put call parity 
$$c+pv(K) = p + S$$
  
protective put, covered call, collar

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1x1 spread(bull/bear), 2x1 spread, calendar spread risk-reversal(short p, long c) straddle, strangle, butterfly, iron butterfly volatility carry, dispersion trade

# Part II

# **Quantitative Investment Theories**

## Chapter 4

# **Quantitative Portfolio Mangement**

#### 4.1 Overview and Baseline Theories

A Basic Quant-trading System needs the following components (maybe from some teams, but need to be integrated)

- 1. Benchmark against appropriate total return index
- 2. Asset Allocation and Portfolio Management framework
- 3. Rebalance and account for dynamic risk
- 4. Risk tolerance and position sizing quantitatively (Kelly's Criterion)
- 5. (Optional) Market Regime Filter
- 6. Cash Management and Cash-like Instruments Management

#### Financial Theories involved

- 1. Efficient Market Hypothesis (Weak, Semi-strong, Strong forms)
- 2. Markowitz Portfolio Optimization

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- Minimum Variance Portfolio / Tangency Portfolio
- Jensen's alpha
- 3. Capital Asset Pricing Model(CAPM) Model

$$r = \beta(r_m - r_f) + r_f$$
 
$$\beta = \frac{cov(r, r_M)}{var(r_M)}$$

- 4. APT(Arbitrage-Free-Pricing) Model
- 5. No-arbitrage(weak, strong) and Law-of-one-price
- 6. Metrics
  - Sharpe Ratio
  - Jensen's alpha
  - Required Rate of Return = Cost of Capital = Risk-adjusted discount rate : Usually from the CAPM
- 7. Valuation using Multiples P/E, P/B

### 4.2 Portfolio Optimization

#### 4.2.1 Problems

• goal-based approach

describing goals, constructing sub-portfolios (selecting a module)

Active Holding Optimization - Goal based

• liability-relative

surplus optimization

hedging/risk-seeking portfolio

integrated asset-liability (non-linear correlation)

#### 4.2.2 Models

1. Single Period Models: Mean-variance models, Stochastic Optimization Models

Mixed Integer Optimization

2. Multi-period Models: Kelly Criterion, Dynamic Portfolio Optimization, Transaction Cost & Taxes

Stochastic and Dynamic Optimization

#### 4.2.3 Mean-variance model

• Optimization

$$\min_{\mathbf{x}} \mathbf{x}^{\mathsf{T}} \mathbf{V} \mathbf{x}$$
$$\mu^{\mathsf{T}} \mathbf{x} \ge \bar{\mu}, \mathbf{x} \in \mathbf{\chi}$$

equivalent to

$$\max_{\mathbf{x}} \mu^T \mathbf{x}$$

$$\mathbf{x}^{\mathsf{T}}\mathbf{V}\mathbf{x} \leq \bar{\sigma^2}, x \in \chi$$

or

$$\max_{\mathbf{x}} \mu^{T} \mathbf{x} - \frac{\gamma}{2} \mathbf{x}^{T} \mathbf{V} \mathbf{x}$$
$$x \in \chi$$

• Two Fund Theorem

$$\max_{\mathbf{x}} \mu^{T} \mathbf{x} - \frac{\gamma}{2} \mathbf{x}^{T} \mathbf{V} \mathbf{x}$$
$$\mathbf{1}^{T} \mathbf{x} = 1$$

Solution

$$\mathbf{x}^* = \lambda \frac{1}{\mathbf{1}^T \mathbf{V}^{-1} \mu} \mathbf{V}^{-1} \mu + (1 - \lambda) \frac{1}{\mathbf{1}^T \mathbf{V}^{-1} \mathbf{1}} \mathbf{V}^{-1} \mathbf{1}$$
$$\lambda = \frac{\mathbf{1}^T \mathbf{V}^{-1} \mu}{\gamma}$$

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Notice,

$$\frac{1}{1^{T}V^{-1}}V^{-1}\mu$$
 is the solution of  $\min_{\mathbf{x}} \mathbf{x}^{T}V\mathbf{x}$ ,  $\mathbf{1}^{T}\mathbf{x} = 1$ 

• One Fund Theorem

Add a risk-free asset into the portfolio

$$\max_{\mathbf{x}} (\boldsymbol{\mu} - r_f \mathbf{1}^{\mathsf{T}}) \mathbf{x} - \frac{\gamma}{2} \mathbf{x}^{\mathsf{T}} \mathbf{V} \mathbf{x}$$

Solution

$$\mathbf{x}^* = \lambda \frac{1}{\mathbf{1}^{\mathsf{T}} \mathbf{V}^{-1} (\mu - r_f \mathbf{1}^{\mathsf{T}})} \mathbf{V}^{-1} (\mu - r_f \mathbf{1}^{\mathsf{T}})$$
$$\lambda = \frac{\mathbf{1}^{\mathsf{T}} \mathbf{V}^{-1} (\mu - r_f \mathbf{1}^{\mathsf{T}})}{\gamma}$$

• Characteristic Portfolio

$$\frac{1}{\mathbf{1}^T V^{-1} a} V^{-1} a$$

for attribute a

- Common Constraints imposed on portfolio optimization would be
  - Long-only
  - Budget Constraint
  - Bounds on exposure to sectors
  - Bounds on individual positions (idiosyncratic risk)
  - Turnover constraints

#### 4.2.3.1 Mean-variance short-comings and solutions

**Problems** 

• Markowitz's Curse: Underperformance to market-cap weighted portfolio and concentration on assets.

- Estimation of mean and covariance matrix
- Allocating to less liquid asset class (no investable benchmark)
- Intergrality constraints: Problem becomes non-convex and difficult to solve

e.g.Using stocks to track benchmark index - need to be solved by heuristic approach

- Forward Selection: start with one, add at a time
- Backward Selection: start with whole set, selecting one creating least loss
- Clustering approach: pick q stocks from different clusters, start with benchmark weight, optimize

$$\arg \max_{\mathbf{x}, \mathbf{y}} \sum_{i} \sum_{j} \rho_{ij} x_{ij}$$
$$\sum_{j} y_{j} = q, \sum_{j} x_{ij} = 1$$
$$x_{ij} \leq y_{j}$$

y is binary to indicates a stock is selected or not

#### Solutions

- Monte-Carlo simulation
- resampled mean-variance optimization
- add additional constriants (other than budget) concentrated position
- resampled mean-variance
- non-normal optimization approach
- Covariance matrix shrinkage estimators

Stein's Paradox

$$\hat{mu} := (1 - \omega)\bar{\mathbf{r}} + \omega(\mu_0 \mathbf{1}), \omega \in [0, 1]$$

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Ledoit-Wolf

$$\hat{\mathbf{V}} := \omega \hat{\mathbf{V}} + (1 - \omega) \mathbf{V}_0, \omega \in [0, 1]$$

 $V_0$  is prior estimator(constant or single-factor implied cov matrix)

