

ZEWAIL CITY OF SCIENCE AND TECHNOLOGY

MINI-PROJECT 1 - CIE552

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## Instructions

- 4 questions.
- Write code where appropriate.
- Feel free to include images or equations.

## Questions

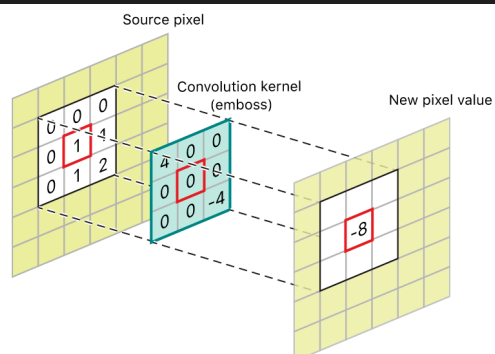
**Q1:** Explicitly describe image convolution: the input, the transformation, and the output. Why is it useful for computer vision?

**A1:**

- Input: image and kernel of the filter.
- Transformation: padding the image to get the same size at the end or the image will shrink.
- Output: the filtered image .

$$g(i, j) = \sum_k^K \sum_l^L I(i + k, j + l) * h(k, l)$$

- $I(x, y)$  is the image intensity at the pixel of coordinates  $(x, y)$
- $h(k, l)$  is the filter used which is called *kernel*
- $K$  is the kernel length
- $L$  is the kernel width
- $i, j$  is the *anchor*, the pixel that we are calculating the correlation for



**Q2:** What is the difference between convolution and correlation? Construct a scenario which produces a different output between both operations.

Please use `scipy.ndimage.convolve` and `scipy.ndimage.correlate` to experiment!

**A2:** The main difference between convolution and correlation is the flip of the filter. So, in case of symmetric filters, there is no difference between them.

symmetric kernel , the same results

```
from scipy import ndimage
c = np.array([[2, 0, 1],
              [1, 0, 0],
              [0, 0, 0]])
k = np.array([[0, 1, 0],
              [0, 1, 0],
              [0, 1, 0],
              [0, 1, 0],
              [0, 1, 0]])
ndimage.convolve(c, k, mode='nearest')

array([[7, 0, 3],
       [5, 0, 2],
       [3, 0, 1]])

[134] ndimage.correlate(c,k,mode='nearest')

array([[7, 0, 3],
       [5, 0, 2],
       [3, 0, 1]])
```

non symmetric kernel by changing one number, different results

```
c = np.array([[2, 0, 1],
              [1, 0, 0],
              [0, 0, 0]])
k = np.array([[0, 1, 0],
              [0, 1, 0],
              [3, 1, 0],
              [0, 1, 0],
              [0, 1, 0]])
ndimage.convolve(c, k, mode='nearest')

array([[7, 3, 6],
       [5, 0, 2],
       [3, 0, 1]])

[136] ndimage.correlate(c,k,mode='nearest')

array([[13, 6, 3],
       [ 8, 3, 2],
       [ 3, 0, 1]])
```

**Q3:** What is the difference between a high pass filter and a low pass filter in how they are constructed, and what they do to the image? Please provide example kernels and output images.

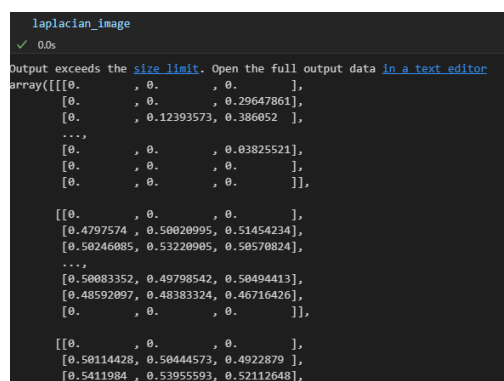
**A3:**

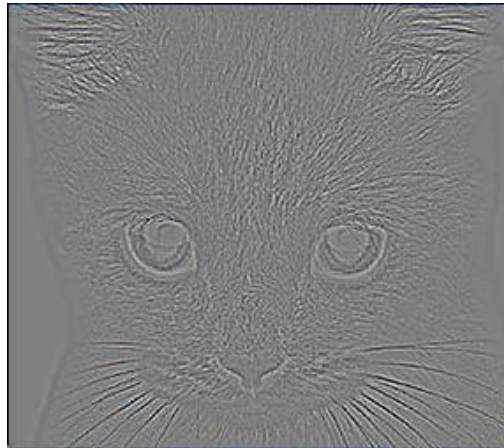
- High pass filter : neglect the low frequencies in the image and preserve the high frequencies which means the sudden changes like edges.
- Low pass filter: the opposite of high pass, it preserve the low frequencies and neglect the sudden transitions. So, it blur the image in most of the cases

Low pass filter



High pass filter

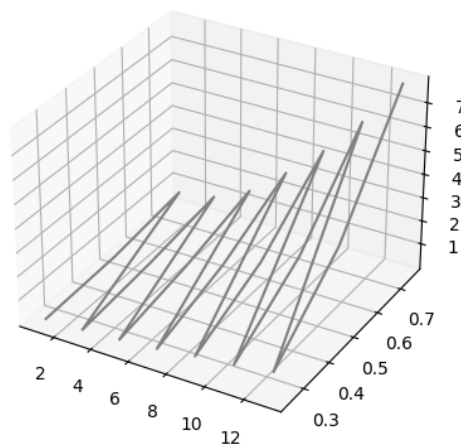




**Q4:** How does computation time vary with filter sizes from  $3 \times 3$  to  $15 \times 15$  (for all odd and square sizes), and with image sizes from 0.25 MPix to 8 MPix (choose your own intervals)? Measure both using `scipy.ndimage.convolve` or `scipy.ndimage.correlate` to produce a matrix of values. Use the `skimage.transform` module to vary the size of an image. Use an appropriate charting function to plot your matrix of results, such as `Axes3D.scatter` or `Axes3D.plot_surface`. Do the results match your expectation given the number of multiply and add operations in convolution? Image: [RISDance.jpg](#) (in the project directory).

**A4:** Increasing the kernel size increases the time and scaling the image also increases the time. Yes, this agrees with our expectations to convolution which is directly proportion to  $N \times M$  which the kernel size and image dimension.

The time on the z axis - scale and kernel size on the x-y axes with correlation2d function



The time on the z axis - scale on the x-y axes using my filter

