

we can get circumference 1 & 2 as  $(C_1, C_2)$  using the encode signal

if we have  $(n)$  equally spaced holes in the disk then  $(n)$  signals will count as 1 rotation

$$C = \theta_f r_{\text{wheel}}$$

Coming to [Fig 1]

$$C_1 = r \theta_f$$

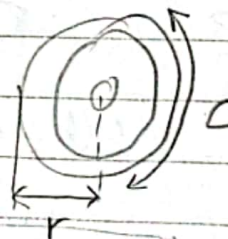
$$C_2 = (r + d_c) \theta_f$$

$$\downarrow [r_1 - r_2 = d_c]$$

$$\frac{C_2}{C_1} = \frac{r + d_c}{r} \Rightarrow r \frac{C_2}{C_1} = r + d_c$$

$$r \left( \frac{C_2}{C_1} - 1 \right) = d_c \Rightarrow r = \frac{d_c}{\left( \frac{C_2}{C_1} - 1 \right)}$$

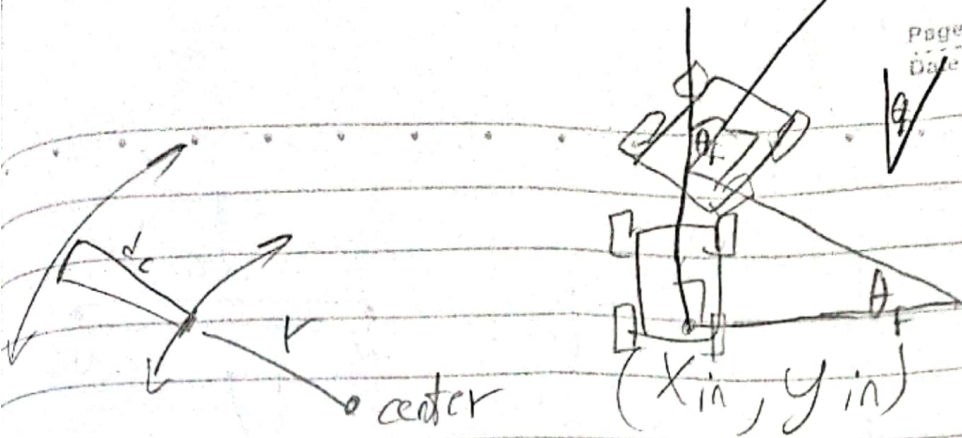
wheel



$$C = r \theta_{\text{rad}}$$

$$\hookrightarrow C = r \frac{n}{N} \times 2\pi$$

Where  $(n)$  is number of signals and  $(N)$  is number of holes per disk



$$r = \frac{d_c}{\frac{c_2}{c_1} - 1}$$

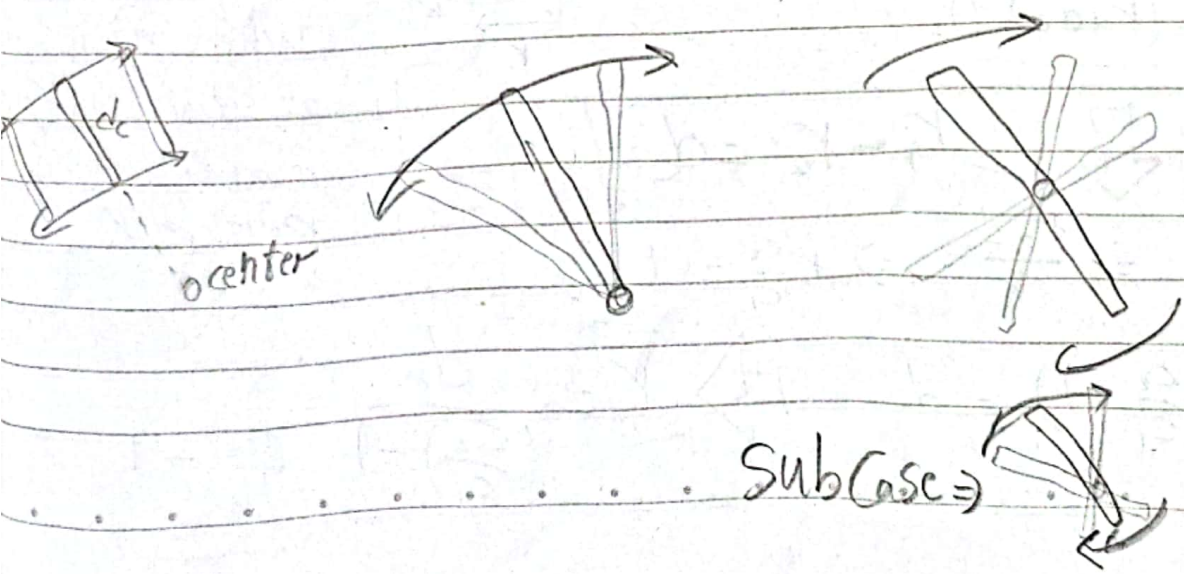
$$\theta_f = \frac{c_2 - c_1}{d_c}$$

$$\theta_{robot} = (\theta_{initial} + \theta_f) \div 360$$

$$X_{robot} = X_{in} + (r + \frac{d_c}{2}) \cos(\theta)$$

$$y_{robot} = y_{in} + (r + \frac{d_c}{2}) \sin(\theta)$$

This equations are applicable on the three expected cases





To adapt the equation  
on the three cases we add  
to  $C$  a coefficient  $d$  to  
detect direction of the motor  
by setting it in the code

$$C = (d) \times r \frac{\pi}{N} \times 2\pi$$

$d$  can be  $\pm 1$

if  $C_1 \approx C_2$  meaning it's moving  
in straight line

$$x_{\text{robot}} = x_{\text{in}} + \frac{C_1 + C_2 \cos(\theta_{\text{robot}})}{2}$$

$$y_{\text{robot}} = y_{\text{in}} + \frac{C_1 + C_2 \sin(\theta_{\text{robot}})}{2}$$