ALGORITHMS TASK

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Task Number 7 K-th Element of Two Sorted Arrays

NAMES

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Introduction

Problem Statement

Given two sorted arrays of sizes m and n, find the element that would be at the k-th position in their merged sorted array.

Examples:

Input:

Array 1 =
$$[2, 3, 6, 7, 9]$$

Array2 = $[1, 4, 8, 10]$
 $k = 5$

Output: 6 (Merged array: [1, 2, 3, 4, 6, 7, 8, 9, 10])







PROBLEMS SOLUTION

Solution 1

NON-RECURSIVE APPROACH

Solution 2

Merge Sort (RECURSIVE APPROACH)

Solution 3

Bubble Sort (RECURSIVE APPROACH)

Solution 4

Insertion Sort (RECURSIVE APPROACH)





NON-RECURSIVE APPROACH



```
function NonRec_Fun(arr1, size1, arr2, size2, k):
   i \leftarrow 0, j \leftarrow 0, count \leftarrow 0
    while i < size1 and j < size2:
        if arr1[i] < arr2[j]:</pre>
             element ← arr1[i]
             i \leftarrow i + 1
        else:
             element ← arr2[j]
             j \leftarrow j + 1
         count ← count + 1
        if count == k:
             return element
    while i ≺ size1:
        element ← arr1[i]
        i \leftarrow i + 1
        count ← count + 1
        if count == k:
             return element
    while j < size2:
        element ← arr2[j]
        j ← j + 1
        count ← count + 1
        if count == k:
             return element
    return -1 // k is out of bounds
```





92 Source code

→ GitHub Link:

O3 Sample of output

```
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Projects Files FSy
                            #include <iostream>

    ₩orkspace

                           using namespace std;
 - - Algo
                           const int MAX SIZE = 1000;
 int Non! 🖾 C:\Users\dell\Downloads\Alga × + v
                                    Enter the size of Array 1: 5
Enter the elements of Array 1 'sorted':
                      10
                      11
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                                    Enter the size of Array 2: 4
Enter the elements of Array 2 'sorted':
                      14
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                                    Enter k position: 5
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                                whire The 5-th element in the merged array is: 6
                      21
                     23
                                    Process returned 0 (0x0) execution time : 27.543 \text{ s}
                                    Press any key to continue.
```





O4 Time Complexity

O(n)

O5 Space Complexity

0(1)





Observed Advantages

- 1- Simple and straightforward implementation
- 2- Easy to understand and verify correctness
- 3- No additional memory allocation needed
- 4- Handles edge cases well (empty arrays, k out of bounds)

O7 Disadvantages

- 1- Not optimal for large arrays when k is large
- 2- Linear time complexity could be improved with a binary search approach







Functionality:

NonRec_Fun: A non-recursive function to merge two sorted arrays into a single sorted array. It uses a while loop to iterate through both arrays and merge them. main: Takes two sorted arrays as input, merges them using NonRec_Fun, and returns the k-th smallest element from the merged array.

Key Steps:

- 1- Input: Reads two sorted arrays (arr_1 and arr_2) and an integer k.
- 2- Merge: Combines the two arrays into sortedArr using NonRec_Fun, maintaining the sorted order.
 - 3- Output: Prints the k-th smallest element from the merged array





Merge Sort (RECURSIVE APPROACH)



```
function mergeRecursive(arr1, size1, arr2, size2, merged, i = 0, j = 0, k = 0):
    if i == size1 AND j == size2: // Base case: both arrays fully processed
        return
   if i == size1: // arr1 exhausted, take from arr2
       merged[k] = arr2[j]
        mergeRecursive(arr1, size1, arr2, size2, merged, i, j + 1, k + 1)
   else if j == size2: // arr2 exhausted, take from arr1
       merged[k] = arr1[i]
        mergeRecursive(arr1, size1, arr2, size2, merged, i + 1, j, k + 1)
   else if arr1[i] < arr2[j]: // arr1 has smaller element
        merged[k] = arr1[i]
        mergeRecursive(arr1, size1, arr2, size2, merged, i + 1, j, k + 1)
   else: // arr2 has smaller or equal element
        merged[k] = arr2[j]
       mergeRecursive(arr1, size1, arr2, size2, merged, i, j + 1, k + 1)
```