• Black-Litterman Model (Reverse Optimization - Also less sensitive to inputs)

$$\mu \sim N(\mathbf{G}, \mathbf{Q})$$

$$P\mu = q$$

(views)

$$\hat{\boldsymbol{\mu}} = \mathbb{E}[\boldsymbol{\mu}|\textit{views}] = \boldsymbol{\pi} + \mathbf{Q}\mathbf{P}^{\mathsf{T}}(\mathbf{P}\mathbf{Q}\mathbf{P}^{\mathsf{T}})^{-1}(\mathbf{q} - \boldsymbol{P}\boldsymbol{\pi})$$

By Solving

$$\min_{\mu}(\mu-\pi)^{T}\mathbf{Q}^{-1}(\mu-\pi)$$

$$P\mu = q$$

 $\pi$  is market consensus returns,  $\mathbf{Q} = \tau \mathbf{V}$ 

- Robust Estimations
- Risk budgeting vs factor based asset allocation(risk parity) to maximize diversification

Marginal Contribution to Risk

$$MRC_i = \frac{\partial \sigma_p}{\partial x_i} = \frac{Vx_i}{\sqrt{\mathbf{x}^T V \mathbf{x}}}$$

Risk Contribution

$$x_i \dot{M}RC_i = \frac{x_i V x_i}{\sqrt{\mathbf{x}^T V \mathbf{x}}} = \frac{\sigma_p}{n}$$

Use Different Risk Measures

- Variance

- Mean Absolute Deviation

$$MAD(r) = \mathbb{E}(|r - \mu|)$$

$$MAD = \sqrt{\frac{2}{\pi}}\sigma$$

under Normal

$$\underset{\mathbf{x}}{\operatorname{arg\,min}} MAD(\mathbf{r}^{\mathsf{T}}\mathbf{x})$$

s.t.  $\mathbf{x} \in \chi$  often solve by scenario optimization

- Value at Risk
- CVAR (Asset Stress Loss)

$$\mathbb{E}(Y|Y \ge VaR_{\alpha}(Y)) = min_{\gamma}(\gamma + \frac{1}{\alpha} \int_{-\infty}^{\infty} max(y - \gamma, 0)f(y)dy)$$

#### 4.2.4 Stochastic Optimization and Multi-Period Model

#### 4.2.4.1 Kelly Crierion

The Kelly Criterion is well-known among gamblers as a way to decide how much to bet when the odds are in your favor.

The simple rule goes like this. Suppose that with probability p you will make a profit of b times what you bet, and otherwise you lose the bet. Then the optimal amount to bet is  $\frac{pb(1p)}{b}$ 

#### 4.2.4.2 Dynamic Portfolio Optimization

Some random variables value will reveal during each stage.

• Simple case. Under log utility U(W) = log(W) or i.i.d. return, a myopic policy is optimization.

Common Problems as

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- Mulit-stage optimization with income
- Portfolio optimization with trading cost

Almgren-Chriss Model

$$S_k = S_{k-1} + \sigma \xi_k - g(y_k), \tilde{S}_k = S_{k-1} - h(y_k)$$

 $\xi_k$  is random shork, g and h are permanet and temporary market impact  $\tilde{S}$  is captured price for trade y.

$$Cost(\mathbf{x}) = S_0 X - \sum_{k=1}^{N} \tilde{S}_k y_k$$
 
$$arg \min(\mathbb{E}(Cost(\mathbf{x})) - \lambda var(Cost(\mathbf{x})))$$

k is trading times,  $t_k = k\tau$ ,  $\mathbf{x} = (x_0, ...x_N)$  is trading trajectory,  $\mathbf{y}$  is "trade list",  $y_k = x_k - x_{k-1}$ 

• Sequential Decision Problem and Bellman's Optimality Principle Solve

$$J(\mathbf{s}_0) = \underset{\mathbf{x}_0, \dots, \mathbf{x}_T}{\arg \max} \left[ \sum_{t=0}^{N} g_t(\mathbf{s}_t, \mathbf{x}_t) + g_{T+1}(\mathbf{s}_{T+1}) \right]$$

by solving the value-to-go of the tail problem

$$J(\mathbf{s}_t) = \underset{\mathbf{x}_t}{\arg\max}[g_t(\mathbf{s}_t, \mathbf{x}_t) + g_{t+1}(\mathbf{s}_{t+1})] = \underset{\mathbf{x}_t}{\arg\max}[g_t(\mathbf{s}_t, \mathbf{x}_t) + g_{t+1}(f_t(\mathbf{s}_t, \mathbf{x}_t))]$$

f is the law of motion, which is needed

#### 4.2.4.3 Garleanu-Pedersen's Model

Model of Dynamic Programming with predictable returns and t-costs

#### **Problem**

- Minimize risk and transaction costs
- Trading Speed trade-off: Trade a lot: more alpha, less risk, more t-costs
- ALpha (Decay) Speed: Fast and slow signals
- Trade-off between tax costs and diversification benefits may depend on the age.

### 4.3 Tax Management in Portfolio Optimization

set up

- Capital gain tax depends on the holding period
- Tax rebate on loss
- Optimal tax trading: always realize loss, sometimes realize gains

# Chapter 5

## **Factor Models**

#### 5.1 Factor Models

Factor Models plays a key role in all components of asset management

- Valuation and Market Expectation: CAPM, APT, alpha signals
- Risk Management: Risk attribution, stress test, risk modelling
- Portfolio Management: Smart beta, portfolio construction
- Performance: Performance attribution, style analysis

#### 5.1.1 Major Types of Factor Models

• Regression Model: Observable factor returns

$$X = a + BZ + U$$

,where **Z** is observable, estimate **B**,  $\mathbf{a}(\beta, \alpha)$ 

$$(\mathbf{a}, \mathbf{B}) = \arg\min \mathbb{E}(\|\mathbf{a} + \mathbf{BZ} - \mathbf{X}\|^2)$$

$$B = cov(\mathbf{X}, \mathbf{Z})var^{-1}(\mathbf{Z}), a = \mathbb{E}(\mathbf{X} - \mathbf{B}\,\mathbb{E}(\mathbf{Z}))$$

Example: CAPM (CAPM beta can be improved by shrinking towards 1

• Cross-sectional Model: **B** (factor loadings) is observed. Usually use weighted list squares

$$X = a + BZ + U$$

Usually solved with Weighted Least Squares:

$$(\mathbf{a}, \mathbf{Z}) = \arg\min \mathbb{E}(\|\mathbf{a} + \mathbf{B}\mathbf{Z} - \mathbf{X}\|_{\Delta^{-1}}^{2})$$
$$Z = (\mathbf{B}^{T} \mathbf{\Delta}^{-1} \mathbf{B})^{-1} \mathbf{B}^{T} \mathbf{\Delta}^{-1} \mathbf{X}, a = \mathbb{E}(\mathbf{X} - \mathbf{B} \mathbb{E}(\mathbf{Z}))$$

 $\Delta$  is often diagonal - associated to preassumed residual sizes. Example: most common models, and risk models such as Aximoa and Barra  $\mathbf{r} = \mathbf{B}\mathbf{f} + \mathbf{u}$ , use time series data of r to compute time series data of f

