

DATA MINING



Clustering:

Clustering is the process of grouping a set of data objects into multiple groups or clusters so that objects within a cluster have high similarity, but are very dissimilar to objects in other clusters.

Cluster analysis or simply clustering is the process of partitioning a set of data objects (or observations) into subsets. Each subset is a cluster, such that objects in a cluster are similar to one another, yet dissimilar to objects in other clusters.

Different clustering methods may generate different clustering on the same data set.

Clustering is useful in that it can lead to the discovery of previously unknown groups within the data.

Clustering:

Cluster analysis can be used as a standalone tool to gain insight into the distribution of data, to observe the characteristics of each cluster, and to focus on a particular set of clusters for further analysis.

It may serve as a preprocessing step for other algorithms, such as characterization, attribute subset selection, and classification, which would then operate on the detected clusters and the selected attributes or features.

Clustering:

k-means cluster

k-means is one of the simplest unsupervised learning algorithms that solve the well known clustering problem.

The procedure follows a simple and easy way to classify a given data set through a certain number of clusters (assume k clusters)

The main idea is to define k centers, one for each cluster.

These centers should be placed in a cunning way because of different location causes different result.

So, the better choice is to place them as much as possible far away from each other.

The next step is to take each point belonging to a given data set and associate it to the nearest center.

Clustering:

k-means cluster

When no point is pending, the first step is completed and an early group age is done.

At this point we need to re-calculate k new centroids as barycenter of the clusters resulting from the previous step.

After we have these k new centroids, a new binding has to be done between the same data set points and the nearest new center.

A loop has been generated.

As a result of this loop we may notice that the k centers change their location step by step until no more changes are done or in other words centers do not move any more.

Clustering:

k-means cluster

Example:

We have the following 5 points and we want to group them in 2 clusters:

i	X	Y
A	1	1
B	1	0
C	0	2
D	2	4
E	3	5

Clustering:

k-means cluster

Solution:

Choose 2 points to be the center of each cluster (selected Randomly)
“A, C”

Step1: Calculate the distance between each point and the 2 selected point

$$length = \sqrt{(X1 - X2)^2 + (Y1 - Y2)^2}$$

i	A (Cluster 1)	C (Cluster 2)
A	0	1.4
B	1	2.2
C	1.4	0
D	3.2	2.8
E	4.5	4.2

Clustering:

k-means cluster

Compare the distance between each point and the 2 selected groups.
This point will belong to the cluster which has the smallest distance to it

Point B, belong to the Cluster of Point “A” (1 less than 2.2)

Point D, belong to the Cluster of Point “C” (2.8 less than 3.2)

Point E, belong to the Cluster of Point “C” (4.2 less than 4.5)

i	X	Y	Cluster
A	1	1	1
B	1	0	1
C	0	2	2
D	2	4	2
E	3	5	2

Clustering:

k-means cluster

Calculate the mean of Cluster 1:

$$X = (1 + 1) / 2 = 1$$

$$Y = (1 + 0) / 2 = 0.5$$

Mean Cluster1 (1, 0.5)

Calculate the mean of Cluster 2:

$$X = (0 + 2 + 3) / 3 = 1.7$$

$$Y = (2 + 4 + 5) / 3 = 3.7$$

Mean Cluster2 (1.7, 3.7)

Clustering:

k-means cluster

Step2: Recalculate the distance from each point to the cluster means

I	Cluster 1	Cluster 2
A	0.5	2.7
B	0.5	3.7
C	1.8	2.4
D	3.6	0.5
E	4.9	1.9

Compare the distance between each point and the 2 cluster mean. This point will belong to the cluster which has the smallest distance to it

Point A, belong to the Cluster 1 (0.5 less than 2.7)

Point B, belong to the Cluster 1 (0.5 less than 3.7)

Clustering:

k-means cluster

Point C, belong to the Cluster 1 (1.8 less than 2.4)

Point D, belong to the Cluster 2 (0.5 less than 3.6)

