

Frames

GPS → Map : $? - \text{originPos} + \text{size}(\text{map})/2$

Map → GPS : $? + \text{originPos} - \text{size}(\text{map})/2$

yourbot → GPS : $\text{rotationMatrix} \times ? + \text{yourbotPos}$

GPS → yourbot : $\text{rotationMatrix}^{-1} \times (? - \text{yourbotPos})$

Init

X Y cell/1m

- map = Occupancy Grid (50, 50, 5): non binary / based on probabilities

→ $0 \leq p < 0.5$: free

→ $p = 0.5$: unknown

→ $0.5 < p \leq 1$: occupied

↳ inflate(map) increase obstacles size

controller = Pure Pursuit (GPS frame)

↳ Linear Velocity = 1 m/s

↳ Max Angular Velocity = 1 rad/s

↳ Look ahead Distance = 1 m



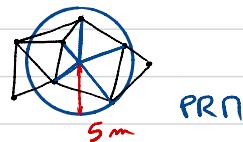
prm = PRN (map frame)

↳ Num Nodes = 50

↳ Connection Distance = 5m

↳ Nav = inflate(copy(map), yobot_radius)

⇒ increase obstacles size of yobot radius



PRN

Mapping

- Map is considered of unknown size and our original position in the whole map is considered unknown.

⇒ Large enough map \oplus original position in the middle of our map

⇒ w/ GetObjectPosition: get GPS original value to have a reference
w/ " Orientation: get orientation " "

⇒ original pose is placed in center of map

⇒ pose_{map} = GetObjectPosition - originalPos + size(map)/2
Dpose with reference

- Hokuyo sensor \Rightarrow ray end points to \oplus points in contact with an obstacle

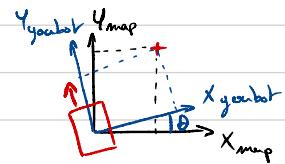
- $3 \times N$ matrix expressed in robot frame
 \Rightarrow need to express in map frame coordinates

$$\left. \begin{array}{l} X_{map} = X_{youbot} \cdot \cos \theta - Y_{youbot} \cdot \sin \theta \\ Y_{map} = Y_{youbot} \cdot \cos \theta + X_{youbot} \cdot \sin \theta \end{array} \right\} + \underbrace{\text{youbotPos} - \text{originPos} + \text{rigidMap}}_{\text{Dpose}} / 12$$

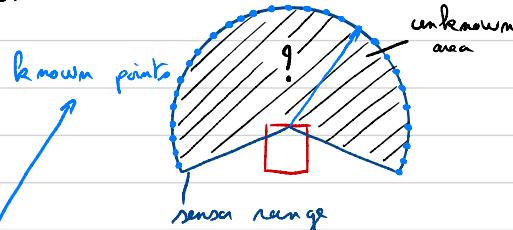
non rotated youbot frame
currentPos

$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}_{\text{map}} = \begin{pmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \end{pmatrix} + \text{goalPos} - \text{originPos} + \text{angle}(\text{map})/2$$

rotation matrix



- only ray end points: unknown points between
 - \Rightarrow OccupancyGrid.insertRay
 - \oplus " . update Occupancy



insertRay(map , $\text{yourbotPos}_{\text{map}}$, $\text{rayEndpoints}_{\text{map}}$, valued)

`values = [0.3 0.5] : mid points and end points
probabilities`

0.5 because end points not necessarily obstacles

$\Rightarrow \text{updateOccupancy}(\text{map}, [\text{navigationMatrix}^* \text{pts}(1:2, \underbrace{\text{contacts}}_{\substack{\text{xyz} \\ \text{logical matrix}}})]^\top + \text{goalbotPos}_{\text{map}})$

very End points map down sampled to increase performances

less endpoints is not problematic because the map is rough compensates number of points w/ large number of map updates

Navigation

- inflatedMap = copy(map) then inflate(map, robotRadius)
to avoid obstacles during navigation

- Choose point of interest to navigate to
 - mesh grid around yourbot
 - not too far nor too close ($3 < d < 4$)

$$R = \text{hypot}(x, y)$$

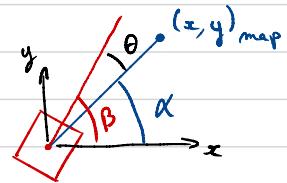
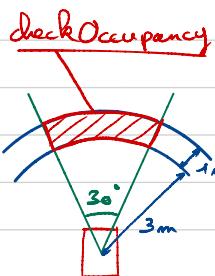
- in front of yourbot (30°)

$$\theta = \text{atan2}(x - y) - \text{yourbotEuler}_z$$

$x - y$ because VREP 0° is $1 - z$

- handle already visited places } how?