Principal Components Model

$$\mathbf{X} = \mathbf{a} + \mathbf{BZ} + \mathbf{U}$$

$$\mathbf{Z} = [Z_1, Z_2, ..., Z_n]^T$$

$$Z_i = \mathbf{e}_i^T (\mathbf{X} - \mathbb{E}(\mathbf{X}))$$

$$\mathbf{e}_i = \underset{\mathbf{e}}{\operatorname{arg max}} var(\mathbf{e}^T \mathbf{X})$$

$$\mathbf{e}$$

$$\|\mathbf{e}\|^2 = 1$$

$$\mathbf{e}_k^T \mathbf{e} = 0, k = 1, ..., i - 1$$

then

$$\mathbf{V} = \mathit{var}(\mathbf{X}) = [\mathbf{e_1}, \mathbf{e_2}, ... \mathbf{e_n}] \begin{bmatrix} \lambda_1^2 & & \\ & \ddots & \\ & & \lambda_n^2 \end{bmatrix} [\mathbf{e_1}, \mathbf{e_2}, ... \mathbf{e_n}]$$

**Principal Components** 

$$X_i^{PC} = \mathbf{e}_i z_i = \mathbf{e}_i \mathbf{e}_i^T (\mathbf{X} - \mathbb{E}(\mathbf{X}))$$
  
 $\mathbf{B} = [\mathbf{e}_1, \mathbf{e}_2, ... \mathbf{e}_n], \mathbf{a} = \mathbb{E}(\mathbf{X})$ 

 Hidden Model: Try to distinguish between systematic and idiosyncratic risk

$$X = a + BZ + U$$

want  $cov(\mathbf{Z}, \mathbf{U})$  to be o and  $var(\mathbf{U}) = \Delta$  diagonal, want  $\mathbf{V} = var(\mathbf{X}) = \mathbf{B}^T var(\mathbf{Z})\mathbf{B}^T + \Delta$  Example: the APT Model

Sometimes, factor models will be used in a multi-layer fashion (eg. decompose return first be sectors, then style factors)

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### 5.1.2 Factor portfolio

Two common approaches

### 5.1.2.1 Signal Portfolio Approach

This is the traditional portfolio construction approach

- 1. From z score form the signal score (standardization, transformation, normalization)
- 2. Form the signal portfolio
  - Long-short: Long equal-weight (or value-weight) portfolio with high signal and equal weight (or value-weight) portfolio with low signal
  - Ranking: use signal to rank securities. The construct a long-short portfolio with holdings

$$w_i = c(rank(s_i) - \frac{\sum_i rank(s_i)}{N})$$

- Sorting: two-fold or k-fold version of the above high-low long-short
- 3. Use signal portfolio to get expected returns( $\alpha$ ), covariance matrix and constraints for the optimization

After this, finalize the rebalancing frequency, investment universe etc.

#### 5.1.2.2 Consistent Portfolio Construction Approach

By Axioma (2011)

$$\mathbf{r} = \mathbf{B}\mathbf{f} + \mathbf{u} = \mathbf{B}_A\mathbf{f}_A + \mathbf{B}_F\mathbf{f}_F\mathbf{u}$$

1. Factor Mimicking Portfolios: with only exposure to one of alpha sigal/factor attributes **a** 

$$\min_{\mathbf{h}} \mathbf{h}^{T} \mathbf{V} \mathbf{h}$$

$$\mathbf{B}^{T}_{A} \mathbf{h} = \mathbf{e}_{j}$$

$$\mathbf{B}^{T}_{R} \mathbf{h} = \mathbf{0}$$

$$\mathbf{h} = \frac{1}{\mathbf{a}^{T} \mathbf{V} \mathbf{a}} \mathbf{V}^{-1} \mathbf{a}$$

( or can be cash neutral instead of factor neutral)

$$\mathbf{1}T\mathbf{h} = 0$$

$$\mathbb{E}(\mathbf{f}_A) = \mathbb{E}(\mathbf{H}^T r), var(\mathbf{f}_A) = \mathbf{H}^T \mathbf{V} \mathbf{H}$$

$$\mathbf{H} := [\mathbf{h}^1, ..., \mathbf{h}^m]$$

, m factors

2. Combine to a target portfolio

$$\mathbf{h}^{\mathbf{P}} = \underset{\mathbf{h}, \mathbf{w}}{\text{arg max}} \mathbb{E}(\mathbf{f})^{T} \mathbf{w} - \frac{\gamma}{2} \mathbf{h}^{T} \mathbf{V} \mathbf{h}$$

$$\mathbf{h} = \mathbf{H} \mathbf{w}$$

3. Find the acceptable portfolio that closest to target portfolio

$$\begin{aligned} \min_{\mathbf{h}}(\mathbf{\alpha}^{P})^{T}\mathbf{h} - \frac{\gamma}{2}\mathbf{h}^{T}\mathbf{V}\mathbf{h} \\ \Leftrightarrow \\ \min_{\mathbf{h}} \frac{1}{2}(\mathbf{h}^{P} - \gamma\mathbf{h})^{T}V(\mathbf{h}^{P} - \gamma\mathbf{h}) \end{aligned}$$

# 5.2 Alpha

• alpha is from signal and based on benchmark/factor models. For example find some signal to score stocks, then compute alpha from z-scores (neutralize for risk factors)

$$\alpha = z - (z^T x_B) fi$$

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 Information Coefficient(IC): Correlation between factor score/prediction and actual outcome (realized return). IC ≥ 0.05 is considered good

• Grinold and Kahns rule of thumb (Alpha scaling)

$$\alpha = IC \times score \times volatility$$

Usually get covariance from risk model providers (Axioma, Bloomberg, Northfield, Barra)

• Benchmarkmark-relative mean-variance models

$$\min_{\mathbf{x}} \mathbf{x}^{\mathsf{T}} \mathbf{V} \mathbf{x}$$

$$\alpha^{\mathsf{T}} \mathbf{x} > \bar{\alpha}, \mathbf{x} \in \mathbf{x}$$

equivalent to

$$\max_{\mathbf{x}} \mathbf{\alpha}^T \mathbf{x} - \frac{\gamma}{2} \mathbf{x}^T \mathbf{V} \mathbf{x}$$
$$\mathbf{x} \in \mathbf{x}$$

we get

$$\mathbf{x} = \frac{1}{\gamma} V^{-1} \boldsymbol{\alpha}$$

• Fundamental law of active management

From above solution

$$IR = \sqrt{\alpha^{T} \mathbf{V}^{-1} \mathbf{\alpha}}$$

$$\alpha_{i} = IC\dot{\alpha}_{i}\dot{z}_{i}, \mathbf{V} = diag(\sigma_{1}^{2}, ..., \sigma_{N}^{2})$$

$$IR = \sqrt{\alpha^{T} \mathbf{V}^{-1} \mathbf{\alpha}} = IC\sqrt{N} = IC\sqrt{BR}$$