Point E, belong to the Cluster 2 (1.9 less than 4.9)

i	X	Y	Cluster
A	1	1	1
B	1	0	1
C	0	2	1
D	2	4	2
E	3	5	2

Clustering:

k-means cluster

Calculate the mean of Cluster 1: (0.7, 1)

Calculate the mean of Cluster 2: (2.5, 4.5)

Step3: Recalculate the distance from each point to the cluster means. In this example we will find no change, so it is the final solution

Clustering:

k-means cluster

Calculate the mean of Cluster 1: (0.7, 1)

Calculate the mean of Cluster 2: (2.5, 4.5)

Step3: Recalculate the distance from each point to the cluster means. In this example we will find no change, so it is the final solution

From the definition of conditional probability,

$$P(A \cap B) = P(A|B)P(B) = P(B|A)P(A)$$

Now, considering the second and last terms in the preceding expression, we can write

$$P(A | B) = \frac{P(B | A)P(A)}{P(B)} \quad \text{for } P(B) > 0$$

Classification:

Naïve Bayes

The Bayes classifier is based on the Bayes theorem for conditional probabilities.

This theorem quantifies the conditional probability of a random variable (class variable), given known observations about the value of another set of random variables (feature variables).

The Bayes theorem is used widely in probability and statistics.

In a Bayesian classifier, the learning agent builds a probabilistic model of the features and uses that model to predict the classification of a new example.

Classification:

Naïve Bayes

Example:

RID	age	Income	student	Credit-rating	Class: buyComputer
1	Youth	High	No	fair	No
2	Youth	High	No	Excellent	No
3	Middle	High	No	Fair	Yes
4	Senior	Medium	No	Fair	Yes
5	Senior	Low	Yes	Fair	Yes
6	Senior	Low	Yes	Excellent	No
7	Middle	Low	Yes	Excellent	Yes
8	Youth	Medium	No	Fair	No
9	Youth	Low	Yes	Fair	Yes
10	Senior	Medium	Yes	Fair	Yes
11	Youth	Medium	Yes	Excellent	Yes
12	Middle	Medium	No	Excellent	Yes
13	Middle	High	Yes	Fair	Yes
14	senior	Medium	no	Excellent	No

Tuple to Classify is:

X(age = youth, income = medium, student = yes, credit = fair), Maximize $P(X|C_i) P(C_i)$

Classification:

Naïve Bayes

Solution:

Step 1: $P(C_i)$

$$\begin{aligned} P(\text{buyComputer} = \text{Yes}) &= \text{number of "Yes"} / \text{Total number} \\ &= 9 / 14 = 0.643 \end{aligned}$$

$$\begin{aligned} P(\text{buyComputer} = \text{No}) &= \text{number of "No"} / \text{Total number} \\ &= 5 / 14 = 0.357 \end{aligned}$$

Step 2: $P(X|C_i)$

Calculate the probability of X for each class, but here I will not going to get the whole X , I will compute the probability of each attribute to each class

$$P(\text{age} = \text{youth} \mid \text{buyComputer} = \text{yes}) = 2 / 9 = 0.222$$

$$P(\text{age} = \text{youth} \mid \text{buyComputer} = \text{no}) = 3 / 5 = 0.600$$

Classification:

Naïve Bayes

Solution:

$$P(\text{income}=\text{medium}|\text{buys_computer}=\text{yes}) = 4 / 9 = 0.444$$

$$P(\text{income}=\text{medium}|\text{buys_computer}=\text{no}) = 2 / 5 = 0.400$$

$$P(\text{student}=\text{yes}|\text{buys_computer}=\text{yes}) = 6 / 9 = 0.667$$

$$P(\text{student}=\text{yes}|\text{buys_computer}=\text{no}) = 1 / 5 = 0.200$$

$$P(\text{credit_rating}=\text{fair}|\text{buys_computer}=\text{yes}) = 6 / 9 = 0.667$$

$$P(\text{credit_rating}=\text{fair}|\text{buys_computer}=\text{no}) = 2 / 5 = 0.400$$

Classification:

