



C interfaces to GALAHAD BGO

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| | |
|-----------------------------------------|-----------|
| 1 GALAHAD C package bgo | 1 |
| 1.1 Introduction | 1 |
| 1.1.1 Purpose | 1 |
| 1.1.2 Authors | 1 |
| 1.1.3 Originally released | 1 |
| 1.1.4 Terminology | 1 |
| 1.1.5 Method | 2 |
| 1.1.6 References | 2 |
| 1.2 Call order | 3 |
| 1.3 Symmetric matrix storage formats | 3 |
| 1.3.1 Dense storage format | 3 |
| 1.3.2 Sparse co-ordinate storage format | 4 |
| 1.3.3 Sparse row-wise storage format | 4 |
| 2 File Index | 5 |
| 2.1 File List | 5 |
| 3 File Documentation | 7 |
| 3.1 bgo.h File Reference | 7 |
| 3.1.1 Data Structure Documentation | 8 |
| 3.1.1.1 struct bgo_control_type | 8 |
| 3.1.1.2 struct bgo_time_type | 9 |
| 3.1.1.3 struct bgo_inform_type | 9 |
| 3.1.2 Function Documentation | 10 |
| 3.1.2.1 bgo_initialize() | 10 |
| 3.1.2.2 bgo_read_specfile() | 10 |
| 3.1.2.3 bgo_import() | 10 |
| 3.1.2.4 bgo_reset_control() | 12 |
| 3.1.2.5 bgo_solve_with_mat() | 12 |
| 3.1.2.6 bgo_solve_without_mat() | 14 |
| 3.1.2.7 bgo_solve_reverse_with_mat() | 17 |
| 3.1.2.8 bgo_solve_reverse_without_mat() | 21 |
| 3.1.2.9 bgo_information() | 24 |
| 3.1.2.10 bgo_terminate() | 25 |
| 4 Example Documentation | 27 |
| 4.1 bgot.c | 27 |
| 4.2 bgotf.c | 34 |
| Index | 43 |

Chapter 1

GALAHAD C package bgo

1.1 Introduction

1.1.1 Purpose

The bgo package uses a **multi-start trust-region method to find an approximation to the global minimizer of a differentiable objective function $f(x)$ of n variables x , subject to simple bounds $x^l \leq x \leq x^u$ on the variables**. Here, any of the components of the vectors of bounds x^l and x^u may be infinite. The method offers the choice of direct and iterative solution of the key trust-region subproblems, and is suitable for large problems. First derivatives are required, and if second derivatives can be calculated, they will be exploited—if the product of second derivatives with a vector may be found but not the derivatives themselves, that may also be exploited.

The package offers both random multi-start and local-minimize-and probe methods to try to locate the global minimizer. There are no theoretical guarantees unless the sampling is huge, and realistically the success of the methods decreases as the dimension and nonconvexity increase.

1.1.2 Authors

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C interface, additionally J. Fowkes, STFC-Rutherford Appleton Laboratory.

1.1.3 Originally released

July 2016, C interface August 2021.

1.1.4 Terminology

The *gradient* $\nabla_x f(x)$ of $f(x)$ is the vector whose i -th component is $\partial f(x)/\partial x_i$. The *Hessian* $\nabla_{xx} f(x)$ of $f(x)$ is the symmetric matrix whose i, j -th entry is $\partial^2 f(x)/\partial x_i \partial x_j$. The Hessian is *sparse* if a significant and useful proportion of the entries are universally zero.

1.1.5 Method

A choice of two methods is available. In the first, local-minimization-and-probe, approach, local minimization and univariate global minimization are intermixed. Given a current champion x_k^S , a local minimizer x_k of $f(x)$ within the feasible box $x^l \leq x \leq x^u$ is found using the GALAHAD package trb. Thereafter m random directions p are generated, and univariate local minimizer of $f(x_k + \alpha p)$ as a function of the scalar α along each p within the interval $[\alpha^L, \alpha^u]$, where α^L and α^u are the smallest and largest α for which $x^l \leq x_k + \alpha p \leq x^u$, is performed using the GALAHAD package ugo. The point $x_k + \alpha p$ that gives the smallest value of f is then selected as the new champion x_{k+1}^S .

The random directions p are chosen in one of three ways. The simplest is to select the components as

$$p_i = \text{pseudo random} \in \begin{cases} [-1,1] & \text{if } x_i^l < x_{k,i} < x_i^u \\ [0,1] & \text{if } x_{k,i} = x_i^l \\ [-1,0] & \text{if } x_{k,i} = x_i^u \end{cases}$$

for each $1 \leq i \leq n$. An alternative is to pick p by partitioning each dimension of the feasible “hypercube” box into m equal segments, and then selecting sub-boxes randomly within this hypercube using GALAHAD’s Latin hypercube sampling package, lhs. Each components of p is then selected in its sub-box, either uniformly or pseudo randomly.

The other, random-multi-start, method provided selects m starting points at random, either componentwise pseudo randomly in the feasible box, or by partitioning each component into m equal segments, assigning each to a sub-box using Latin hypercube sampling, and finally choosing the values either uniformly or pseudo randomly. Local minimizers within the feasible box are then computed by the GALAHAD package trb, and the best is assigned as the current champion. This process is then repeated until evaluation limits are achieved.

If $n = 1$, the GALAHAD package UGO is called directly.

We reiterate that there are no theoretical guarantees unless the sampling is huge, and realistically the success of the methods decreases as the dimension and nonconvexity increase. Thus the methods used should best be viewed as heuristics.