• The Fundamental Law and Transfer Coefficient

$$IR = \frac{\alpha^T h}{\sqrt{h^T V h}} = \frac{\alpha^T h}{\sqrt{\alpha^T V^{-1} \alpha} \sqrt{h^T V h}} \sqrt{\alpha^T V^{-1} \alpha}$$

### 5.3 Smart beta and Smart Alpha

long-short STS strategy short extension( 120/20 ) Strategy alpha and beta separation portable alpha

long short equities (factor) convertible arbitrage

# 5.4 Risk Premia Factors

### 5.4.1 Size

- Small-Minus-Big factor in equity clas
- No longer significant as value
- Structural Bias Less information from smaller business
- Risk Sharing Investor's Reluctance to invest in smaller firms

### 5.4.2 Value

- High-Minus-Low
- Behavior Bias Rebalancing Contrarian Timing Reversals
  - Over-extrapolation of past growth
  - Delayed overreaction to price trends
  - Discomfort with "dogs" and distress
  - generic risk premium (1/P)
  - rational based on distress risk, dynamic betas
- Who is on the other side
  - Over-extrapolation or multi-year growth
  - Long Term overreactors( chasing returns at 3-5 yr when reversal dominate)
  - Managers attracted to glamor stocks
  - Investors averse to some risks in value stocks

### 5.4.3 Momentum

- Behavior Bias
  - Herding, Confirmation Bias, Fund Flows
  - Under-reaction to public news
  - over-reaction to price trends
  - Pro-cyclical risk tolerance or risk management
  - Disposition effect
- Who is on the other side
  - Inattentioned, conservative, overconfident
  - contrarians resisting the herd
  - investors without stop-loss rules
  - those handing on the losers

### 5.4.4 Carry

- Behavior Bias
  - Skew/Tail Preference volatility jump premia
  - Overconfident expectations of capital losses (mkt moves) that would offset the carry trade non-profit-driven flows supporting high carry
  - generic risk premium(1/P)
  - liquidity needs, price pressure
- Who is the other side
  - tail insurance buyers, skewness lovers, crash protection seekers
  - overconfident holders of salient macro views
  - non-profit driven actors(central banks)
  - Impatient/short-horizon investors, those needing immediacy in trading
- Risk Sharing

- Options: Volatility Carry, Volatility Selling
- Credit beta-neutral relative value trade, benefit from investor's portfolio limits(structural) providing market with insurance against credit(risk sharing)
- CO Curve provide liquidity to hedgers/producers (risk sharing), higher demand from investors on near dated contracts and supply from hedgers on far dated

#### • Structural

- Commodity Carry: Imbalance in inventory levels and subsequent hedging pressure as reflected in time spreads (eg. contango suggests selling pressure due to inventory surplus with the expectation of future price depreciation)
- Koijen el el(2013) Approach

$$C_t = \frac{S_t - F_t}{X_t}$$

 $S_t$ : Spot price,  $F_t$ : Futures price,  $X_t$ : Capital to finance futures contracts e.g

Currency(CIP holds): 
$$\frac{S_t - F_t}{F_t} = \frac{r_t^{f,*} - r_t^f}{1 + r_t^f}$$

Equity: 
$$\frac{S_t - F_t}{F_t} = \left(\frac{\mathbb{E}(D_t(t+1))}{S_t} - f_t^f\right) \frac{S_t}{F_t}$$
$$F_t = F_t(1 + r_t^f) - \mathbb{E}(D_{t+1})$$

Commodity(storage cost): 
$$\frac{S_t - F_t}{F_t} = \frac{\delta_t - r_t^f}{1 + r_t^f - \delta_t}$$
$$F_t = S_t(1 + r_t^f - \delta_t)$$

Zero-Coupon Bond: 
$$\frac{f_t^{(n)} - r_t^f}{1 + r_t^f}$$

$$S_t^{(n)} = \frac{1}{(1 + y_t^{(n)})^n}, F_t^{(n)} = (1 + r_t^f)S_t^{(n)}$$

$$C_t \approx (y_t^{(n)} - r_t^f) - D^{mod}(y_t^{(n-1)} - y_t^{(n)})$$

(slope and roll-down)

Option Carry: 
$$\frac{P_{j}(\tau - 1, K, S_{t}, \sigma_{t,\tau - 1})}{(1 + r_{f}^{t})P_{j}(\tau, K, S_{t}, \sigma_{t,\tau})} - 1 \approx \frac{-\theta_{t}^{j} + \nu_{t}^{j}(\sigma_{t,\tau - 1} - \sigma_{t,\tau})}{(1 + r_{f}^{t})P_{j}(\tau, K, S_{t}, \sigma_{t,\tau})} - \frac{r_{t}^{f}}{1 + r_{t}^{f}}$$

Portfolio weights

$$w_i = z(rank(C_i) - \frac{N+1}{2})$$

z is scalar makes long-short position equals 1, N is number of stocks

$$r_{t+1}^i = a^i + b_t + cC_t^i + \epsilon_{t+1}^i$$

### 5.4.5 Betting-against Beta

- Behavior Bias
  - Quality, Risk Parity
  - Behavior Bias
  - leverage aversion
  - lottery seeking
  - relative risk preferences, conventionality
  - active managers seeking maximal bang for the (unlevered) buck
  - Underreaction to quality
- The other side
  - constrained investors who avoid levering up low-risk opportunities with better SRs and instread choose concentrated high-risk exposures
  - investors who prefer lotteries and positive skewness

- benchmarked managers who care more about tracking error than total portfolio risk
- overconfident and constrained active managers
- inattentioned, story-telling investors
- From Margin CAPM Model(Black): Security Market Line is flatter than it should be because of margin constraints of investors
- Frazzini-Pedersen construction

$$\hat{\beta} = \hat{\beta}_{i} = \hat{\rho}_{i} \frac{\sigma_{i}}{\hat{\sigma}_{M}}, \beta_{i} = \omega + (1 - \omega) \hat{\beta}_{i}$$

$$z = rank(\beta), \hat{z} = \frac{\mathbf{1}^{T} z}{n} \mathbf{1}$$

$$w_{H/L} := \frac{1}{\mathbf{1}^{T} (z - \hat{z})^{+/-}} (z - \hat{z})^{+/-}$$

$$r_{BAB,t} = \frac{1}{\beta_{L,t}} r_{L,t} - \frac{1}{\beta_{H,t}} r_{H,t}$$
Solve
$$\max_{x} (\mathbb{E} (\mathbf{P^{1}} - \mathbf{P^{0}})^{T} \mathbf{x} - \frac{\gamma_{i}}{2} \mathbf{x}^{T} \mathbf{\Omega} \mathbf{x}$$

$$m_{i} (\mathbf{P^{0}})^{T} \mathbf{x} \leq W_{i}$$

$$\mathbf{x}^{*} = \frac{1}{\gamma} (\mathbb{E} (\mathbf{P^{1}}) - (1 + \phi) \mathbf{P^{0}})$$

$$\mathbb{E} (r_{BAB}) = \frac{\beta_{H} - \beta_{L}}{\beta_{H} \beta_{L}}$$

- Credit: Jump-to-Default
  - IR Curve/CR Curve Benediting from the average investor's leverage constraints

