

Earlist Deadline First
Project

Calculating CPU Utilization for the following Tasks to Prove Schedulability:

Button_1(P: 50, D: 50, E: 2)

Button_2(P: 50, D: 50, E: 2)

Period_Transmission(P: 100, D: 100, E: 2)

Uart_Receive(P: 20, D: 20, E: 1.2)

$$U = \sum_{i=1}^n \frac{C_i}{P_i} \leq n \left(2^{\frac{1}{n}} - 1 \right) \quad U = \text{Total Utilization},$$

*n = number of Tasks, C = Execution time,
P = hyper Period*

$$U = \left(\frac{2 * 2}{100} \right) + \left(\frac{2 * 2}{100} \right) + \left(\frac{2}{100} \right) + \left(\frac{5 * 1.2}{100} \right) = 0.16$$

$$URM = 4 * \left(2^{\frac{1}{4}} - 1 \right) = 0.76 \quad URM = \text{Rate Monotonic Utilization}$$

$$\therefore U \leq URM$$

\therefore The System is Schedulable for Fixed Priority Task with Only 4 Tasks

Now to recalculate using Time Demand Analysis for The 4 main Tasks:

for (Task 4):

$$w(1) = 1.2 + 0 = 1.2$$

$$w(2) = 1.2 + 0 = 1.2$$

$$w(3) = 1.2 + 0 = 1.2$$

$$w(4) = 1.2 + 0 = 1.2$$

$$w(5) = 1.2 + 0 = 1.2$$

$$w(6) = 1.2 + 0 = 1.2$$

$$w(7) = 1.2 + 0 = 1.2$$

$$w(8) = 1.2 + 0 = 1.2$$

$$w(9) = 1.2 + 0 = 1.2$$

$$w(10) = 1.2 + 0 = 1.2 \text{ till } w(20) = 1.2 + 0 = 1.2$$

$$w(20) < D = 1.2 < 20, \quad \therefore T4 \text{ is schedulable}$$

now tasks (1) and (2) are going to enter:

$$w(1) = 2 + 2 + (1.2 * 1) = 5.2$$

$$\text{till } w(20) = 2 + 2 + (1.2 * 1) = 5.2$$

$$\text{from } w(21) \text{ till } w(40) = 2 + 2 + (1.2 * 2) = 6.4$$

$$\text{from } w(41) \text{ till } w(50) = 2 + 2 + (1.2 * 3) = 7.6 < D = 20$$

$\therefore T1$ and $T2$ are schedulable

Now to add the last task ($T3$):

$$w(1) \text{ till } w(20) = 5.2 + 2 = 7.2$$

$$\text{from } w(21) \text{ till } w(40) = 6.4 + 2 = 8.4$$

$$\text{from } w(41) \text{ till } w(50) = 7.6 + 2 = 9.6$$

$$\text{from } w(51) \text{ till } w(60) = 2 + (2 * 2) + (2 * 2) + (1.2 * 3) = 13.6$$

$$\text{from } w(61) \text{ till } w(80) = 2 + (2 * 2) + (2 * 2) + (1.2 * 4) = 14.8$$

$$\text{from } w(81) \text{ till } w(100) = 2 + (2 * 2) + (2 * 2) + (1.2 * 5) = 16 < D$$

$= 100, \therefore T3$ is Schedulable.

Now to recalculate using Time Demand Analysis for The 6 Tasks with system load:

for (Task 5):

$$w(1) = 5 + 0 = 5$$

$$w(2) = 5 + 0 = 5$$

$$w(3) = 5 + 0 = 5$$

$$w(4) = 5 + 0 = 5$$

$$w(5) = 5 + 0 = 5$$

$$w(6) = 5 + 0 = 5$$

$$w(7) = 5 + 0 = 5$$

$$w(8) = 5 + 0 = 5$$

$$w(9) = 5 + 0 = 5$$

$$w(10) = 5 + 0 = 5 < D = 10 \therefore T5 \text{ is Schedulable}$$

for (Task 4):

$$w(1) = 1.2 + 5 = 6.2$$

$$w(2) = 1.2 + 5 = 6.2$$

$$w(3) = 1.2 + 5 = 6.2$$

$$w(4) = 1.2 + 5 = 6.2$$

$$w(5) = 1.2 + 5 = 6.2$$

$$w(6) = 1.2 + 5 = 6.2$$

$$w(7) = 1.2 + 5 = 6.2$$

$$w(8) = 1.2 + 5 = 6.2$$

$$w(9) = 1.2 + 5 = 6.2$$

$$w(10) = 1.2 + 5 = 6.2$$

$$\text{from } w(11) \text{ till } w(20) = 1.2 + (5 * 2) = 11.2$$

$$w(20) < D = 11.2 < 20, \quad \therefore T4 \text{ is schedulable}$$

now tasks (1) and (2) are going to enter:

$$w(1) = 2 + 2 + (1.2 * 1) + (5 * 1) = 10.2$$

$$\text{till } w(10) = 2 + 2 + (1.2 * 1) + (5 * 1) = 10.2$$

$$\text{from } w(11) \text{ till } w(20) = 2 + 2 + (1.2 * 1) + (5 * 2) = 15.2$$

$$\text{from } w(21) \text{ till } w(30) = 2 + 2 + (1.2 * 2) + (5 * 3) = 21.4$$

$$\text{from } w(31) \text{ till } w(40) = 2 + 2 + (1.2 * 2) + (5 * 4) = 26.4$$

$$\text{from } w(41) \text{ till } w(50) = 2 + 2 + (1.2 * 3) + (5 * 5) = 32.6 < D = 50,$$

$$\therefore T1 \text{ and } T2 \text{ are schedulable}$$

Now to add the task (T3) & (T6):

$$\begin{aligned} \text{from } w(51) \text{ till } w(60) &= 2 + (2 * 2) + (2 * 2) + (1.2 * 3) + (5 * 6) + 12 \\ &= 55.6 \end{aligned}$$

$$\begin{aligned} \text{from } w(61) \text{ till } w(70) \\ &= 2 + (2 * 2) + (2 * 2) + (1.2 * 4) + (5 * 7) + 12 = 61.8 \end{aligned}$$

$$\begin{aligned} \text{from } w(71) \text{ till } w(80) \\ &= 2 + (2 * 2) + (2 * 2) + (1.2 * 4) + (5 * 8) + 12 = 66.8 \end{aligned}$$

$$\begin{aligned} \text{from } w(81) \text{ till } w(90) \\ &= 2 + (2 * 2) + (2 * 2) + (1.2 * 5) + (5 * 9) + 12 = 73 \end{aligned}$$

$$\begin{aligned} \text{from } w(91) \text{ till } w(100) \\ &= 2 + (2 * 2) + (2 * 2) + (1.2 * 5) + (5 * 10) + 12 = 78 \end{aligned}$$

$$< D = 100, \therefore T3 \text{ and } T6 \text{ are Schedulable.}$$

\therefore Based on time Demand Analysis the System is fully Schedulable.

Figure (1) shows the Schedulable System, while Figure (2) will show the System is going to be not Schedulable when it comes to Fixed Priority.