1.1.6 References

The generic bound-constrained trust-region method is described in detail in

A. R. Conn, N. I. M. Gould and Ph. L. Toint (2000), Trust-region methods. SIAM/MPS Series on Optimization,

the univariate global minimization method employed is an extension of that due to

D. Lera and Ya. D. Sergeyev (2013), “Acceleration of univariate global optimization algorithms working with Lipschitz functions and Lipschitz first derivatives” SIAM J. Optimization Vol. 23, No. 1, pp. 508–529,

while the Latin-hypercube sampling method employed is that of

B. Beachkofski and R. Grandhi (2002). “Improved Distributed Hypercube Sampling”, 43rd AIAA structures, structural dynamics, and materials conference, pp. 2002-1274.

1.2 Call order

To solve a given problem, functions from the bgo package must be called in the following order:

- `bgo_initialize` - provide default control parameters and set up initial data structures
- `bgo_read_specfile` (optional) - override control values by reading replacement values from a file
- `bgo_import` - set up problem data structures and fixed values
- `bgo_reset_control` (optional) - possibly change control parameters if a sequence of problems are being solved
- solve the problem by calling one of
 - `bgo_solve_with_mat` - solve using function calls to evaluate function, gradient and Hessian values
 - `bgo_solve_without_mat` - solve using function calls to evaluate function and gradient values and Hessian-vector products
 - `bgo_solve_reverse_with_mat` - solve returning to the calling program to obtain function, gradient and Hessian values, or
 - `bgo_solve_reverse_without_mat` - solve returning to the calling program to obtain function and gradient values and Hessian-vector products
- `bgo_information` (optional) - recover information about the solution and solution process
- `bgo_terminate` - deallocate data structures

See Section 4.1 for examples of use.

1.3 Symmetric matrix storage formats

The symmetric n by n matrix $H = \nabla_{xx}f$ may be presented and stored in a variety of formats. But crucially symmetry is exploited by only storing values from the lower triangular part (i.e, those entries that lie on or below the leading diagonal).

Both C-style (0 based) and fortran-style (1-based) indexing is allowed. Choose `control.f_indexing` as `false` for C style and `true` for fortran style; the discussion below presumes C style, but add 1 to indices for the corresponding fortran version.

Wrappers will automatically convert between 0-based (C) and 1-based (fortran) array indexing, so may be used transparently from C. This conversion involves both time and memory overheads that may be avoided by supplying data that is already stored using 1-based indexing.

1.3.1 Dense storage format

The matrix H is stored as a compact dense matrix by rows, that is, the values of the entries of each row in turn are stored in order within an appropriate real one-dimensional array. Since H is symmetric, only the lower triangular part (that is the part H_{ij} for $0 \leq j \leq i \leq n - 1$) need be held. In this case the lower triangle should be stored by rows, that is component $i * i/2 + j$ of the storage array `H_val` will hold the value H_{ij} (and, by symmetry, H_{ji}) for $0 \leq j \leq i \leq n - 1$.

1.3.2 Sparse co-ordinate storage format

Only the nonzero entries of the matrices are stored. For the l -th entry, $0 \leq l \leq ne - 1$, of H , its row index i , column index j and value H_{ij} , $0 \leq j \leq i \leq n - 1$, are stored as the l -th components of the integer arrays H_row and H_col and real array H_val , respectively, while the number of nonzeros is recorded as $H_ne = ne$. Note that only the entries in the lower triangle should be stored.

1.3.3 Sparse row-wise storage format

Again only the nonzero entries are stored, but this time they are ordered so that those in row i appear directly before those in row $i+1$. For the i -th row of H the i -th component of the integer array H_ptr holds the position of the first entry in this row, while $H_ptr(n)$ holds the total number of entries plus one. The column indices j , $0 \leq j \leq i$, and values H_{ij} of the entries in the i -th row are stored in components $l = H_ptr(i), \dots, H_ptr(i+1)-1$ of the integer array H_col , and real array H_val , respectively. Note that as before only the entries in the lower triangle should be stored. For sparse matrices, this scheme almost always requires less storage than its predecessor.

Chapter 2

File Index

2.1 File List

Here is a list of all files with brief descriptions:

| | |
|---------------------------------|---|
| bgo.h | 7 |
|---------------------------------|---|

Chapter 3

File Documentation

3.1 bgo.h File Reference

```
#include <stdbool.h>
#include "galahad_precision.h"
#include "trb.h"
#include "ugo.h"
#include "lhs.h"
```

Data Structures

- struct [bgo_control_type](#)
- struct [bgo_time_type](#)
- struct [bgo_inform_type](#)