- privilege corners } not implemented yet



check conditions on each combinations of x and y

=> convert $(x, y)_{\text{map}}$ coordinates to grid coordinates to remove duplicates

=> checkOccupancy(map, cells, 'grid')

=> get only free cells coordinates

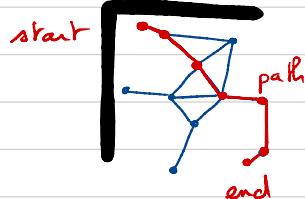
=> convert to map (x, y) then to GPS: gridToWorld(mapping, targetGridCell)

targetGridCell random free cell, no algorithm to choose particular path

D If no point found: can't increase max distance because of sensor max range. So increase front angle by 10° each time

■ Update Probability Roadmap

- pass inflated map to PRN $\Rightarrow \begin{bmatrix} \text{start} \\ \vdots \\ \text{end} \end{bmatrix}$
- update nodes
- findpath



① If no path found, add 10 nodes and update PRN

→ get path coordinates in GPS frame

$$\text{path} = \text{path} - \text{size}(\text{map})/2 + \text{originPos} \quad \text{map} \rightarrow \text{GPS}$$

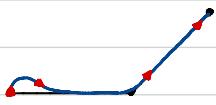
→ set path to controller

→ push each points in FIFO list to get current intermediate target

Driving

- If we have path registered and encounter goal while driving: repath
- Each time we reach an intermediate point (radius 0.2 ~ 0.3)
 - if FIFO list is nearly empty: clear and repath
 - else, pop top and set current target as front object

To drive, we use Pure Pursuit controller which provides linear and angular velocity when passing current position and orientation



Base behavior



Wanted behavior

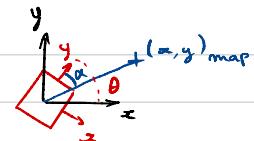
Youbot has omnidirectional wheels so it can move sideways
 \hookrightarrow compose speed

\Rightarrow get angle between front axis and target
 \hookrightarrow get target position in youbot frame

GPS \rightarrow youbot

$$(x, y)_{\text{youbot}} = \text{rotationMatrix}^{-1} [(x, y)_{\text{GPS}} - \text{youbotPos}_{\text{GPS}}]$$

$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}_{\text{youbot}} = \underbrace{\begin{pmatrix} \cos \theta & \sin \theta & 0 \\ -\sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{rotationMatrix}^{-1}} \begin{pmatrix} X \\ Y \\ Z \end{pmatrix}_{\text{GPS}} - \text{youbotPos}_{\text{GPS}}$$



$$(X \ Y \ Z)_{\text{youbot}} = [(X \ Y \ Z)_{\text{GPS}} - \text{youbotPos}_{\text{GPS}}] \underbrace{\begin{pmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{(\text{rotationMatrix}')^{-1}}$$

front and back inverted

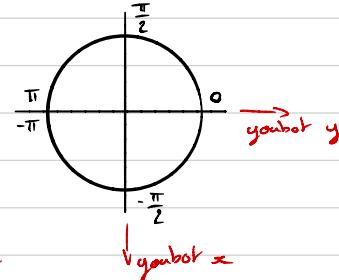
$$\Rightarrow \theta' = \theta + \pi \Rightarrow \text{pos}'_{\text{youbot}} = -\text{pos}_{\text{youbot}}$$

\Rightarrow angle between youbot front axis and target

$$\alpha = \arctan 2(-x, y)$$

\Rightarrow compute target rotation matrix

$$\text{TargetRMatrix} = \begin{bmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{bmatrix} \left. \begin{array}{l} \text{because multiply} \\ \text{line matrix} \end{array} \right.$$



robot velocity: $[v \ 0] \rightarrow [v \cdot \cos \alpha \ v \cdot \sin \alpha]$

$$\Rightarrow \text{youbot_drive}(\underbrace{\text{robotVel}(1), \text{robotVel}(2)}_{\text{because youbot motors are reversed}}, \text{rotateVel})$$