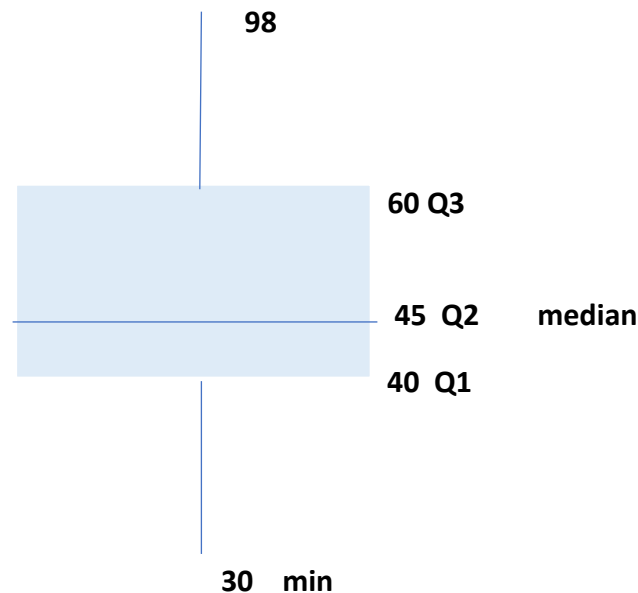


Given the following measures on the Statistics scores for a group of 25 second year's students:

The smallest 3 values	The first quartile	The median	The third quartile	The largest 3 values
30, 33, 37	40	45	60	72, 80, 98

- 1) Draw the Box-Plot.
- 2) Find a measure of central tendency
- 3) Is the value "15" an outlier? Why?
- 4) Determine the direction of the skewness (without calculation).
- 5) Calculate the coefficient of skewness, and comment.
- 6) Is it a difficult exam? Why?

1) Draw the Box-Plot.



2) Measure of Central.

Answer :- The median is 45

3) Checking if "15" is an Outlier

Calculate IQR = $Q_3 - Q_1 = 60 - 40 = 20$

Calculate upper limit = $Q_3 + 1.5 * IQR = 60 + 1.5 * 20 = 90$

Calculate lower limit = $Q_1 - 1.5 * IQR = 40 - 1.5 * 20 = 10$

So 15 is not outlier because $15 > \text{lower limit (10)}$

4) Direction of Skewness (Without Calculation)

the distribution is **right-skewed (positive)** because distance from central to max is larger than distance from min to central .

5) Calculating Coefficient of Skewness

$$\beta = \frac{(Q_3 - Q_2) - (Q_2 - Q_1)}{(Q_3 - Q_1)}$$

$$= (60 - 45) - (45 - 40) / (60 - 40) = 0.5$$

This positive value confirms the right-skewness we observed .

6) is it a difficult exam ? why ?

Yes the exam is difficult .

Because 50 % of students scored $< \text{or} = 45$ and 75 % of students scored $< \text{or} = 60$.

Some Exercises

- (1) What name is given to a table that lists all the values that a discrete random variable X can assume and their corresponding probabilities?
- (2) For the probability distribution of a discrete random variable, the probability of any single value of X is always
- a. In the range 0 to 1 b. 1.0 c. less than zero
- (3) For the probability distribution of a discrete random variable, the sum of the probabilities is always
- (4) The parameters of the binomial probability distribution are and
- (5) The binomial distribution is skewed to the right if $\pi \dots 0.5$
- (6) The parameter/ parameters of the Poisson probability distribution is/ are
- (7) Find the mean and the standard deviation from the following table

x	-4	0	1	2
$P(X = x)$	0.2	0.3	0.3	0.2

- (8) A factory has eight machines. The probability is 0.04 that any machine will break down at any time. Find the probability that at any given time:
- a. All eight machines will be broken down
- b. Exactly two machines will be broken down
- c. None of the machines will be broken down
- (10) A high school boys' basketball team averages 1.2 technical fouls per game. Find the probability that in a given game this team will commit:
- a. Exactly three technical fouls
- b. At least two technical fouls
- c. Find the mean and the standard deviation

1) Probability mass function (pmf).

2) In the range 0 to 1

3) 1

4) **N and P** where **n** is total number of trials and **P** is probability of success.

5) If $\pi < 0.5$, the distribution is skewed to the right.

6) λ (average number of occurrences)

7) Mean of $x = \mu_x = E(X) = \sum X \cdot p(x) =$

$$(-4)(0.2) + (0)(0.3) + (1)(0.3) + (2)(0.2) = -0.8 + 0 + 0.3 + 0.4 = -0.1$$

Calculate Variance :-

x	p(x)	x.p(x)	x².p(x)
-4	0.2	-0.8	3.2
0	0.3	0	0
1	0.3	0.3	0.3
2	0.2	0.4	0.8
total	1	-0.1	4.3

Variance = $4.3 - 0.01 = 4.29$

Standard deviation = 2.07

8)

- a) $P(x=8) = (0.04)^8 = 6.55 \cdot 10^{-12}$
- b) $P(X=2) = 28 \cdot 0.04^2 \cdot 0.96^6 = 0.035$
- c) $P(X=0) = 1 \cdot 0.04^0 \cdot 0.96^8 = 0.721$

10)

a) $\lambda=1.2 \quad P(X=3) = e^{-1.2} \cdot (1.2)^3 / 3! = 0.0867$

b) $P(X \geq 2) = 1 - P(X=0) - P(X=1)$

$$P(X=0) = e^{-1.2} = 0.3012$$

$$P(X=1) = e^{-1.2} \cdot (1.2)^1 = 0.3614$$

$$P(X \geq 2) = 1 - 0.3012 - 0.3614 = 0.3374$$

c) $Mean (\mu) = \lambda = 1.2 = 1.2$

$$Standard\ Deviation (\sigma) = \lambda^{1/2} = 1.2^{1/2} = 1.095$$