Functions

- void [bgo_initialize](#) (void **data, struct [bgo_control_type](#) *control, int *status)
- void [bgo_read_specfile](#) (struct [bgo_control_type](#) *control, const char specfile[])
- void [bgo_import](#) (struct [bgo_control_type](#) *control, void **data, int *status, int n, const real_wp_ x_l[], const real_wp_ x_u[], const char H_type[], int ne, const int H_row[], const int H_col[], const int H_ptr[])
- void [bgo_reset_control](#) (struct [bgo_control_type](#) *control, void **data, int *status)
- void [bgo_solve_with_mat](#) (void **data, void *userdata, int *status, int n, real_wp_ x[], real_wp_ g[], int ne, int(*eval_f)(int, const real_wp_[], real_wp_ *, const void *), int(*eval_g)(int, const real_wp_[], real_wp_ [], const void *), int(*eval_h)(int, int, const real_wp_[], real_wp_[], const void *), int(*eval_hprod)(int, const real_wp_[], real_wp_[], const real_wp_[], bool, const void *), int(*eval_prec)(int, const real_wp_[], real_wp_ [], const real_wp_[], const void *))
- void [bgo_solve_without_mat](#) (void **data, void *userdata, int *status, int n, real_wp_ x[], real_wp_ g[], int(*eval_f)(int, const real_wp_[], real_wp_ *, const void *), int(*eval_g)(int, const real_wp_[], real_wp_ [], const void *), int(*eval_hprod)(int, const real_wp_[], real_wp_[], const real_wp_[], bool, const void *), int(*eval_shprod)(int, const real_wp_[], int, const int[], const real_wp_[], int *, int[], real_wp_[], bool, const void *), int(*eval_prec)(int, const real_wp_[], real_wp_[], const real_wp_[], const void *))
- void [bgo_solve_reverse_with_mat](#) (void **data, int *status, int *eval_status, int n, real_wp_ x[], real_wp_ f, real_wp_ g[], int ne, real_wp_ H_val[], const real_wp_ u[], real_wp_ v[])
- void [bgo_solve_reverse_without_mat](#) (void **data, int *status, int *eval_status, int n, real_wp_ x[], real_wp_ f, real_wp_ g[], real_wp_ u[], real_wp_ v[], int index_nz_v[], int *nnz_v, const int index_nz_u[], int nnz_u)
- void [bgo_information](#) (void **data, struct [bgo_inform_type](#) *inform, int *status)
- void [bgo_terminate](#) (void **data, struct [bgo_control_type](#) *control, struct [bgo_inform_type](#) *inform)

3.1.1 Data Structure Documentation

3.1.1.1 struct bgo_control_type

Examples

[bgot.c](#), and [bgotf.c](#).

Data Fields

| | | |
|----------|--------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| bool | f_indexing | use C or Fortran sparse matrix indexing |
| int | error | error and warning diagnostics occur on stream error |
| int | out | general output occurs on stream out |
| int | print_level | the level of output required. Possible values are: <ul style="list-style-type: none"> • ≤ 0 no output, • 1 a one-line summary for every improvement • 2 a summary of each iteration • ≥ 3 increasingly verbose (debugging) output |
| int | attempts_max | the maximum number of random searches from the best point found so far |
| int | max_evals | the maximum number of function evaluations made |
| int | sampling_strategy | sampling strategy used. Possible values are <ul style="list-style-type: none"> • 1 uniformly spread • 2 Latin hypercube sampling • 3 niformly spread within a Latin hypercube |
| int | hypercube_discretization | hyper-cube discretization (for sampling strategies 2 and 3) |
| int | alive_unit | removal of the file alive_file from unit alive_unit terminates execution |
| char | alive_file[31] | see alive_unit |
| real_wp_ | infinity | any bound larger than infinity in modulus will be regarded as infinite |
| real_wp_ | obj_unbounded | the smallest value the objective function may take before the problem is marked as unbounded |
| real_wp_ | cpu_time_limit | the maximum CPU time allowed (-ve means infinite) |
| real_wp_ | clock_time_limit | the maximum elapsed clock time allowed (-ve means infinite) |
| bool | random_multistart | perform random-multistart as opposed to local minimize and probe |
| bool | hessian_available | is the Hessian matrix of second derivatives available or is access only via matrix-vector products? |
| bool | space_critical | if .space_critical true, every effort will be made to use as little space as possible. This may result in longer computation time |
| bool | deallocate_error_fatal | if .deallocate_error_fatal is true, any array/pointer deallocation error will terminate execution. Otherwise, computation will continue |

Data Fields

| | | |
|-------------------------|-------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------|
| char | prefix[31] | all output lines will be prefixed by .prefix(2:LEN(TRIM(.prefix))-1) where .prefix contains the required string enclosed in quotes, e.g. "string" or 'string' |
| struct trb_control_type | trb_control | control parameters for TRB |
| struct ugo_control_type | ugo_control | control parameters for UGO |
| struct lhs_control_type | lhs_control | control parameters for LHS |

3.1.1.2 struct bgo_time_type

Data Fields

| | | |
|----------|--------------------------|-----------------------------------------------------------------|
| real_sp_ | total | the total CPU time spent in the package |
| real_sp_ | univariate_global | the CPU time spent performing univariate global optimization |
| real_sp_ | multivariate_local | the CPU time spent performing multivariate local optimization |
| real_wp_ | clock_total | the total clock time spent in the package |
| real_wp_ | clock_univariate_global | the clock time spent performing univariate global optimization |
| real_wp_ | clock_multivariate_local | the clock time spent performing multivariate local optimization |

3.1.1.3 struct bgo_inform_type

Examples

[bgot.c](#), and [bgotf.c](#).

Data Fields

| | | |
|--------------------------------------|---------------|---------------------------------------------------------------------------------------------------------------------------|
| int | status | return status. See BGO_solve for details |
| int | alloc_status | the status of the last attempted allocation/deallocation |
| char | bad_alloc[81] | the name of the array for which an allocation/deallocation error occurred |
| int | f_eval | the total number of evaluations of the objection function |
| int | g_eval | the total number of evaluations of the gradient of the objection function |
| int | h_eval | the total number of evaluations of the Hessian of the objection function |
| real_wp_ | obj | the value of the objective function at the best estimate of the solution determined by BGO_solve |
| real_wp_ | norm_pg | the norm of the projected gradient of the objective function at the best estimate of the solution determined by BGO_solve |
| struct bgo_time_type | time | timings (see above) |
| struct trb_inform_type | trb_inform | inform parameters for TRB |
| struct ugo_inform_type | ugo_inform | inform parameters for UGO |
| struct lhs_inform_type | lhs_inform | inform parameters for LHS |

3.1.2 Function Documentation

3.1.2.1 `bgo_initialize()`

```
void bgo_initialize (
    void ** data,
    struct bgo_control_type * control,
    int * status )
```

Set default control values and initialize private data

Parameters

| | | |
|---------|----------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| in, out | <i>data</i> | holds private internal data |
| out | <i>control</i> | is a struct containing control information (see bgo_control_type) |
| out | <i>status</i> | is a scalar variable of type int, that gives the exit status from the package. Possible values are (currently): <ul style="list-style-type: none"> • 0. The import was succesful. |

Examples

[bgot.c](#), and [bgotf.c](#).