Naïve Bayes

Solution:

$$\begin{aligned} P(X \mid \text{buyComputer} = \text{Yes}) &= P(\text{age=youth} \mid \text{buys_computer=yes}) * \\ &P(\text{income=medium} \mid \text{buys_computer=yes}) * \\ &P(\text{student=yes} \mid \text{buys_computer=yes}) * \\ &P(\text{credit_rating=fair} \mid \text{buys_computer=yes}) \\ &= 0.044 \end{aligned}$$

$$\begin{aligned} P(X \mid \text{buyComputer} = \text{No}) &= P(\text{age=youth} \mid \text{buys_computer=No}) * \\ &P(\text{income=medium} \mid \text{buys_computer=No}) * \\ &P(\text{student=yes} \mid \text{buys_computer=No}) * \\ &P(\text{credit_rating=fair} \mid \text{buys_computer=No}) \\ &= 0.019 \end{aligned}$$

Classification:

Naïve Bayes

Solution:

Step 3: $P(X|C_i) P(C_i)$

$$P(X|\text{buys_computer=yes})P(\text{buys_computer=yes}) = 0.044 * 0.643 \\ = 0.028$$

$$P(X|\text{buys_computer=no})P(\text{buys_computer=no}) = 0.019 * 0.357 \\ = 0.007$$

The naïve Bayesian Classifier predicts `buys_computer=yes` for tuple **X**

The **Naïve Bayes classifier** is a probabilistic machine learning model based on **Bayes' Theorem**. It is widely used for classification tasks, especially in text classification, spam filtering, and sentiment analysis. The model is called "naïve" because it makes a strong assumption that all features (variables) are **conditionally independent** of each other given the class label. This assumption simplifies computation but may not always reflect real-world scenarios.

Key Assumptions of the Naïve Bayes Classifier:

1. Conditional Independence:

- It assumes that the value of a feature is independent of the value of any other feature given the class label.
- Mathematically, for features x_1, x_2, \dots, x_n and class C :

$$P(x_1, x_2, \dots, x_n|C) = P(x_1|C) \cdot P(x_2|C) \cdot \dots \cdot P(x_n|C)$$

- This assumption significantly simplifies the computation of joint probabilities.

Implications of These Assumptions:

1. Simplified Computation:

- Because of the independence assumption, the model computes probabilities for each feature separately, making it computationally efficient even for high-dimensional data.

2. Potential Inaccuracy:

- In many real-world problems, features are not truly independent. Despite this, Naïve Bayes often performs well in practice, likely due to its robust handling of probabilities and relative insensitivity to feature dependencies.

3. Scalability:

- The model is scalable to large datasets because of its simplicity and the independence assumption.

Assignment

Example

Given all the previous patients I've seen (below are their symptoms and diagnosis)...

