IPCV Part III miniproject 2

Last updated on 2020-05-21

SESSION 1:

- This assingment is centered in the use of Keras
- Keras is an open-source neural-network library. Designed to enable fast experimentation with deep neural networks, it focuses on being user-friendly, modular, and extensible.
- Keras itself can work using different motors. We will use it with TensorFlow under the hood.
- We will analyze the vanishing gradient problem and initialization methods together with other optimization methods.

Import the libraries

TensorFlow officially included Keras, so if you have TensorFlow, you have keras!

```
# Imports
In [21]:
          import numpy as np
          import matplotlib.pyplot as plt
          import tensorflow as tf
          from tensorflow import keras
          import keras as k
          from keras.models import Sequential
          from keras.layers import Dense
          from sklearn.preprocessing import StandardScaler
          !git clone https://github.com/luisferuam/DLFBT-LAB
 In [3]:
          import sys
          sys.path.append('DLFBT-LAB')
          import dlfbt
         Cloning into 'DLFBT-LAB'...
```

remote: Total 99 (delta 49), reused 71 (delta 24), pack-reused 0

Data set

remote: Enumerating objects: 99, done.

Unpacking objects: 100% (99/99), done.

remote: Counting objects: 100% (99/99), done. remote: Compressing objects: 100% (73/73), done.

```
In [22]:
          dataset url = 'https://raw.githubusercontent.com/jbrownlee/Datasets/master/phone
          # Details https://raw.githubusercontent.com/jbrownlee/Datasets/master/phoneme.na
          dataset = np.loadtxt(dataset url, delimiter=',')
          # Split database in atributtes and classes
          print("dataset shape =", dataset.shape)
          # TO-DO block: Divide attributes and classes/labels. Store the numer of atrribut
          x = dataset[:,:-1]
          y = dataset[:, -1:]
          x_size = x.shape
          print("features shape =", x.shape)
          print("labels shape =", y.shape)
          # End of TO-DO block
         dataset shape = (5404, 6)
         features shape = (5404, 5)
         labels
                shape = (5404, 1)
 In [5]:
          # Final result with the classes stored in y
          print(x size)
          print(x)
          print(y)
         (5404, 5)
         [[ 1.24
                   0.875 -0.205 -0.078 0.067]
          [ 0.268 1.352 1.035 -0.332 0.217]
          [ 1.567  0.867  1.3
                                1.041 0.5591
          [ 1.031 0.584 1.866 1.532 -0.671]
                   0.933 2.363 -0.742 -0.617]
          [ 0.15
          [ 0.137  0.714  1.35
                                 0.972 -0.63 11
         [[0.]
          [0.]
          [0.]
          [1.]
          [0.]
          [1.]]
          np.unique(y)
 In [6]:
 Out[6]: array([0., 1.])
         # Normalize the data
In [23]:
          scaler = StandardScaler()
          scaler.fit(x)
          x = scaler.transform(x)
```

Defining our model

- From the input to the output in keras we can define the properties of each laye (size, activation function, connectivity topology...) with the sequential mode.
- In this case we are going to create our basic multilayer feedforward network

Compile the network

- Compile is the step where our network is created
- Here we have to define different aspects involved in the training of the network
- In each section you have an URL to the official documentation. Take a look at the availability of different strategies in each case.
- It is possible to also define your own functions for this.

Optimizer

Strategy to calculate the weights corrections

https://keras.io/api/optimizers/

Loss function

The purpose of loss functions is to compute the quantity that a model should seek to minimize during training.

https://keras.io/api/losses/

Metrics (results)

A metric is a function that is used to judge the performance of your model.

Metric functions are similar to loss functions, except that the results from evaluating a metric are not used when training the model. Note that you may use any loss function as a metric.

https://keras.io/api/metrics/

Initialization

Initializers define the way to set the initial weights weights of your network layers.

https://keras.io/api/layers/initializers/

Train the network

The Fit method trains the network according to the data.

Here we introduce all the data together and select a 20% of the data for validation purposes.

Other ways to do this are allowed, including the optimization of the parameters.

https://keras.io/api/models/model_training_apis/#fit-method

```
tf.keras.backend.set floatx('float64')
In [ ]:
         # Fit
In [ ]:
         history = nn.fit(x, y, epochs=500, verbose=2, validation split=0.2)
         \#history = nn.fit(x, y, epochs=500, verbose=0, validation split=0.2)
        Epoch 1/500
        136/136 - 4s - loss: 0.6276 - accuracy: 0.7030 - val loss: 0.6153 - val accurac
        y: 0.7206
        Epoch 2/500
        136/136 - 0s - loss: 0.6143 - accuracy: 0.7030 - val loss: 0.6020 - val accurac
        y: 0.7206
        Epoch 3/500
        136/136 - 0s - loss: 0.6032 - accuracy: 0.7030 - val_loss: 0.5912 - val_accurac
        y: 0.7206
        Epoch 4/500
        136/136 - 0s - loss: 0.5942 - accuracy: 0.7030 - val_loss: 0.5819 - val_accurac
        y: 0.7206
        Epoch 5/500
        136/136 - 0s - loss: 0.5865 - accuracy: 0.7030 - val_loss: 0.5741 - val_accurac
        y: 0.7206
        Epoch 6/500
        136/136 - 0s - loss: 0.5800 - accuracy: 0.7030 - val loss: 0.5674 - val accurac
        y: 0.7206
        Epoch 7/500
        136/136 - 0s - loss: 0.5745 - accuracy: 0.7030 - val loss: 0.5617 - val accurac
        y: 0.7206
        Epoch 8/500
        136/136 - 0s - loss: 0.5697 - accuracy: 0.7030 - val_loss: 0.5569 - val_accurac
        y: 0.7206
```

```
y: 0.8113
        Epoch 486/500
        136/136 - 0s - loss: 0.3834 - accuracy: 0.8075 - val loss: 0.3814 - val accurac
        v: 0.8113
        Epoch 487/500
        136/136 - 0s - loss: 0.3832 - accuracy: 0.8075 - val loss: 0.3813 - val accurac
        y: 0.8113
        Epoch 488/500
        136/136 - 0s - loss: 0.3831 - accuracy: 0.8082 - val loss: 0.3812 - val accurac
        y: 0.8113
        Epoch 489/500
        136/136 - 0s - loss: 0.3829 - accuracy: 0.8073 - val loss: 0.3811 - val accurac
        y: 0.8122
        Epoch 490/500
        136/136 - 0s - loss: 0.3828 - accuracy: 0.8082 - val loss: 0.3810 - val accurac
        y: 0.8122
        Epoch 491/500
        136/136 - 0s - loss: 0.3826 - accuracy: 0.8082 - val_loss: 0.3809 - val accurac
        y: 0.8122
        Epoch 492/500
        136/136 - 0s - loss: 0.3825 - accuracy: 0.8089 - val loss: 0.3808 - val accurac
        y: 0.8122
        Epoch 493/500
        136/136 - 0s - loss: 0.3824 - accuracy: 0.8094 - val loss: 0.3808 - val accurac
        y: 0.8131
        Epoch 494/500
        136/136 - 0s - loss: 0.3822 - accuracy: 0.8092 - val loss: 0.3808 - val accurac
        y: 0.8131
        Epoch 495/500
        136/136 - Os - loss: 0.3821 - accuracy: 0.8087 - val loss: 0.3806 - val accurac
        v: 0.8131
        Epoch 496/500
        136/136 - 0s - loss: 0.3819 - accuracy: 0.8094 - val loss: 0.3804 - val accurac
        y: 0.8131
        Epoch 497/500
        136/136 - 0s - loss: 0.3818 - accuracy: 0.8089 - val_loss: 0.3804 - val_accurac
        y: 0.8131
        Epoch 498/500
        136/136 - 0s - loss: 0.3817 - accuracy: 0.8087 - val loss: 0.3801 - val accurac
        y: 0.8122
        Epoch 499/500
        136/136 - 0s - loss: 0.3815 - accuracy: 0.8087 - val loss: 0.3799 - val accurac
        y: 0.8131
        Epoch 500/500
        136/136 - 0s - loss: 0.3814 - accuracy: 0.8089 - val loss: 0.3799 - val accurac
        v: 0.8131
In [ ]: # Network details
         nn.summary()
         print('\n\n')
         # Evaluate (similar to fit but just considering 1 epoch iteration without changi
         loss, accuracy = nn.evaluate(x, y)
         print('Accuracy: %.2f' % (accuracy*100))
         # Also, the predict method is available to classify unlabeled data
        Model: "sequential 1"
```