3.1.2.2 `bgo_read_specfile()`

```
void bgo_read_specfile (
    struct bgo_control_type * control,
    const char specfile[] )
```

Read the content of a specification file, and assign values associated with given keywords to the corresponding control parameters

Parameters

| | | |
|---------|-----------------|------------------------------------------------------------------------------------|
| in, out | <i>control</i> | is a struct containing control information (see bgo_control_type) |
| in | <i>specfile</i> | is a character string containing the name of the specification file |

3.1.2.3 `bgo_import()`

```
void bgo_import (
    struct bgo_control_type * control,
```

```

void ** data,
int * status,
int n,
const real_wp_ x_l[],
const real_wp_ x_u[],
const char H_type[],
int ne,
const int H_row[],
const int H_col[],
const int H_ptr[] )

```

Import problem data into internal storage prior to solution.

Parameters

| | | |
|---------|----------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| in | <i>control</i> | is a struct whose members provide control paramters for the remaining prcedures (see bgo_control_type) |
| in, out | <i>data</i> | holds private internal data |
| in, out | <i>status</i> | is a scalar variable of type int, that gives the exit status from the package. Possible values are: <ul style="list-style-type: none"> • 1. The import was succesful, and the package is ready for the solve phase • -1. An allocation error occurred. A message indicating the offending array is written on unit control.error, and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. • -2. A deallocation error occurred. A message indicating the offending array is written on unit control.error and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. • -3. The restriction $n > 0$ or requirement that type contains its relevant string 'dense', 'coordinate', 'sparse_by_rows', 'diagonal' or 'absent' has been violated. |
| in | <i>n</i> | is a scalar variable of type int, that holds the number of variables. |
| in | <i>x_l</i> | is a one-dimensional array of size n and type double, that holds the values x^l of the lower bounds on the optimization variables x . The j-th component of x_l , $j = 0, \dots, n - 1$, contains x_j^l . |
| in | <i>x_u</i> | is a one-dimensional array of size n and type double, that holds the values x^u of the upper bounds on the optimization variables x . The j-th component of x_u , $j = 0, \dots, n - 1$, contains x_j^u . |
| in | <i>H_type</i> | is a one-dimensional array of type char that specifies the symmetric storage scheme used for the Hessian. It should be one of 'coordinate', 'sparse_by_rows', 'dense', 'diagonal' or 'absent', the latter if access to the Hessian is via matrix-vector products; lower or upper case variants are allowed. |
| in | <i>ne</i> | is a scalar variable of type int, that holds the number of entries in the lower triangular part of H in the sparse co-ordinate storage scheme. It need not be set for any of the other three schemes. |
| in | <i>H_row</i> | is a one-dimensional array of size ne and type int, that holds the row indices of the lower triangular part of H in the sparse co-ordinate storage scheme. It need not be set for any of the other three schemes, and in this case can be NULL |
| in | <i>H_col</i> | is a one-dimensional array of size ne and type int, that holds the column indices of the lower triangular part of H in either the sparse co-ordinate, or the sparse row-wise storage scheme. It need not be set when the dense or diagonal storage schemes are used, and in this case can be NULL |

Parameters

| | | |
|----|--------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| in | <i>H_ptr</i> | is a one-dimensional array of size n+1 and type int, that holds the starting position of each row of the lower triangular part of H, as well as the total number of entries plus one, in the sparse row-wise storage scheme. It need not be set when the other schemes are used, and in this case can be NULL |
|----|--------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Examples

[bgot.c](#), and [bgotf.c](#).

3.1.2.4 bgo_reset_control()

```
void bgo_reset_control (
    struct bgo_control_type * control,
    void ** data,
    int * status )
```

Reset control parameters after import if required.

Parameters

| | | |
|---------|----------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| in | <i>control</i> | is a struct whose members provide control paramters for the remaining pcedures (see bgo_control_type) |
| in, out | <i>data</i> | holds private internal data |
| in, out | <i>status</i> | is a scalar variable of type int, that gives the exit status from the package. Possible values are: <ul style="list-style-type: none"> 1. The import was succesful, and the package is ready for the solve phase |

3.1.2.5 bgo_solve_with_mat()

```
void bgo_solve_with_mat (
    void ** data,
    void * userdata,
    int * status,
    int n,
    real_wp_ x[],
    real_wp_ g[],
    int ne,
    int(*) (int, const real_wp_[], real_wp_ *, const void *) eval_f,
    int(*) (int, const real_wp_[], real_wp_[], const void *) eval_g,
    int(*) (int, int, const real_wp_[], real_wp_[], const void *) eval_h,
    int(*) (int, const real_wp_[], real_wp_[], const real_wp_[], bool, const void *)
eval_hprod,
    int(*) (int, const real_wp_[], real_wp_[], const real_wp_[], const void *) eval_↔
prec )
```


Find an approximation to the global minimizer of a given function subject to simple bounds on the variables using a multistart trust-region method.

This call is for the case where $H = \nabla_{xx}f(x)$ is provided specifically, and all function/derivative information is available by function calls.