# 5.4.6 Volatility Carry

• CVA Desk vs Real Trade

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### 5.4.7 Factor Interactions

Value and Momentum are negatively correlated and provides diversification benefits ("Value and Momentum Everywhere")

### 5.4.8 Others

- Liquidity Risk Premia
- Five Factor Model by Fama-French: Profitability (RMW-robustness, high OP), Investment(CMA-conservative, low INV)
- Seasonality: Benefiting from the market's ability to correctly estimate the seasonality of commodities (behavioral) and assume seasonality risk
- : COT : benefiting from the market's inability to process positioning data (behavioral and the average investor's constraints in positioning according to such data
- Equity Intraday Momentum

## 5.5 Bond Factors

Some bond specific risk-premia study

• Fama-Bliss(1987) and Cochrane-Piazzesi(2005) on excess log return and forward spread

$$rx_{t+1}^{(n)} = \alpha + \beta(f_t^{(n)} - y_t^{(1)}) + \varepsilon_{t+1}^n$$

• Ludvingson-Ng (2009) form factor of macroeconomic variables

$$rx_{t+1}^{(n)} = \boldsymbol{\alpha}^T \boldsymbol{F}_t + \boldsymbol{\beta}^T \boldsymbol{Z}_t + \varepsilon_{t+1}$$

### 5.6 Market Anomalies

#### 5.6.1 Behavioral Finance

Behavioral Finance Theories Includes Prospect Theory( People suffice rather than optimize, the utility curve is concave at the gain part and convex at the loss part(loss aversion). Bounded Rationality and Behavioral Market Anomalies/bias

- 1. loss aversion(herding)
- 2. illusion of control(TAA)
- 3. Mental accounting(goal),
- 4. availability bias(familiarity, home-bias)
- 5. recency bias(tactical shifts)
- 6. framing(risk-return presented in a different way)

other: liquidity risk premia

- 1. Risk Management and Hedging
- 2. Leverage
- 3. Correlation
- 4. Strategy replacements, leverage rebalancing and rebalancing frequency, leverage reset

other: liquidity risk premia

- 1. Risk Management and Hedging
- 2. Leverage
- 3. Correlation
- 4. Strategy replacements, leverage rebalancing and rebalancing frequency, leverage reset

# Statistical Arbitrage

## 6.1 mean-reversion

intraday mean-reversion

hedge fund strategies

merger/risk arbitrage

fixed income arbitrage swap spread arbitrage yield-curve spread arbitrage mortgage spread arbitrage ( on prepayment rates) capital structure/credit arbitrage volatility trading interest cap vol) arbitrage

# **Quantitative Trading Strategies**

## 7.1 Strategy Toolbox List

• Signal

Multi-signal mix: Multi-window multi-signal Signal Smoothing:

Exponential Decay, half-life length

Weighting and Rebalancing

Strategy Groups

Signal Speed: for example, for volatility carry strategies, drawdown recovers fast -Using Asset Stress Loss is more appropriate. For trend strategies, positive weight and negative weight changes fast, so use parity when put into top level. Inside the strategy group, use weight smoothing

Risk

Portfolio Volatility Control, Sub Portfolio Volatility Control

Correlation

Leverage Control

Volatility Target

Idiosyncratic Risk

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Special Concerns on the tradability/capacity of the strategy

- Trading Cost and Market Impact : empirical analysis, trading cost models(quadratic impact) and rebalance frequency control
- Tax, Tax-aware investing

Different rules applied to ordinary income, capital gains, capital losses. There are differences in the tax rates for long-term vs short capital gains. Wash-sale restrictions.

# 7.2 Equity

# 7.3 Volatility and Dispersion Trades

## 7.3.1 Volatility Models and Time-Series Models

# 7.4 fixed income + macro

# 7.5 fixed income derivatives

MBS Convexity Trade

- 1. real estate-direct vs indirect environment 2. benchmarks of real estate
- 3. other alternative, commodity to hedge

- 7.6 credit
- 7.7 commodities
- 7.8 Cross Asset
  - 1. Cross-Asset Risk Premia
  - 2. Cross-Asset Trend

# **Quant Strategies and Long-short Strategies**

Stat Arb (typically high volume), Merger Arb, Relative Value, IntraCap Pairs

# Part III

# **Quantitative Modeling and Strategies Implementation**

# **Strategy Development Overview**

Typically, need the sub functions/sub teams including:

- 1. Data Curator: Data collection, cleaning, indexing, storing, adjusting and delivering
- 2. Feature Engineering and Analytics: Data Mining, Signal Extraction and Processing using information theory, Data visualization, labeling, filtering, classifiers building try to extract features
- 3. Strategies Research: Make sense of features, market observation, instrument knowledge and try to formulate general theory/intuition that explains market mechanics. Submit code to the backtesting team
- 4. Backtesting: Statistical, Stochastic, Econometric tests of strategies/portfolios
- Deployment: Rely heavily on computing, process schedulers, automation servers, vectorization, multithreading, multiprocessing, Big Data, Machine Learning on Big Data and High-performance computing

Back office and Risk Management (See Risk Management chapter)

- 1. Portfolio Aggregation
- 2. Portfolio Evaluation
- 3. Performance/Risk Attribution

Also, teams should also maintain and select current strategies, typically, a strategy experiences Embargo, Paper Trading, Real-money trading, Re-allocation and Decommission.

### Some Major Challenges:

- 1. Traditional Portfolio Mangers work in silos and make decisions alone. While quant investing need to cut-down the decision making process to small research projects and run as a strategy factor
- 2. Combine "black-box" PM views/market intuition with quant research results from data/math.
- 3. Combine machine learning algorithm with existing traditional strategies.
- 4. "Backtest overfitting": Without limitation on number of trials, Sharpe ratio in back test could be very high.

# Financial Data Modeling

### 10.1 Financial Data Structure

Basic Assumptions: Most time should check implicit assumptions

- Equities  $log(\frac{V_{t+1}}{V_t}$  i.i.d. Liquidity varies a lot. Benchmark indices can be misleading: eg. DJIA is priced-weighted. S&P 500 leans towards large market cap companies and not include **dividend** reinvestment (S&P Total Return Index include)
- Fixed Income  $Y_t(\tau) = -\frac{1}{\tau}log(V_t(t+\tau))$  i.i.d shock on interest rate (bond yield)
- Risk drivers/factors  $\mathbf{X}_t = [X_{1,t}...X_{\bar{d},t}]$  homogeneous in time, and determines the joint PnL of instruments

### Data Problems

- Financial Data, especially economic data can be series lagged.
   (important data can be officially reported/audited with a quarter lag, IMF reports some country data with 2 years lag)
- Data Measurement errors and biases: transcription errors, survivorship bias(\*), Appraisal Data (Smoothed data, which seriously influences volatility estimation, volatility factor is needed)

- Sampling's interaction with market regime and non-stationarity
- return measured less than a year includes implicit extrapolation
- illiquid and infrequent priced assets may be priced with