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 5)	30
dense_1 (Dense)	(None, 100)	600

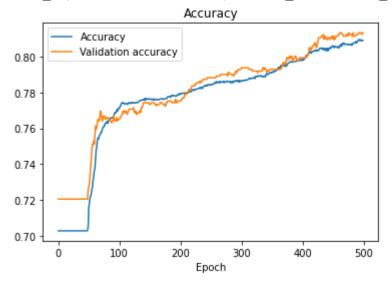
dense_2 (Dense)	(None, 100)	10100
dense_3 (Dense)	(None, 1)	101
Total params: 10,831 Trainable params: 10,831 Non-trainable params: 0		

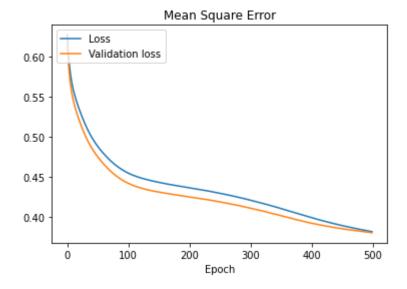
Plot data

History object saves the different epoch data

```
# Plot history
In [ ]:
         print(history.history.keys())
         plt.plot(history.history['accuracy'], label='Accuracy')
         plt.plot(history.history['val_accuracy'], label='Validation accuracy')
         plt.title('Accuracy')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         plt.plot(history.history['loss'], label='Loss')
         plt.plot(history.history['val_loss'], label='Validation loss')
         plt.title('Mean Square Error')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
```

dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])





TO-DO block: Explain what you observe

Using a small number of neurons in the hidden layer (~= input layer)

When using a small number of neurons, smaller/equal than the input layer, the accuracy is not very high unless the number of epochs is increased. Using a 5 neurons for example and 5 epochs, the accuracy remains stable at 66%, while if the epochs is increased to 500, the accuracy increases up to 88%. From a bigger number of epochs we can also observe a smoother plot

Using a big number of neurons in the hidden layer (>> input layer)

There will be overfitting, increasing the number of layers up to 500 and 8 layers depth, of almost a 6%.

End of TO-DO block

Optimize the network design

- Change the network architecture, introducing more layers and neurons to obtain a better result.
 You can:
 - Add more and different type of layers
 - Change the activation funcions
 - Change the loss / optimizer
 - Change your initialization

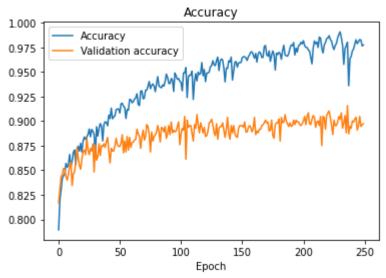
```
In [8]:
         from keras.optimizers import SGD
         # TO-DO block: Include your code below
         input size = 5
         output size = 1
         hidden layer size = 500
         nn = tf.keras.Sequential([ # Sequential means a linear stack of layers
             tf.keras.layers.Dense(hidden_layer_size,input_dim=5,activation='relu', kerne
             tf.keras.layers.Dense(hidden layer size,activation='relu'),
             tf.keras.layers.Dense(hidden layer size,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
             tf.keras.layers.Dense(hidden layer size,activation='tanh'),
             tf.keras.layers.Dense(output size,activation='sigmoid')
         1)
         opt = SGD(lr=0.01, momentum=0.9)
         nn.compile(loss='binary crossentropy', optimizer=opt,metrics=['accuracy'])
         # End of TO-DO block
         # Fit
         history = nn.fit(x, y, epochs=250, verbose=0, validation split=0.2)
         # Plot history
         print(history.history.keys())
         plt.plot(history.history['accuracy'], label='Accuracy')
         plt.plot(history.history['val_accuracy'], label='Validation accuracy')
         plt.title('Accuracy')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
```

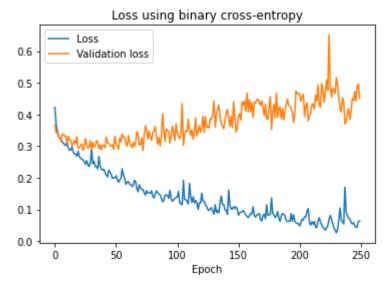
```
plt.plot(history.history['loss'], label='Loss')
plt.plot(history.history['val_loss'], label='Validation loss')
plt.title('Loss using binary cross-entropy')
plt.ylabel('')
plt.ylabel('Epoch')
plt.legend(loc="upper left")
plt.legend(loc="upper left")
plt.show()

# Network details
nn.summary()
print('\n\n')

# Evaluate (similar to fit but just 1 epoch iteration without changing the netwood loss, accuracy = nn.evaluate(x, y)
print('Accuracy: %.2f' % (accuracy*100))
```

dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])