Parameters

| | | |
|---------|-----------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| in, out | <i>data</i> | holds private internal data |
| in | <i>userdata</i> | is a structure that allows data to be passed into the function and derivative evaluation programs. |
| in, out | <i>status</i> | <p>is a scalar variable of type int, that gives the entry and exit status from the package. On initial entry, status must be set to 1. Possible exit are:</p> <ul style="list-style-type: none"> • 0. The run was succesful • -1. An allocation error occurred. A message indicating the offending array is written on unit control.error, and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. • -2. A deallocation error occurred. A message indicating the offending array is written on unit control.error and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. • -3. The restriction $n > 0$ or requirement that type contains its relevant string 'dense', 'coordinate', 'sparse_by_rows', 'diagonal' or 'absent' has been violated. • -7. The objective function appears to be unbounded from below • -9. The analysis phase of the factorization failed; the return status from the factorization package is given in the component inform.factor_status • -10. The factorization failed; the return status from the factorization package is given in the component inform.factor_status. • -11. The solution of a set of linear equations using factors from the factorization package failed; the return status from the factorization package is given in the component inform.factor_status. • -16. The problem is so ill-conditioned that further progress is impossible. • -18. Too many iterations have been performed. This may happen if control.maxit is too small, but may also be symptomatic of a badly scaled problem. • -19. The CPU time limit has been reached. This may happen if control.cpu_time_limit is too small, but may also be symptomatic of a badly scaled problem. • -40. The user has forced termination of solver by removing the file named control.alive_file from unit unit control.alive_unit. |
| in | <i>n</i> | is a scalar variable of type int, that holds the number of variables |
| in, out | <i>x</i> | is a one-dimensional array of size n and type double, that holds the values x of the optimization variables. The j-th component of x , $j = 0, \dots, n-1$, contains x_j . |
| in, out | <i>g</i> | is a one-dimensional array of size n and type double, that holds the gradient $g = \nabla_x f(x)$ of the objective function. The j-th component of g , $j = 0, \dots, n-1$, contains g_j . |

Parameters

| | | |
|-----------------|------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>in</code> | <code>ne</code> | is a scalar variable of type <code>int</code> , that holds the number of entries in the lower triangular part of the Hessian matrix H . |
| | <code>eval_f</code> | is a user-supplied function that must have the following signature: <pre>int eval_f(int n, const double x[], double *f, const void *userdata)</pre> The value of the objective function $f(x)$ evaluated at $x = x$ must be assigned to <code>f</code> , and the function return value set to 0. If the evaluation is impossible at x , return should be set to a nonzero value. Data may be passed into <code>eval_f</code> via the structure <code>userdata</code> . |
| | <code>eval_g</code> | is a user-supplied function that must have the following signature: <pre>int eval_g(int n, const double x[], double g[], const void *userdata)</pre> The components of the gradient $g = \nabla_x f(x)$ of the objective function evaluated at $x = x$ must be assigned to <code>g</code> , and the function return value set to 0. If the evaluation is impossible at x , return should be set to a nonzero value. Data may be passed into <code>eval_g</code> via the structure <code>userdata</code> . |
| | <code>eval_h</code> | is a user-supplied function that must have the following signature: <pre>int eval_h(int n, int ne, const double x[], double h[], const void *userdata)</pre> The nonzeros of the Hessian $H = \nabla_{xx} f(x)$ of the objective function evaluated at $x = x$ must be assigned to <code>h</code> in the same order as presented to <code>bgo_import</code> , and the function return value set to 0. If the evaluation is impossible at x , return should be set to a nonzero value. Data may be passed into <code>eval_h</code> via the structure <code>userdata</code> . |
| | <code>eval_prec</code> | is an optional user-supplied function that may be <code>NULL</code> . If non- <code>NULL</code> , it must have the following signature: <pre>int eval_prec(int n, const double x[], double u[], const double v[], const void *userdata)</pre> The product $u = P(x)v$ of the user's preconditioner $P(x)$ evaluated at x with the vector $v = v$, the result u must be returned in <code>u</code> , and the function return value set to 0. If the evaluation is impossible at x , return should be set to a nonzero value. Data may be passed into <code>eval_prec</code> via the structure <code>userdata</code> . |

Examples

[bgot.c](#), and [bgotf.c](#).

3.1.2.6 bgo_solve_without_mat()

```
void bgo_solve_without_mat (
    void ** data,
    void * userdata,
    int * status,
    int n,
    real_wp_ x[],
    real_wp_ g[],
    int(*) (int, const real_wp_[], real_wp_ *, const void *) eval_f,
    int(*) (int, const real_wp_[], real_wp_[], const void *) eval_g,
    int(*) (int, const real_wp_[], real_wp_[], const real_wp_[], bool, const void *)
eval_hprod,
    int(*) (int, const real_wp_[], int, const int[], const real_wp_[], int *, int[],
real_wp_[], bool, const void *) eval_shprod,
    int(*) (int, const real_wp_[], real_wp_[], const real_wp_[], const void *) eval_←
prec )
```

Find an approximation to the global minimizer of a given function subject to simple bounds on the variables using a multistart trust-region method.

This call is for the case where access to $H = \nabla_{xx}f(x)$ is provided by Hessian-vector products, and all function/derivative information is available by function calls.