Matrix pricing (common in bond market)

Consensus/Expert Data

Appraisal Data: without public information, risks is underestimated

- Bonds: Recall, Termination (Aging), Exchanged
- Stock: Corporate Actions (Splits, Reverse Splits, Voting Rights, etc)
- Futures and Options: Termination and Rolling
- Currencies: Not Traded in centralized order book
- Different data collection principles and definitions, error rates in collection, change in calculation formula (eg. CPI, rescale of index), data re-scale ("rebase" of economic data)
- Benchmark formormulation methods, liquidity, investability,

### Signals

- Quote Offers canceling/replacing with sell orders o potnetial sell off information
- Limit Orders vs Market Orders

# 10.2 Financial Data Sampling

- 10.2.1 Data Sampling Methods
- 10.2.2 Data Sampling Weights
- 10.3 Time-series Data Modeling
- 10.4 Data Labeling in Strategy Research
- 10.5 Estimators

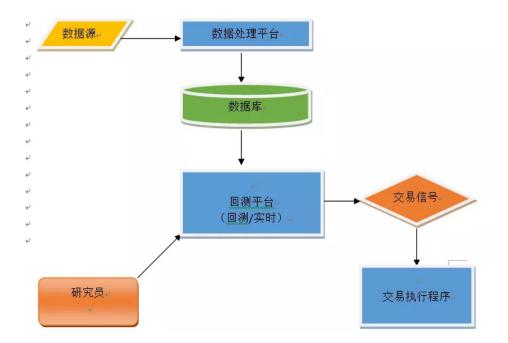
Distinguish between

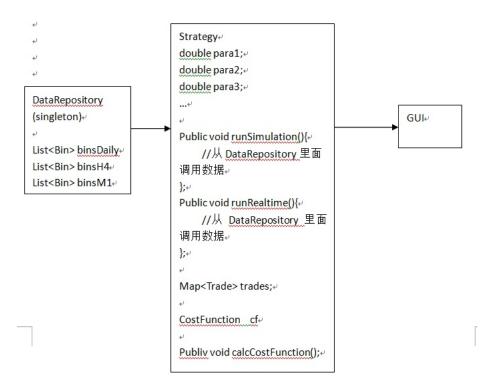
- Sample Estimator
- Shrinkage Estimator
- Factor Models(imposed factor structures/PCA Structures)

# **Trading System**

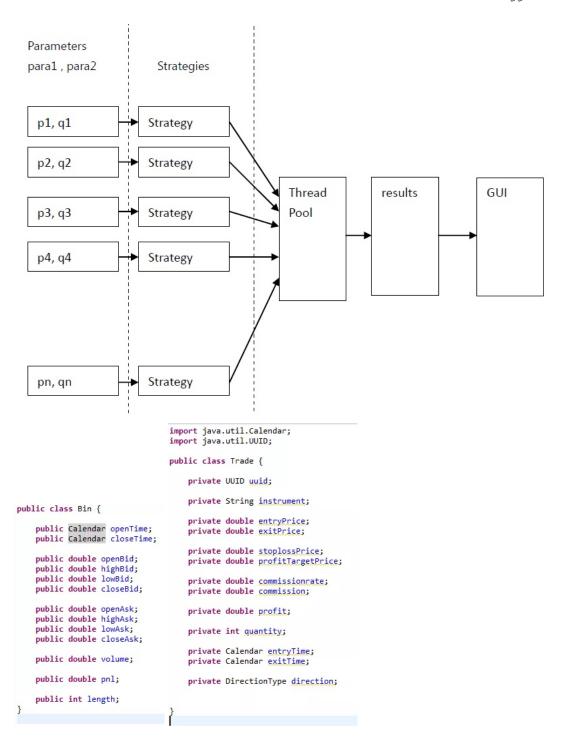
# 11.1 Strategy Development Pipeline(Single/Linear Strategy)

# 11.1.1 Basic Architecture/System





### 11.1. STRATEGY DEVELOPMENT PIPELINE(SINGLE/LINEAR STRATEGY) 55



Historical Data is a singleton. All Market Data (eg. a candle stick ) should be organized to feed the researcher to program strategies on the backtester (eg. like quantopian). All back-testing should be parallized (ideally on GPU) to display parameter-profit relationship. (heatmap, stock charts, etc.) Ideally the optimization process could be visualized (like Tensorflow)

All like a research facility feedback cycle.

Key Details: API Design, Module Separation etc.

#### 11.1.2 Data

Key is a real-time listener. Technical Considerations: KDB, Hadoop and HDFI(?), SQL Like, Mongo Db to store Archive Data. Market Data Providers consideration buying from Wind, BBG, Reuters, Etc. teams: platform operation engineer, analytics builder, strategy control/management and risk management, data team, execution team, researcher team ( 3 x tech ) data licensing and data quality insurance data base, text file archive, big data issue cheap data: brokerage: interative brokers.

#### 11.1.3 Backtester/Simulator

**Key Components** 

\*Send Singal to Quoting/Trading/Exection Tool(Real Time) \*Market Data Objects (eg. loop for every time bins) \*stop loss/risk control system integration \*parameter-backtest profit/statistics result: optimization and loss function set function to tune the parameters \*multi-thread: Java backter (Java thread pool\*) \*human selection of parameters: parameter table and visualization

### 11.1.4 Trade Record and Money Management

record every trade, summarize execution shortfall, statistical trends and information (shortcomings of strategy executions) and market information ( learning material) build statistics and storage

More: order book and trade book level data handling

### 11.1.5 Analytics

### 11.1.5.1 Strategy Management

, Sharpe Anslysis, Holding Period, Slippage visualization to better assistant strategic allocation

### 11.1.5.2 Execution Analysis and Cost

quantitative trading/systematic trading strategies: \* equity long/short

#### 11.1.6 Research Team

Key problems: \* Optimization and Combination of Sub-Strategies (Eg. factors) \* Market Regime Change Detection(problem not solved): Distinguish between trend and oscillation market \* market supply/demand imbalance analysis (risk-premia) \* volatility trading, dispersion trading - 2nd and 3rd degree trading, (vol model, vol clustering effect, vol leverage effect) \* hedging/overlay strategy research: hedging cost and hedging risk management, how to adjust hedge

according to market condition. \* common ideas: market imbalance, mean-reversion, autocorrelation patterns etc (find patterns and trade) - based on statistics. Risk factors, implied arbitrage - based on math.