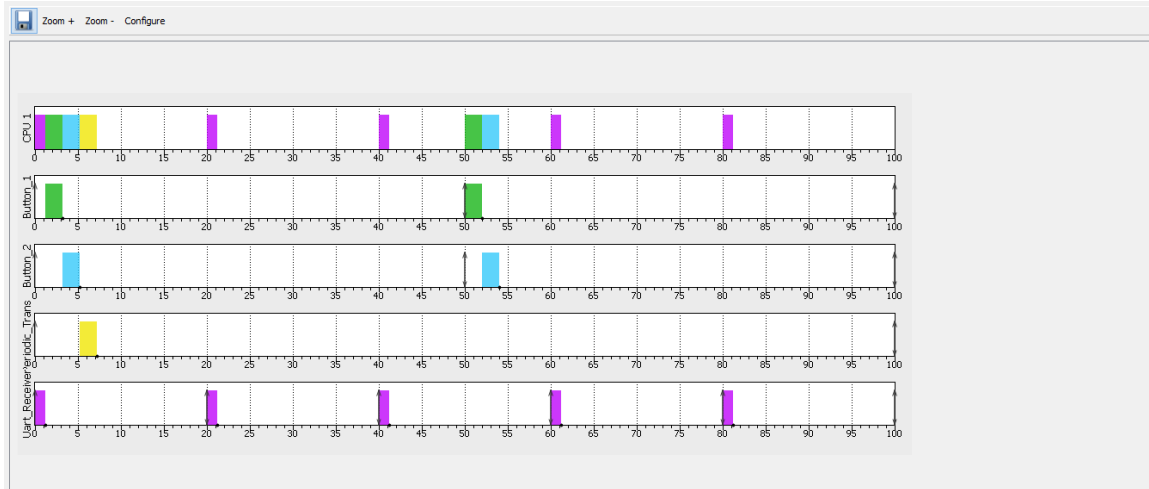


Figure (1) Rate Monotonic Schedulability for the 4 Main Tasks

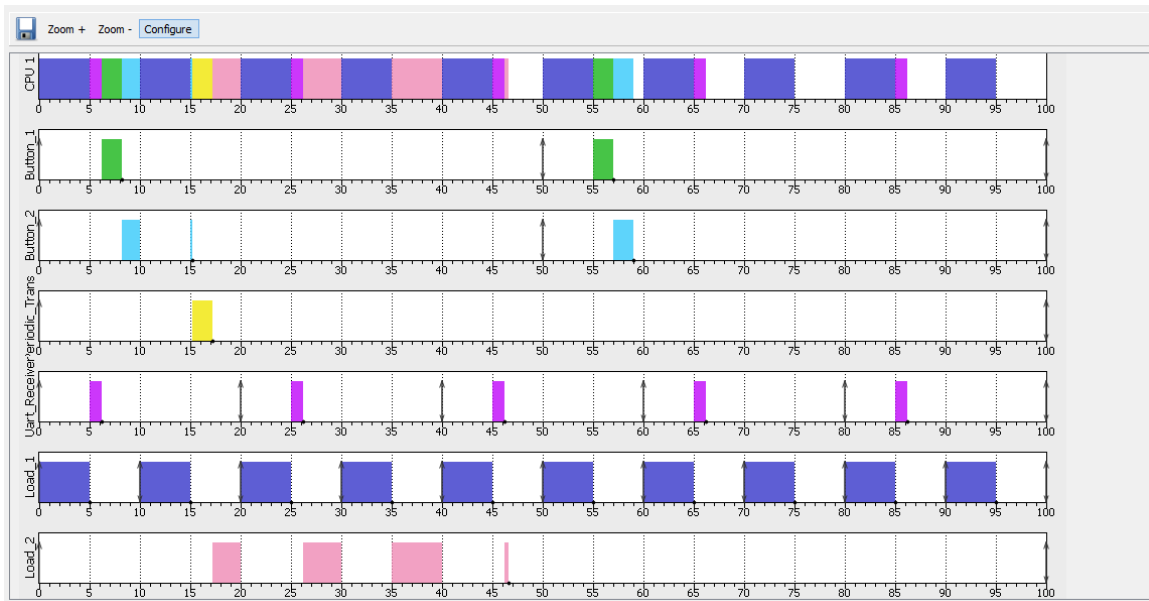


Figure (2) Rate-monotonic with all 6 Tasks added to CPU Load

The Following Figure is showing the Behavior of the system based on Events as follows:

Using Logic Analyzer:

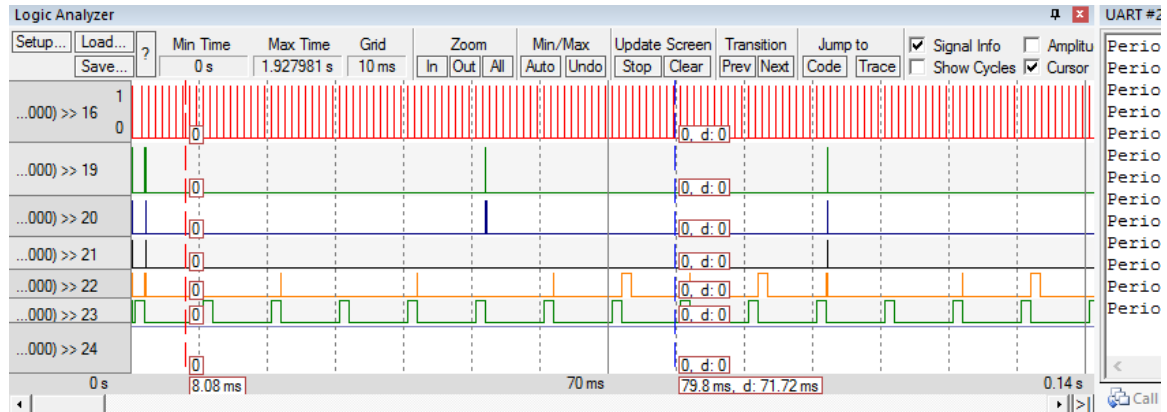


Figure (3) Logic Analyzer showing the behavior of the System with both load Functions sequentially