Parameters

| | | |
|----------------|-----------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <i>in, out</i> | <i>data</i> | holds private internal data |
| <i>in</i> | <i>userdata</i> | is a structure that allows data to be passed into the function and derivative evaluation programs. |
| <i>in, out</i> | <i>status</i> | <p>is a scalar variable of type int, that gives the entry and exit status from the package. On initial entry, status must be set to 1. Possible exit are:</p> <ul style="list-style-type: none"> • 0. The run was succesful • -1. An allocation error occurred. A message indicating the offending array is written on unit control.error, and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. • -2. A deallocation error occurred. A message indicating the offending array is written on unit control.error and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. • -3. The restriction $n > 0$ or requirement that type contains its relevant string 'dense', 'coordinate', 'sparse_by_rows', 'diagonal' or 'absent' has been violated. • -7. The objective function appears to be unbounded from below • -9. The analysis phase of the factorization failed; the return status from the factorization package is given in the component inform.factor_status • -10. The factorization failed; the return status from the factorization package is given in the component inform.factor_status. • -11. The solution of a set of linear equations using factors from the factorization package failed; the return status from the factorization package is given in the component inform.factor_status. • -16. The problem is so ill-conditioned that further progress is impossible. • -18. Too many iterations have been performed. This may happen if control.maxit is too small, but may also be symptomatic of a badly scaled problem. • -19. The CPU time limit has been reached. This may happen if control.cpu_time_limit is too small, but may also be symptomatic of a badly scaled problem. • -40. The user has forced termination of solver by removing the file named control.alive_file from unit unit control.alive_unit. |
| <i>in</i> | <i>n</i> | is a scalar variable of type int, that holds the number of variables |
| <i>in, out</i> | <i>x</i> | is a one-dimensional array of size n and type double, that holds the values x of the optimization variables. The j-th component of x , $j = 0, \dots, n-1$, contains x_j . |
| <i>in, out</i> | <i>g</i> | is a one-dimensional array of size n and type double, that holds the gradient $g = \nabla_x f(x)$ of the objective function. The j-th component of g , $j = 0, \dots, n-1$, contains g_j . |

Parameters

| | | |
|--|--------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| | <i>eval_f</i> | <p>is a user-supplied function that must have the following signature:</p> <pre>int eval_f(int n, const double x[], double *f, const void *userdata)</pre> <p>The value of the objective function $f(x)$ evaluated at $x = x$ must be assigned to f, and the function return value set to 0. If the evaluation is impossible at x, return should be set to a nonzero value. Data may be passed into <i>eval_f</i> via the structure <i>userdata</i>.</p> |
| | <i>eval_g</i> | <p>is a user-supplied function that must have the following signature:</p> <pre>int eval_g(int n, const double x[], double g[], const void *userdata)</pre> <p>The components of the gradient $g = \nabla_x f(x)$ of the objective function evaluated at $x = x$ must be assigned to g, and the function return value set to 0. If the evaluation is impossible at x, return should be set to a nonzero value. Data may be passed into <i>eval_g</i> via the structure <i>userdata</i>.</p> |
| | <i>eval_hprod</i> | <p>is a user-supplied function that must have the following signature:</p> <pre>int eval_hprod(int n, const double x[], double u[], const double v[], bool got_h, const void *userdata)</pre> <p>The sum $u + \nabla_{xx} f(x)v$ of the product of the Hessian $\nabla_{xx} f(x)$ of the objective function evaluated at $x = x$ with the vector $v = v$ and the vector u must be returned in u, and the function return value set to 0. If the evaluation is impossible at x, return should be set to a nonzero value. The Hessian has already been evaluated or used at x if <i>got_h</i> is true. Data may be passed into <i>eval_hprod</i> via the structure <i>userdata</i>.</p> |
| | <i>eval_shprod</i> | <p>is a user-supplied function that must have the following signature:</p> <pre>int eval_shprod(int n, const double x[], int nnz_v, const int index_nz_v[], const double v[], int *nnz_u, int index_nz_u[], double u[], bool got_h, const void *userdata)</pre> <p>The product $u = \nabla_{xx} f(x)v$ of the Hessian $\nabla_{xx} f(x)$ of the objective function evaluated at x with the sparse vector $v = v$ must be returned in u, and the function return value set to 0. Only the components $\text{index_nz_v}[0:\text{nnz_v}-1]$ of v are nonzero, and the remaining components may not have been set. On exit, the user must indicate the <i>nnz_u</i> indices of u that are nonzero in $\text{index_nz_u}[0:\text{nnz_u}-1]$, and only these components of u need be set. If the evaluation is impossible at x, return should be set to a nonzero value. The Hessian has already been evaluated or used at x if <i>got_h</i> is true. Data may be passed into <i>eval_prec</i> via the structure <i>userdata</i>.</p> |
| | <i>eval_prec</i> | <p>is an optional user-supplied function that may be NULL. If non-NULL, it must have the following signature:</p> <pre>int eval_prec(int n, const double x[], double u[], const double v[], const void *userdata)</pre> <p>The product $u = P(x)v$ of the user's preconditioner $P(x)$ evaluated at x with the vector $v = v$, the result u must be returned in u, and the function return value set to 0. If the evaluation is impossible at x, return should be set to a nonzero value. Data may be passed into <i>eval_prec</i> via the structure <i>userdata</i>.</p> |

Examples

[bgotf.c](#), and [bgotf.c](#).

3.1.2.7 bgo_solve_reverse_with_mat()

```
void bgo_solve_reverse_with_mat (
    void ** data,
    int * status,
```

```

    int * eval_status,
    int n,
    real_wp_ x[],
    real_wp_ f,
    real_wp_ g[],
    int ne,
    real_wp_ H_val[],
    const real_wp_ u[],
    real_wp_ v[] )

```

Find an approximation to the global minimizer of a given function subject to simple bounds on the variables using a multistart trust-region method.