Model: "sequential_2"

Layer (type)	Output Shape	Param #
dense_14 (Dense)	(None, 500)	3000
dense_15 (Dense)	(None, 500)	250500

dense_16 (Dense)	(None,	500)	250500
dense_17 (Dense)	(None,	500)	250500
dense_18 (Dense)	(None,	500)	250500
dense_19 (Dense)	(None,	500)	250500
dense_20 (Dense)	(None,	1)	501
Total params: 1,256,001 Trainable params: 1,256,001 Non-trainable params: 0			

SESSION 2

Dataset input

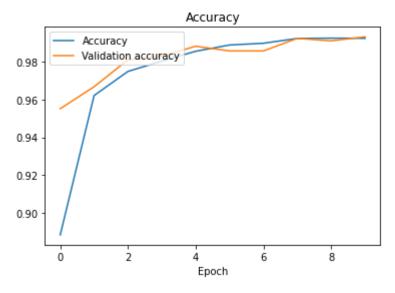
```
In [28]:
          # Load here your selected dataset considering input and output dimensions
          import tensorflow_datasets as tfsd
          mnist dataset,mnist info=tfsd.load(name='mnist',with info=True, as supervised=Tr
          mnist train,mnist test = mnist dataset['train'],mnist dataset['test']
In [29]:
          num validation samples = 0.1*mnist info.splits['train'].num examples
          num_validation_samples = tf.cast(num_validation_samples,tf.int64)
          num_test_samples = mnist info.splits['test'].num examples
          num test samples = tf.cast(num test samples,tf.int64)
In [32]:
          def scale(image, label):
              image=tf.cast(image,tf.float32)
              image/=255.
              return image,label
          scaled train and validation data=mnist train.map(scale)
          scaled test data = mnist test.map(scale)
          BUFFER SIZE=10000
          BATCH SIZE=300
          input size = 784
          output size = 10
          hidden layer size = 300
          hidden_layer_size2 = 150
          hidden_layer_size2 = 150
          hidden layer size2 = 150
          shuffled train and validation data = scaled train and validation data.shuffle(Bl
          validation data = shuffled train and validation data.take(num validation samples
          train data = shuffled train and validation data.skip(num validation samples)
          train data=train data.batch(BATCH SIZE)
```

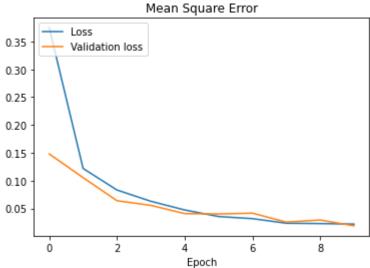
```
validation_data = validation_data.batch(num_validation_samples)
test_data = scaled_test_data.batch(num_test_samples)
validation_inputs, validation_targets = next(iter(validation_data))
```

Standar choice

- Evaluate the training with a standard choice of cost and activation functions, learning rate, weight initialization and network topology.
- · Generate the loss and accuracy figures

```
In [33]:
          model = tf.keras.Sequential([
              tf.keras.layers.Flatten(input shape=(28,28,1)),
              tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
              tf.keras.layers.Dense(hidden layer size2,activation='relu'),
              tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
              tf.keras.layers.Dense(hidden layer size2,activation='relu'),
              tf.keras.layers.Dense(hidden layer size2,activation='relu'),
              tf.keras.layers.Dense(output size,activation='softmax')
          ])
          opt = keras.optimizers.Nadam(learning rate=0.001)
          model.compile(optimizer='Adam',loss='sparse_categorical_crossentropy',metrics=[
          NUM EPOCHS= 10
          history = model.fit(train data,epochs=NUM EPOCHS,validation data=(validation ing
          plt.plot(history.history['accuracy'], label='Accuracy')
In [34]:
          plt.plot(history.history['val accuracy'], label='Validation accuracy')
          plt.title('Accuracy')
          plt.ylabel('')
          plt.xlabel('Epoch')
          plt.legend(loc="upper left")
          plt.show()
          plt.plot(history.history['loss'], label='Loss')
          plt.plot(history.history['val loss'], label='Validation loss')
          plt.title('Mean Square Error')
          plt.ylabel('')
          plt.xlabel('Epoch')
          plt.legend(loc="upper left")
          plt.show()
          # Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
          loss, accuracy = model.evaluate(test data)
          print('Accuracy: %.2f' % (accuracy*100))
```





Accuracy: 98.07

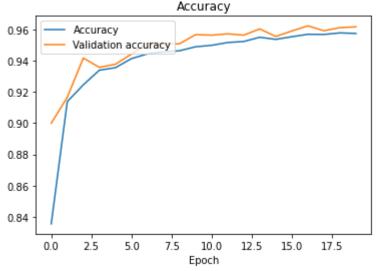
Optimizations

- Evaluate each of the following optimization methods using the same representation and the duration of the training in terms of epochs to reach a choice of error and also in terms of time taken.
 - a) Regularization
 - b) Dropout
 - c) Stochastic gradient descent
 - d) Momentum (including Nesterov version)
 - e) AdaGrad
 - f) RMSProp

g) Adam

h) Optimize

```
# a) Regularization
In [ ]:
         # Code
         model = tf.keras.Sequential([
             tf.keras.layers.Flatten(input shape=(28,28,1)),
             tf.keras.layers.Dense(hidden layer size,activation='relu',kernel regularizer
             tf.keras.layers.Dense(hidden layer size2,activation='relu',kernel regularize
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu',kernel_regularize
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu',kernel_regularize
             tf.keras.layers.Dense(hidden layer size2,activation='relu',kernel regularize
             tf.keras.layers.Dense(output size,activation='softmax')
         1)
         opt = keras.optimizers.Nadam(learning rate=0.001)
         model.compile(optimizer='Adam',loss='sparse_categorical_crossentropy',metrics=[
         NUM EPOCHS= 20
         history = model.fit(train data,epochs=NUM EPOCHS,validation data=(validation ing
In [ ]:
         plt.plot(history.history['accuracy'], label='Accuracy')
         plt.plot(history.history['val accuracy'], label='Validation accuracy')
         plt.title('Accuracy')
         plt.vlabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         plt.plot(history.history['loss'], label='Loss')
         plt.plot(history.history['val loss'], label='Validation loss')
         plt.title('Mean Square Error')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         # Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
         loss, accuracy = model.evaluate(test data)
         print('Accuracy: %.2f' % (accuracy*100))
```