#### 11.1.6.1 Parameter Optmization and Control

Rely on GUI - parameter distribution and selection optmization methologies from machine learning ( see optimization chapter) robustness analysis and out-of sample test \*\* ( random cut the universe of rolling window on selection period )

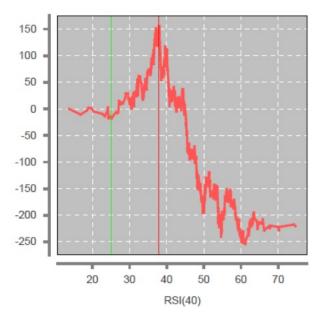
#### 11.1.6.2 Signal Indicator Design

For example, based on fundemental ratio and technical indicators - design a formula. And check the level of prediction power (if any)

1.seeking stationarity: find a stationary time series use difference, integration, and normalize with volatility 2.find signal level, plot cumulative back-test return against different signal level (use own quotes, and use signal level to filter quotes)

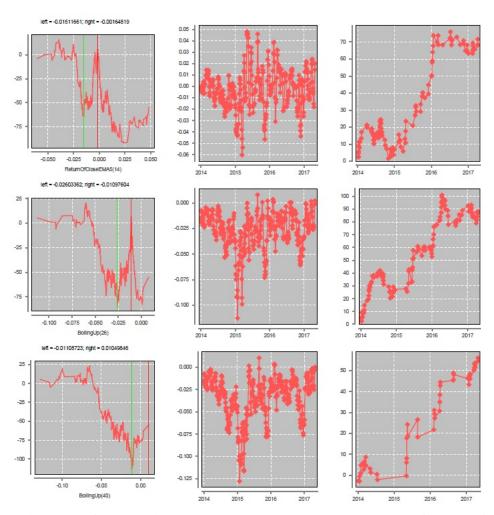
### 11.1. STRATEGY DEVELOPMENT PIPELINE(SINGLE/LINEAR STRATEGY) 59

left = 25.12895746; right = 37.92960233



customized indicators

3.Check stability of



4. check overfitting and type-II error in all settings, apply noise filtering if possible 5. design a interface to input indicator(math formula parser to read string) and visualize information using GUI.(HTML/XML Render)

### 11.1. STRATEGY DEVELOPMENT PIPELINE(SINGLE/LINEAR STRATEGY) 61

```
<?xml version="1.0"?>
<indicators>
</
    <indicator>
        <f>OpenDivEMA(\i)</f>
        <i>>2,3,4,5,7,10,14,20,24,26,30,36,40,42,46,48,50</i>
    </indicator>
    <indicator>
        <f>CloseDivEMA(\i)</f>
        <i>>2,3,4,5,7,10,14,20,24,26,30,36,40,42,46,48,50</i>
    </indicator>
    <indicator>
        <f>HighDivEMA(\i)</f>
        <i>>2,3,4,5,7,10,14,20,24,26,30,36,40,42,46,48,50</i>
    <indicator>
        <f>LowDivEMA(\i)</f>
        <i>>2,3,4,5,7,10,14,20,24,26,30,36,40,42,46,48,50</i>
     </indicator>
 </section>
<section name="ReturnEMA">
    <indicator>
        <f>ReturnOfOpenEMA5(\i)</f>
        <i>>2,3,4,5,7,10,14,20,24,26,30,36,40,42,46,48,50</i>
    </indicator>
       <f>ReturnOfCloseEMA5(\i)</f>
        <i>>2,3,4,5,7,10,14,20,24,26,30,36,40,42,46,48,50</i>
    </indicator>
    <indicator>
        <f>ReturnOfHighEMA5(\i)</f>
        <i>>2,3,4,5,7,10,14,20,24,26,30,36,40,42,46,48,50</i>
     </indicator>
    <indicator>
        <f>ReturnOfLowEMA5(\i)</f>
        <i>>2,3,4,5,7,10,14,20,24,26,30,36,40,42,46,48,50</i>
     </indicator>
-</section>
```

```
public static HashMap<String, List<String>> parseXML(File fXmlFile) {
    HashMap<String, List<String>> map = new HashMap<String, List<String>>();
    DocumentBuilderFactory dbFactory = DocumentBuilderFactory.newInstance();
    DocumentBuilder dBuilder = null;
        dBuilder = dbFactory.newDocumentBuilder();
    } catch (ParserConfigurationException e) {
        e.printStackTrace();
    Document doc = null;
        doc = dBuilder.parse(fXmlFile);
      catch (SAXException | IOException e) {
        e.printStackTrace();
    doc.getDocumentElement().normalize();
    NodeList nList = doc.getElementsByTagName("section");
    for (int i = 0; i < nList.getLength(); i++) {
        Node nNode = nList.item(i);
        if (nNode.getNodeType() == Node.ELEMENT_NODE) {
    Element element = (Element) nNode;
             String sectionName = element.getAttribute("name");
             map.put(sectionName, new ArrayList<String>());
            NodeList childList = element.getElementsByTagName("indicator");
             for (int j = 0; j < childList.getLength(); j++) {</pre>
                 Node childNode = childList.item(j);
                 Element cElement = (Element) childNode;
                 String indicatorNameOrigin = cElement.getElementsByTagName("f").item(0).getChildNodes().item(0)
                         .getNodeValue();
                 if (cElement.getElementsByTagName("i").getLength() > 0) {
   String indicatorParaList = cElement.getElementsByTagName("i").item(0).getChildNodes().item(0)
                     .getNodeValue();
String[] indicatorParas = indicatorParaList.split(",");
                     for (String indicatorPara : indicatorParas) {
                          String indicatorName = indicatorNameOrigin.replace("\\i", indicatorPara);
                          map.get(sectionName).add(indicatorName);
                 } else {
                     map.get(sectionName).add(indicatorNameOrigin);
        }
    return map;
```

6. aggregate all indicators( eg. macd, ead ). Aggregate all strategies using optimization framework or selection framework to gain statistical alpha 7. indicator effectiveness test 1. test correlation - the correlation between indicator and profit vs. the correlation between correlation and white noise(hypothesis test) \* use spearman correlation rather than pearson correlation\* 2. Use Monte Carlo Simulation to do permutation test of effectiveness of indicator 3. Very very hard - detect sensentivity to market regime change(osicallation and trend) and identify market regime

#### 11.1. STRATEGY DEVELOPMENT PIPELINE(SINGLE/LINEAR STRATEGY) 63

change.

### 11.1.6.3 Integration of single indicators and portfolio theory

Form indicator as factors: standardization to mean-o, normal/t-distributed scores. Select powerful ones (ones that passed the permutation test). Optimize to maximize holdings exposure to factor with risk penalty. The key is still feature engineering.

$$h'f - ah'Vh$$

h:列向量, portfolio 里各个品种的持仓

f:列向量, expected return

a 常数: risk aversion

V: covariance matrix

' 意思是矩阵转秩

For Covariance, See section "covariance matrix".

#### 11.1.6.4 Strategy Risk Management and Money management

small stop loss, big stop gain level on reversion strategies.bigger stop loss, smaller stop gains on volatile markets - based on experience, market analysis.

Choose symmeteric/non-symmetric risk control based on market belief

Hedging and Market Exposture Management - Volatility Control and Automatic de-leveraging.

together with cost consdieration.