This call is for the case where $H = \nabla_{xx}f(x)$ is provided specifically, but function/derivative information is only available by returning to the calling procedure

Parameters

| | | |
|---------|-------------|-----------------------------|
| in, out | <i>data</i> | holds private internal data |
|---------|-------------|-----------------------------|

Parameters

| | | |
|----------------------|---------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>in, out</code> | <code>status</code> | <p>is a scalar variable of type <code>int</code>, that gives the entry and exit status from the package.</p> <p>On initial entry, <code>status</code> must be set to 1. Possible exit are:</p> <ul style="list-style-type: none"> • 0. The run was succesful • -1. An allocation error occurred. A message indicating the offending array is written on <code>unit.control.error</code>, and the returned allocation status and a string containing the name of the offending array are held in <code>inform.alloc_status</code> and <code>inform.bad_alloc</code> respectively. • -2. A deallocation error occurred. A message indicating the offending array is written on <code>unit.control.error</code> and the returned allocation status and a string containing the name of the offending array are held in <code>inform.alloc_status</code> and <code>inform.bad_alloc</code> respectively. • -3. The restriction $n > 0$ or requirement that <code>type</code> contains its relevant string 'dense', 'coordinate', 'sparse_by_rows', 'diagonal' or 'absent' has been violated. • -7. The objective function appears to be unbounded from below • -9. The analysis phase of the factorization failed; the return status from the factorization package is given in the component <code>inform.factor_status</code> • -10. The factorization failed; the return status from the factorization package is given in the component <code>inform.factor_status</code>. • -11. The solution of a set of linear equations using factors from the factorization package failed; the return status from the factorization package is given in the component <code>inform.factor_status</code>. • -16. The problem is so ill-conditioned that further progress is impossible. • -18. Too many iterations have been performed. This may happen if <code>control.maxit</code> is too small, but may also be symptomatic of a badly scaled problem. • -19. The CPU time limit has been reached. This may happen if <code>control.cpu_time_limit</code> is too small, but may also be symptomatic of a badly scaled problem. • -40. The user has forced termination of solver by removing the file named <code>control.alive_file</code> from unit <code>unit.control.alive_unit</code>. |
|----------------------|---------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Parameters

| | | |
|----------------|--------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| | <i>status</i> | <p>(continued)</p> <ul style="list-style-type: none"> • 2. The user should compute the objective function value $f(x)$ at the point x indicated in x and then re-enter the function. The required value should be set in f, and $eval_status$ should be set to 0. If the user is unable to evaluate $f(x)$— for instance, if the function is undefined at x— the user need not set f, but should then set $eval_status$ to a non-zero value. • 3. The user should compute the gradient of the objective function $\nabla_x f(x)$ at the point x indicated in x and then re-enter the function. The value of the i-th component of the g gradient should be set in $g[i]$, for $i = 0, \dots, n-1$ and $eval_status$ should be set to 0. If the user is unable to evaluate a component of $\nabla_x f(x)$ — for instance if a component of the gradient is undefined at x — the user need not set g, but should then set $eval_status$ to a non-zero value. • 4. The user should compute the Hessian of the objective function $\nabla_{xx} f(x)$ at the point x indicated in x and then re-enter the function. The value l-th component of the Hessian stored according to the scheme input in the remainder of H should be set in $H_val[l]$, for $l = 0, \dots, ne-1$ and $eval_status$ should be set to 0. If the user is unable to evaluate a component of $\nabla_{xx} f(x)$ — for instance, if a component of the Hessian is undefined at x — the user need not set H_val, but should then set $eval_status$ to a non-zero value. • 5. The user should compute the product $\nabla_{xx} f(x)v$ of the Hessian of the objective function $\nabla_{xx} f(x)$ at the point x indicated in x with the vector v, add the result to the vector u and then re-enter the function. The vectors u and v are given in u and v respectively, the resulting vector $u + \nabla_{xx} f(x)v$ should be set in u and $eval_status$ should be set to 0. If the user is unable to evaluate the product— for instance, if a component of the Hessian is undefined at x — the user need not alter u, but should then set $eval_status$ to a non-zero value. • 6. The user should compute the product $u = P(x)v$ of their preconditioner $P(x)$ at the point x indicated in x with the vector v and then re-enter the function. The vector v is given in v, the resulting vector $u = P(x)v$ should be set in u and $eval_status$ should be set to 0. If the user is unable to evaluate the product— for instance, if a component of the preconditioner is undefined at x — the user need not set u, but should then set $eval_status$ to a non-zero value. • 23. The user should follow the instructions for 2 and 3 above before returning. • 25. The user should follow the instructions for 2 and 5 above before returning. • 35. The user should follow the instructions for 3 and 5 above before returning. • 235. The user should follow the instructions for 2, 3 and 5 above before returning. |
| <i>in, out</i> | <i>eval_status</i> | is a scalar variable of type int, that is used to indicate if objective function/gradient/Hessian values can be provided (see above) |
| <i>in</i> | <i>n</i> | is a scalar variable of type int, that holds the number of variables |
| <i>in, out</i> | <i>x</i> | is a one-dimensional array of size n and type double, that holds the values x of the optimization variables. The j -th component of x , $j = 0, \dots, n-1$, contains x_j . |
| <i>in</i> | <i>f</i> | is a scalar variable pointer of type double, that holds the value of the objective function. |

Parameters

| | | |
|---------|--------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| in, out | <i>g</i> | is a one-dimensional array of size n and type double, that holds the gradient $g = \nabla_x f(x)$ of the objective function. The j-th component of g, $j = 0, \dots, n-1$, contains g_j . |
| in | <i>ne</i> | is a scalar variable of type int, that holds the number of entries in the lower triangular part of the Hessian matrix H . |
| in | <i>H_val</i> | is a one-dimensional array of size ne and type double, that holds the values of the entries of the lower triangular part of the Hessian matrix H in any of the available storage schemes. |
| in | <i>u</i> | is a one-dimensional array of size n and type double, that is used for reverse communication (see above for details) |
| in, out | <i>v</i> | is a one-dimensional array of size n and type double, that is used for reverse communication (see above for details) |

Examples

[bgot.c](#), and [bgottf.c](#).