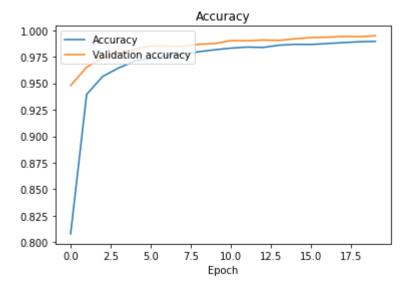


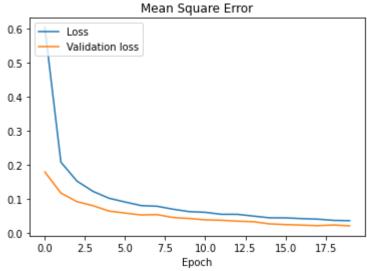
```
0.9587
Accuracy: 95.87
```

```
In [ ]:
         # Code
         model = tf.keras.Sequential([
             tf.keras.layers.Flatten(input_shape=(28,28,1)),
             tf.keras.layers.Dense(hidden layer size,activation='relu'),
             tf.keras.layers.Dropout(0.25),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dropout(0.25),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dropout(0.25),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dropout(0.25),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(output size,activation='softmax')
         1)
         opt = keras.optimizers.Nadam(learning_rate=0.001)
         model.compile(optimizer='Adam',loss='sparse categorical crossentropy',metrics=[
         NUM EPOCHS= 20
         history = model.fit(train data,epochs=NUM EPOCHS,validation data=(validation ing
```

```
plt.plot(history.history['accuracy'], label='Accuracy')
In [ ]:
         plt.plot(history.history['val accuracy'], label='Validation accuracy')
         plt.title('Accuracy')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         plt.plot(history.history['loss'], label='Loss')
         plt.plot(history.history['val_loss'], label='Validation loss')
         plt.title('Mean Square Error')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         # Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
```

```
loss, accuracy = model.evaluate(test_data)
print('Accuracy: %.2f' % (accuracy*100))
```

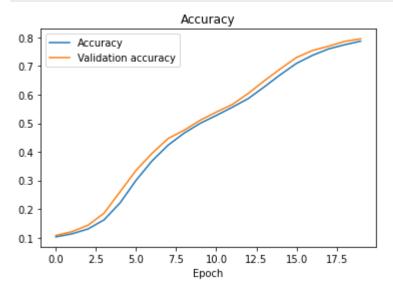


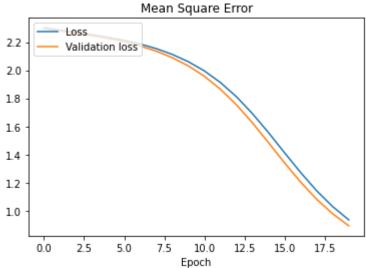


```
In [ ]:
         # c) Stochastic gradient descent
         # Code
         model = tf.keras.Sequential([
             tf.keras.layers.Flatten(input_shape=(28,28,1)),
             tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(output_size,activation='softmax')
         ])
         opt = keras.optimizers.SGD(learning_rate=0.001)
         model.compile(optimizer=opt,loss='sparse_categorical_crossentropy',metrics=['acc
         NUM EPOCHS= 20
         history = model.fit(train data,epochs=NUM EPOCHS,validation data=(validation ing
```

plt.plot(history.history['accuracy'], label='Accuracy')

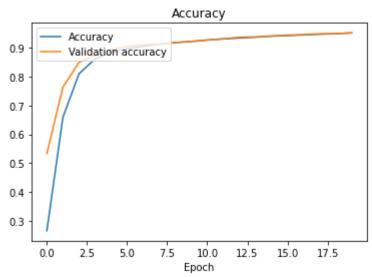
```
plt.plot(history.history['val accuracy'], label='Validation accuracy')
plt.title('Accuracy')
plt.ylabel('')
plt.xlabel('Epoch')
plt.legend(loc="upper left")
plt.show()
plt.plot(history.history['loss'], label='Loss')
plt.plot(history.history['val_loss'], label='Validation loss')
plt.title('Mean Square Error')
plt.ylabel('')
plt.xlabel('Epoch')
plt.legend(loc="upper left")
plt.show()
# Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
loss, accuracy = model.evaluate(test data)
print('Accuracy: %.2f' % (accuracy*100))
```





```
In [ ]: # d) Momentum (including Nesterov version)
# Code
model = tf.keras.Sequential([
```

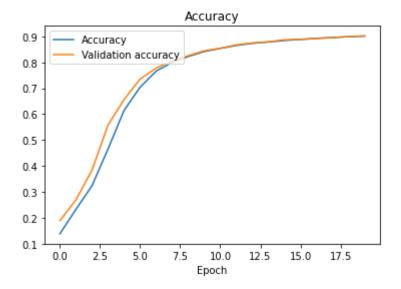
```
tf.keras.layers.Flatten(input shape=(28,28,1)),
             tf.keras.layers.Dense(hidden layer size,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(output size,activation='softmax')
         ])
         opt = keras.optimizers.SGD(learning_rate=0.001, momentum=0.9)
         model.compile(optimizer= opt,loss='sparse categorical crossentropy',metrics=['ac
         NUM EPOCHS= 20
         history = model.fit(train data,epochs=NUM EPOCHS,validation data=(validation in
         plt.plot(history.history['accuracy'], label='Accuracy')
In [ ]:
         plt.plot(history.history['val_accuracy'], label='Validation accuracy')
         plt.title('Accuracy')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         plt.plot(history.history['loss'], label='Loss')
         plt.plot(history.history['val_loss'], label='Validation loss')
         plt.title('Mean Square Error')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         # Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
         loss, accuracy = model.evaluate(test_data)
         print('Accuracy: %.2f' % (accuracy*100))
```

