

# Red-Black Tree

## Introduction:

When it comes to searching and sorting data, one of the most fundamental data structures is the binary search tree. However, the performance of a binary search tree is highly dependent on its shape, and in the worst case, it can degenerate into a linear structure with a time complexity of  $O(n)$ . This is where Red Black Trees come in, they are a type of balanced binary search tree that use a specific set of rules to ensure that the tree is always balanced. This balance guarantees that the time complexity for operations such as insertion, deletion, and searching is always  $O(\log n)$ , regardless of the initial shape of the tree.

Red Black Trees are self-balancing, meaning that the tree adjusts itself automatically after each insertion or deletion operation. It uses a simple but powerful mechanism to maintain balance, by coloring each node in the tree either red or black.

## Red Black Tree-

Red-Black tree is a binary search tree in which every node is colored with either red or black. It is a type of self balancing binary search tree. It has a good efficient worst case running time complexity.

## Properties of Red Black Tree:

The Red-Black tree satisfies all the properties of binary search tree in addition to that it satisfies following additional properties –

1. Root property: The root is black.
2. External property: Every leaf (Leaf is a NULL child of a node) is black in Red-Black tree.
3. Internal property: The children of a red node are black. Hence possible parent of red node is a black node.
4. Depth property: All the leaves have the same black depth.
5. Path property: Every simple path from root to descendant leaf node contains same number of black nodes.

The result of all these above-mentioned properties is that the Red-Black tree is roughly balanced.

Rules That Every Red-Black Tree Follows:

1. Every node has a color either red or black.
2. The root of the tree is always black.
3. There are no two adjacent red nodes (A red node cannot have a red parent or red child).
4. Every path from a node (including root) to any of its descendants NULL nodes has the same number of black nodes.
5. Every leaf (e.i. NULL node) must be colored BLACK.

### Applications:

1. Most of the self-balancing BST library functions like map, multiset, and multimap in C++ ( or java packages like java.util.TreeMap and java.util.TreeSet ) use Red-Black Trees.
2. It is used to implement CPU Scheduling Linux. Completely Fair Scheduler uses it.
3. It is also used in the K-mean clustering algorithm in machine learning for reducing time complexity.
4. Moreover, MySQL also uses the Red-Black tree for indexes on tables in order to reduce the searching and insertion time.
5. Red Black Trees are used in the implementation of the virtual memory manager in some operating systems, to keep track of memory pages and their usage.
6. Many programming languages such as Java, C++, and Python have implemented Red Black Trees as a built-in data structure for efficient searching and sorting of data.
7. Red Black Trees are used in the implementation of graph algorithms such as Dijkstra's shortest path algorithm and Prim's minimum spanning tree algorithm.
8. Red Black Trees are used in the implementation of game engines.

### Advantages:

1. Red Black Trees have a guaranteed time complexity of  $O(\log n)$  for basic operations like insertion, deletion, and searching.
2. Red Black Trees are self-balancing.

3. Red Black Trees can be used in a wide range of applications due to their efficient performance and versatility.

4. The mechanism used to maintain balance in Red Black Trees is relatively simple and easy to understand.

#### Disadvantages:

1. Red Black Trees require one extra bit of storage for each node to store the color of the node (red or black).

2. Complexity of Implementation.

3. Although Red Black Trees provide efficient performance for basic operations, they may not be the best choice for certain types of data or specific use cases.