92 Source code

→ GitHub Link:

O3 Sample of output

```
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                              Management × ☐ main[1].cpp X
                    1 #include <iostream>

    ₩orkspace

                        using namespace std;
Algo
 ■ Sources
                    4 □void mergeRecursive(int arr1[], int size1, int arr2[], int size2,
                                          int merged[], int i = 0, int j = 0, int k = 0) {
                            // Base case
                           if (i == sizel && j == size2) {
                               return;
                              © C:\Users\dell\Downloads\Alga × + v
                   11
12
                              Enter the size of Array 1: 5
                              Enter the elements of Array 1 'sorted':
                   13
14
15
                   16
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18
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22
23
                              Enter the size of Array 2: 4
                              Enter the elements of Array 2 'sorted':
                             Enter k position: 5
                              The 5-th element in the merged array is: 6
```





04 Time Complexity

Best Case: O(m+n) - When all elements need to be processed

Average Case: O(m+n)

Worst Case: O(m+n)

5 Space Complexity

O(m+n) for the merged array
O(m+n) for recursion stack in worst case
(though tail recursion optimization may reduce this)



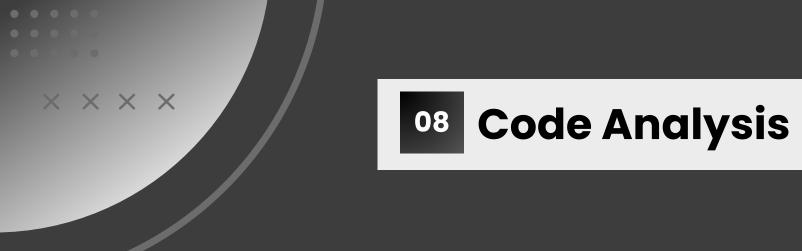


- 1- Simple recursive implementation
- 2-Clearly demonstrates the divide-and-conquer approach
- 3- No need for explicit loop management

O7 Disadvantages

- 1- Recursion overhead for large arrays
- 2- Potential stack overflow for very large arrays
- 3- Slightly more difficult to understand than iterative version







Functionality:

mergeRecursive: A recursive function to merge two sorted arrays into a single sorted array. It compares elements from both arrays and places the smaller one into the merged array. main: Takes two sorted arrays as input, merges them using mergeRecursive, and returns the k-th smallest element from the merged array.

Key Steps:

- 1- Input: Reads two sorted arrays (A and B) and an integer k.
- 2- Merge: Combines the two arrays into mergedArr using mergeRecursive, maintaining the sorted order.
 - 3- Output: Prints the k-th smallest element from the merged array.





1. Pseudo-code

Bubble Sort (RECURSIVE APPROACH)

```
function bubbleSortRec(arr, n):
    if n == 1:
        return

// Perform one full pass of bubble sort
    for i from 0 to n - 2:
    if arr[i] > arr[i + 1]:
        swap(arr[i], arr[i + 1])

// Recurse on the remaining array
bubbleSortRec(arr, n - 1)
end function
```





O2 Source code

→ GitHub Link:

O3 Sample of output

```
Projects Files FSy
                                                                                                          1 #include <iostream>
using namespace std;
                                                                                                                             const int MAX_SIZE = 1000;
                                                                                                                       pvoid bubbleSortRec(int arr[], int n) {
                                                                                                                                              if (n == 1) return;
                                                                                                                                                 for (int i = 0; i < n - 1; i++) {
                                                                                                                                                                 © C:\Users\dell\Downloads\Alga × + v
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Enter the elements of Array 1 'sorted':
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                                                                                                                                                            Enter the elements of Array 2 'sorted':
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                                                                               (x86)\Microsoft SQL Se:\Launcher;C:\U3ers\dell\\Process returned 0 (0x0) execution time : 15.850 s\U3ers\dell\AppBatalor\\Press any key to continue.
```





O4 Time Complexity

Worst-case: O(n²) - When the array is sorted in reverse order

Best-case: O(n) - When the array is already sorted (with optimized version)

Average-case: O(n²)