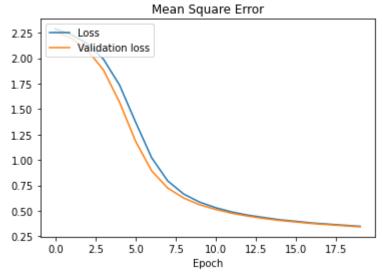


Mean Square Error Loss Validation loss 2.0 1.5 1.0 0.5 2.5 7.5 10.0 12.5 15.0 17.5 0.0 5.0 Epoch

```
# e) AdaGrad
In [ ]:
         # Code
         model = tf.keras.Sequential([
             tf.keras.layers.Flatten(input_shape=(28,28,1)),
             tf.keras.layers.Dense(hidden layer size,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(output size,activation='softmax')
         ])
         opt = keras.optimizers.Adagrad(learning rate=0.001)
         model.compile(optimizer=opt,loss='sparse categorical crossentropy',metrics=['acc
         NUM EPOCHS= 20
         history = model.fit(train_data,epochs=NUM_EPOCHS,validation_data=(validation_ing
```

```
plt.plot(history.history['accuracy'], label='Accuracy')
In [ ]:
         plt.plot(history.history['val accuracy'], label='Validation accuracy')
         plt.title('Accuracy')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         plt.plot(history.history['loss'], label='Loss')
         plt.plot(history.history['val_loss'], label='Validation loss')
         plt.title('Mean Square Error')
         plt.vlabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         # Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
         loss, accuracy = model.evaluate(test data)
         print('Accuracy: %.2f' % (accuracy*100))
```





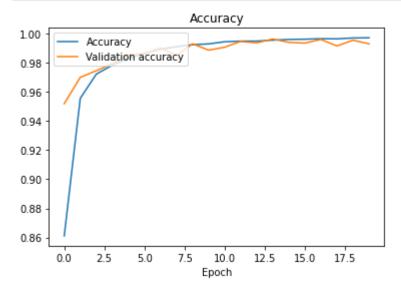
```
# f) RMSProp
In [ ]:
         # Code
         model = tf.keras.Sequential([
             tf.keras.layers.Flatten(input shape=(28,28,1)),
             tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(output size,activation='softmax')
         ])
         opt = keras.optimizers.RMSprop(learning_rate=0.001)
         model.compile(optimizer=opt,loss='sparse_categorical_crossentropy',metrics=['acc
         NUM EPOCHS= 20
         history = model.fit(train data,epochs=NUM EPOCHS,validation data=(validation ing
```

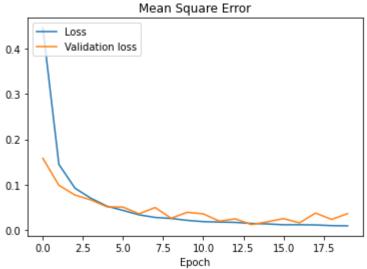
```
In [ ]: plt.plot(history.history['accuracy'], label='Accuracy')
   plt.plot(history.history['val_accuracy'], label='Validation accuracy')
```

```
plt.title('Accuracy')
plt.ylabel('')
plt.xlabel('Epoch')
plt.legend(loc="upper left")
plt.show()

plt.plot(history.history['loss'], label='Loss')
plt.plot(history.history['val_loss'], label='Validation loss')
plt.title('Mean Square Error')
plt.ylabel('')
plt.xlabel('Epoch')
plt.legend(loc="upper left")
plt.legend(loc="upper left")
plt.show()

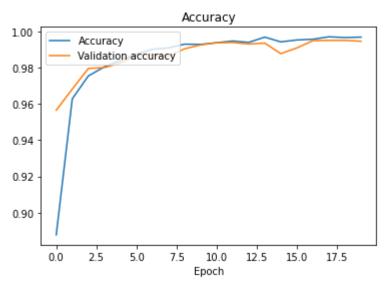
# Evaluate (similar to fit but just 1 epoch iteration without changing the netwood loss, accuracy = model.evaluate(test_data)
print('Accuracy: %.2f' % (accuracy*100))
```





Accuracy: 98.09

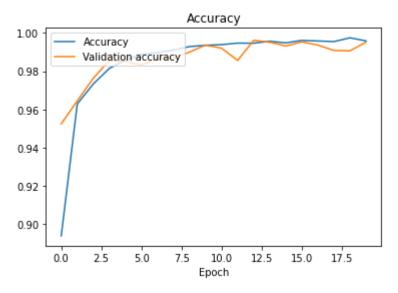
```
tf.keras.layers.Dense(hidden layer size,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(output size,activation='softmax')
         ])
         opt = keras.optimizers.Adam(learning rate=0.001)
         model.compile(optimizer=opt,loss='sparse categorical crossentropy',metrics=['acc
         NUM EPOCHS= 20
         history = model.fit(train data,epochs=NUM EPOCHS,validation data=(validation in
         plt.plot(history.history['accuracy'], label='Accuracy')
In [ ]:
         plt.plot(history.history['val accuracy'], label='Validation accuracy')
         plt.title('Accuracy')
         plt.vlabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         plt.plot(history.history['loss'], label='Loss')
         plt.plot(history.history['val loss'], label='Validation loss')
         plt.title('Mean Square Error')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         # Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
         loss, accuracy = model.evaluate(test data)
         print('Accuracy: %.2f' % (accuracy*100))
```

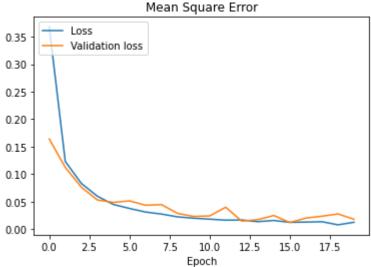


Mean Square Error Loss 0.35 Validation loss 0.30 0.25 0.20 0.15 0.10 0.05 0.00 2.5 5.0 7.5 10.0 12.5 15.0 17.5 0.0 Epoch

```
# h) Optimize
In [ ]:
         # Code
         model = tf.keras.Sequential([
             tf.keras.layers.Flatten(input_shape=(28,28,1)),
             tf.keras.layers.Dense(hidden layer size,activation='relu'),
             tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(hidden layer size2,activation='relu'),
             tf.keras.layers.Dense(output size,activation='softmax')
         ])
         opt = keras.optimizers.Nadam(learning rate=0.001)
         model.compile(optimizer='Adam',loss='sparse categorical crossentropy',metrics=[
         NUM EPOCHS= 20
         history = model.fit(train_data,epochs=NUM_EPOCHS,validation_data=(validation_ing
```

```
In [ ]:
         plt.plot(history.history['accuracy'], label='Accuracy')
         plt.plot(history.history['val accuracy'], label='Validation accuracy')
         plt.title('Accuracy')
         plt.ylabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         plt.plot(history.history['loss'], label='Loss')
         plt.plot(history.history['val_loss'], label='Validation loss')
         plt.title('Mean Square Error')
         plt.vlabel('')
         plt.xlabel('Epoch')
         plt.legend(loc="upper left")
         plt.show()
         # Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
         loss, accuracy = model.evaluate(test data)
         print('Accuracy: %.2f' % (accuracy*100))
```





Implement parallelization in Keras with the best optimization

- Run tests for GPU presence
- Use your best implementation from the previous exercise here and compare the training time both with GPUs and without GPUs.