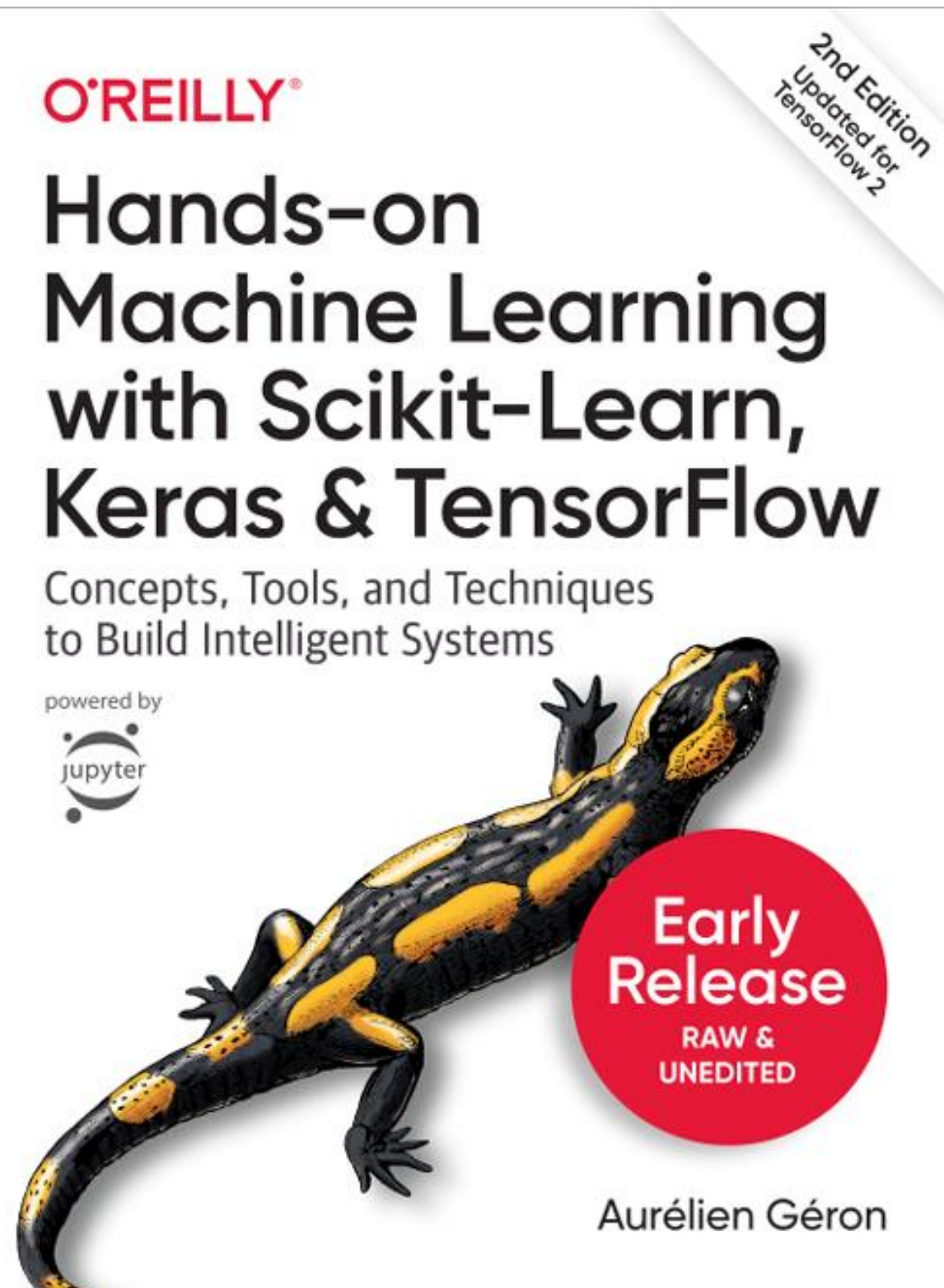
chills	runny nose	headache	fever	flu?
Y	N	Mild	Y	N
Y	Y	No	N	Y
Y	N	Strong	Y	Y
N	Y	Mild	Y	Y
N	N	No	N	N
N	Y	Strong	Y	Y
N	Y	Strong	N	N
Y	Y	Mild	Y	Y

Do I believe that a patient with the following symptoms has the flu?

chills	runny nose	headache	fever	flu?
Y	N	Mild	Y	?

- **Bernoulli Naive Bayes** : It assumes that all our features are binary such that they take only two values. Means 0s can represent “word does not occur in the document” and 1s as "word occurs in the document" .
- **Multinomial Naive Bayes**: It is used when we have discrete data (e.g. movie ratings ranging from 1 to 5 as each rating will have a certain frequency to represent). In text learning we have the count of each word to predict the class or label.
- **Gaussian Naive Bayes** : Because of the assumption of the normal distribution, Gaussian Naive Bayes is used in cases when all our features are continuous. For example in Iris dataset features are sepal width, petal width, sepal length, petal length. So its features can have different values in data set as width and length can vary. We can't represent features in terms of their occurrences. This means data is continuous. Hence we use Gaussian Naive Bayes here

Extra Mile



شرح الكتاب بالعربي فيديو هات

Thank you



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