O5 Space Complexity

O(n)





- 1- Simple to understand and implement
- 2- Stable sorting algorithm
- 3- In-place sorting

O7 Disadvantages

- 1- Consistently poor performance (even on sorted input)
- 2- No practical advantages over other sorts
- 3- Recursion provides no benefit over iterative version
- 4- Least efficient of all four approaches









Functionality:

bubbleSortRec: A recursive implementation of the bubble sort algorithm. It sorts an array by repeatedly swapping adjacent elements if they are in the wrong order.

mergeArrays: Merges two arrays into a single array by concatenating them.

main: Takes two sorted arrays as input, merges them, sorts the merged array using bubbleSortRec, and returns the k-th smallest element.

Key Steps:

- 1- Input: Reads two sorted arrays (arr_1 and arr_2) and an integer k.
- 2- Merge: Combines the two arrays into sortedArr using mergeArrays.
 - 3- Sort: Sorts the merged array recursively using bubbleSortRec.
 - 4- Output: Prints the k-th smallest element from the sorted array.





insertion sort (RECURSIVE APPROACH)



```
function insertionSortRec(arr, n):
         if n <= 1:
             return
         insertionSortRec(arr, n-1) // Sort first n-1 elements
         last = arr[n-1]
                                     // Last element to be inserted
         j = n - 2
         while j \ge 0 and arr[j] > last:
10 🗸
             arr[j + 1] = arr[j]
11
             j = j - 1
12
13
         arr[j + 1] = last
14
     end function
15
16
```





92 Source code

→ GitHub Link:

O3 Sample of output

```
1 #include <iostream>

    Workspace

                        using namespace std;
- Algo
 const int MAX SIZE = 1000;
                       void insertionSortRec(int arr[], int n) {
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Enter the elements of Array 1 'sorted':
                               Enter the size of Array 2: 4
Enter the elements of Array 2 'sorted':
                                 Enter k position: 5
                                The 5-th element in the merged array is: 6
               \Users\dell\AppData\Local\
Executing: "D:\CodeBlocks/
```





O4 Time Complexity

Worst-case: O(n²) - When the array is sorted in reverse order Best-case: O(n) - When the array is already sorted Average-case: O(n²)

O5 Space Complexity

O(n)





- 1- Efficient for small or nearly-sorted arrays
- 2- Stable algorithm (preserves order of equal elements)
- 3- In-place sorting (no additional space needed beyond recursion stack)

O7 Disadvantages

- 1- Quadratic time makes it impractical for large arrays
- 2- Poor performance on reverse-sorted input
- 3- Recursion adds unnecessary overhead vs iterative version









Functionality:

insertionSortRec: A recursive implementation of the insertion sort algorithm. It sorts an array by iteratively placing each element in its correct position within the already sorted part of the array. mergeArrays: Merges two arrays into a single array by concatenating them. main: Takes two sorted arrays as input, merges them, sorts the merged array using insertionSortRec, and returns the k-th smallest element.

Key Steps:

- 1- Input: Reads two sorted arrays (arr_1 and arr_2) and an integer k.
- 2- Merge: Combines the two arrays into sortedArr using mergeArrays.
 - 3- Sort: Sorts the merged array recursively using insertionSortRec.
 - 4- Output: Prints the k-th smallest element from the sorted array.



PERFORMANCE COMPARISON



Algorithm

Time Complexity

Space Complexity

Best For

Non-recursive Merge

O(n)

O(1)

Large sorted arrays

Recursive Merge

O(n+m)

O(n+m) Medium sorted arrays

Recursive Insertion Sort

 $O(n^2)$

O(n)

Small arrays

Recursive Bubble Sort

 $O(n^2)$

O(n)

Educational purposes





Conclusion

The comparison clearly shows that when merging two already sorted arrays, the merge approaches (especially the non-recursive one) are vastly superior to the sorting approaches. The sorting approaches become useful only when the input arrays aren't guaranteed to be sorted, though even then more efficient sorting algorithms than insertion or bubble sort would typically be preferred. This exercise demonstrates how algorithm choice dramatically affects performance, with the merge approaches being O(n) while the sorting approaches are O(n²) for this problem.



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THANKYOU