Comment all your results.

```
In [23]: %tensorflow_version 2.x
import tensorflow as tf
print("Tensorflow version " + tf.__version__)

try:
    tpu = tf.distribute.cluster_resolver.TPUClusterResolver() # TPU detection
    print('Running on TPU ', tpu.cluster_spec().as_dict()['worker'])
    except ValueError:
    raise BaseException('ERROR: Not connected to a TPU runtime; please see the pre
tf.config.experimental_connect_to_cluster(tpu)
```

```
tf.tpu.experimental.initialize tpu system(tpu)
tpu strategy = tf.distribute.experimental.TPUStrategy(tpu)
Tensorflow version 2.4.1
Running on TPU ['10.16.57.162:8470']
WARNING:tensorflow:TPU system grpc://10.16.57.162:8470 has already been initiali
zed. Reinitializing the TPU can cause previously created variables on TPU to be
lost.
WARNING:tensorflow:TPU system grpc://10.16.57.162:8470 has already been initiali
zed. Reinitializing the TPU can cause previously created variables on TPU to be
INFO:tensorflow:Initializing the TPU system: grpc://10.16.57.162:8470
INFO:tensorflow:Initializing the TPU system: grpc://10.16.57.162:8470
INFO:tensorflow:Clearing out eager caches
INFO:tensorflow:Clearing out eager caches
INFO:tensorflow:Finished initializing TPU system.
INFO:tensorflow:Finished initializing TPU system.
WARNING:absl:`tf.distribute.experimental.TPUStrategy` is deprecated, please use
the non experimental symbol `tf.distribute.TPUStrategy` instead.
INFO:tensorflow:Found TPU system:
INFO:tensorflow:Found TPU system:
INFO:tensorflow:*** Num TPU Cores: 8
INFO:tensorflow:*** Num TPU Cores: 8
INFO:tensorflow:*** Num TPU Workers: 1
INFO:tensorflow:*** Num TPU Workers: 1
INFO:tensorflow:*** Num TPU Cores Per Worker: 8
INFO:tensorflow:*** Num TPU Cores Per Worker: 8
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:localhost/replica:
0/task:0/device:CPU:0, CPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:localhost/replica:
0/task:0/device:CPU:0, CPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:CPU:0, CPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:CPU:0, CPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:0, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:0, TPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:1, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:1, TPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:2, TPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:2, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:3, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:3, TPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:4, TPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:4, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:5, TPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:5, TPU, 0, 0)
INFO:tensorflow:*** Available Device: DeviceAttributes(/job:worker/replica:0/ta
```

```
sk:0/device:TPU:6, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:6, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:7, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU:7, TPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU_SYSTEM:0, TPU_SYSTEM, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:TPU_SYSTEM:0, TPU_SYSTEM, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:XLA_CPU:0, XLA_CPU, 0, 0)
INFO:tensorflow:*** Available Device: _DeviceAttributes(/job:worker/replica:0/ta
sk:0/device:XLA_CPU:0, XLA_CPU, 0, 0)
```

Guess the year comparason with CPU - GPU - TPU

```
input size = 5
In [26]:
          output size = 1
          hidden layer size = 500
          nn = tf.keras.Sequential([ # Sequential means a linear stack of layers
              tf.keras.layers.Dense(hidden layer size,input dim=5,activation='relu', kerne
              tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
              tf.keras.layers.Dense(hidden layer size,activation='relu'),
              tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
              tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
              tf.keras.layers.Dense(hidden layer size,activation='tanh'),
              tf.keras.layers.Dense(output size,activation='sigmoid')
          1)
          opt = SGD(lr=0.01, momentum=0.9)
          nn.compile(loss='binary crossentropy', optimizer=opt,metrics=['accuracy'])
          # End of TO-DO block
          #----
          import time
          s = time.time()
          # Fit
          history = nn.fit(x, y, epochs=5,batch size=1024, verbose=1, validation split=0.2
          e = time.time()
          print(e - s)
          # Plot history
          print(history.history.keys())
          plt.plot(history.history['accuracy'], label='Accuracy')
          plt.plot(history.history['val accuracy'], label='Validation accuracy')
          plt.title('Accuracy')
          plt.ylabel('')
          plt.xlabel('Epoch')
          plt.legend(loc="upper left")
          plt.show()
```

```
plt.plot(history.history['loss'], label='Loss')
plt.plot(history.history['val loss'], label='Validation loss')
plt.title('Loss using binary cross-entropy')
plt.ylabel('')
plt.xlabel('Epoch')
plt.legend(loc="upper left")
plt.show()
# Network details
nn.summary()
print('\n\n')
# Evaluate (similar to fit but just 1 epoch iteration without changing the netwo
loss, accuracy = nn.evaluate(x, y)
print('Accuracy: %.2f' % (accuracy*100))
Epoch 1/5
0.6773 - val loss: 0.5084 - val accuracy: 0.7206
Epoch 2/5
0.7288 - val loss: 0.4527 - val accuracy: 0.7956
0.7943 - val loss: 0.4290 - val accuracy: 0.7882
Epoch 4/5
0.7824 - val_loss: 0.4119 - val_accuracy: 0.8057
Epoch 5/5
0.8123 - val_loss: 0.3996 - val_accuracy: 0.8020
4.068118333816528
dict keys(['loss', 'accuracy', 'val loss', 'val accuracy'])
               Accuracy
      Accuracy
0.80
      Validation accuracy
0.78
0.76
0.74
0.72
0.70
```

0.0

0.5

1.5

1.0

2.0

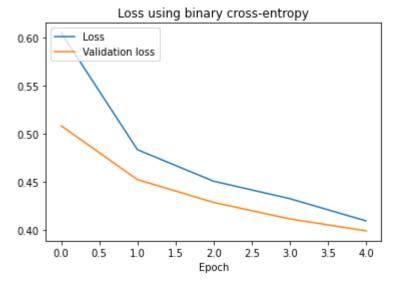
Epoch

2.5

3.0

3.5

4.0



Model: "sequential_13"

Layer (type)	Output Shape	Param #
dense_76 (Dense)	(None, 500)	3000
dense_77 (Dense)	(None, 500)	250500
dense_78 (Dense)	(None, 500)	250500
dense_79 (Dense)	(None, 500)	250500
dense_80 (Dense)	(None, 500)	250500
dense_81 (Dense)	(None, 500)	250500
dense_82 (Dense)	(None, 1)	501