# 11.2 Backtesting

- 1. Surviorship-bias
- 2. Look ahead-bias
- 3. In-sample bias

# Portfolio Risk Management

# 12.1 Key Questions

- Position Sizing: How much to bet per desired asset?
- Vol, Skew and Kurtosis The historical distribution of portfolio returns
- Non-stationarity of Returns: Regime Filtering, Back Testing Results
- Counter-party Risk
- Operation Risk (Trading Infra fails)

# 12.2 Derivatives and Hedging Strategies

Sell Side Risk

Coherent Risk measure

monotonicity

subadditivity

positive homogeneity

translation invariance

liquidity risk

funding liduitdity market liquidity (brokerage fees, execution price compared to mid-point, impact of transaction in the market price, the speed of transaction execution)

evidence that liquidity good: stable quoted bid-ask spread, order book depth deep, falling realized bid-ask spread, evidence for bad liquidity: large trades have more market impact, average trade size fall, increased bifurcation in the corporate bond market( different liquidity preferring on-the-run)

influncers

regulators( e.g. leverage, Volker Rule)

Central bank bank funding channel market functioning channel risk appetite channel

liquidity measures bid-ask spread effective spread Rolls price reversal Corwin and Schultz high-low spread price impact turnover Amihuds measure Markits liquidity score Dealer count Quote depth Imputed round-trip cost

tightness: cost of a round-trip transaction market depth: how much moved by a large order resiliency: length of time for which a lumpy order moves the market away from the equilibrium price adverse price impact slippage( the amount of deterioration in the market price induced by the amount of time it takes to get a trade done)

model validation quantitative)

validation of inputs and parameters(assumptions) model replication benchmarking and hypothetical portfolio testing (with another strategy) backtesting profit and loss distribution stress testing

2. risk management 1. Var - historical, analytical, MC good and bad 2. credit risk exposure (pv only swap has) 3. derivatives 1. futures, hedge, synthetic equity/cash, pre-investing 2. options 1. spread-bull bear, butterfly 2. straddle, collar, box spread(bull, bear spread- risk free rate)

- 3. interest rate swap leveraged floating-rate notes, inverse floater; currency swap 4. swaption payer, receiver use receiver to add/remove callable bond features
- 1. fixed income 1. duration matching 1. requirements 2. vs cashflow matching(tenor offer), contingent immunization, horizon matching 2. index and challenges 1. index vs mutual fund,ETF, synthetic strategies(total return swap, less cash but counterparyt risk) 3. yield curve strategies 1. laddered, bullet, barbell vs level slope curvature 2. barbell vs bullet, condor and butterfly long short at level change, slope change, curvature change, yield volatility change performance and strategy (wing and body) 4. high yield and credit stprad 1. IGB HYB: credit risk, credit migration risk, interest rate risk, liquidity risk 2. access liquidity risk and tail risk 3. emerging market difference

# 12.3 FX risk management

currency management 1. forward price (long/short base currency) 2.
 options- risk reversal, put spread, seagull spread 2. index and benchmark
 capitalization-weighted, price-weighted, equal-weighted index, fundamental-weighted indexes

# Monitoring and Performance Evaluation

# 13.1 Monitoring

1. rebalancing corridor width 2. CPPI/ swaption etc

# 13.2 Performance Analysis

1. Performance Measurement

Measure returns: Time-weighted(TWRR) or money-weighted (MWRR)  $\,$ 

2. Performance Attribution

Key is benchmark

3. Performance Appraisal

Different Performance Measures

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### 13.2.1 Performance Attribution and Style Analysis

Key to do performance attribution and portfolio risk management is the selection of benchmarks (ideally liquid, investable, and reflects style). Common ones like indices, manager's universe, factor model or customized benchmark can be tested by

- Minimal systematic bias: (historical beta of portfolio of benchmark should be close to 1, correlation between P-B and B-M should be zero
- Tracking Error should be minimal
- Exposure to systematic risks should be similar to the portfolio
- Coverage (percent of market value of portfolio) should be maximal
- Turn over should not be excessive
- Active positions should be measurable and positive

#### Performance Attribution

- Macro Performance Attribution: From fund sponsor's perspective.
   Usually from asset class perspective: Policy Allocation +
   benchmark asset return + fund returns, variations, cash flows
- Micro Performance Attribution: To stock/asset level or to factor level (see: style analysis). e.g.

$$r_v = \sum_j (w_{Pj} - w_{Bj})(r_{Bj} - r_B) + \sum_j (w_{Pj} - w_{Bj})(r_{Pj} - r_{Bj}) + \sum_j w_B(r_{Pj} - r_{Bj})$$

• Style Analysis

$$r_p(t) = \sum w_i f_i(t) + u_p(t)$$

Solve quadratic optimization

$$arg min var(u_p(t))$$

$$w_i \geq 0, \sum w_i = 1$$

(notice, not minimize squared error, use t - T period to estimate  $w_i$ , then get the selection return(specific risk)

- Variations include
  - weight change over time, the will cause the solution to be undetermined, need to discourage large movements by regularization.
  - factors usage:

fundamental factor model

sector factor: from return to get exposure

style factor: from exposure (factor loading/factor scores) to get return. (See Factor Models)

macroeconomic factor models(economic factors as GDP,

macroeconomic factor models(economic factors as GDP, rates)

statistical factor models(PCA, Asymptotic PCAs and time varying factors)

• Then decompose the risk with factors: the risk of k-th exposure weighted factor:

$$\sqrt{\frac{1}{T}\sum_{l=1}^{T}(w_k f_k(l) - \overline{w_k f_k})^2}$$

• Bond portfolio performance Attribution: Same spirit but more complicated than equity portfolio: Need to separate

**External Interest Rate Environment** 

returns on default free bonds with no forward rate change return due to the change of forward curves

**Management Process** 

Interest Rate Management Effect: treat as if default free bonds

Sector Quality Effect: sector and quality group

Security Selection: within group selection

Trading Activity: residual

### 13.2.2 Measure Performance

The key purpose is to collect data and do statistical tests on alpha.

Common Performance Measures

ullet Jensen's Alpha (expost  $E(r_p)-E(r_b)$ 

$$r_p(t) = \alpha_p + \beta_P r_B(t) + \epsilon_p(t)$$

t-test on  $\frac{\alpha_P}{SE_{\alpha_P}}$  usually use 2 as a thredhold

Rule of Thumb:

$$IR = \frac{t - stat}{\sqrt{T}}$$

Can be used with a single benchmark, sector or style multi-factor models

• Ratio Measures

Total Risk: Sharpe, M2 Measure

Systematic Risk: Treynor Ratio

Information Ratio:

$$\frac{r_A - r_B}{\sigma_{A/B}}$$

# Alternative Data and General Machine Learning

# E-trading and Execution

Program Trading: Trading a group of instruments, typically cash equities, as single unit (Portfolio Trading or Basket Trading) Commissions from 3bps to 15 bps (2018). Used by active funds, arbitragers (derivatives to cash (eg. Treasury and Treasury Futures)etc)

Hedge Funds use it as part of Stat Arb (typically high volume), Merger Arb, Relative Value, IntraCap Pairs

Execution, Market Impact, VWAP

# Bibliography

[1] Marcos Lopez De Pardo, *Advances in Financial Machine Learning*. Wiley, 1st Edition, 2018