Total params: 1,256,001 Trainable params: 1,256,001 Non-trainable params: 0

y: 0.8077

Accuracy: 80.77

Computational time between CPU - GPU - TPU for best model - guess the year dataset

Epoch time

Batch Size	\mathbf{CPU}	GPU	\mathbf{TPU}^{-1}
256	5.038s	1.60s	1.63s
512	4.430s	1.35s	1.98s
1024	4.06s	1.258s	1.635s

Step time per epoch

Batch Size	\mathbf{CPU}	\mathbf{GPU}	\mathbf{TPU}
256	$1s/51 \mu s$	$0s/14\mu s$	$1s/22\mu s$
512	$1s/80 \mu s$	$0s/14\mu s$	$1s/24\mu s$
1024	$1s/133 \mu s$	$0s/19\mu s$	$0/42 \mu s$

Mnist comparason with CPU - GPU

```
from keras.optimizers import SGD
In [35]:
          import timeit
          import time
          #from tensorflow.contrib.tpu.python.tpu import keras support
          def get model():
            model = tf.keras.Sequential([
              tf.keras.layers.Flatten(input shape=(28,28,1)),
              tf.keras.layers.Dense(hidden_layer_size,activation='relu'),
              tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
              tf.keras.layers.Dense(hidden layer size2,activation='relu'),
              tf.keras.layers.Dense(hidden_layer_size2,activation='relu'),
              tf.keras.layers.Dense(hidden layer size2,activation='relu'),
              tf.keras.layers.Dense(output size,activation='softmax')
            opt = keras.optimizers.Nadam(learning rate=0.001)
            model.compile(optimizer='Adam',loss='sparse categorical crossentropy',metrics=
            return model
          # End of TO-DO block
          model = get model()
          NUM EPOCHS= 20
          s = time.time()
          history = model.fit(train data,epochs=NUM EPOCHS,
                    batch size=256,
                   validation_data=(validation_inputs, validation_targets),verbose=0)
          #history = model.fit(train data,epochs=NUM EPOCHS,validation data=(validation in
          e = time.time()
          print("The computation time was: ", e - s)
          # Plot history
          print(history.history.keys())
          plt.plot(history.history['accuracy'], label='Accuracy')
          plt.plot(history.history['val_accuracy'], label='Validation accuracy')
          plt.title('Accuracy')
          plt.ylabel('')
          plt.xlabel('Epoch')
          plt.legend(loc="upper left")
```

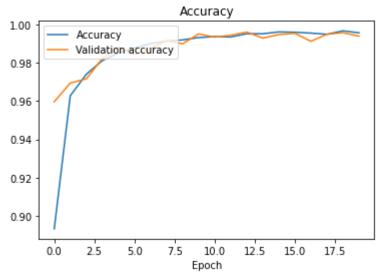
```
plt.show()

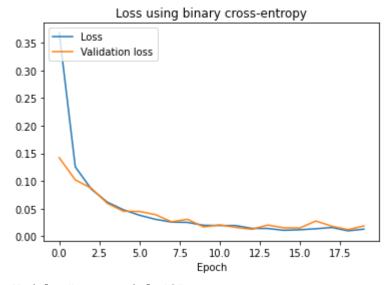
plt.plot(history.history['loss'], label='Loss')
plt.plot(history.history['val_loss'], label='Validation loss')
plt.title('Loss using binary cross-entropy')
plt.ylabel('')
plt.xlabel('Epoch')
plt.legend(loc="upper left")
plt.show()

# Network details
model.summary()
print('\n\n')

# Evaluate (similar to fit but just 1 epoch iteration without changing the netwoloss, accuracy = model.evaluate(test_data)
print('Accuracy: %.2f' % (accuracy*100))
```

The computation time was: 98.12066292762756 dict_keys(['loss', 'accuracy', 'val_loss', 'val_accuracy'])





Model: "sequential_18"

Layer (type)	Output Shape	Param #
flatten_15 (Flatten)	(None, 784)	0

dense_107	(Dense)	(None,	300)	235500
dense_108	(Dense)	(None,	150)	45150
dense_109	(Dense)	(None,	150)	22650
dense_110	(Dense)	(None,	150)	22650
dense_111	(Dense)	(None,	150)	22650
dense_112	(Dense)	(None,	10)	1510

Total params: 350,110 Trainable params: 350,110 Non-trainable params: 0

0.9798

Accuracy: 97.98

Computational time between CPU - GPU - TPU for best model - MNIST model

Epoch time

Batch Size	\mathbf{CPU}	GPU]
256	104.6067s	75.24s
512	102s	74.6s
1024	103.75s	80.05s

Step time per epoch

Batch Size	\mathbf{CPU}	GPU -
256	$5.2s/25.5 \mu s$	$4s/17\mu s$
512	$5.1s/24 \mu s$	$4s/17\mu s$
1024	$5s/24\mu s$	$4s/17\mu s$

Convolutional Neural Networks

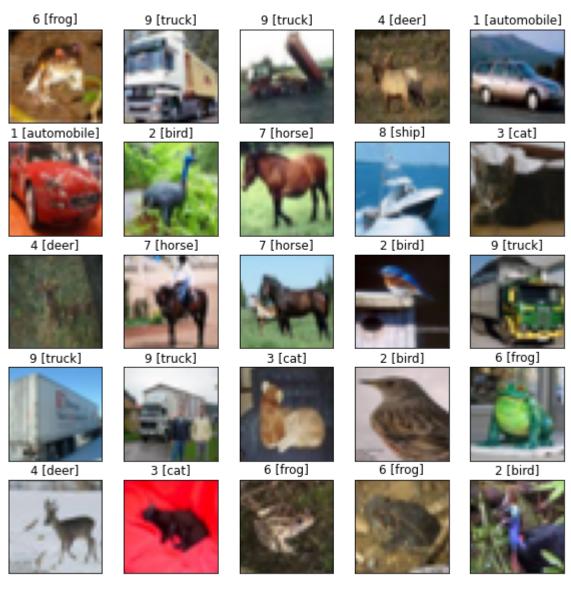
Implement a convolutional neural network and apply it to classify the images of the CIFAR-10 dataset. The network should have at least the following characteristics:

Convolutional layers.
Pooling layers.
Some regularization mechanism, such as dropout or L2 regularization.

Batch normalization layers.

The network should obtain at least 75% accuracy on the test set.

```
#%tensorflow version 2.x
In [ ]:
         import tensorflow as tf
         from tensorflow import keras
         from keras import backend as K
         from keras.utils.vis utils import plot model
         import numpy as np
         import matplotlib.pyplot as plt
In [ ]:
         (train images, train labels), (test images, test labels) = tf.keras.datasets.ci1
         class_names = ['airplane', 'automobile', 'bird', 'cat', 'deer', 'dog', 'frog',
         print(train_images.shape)
         print(train_labels.shape)
         for t in train_labels[:10]:
           print(t[0], class names[t[0]])
         print(test_images.shape)
         print(test_labels.shape)
         for t in test_labels[:10]:
           print(t[0], class names[t[0]])
        (50000, 32, 32, 3)
        (50000, 1)
        6 frog
        9 truck
        9 truck
        4 deer
        1 automobile
        1 automobile
        2 bird
        7 horse
        8 ship
        3 cat
        (10000, 32, 32, 3)
        (10000, 1)
        3 cat
        8 ship
        8 ship
        0 airplane
        6 frog
        6 frog
        1 automobile
        6 frog
        3 cat
        1 automobile
         plt.figure(figsize=(10, 10))
In [ ]:
         for i in range(25):
             plt.subplot(5, 5, i+1)
             plt.xticks([])
             plt.yticks([])
             plt.grid(False)
             plt.imshow(train images[i])
             plt.title("%d [%s]" % (train_labels[i][0], class_names[train_labels[i][0]]))
```



```
In [ ]: train_images.mean(axis=0).shape
```

Out[]: (32, 32, 3)

Normalization: Data - column-wise mean

```
In []: train_images_orig = train_images
    test_images_orig = test_images
    mean_img = train_images.mean(axis=0) # axis 0 (columns), axis 1 (rows) -> shape
    train_images = train_images - mean_img
    test_images = test_images - mean_img
```

Hot encoding labels

```
In [ ]:
         from keras.preprocessing.image import ImageDataGenerator
         datagen = ImageDataGenerator(width shift range=0.1,
                                      height shift range=0.1,
                                      rotation range=15,
                                      horizontal flip=True)
         iter = datagen.flow(train_images_orig[:10], train_labels[:10], batch_size=10)
In [ ]:
         K.clear session()
         model = tf.keras.Sequential()
         model.add(tf.keras.layers.Input(shape=(32, 32, 3)))
         model.add(tf.keras.layers.Conv2D(32, kernel size=3, activation='relu', padding=
         model.add(tf.keras.layers.BatchNormalization())
         model.add(tf.keras.layers.Conv2D(32, kernel size=3, activation='relu', padding=
         model.add(tf.keras.layers.BatchNormalization())
         model.add(tf.keras.layers.MaxPool2D(pool size=2))
         model.add(tf.keras.layers.Conv2D(64, kernel size=3, activation='relu', padding='
         model.add(tf.keras.layers.BatchNormalization())
         model.add(tf.keras.layers.Conv2D(64, kernel size=3, activation='relu', padding=
         model.add(tf.keras.layers.BatchNormalization())
         model.add(tf.keras.layers.MaxPool2D(pool size=2))
         model.add(tf.keras.layers.Conv2D(128, kernel size=3, activation='relu', padding=
         model.add(tf.keras.layers.BatchNormalization())
         model.add(tf.keras.layers.Conv2D(128, kernel size=3, activation='relu', padding=
         model.add(tf.keras.layers.BatchNormalization())
         model.add(tf.keras.layers.MaxPool2D(pool size=2))
         model.add(tf.keras.layers.Flatten())
         model.add(tf.keras.layers.Dense(512, activation='relu'))
         model.add(tf.keras.layers.BatchNormalization())
         model.add(tf.keras.layers.Dropout(0.5))
         model.add(tf.keras.layers.Dense(10, activation='softmax'))
         print(model.summary())
         plot model(model, show shapes=True, show layer names=True)
         model.compile(optimizer=keras.optimizers.Adam(learning rate=1.e-3), loss='catego'
         iter = datagen.flow(train images, train labels one hot, batch size=1000)
         nepochs = 50
         history = model.fit(iter,
                             epochs=nepochs,
                             steps per epoch=50,
                             validation data=(test images, test labels one hot))
        Model: "sequential"
```

Layer (type)	Output Sha	ре		Param #
conv2d (Conv2D)	(None, 32,	32,	32)	896
batch_normalization (BatchNo	(None, 32,	32,	32)	128

conv2d_1 (Conv2D)	(None, 32, 32, 32)	9248
batch_normalization_1 (Batch	(None, 32, 32, 32)	128
max_pooling2d (MaxPooling2D)	(None, 16, 16, 32)	0
conv2d_2 (Conv2D)	(None, 16, 16, 64)	18496
batch_normalization_2 (Batch	(None, 16, 16, 64)	256
conv2d_3 (Conv2D)	(None, 16, 16, 64)	36928
batch_normalization_3 (Batch	(None, 16, 16, 64)	256
<pre>max_pooling2d_1 (MaxPooling2</pre>	(None, 8, 8, 64)	0
conv2d_4 (Conv2D)	(None, 8, 8, 128)	73856
batch_normalization_4 (Batch	(None, 8, 8, 128)	512
conv2d_5 (Conv2D)	(None, 8, 8, 128)	147584
batch_normalization_5 (Batch	(None, 8, 8, 128)	512
max_pooling2d_2 (MaxPooling2	(None, 4, 4, 128)	0
flatten (Flatten)	(None, 2048)	0
dense (Dense)	(None, 512)	1049088
batch_normalization_6 (Batch	(None, 512)	2048
dropout (Dropout)	(None, 512)	0
dense_1 (Dense)	(None, 10)	5130
Total params: 1,345,066 Trainable params: 1,343,146		
Non-trainable params: 1,920		
None Epoch 1/50		
50/50 [====================================		p - loss: 2.1858 - acc: 0.
Epoch 2/50 50/50 [====================================	_	p - loss: 1.4189 - acc: 0.
5141 - val_loss: 1.6698 - va Epoch 3/50	l_acc: 0.4085	•
50/50 [====================================		p - loss: 1.2260 - acc: 0.
Epoch 4/50 50/50 [====================================	_	p - loss: 1.0888 - acc: 0.
6263 - val_loss: 1.1979 - va Epoch 5/50		,
50/50 [====================================		p - loss: 0.9782 - acc: 0.
Epoch 6/50 50/50 [====================================	_	p - loss: 0.9092 - acc: 0.
6896 - val_loss: 1.0435 - va Epoch 7/50		•
50/50 [====================================		p - loss: 0.8468 - acc: 0.
Epoch 8/50 50/50 [====================================	_	p - loss: 0.7950 - acc: 0.
7291 - val_loss: 0.7628 - va		,