3.1.2.8 bgo_solve_reverse_without_mat()

```
void bgo_solve_reverse_without_mat (
    void ** data,
    int * status,
    int * eval_status,
    int n,
    real_wp_ x[],
    real_wp_ f,
    real_wp_ g[],
    real_wp_ u[],
    real_wp_ v[],
    int index_nz_v[],
    int * nnz_v,
    const int index_nz_u[],
    int nnz_u )
```

Find an approximation to the global minimizer of a given function subject to simple bounds on the variables using a multistart trust-region method.

This call is for the case where access to $H = \nabla_{xx} f(x)$ is provided by Hessian-vector products, but function/derivative information is only available by returning to the calling procedure.

Parameters

| | | |
|---------|-------------|-----------------------------|
| in, out | <i>data</i> | holds private internal data |
|---------|-------------|-----------------------------|

Parameters

| | | |
|----------------------|---------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>in, out</code> | <code>status</code> | <p>is a scalar variable of type <code>int</code>, that gives the entry and exit status from the package.</p> <p>On initial entry, status must be set to 1. Possible exit are:</p> <ul style="list-style-type: none"> • 0. The run was succesful • -1. An allocation error occurred. A message indicating the offending array is written on <code>unit control.error</code>, and the returned allocation status and a string containing the name of the offending array are held in <code>inform.alloc_status</code> and <code>inform.bad_alloc</code> respectively. • -2. A deallocation error occurred. A message indicating the offending array is written on <code>unit control.error</code> and the returned allocation status and a string containing the name of the offending array are held in <code>inform.alloc_status</code> and <code>inform.bad_alloc</code> respectively. • -3. The restriction $n > 0$ or requirement that type contains its relevant string 'dense', 'coordinate', 'sparse_by_rows', 'diagonal' or 'absent' has been violated. • -7. The objective function appears to be unbounded from below • -9. The analysis phase of the factorization failed; the return status from the factorization package is given in the component <code>inform.factor_status</code> • -10. The factorization failed; the return status from the factorization package is given in the component <code>inform.factor_status</code>. • -11. The solution of a set of linear equations using factors from the factorization package failed; the return status from the factorization package is given in the component <code>inform.factor_status</code>. • -16. The problem is so ill-conditioned that further progress is impossible. • -18. Too many iterations have been performed. This may happen if <code>control.maxit</code> is too small, but may also be symptomatic of a badly scaled problem. • -19. The CPU time limit has been reached. This may happen if <code>control.cpu_time_limit</code> is too small, but may also be symptomatic of a badly scaled problem. • -40. The user has forced termination of solver by removing the file named <code>control.alive_file</code> from unit <code>unit control.alive_unit</code>. |
|----------------------|---------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Parameters

| | | |
|----------------|--------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| | <i>status</i> | <p>(continued)</p> <ul style="list-style-type: none"> • 2. The user should compute the objective function value $f(x)$ at the point x indicated in x and then re-enter the function. The required value should be set in f, and <code>eval_status</code> should be set to 0. If the user is unable to evaluate $f(x)$ — for instance, if the function is undefined at x — the user need not set f, but should then set <code>eval_status</code> to a non-zero value. • 3. The user should compute the gradient of the objective function $\nabla_x f(x)$ at the point x indicated in x and then re-enter the function. The value of the i-th component of the gradient should be set in $g[i]$, for $i = 0, \dots, n-1$ and <code>eval_status</code> should be set to 0. If the user is unable to evaluate a component of $\nabla_x f(x)$ — for instance if a component of the gradient is undefined at x — the user need not set g, but should then set <code>eval_status</code> to a non-zero value. • 5. The user should compute the product $\nabla_{xx} f(x)v$ of the Hessian of the objective function $\nabla_{xx} f(x)$ at the point x indicated in x with the vector v, add the result to the vector u and then re-enter the function. The vectors u and v are given in u and v respectively, the resulting vector $u + \nabla_{xx} f(x)v$ should be set in u and <code>eval_status</code> should be set to 0. If the user is unable to evaluate the product — for instance, if a component of the Hessian is undefined at x — the user need not alter u, but should then set <code>eval_status</code> to a non-zero value. • 6. The user should compute the product $u = P(x)v$ of their preconditioner $P(x)$ at the point x indicated in x with the vector v and then re-enter the function. The vector v is given in v, the resulting vector $u = P(x)v$ should be set in u and <code>eval_status</code> should be set to 0. If the user is unable to evaluate the product — for instance, if a component of the preconditioner is undefined at x — the user need not set u, but should then set <code>eval_status</code> to a non-zero value. • 7. The user should compute the product $u = \nabla_{xx} f(x)v$ of the Hessian of the objective function $\nabla_{xx} f(x)$ at the point x indicated in x with the sparse vector $v = v$ and then re-enter the function. The nonzeros of v are stored in <code>v[index_nz_v[0:nnz_v-1]]</code> while the nonzeros of u should be returned in <code>u[index_nz_u[0:nnz_u-1]]</code>; the user must set <code>nnz_u</code> and <code>index_nz_u</code> accordingly, and set <code>eval_status</code> to 0. If the user is unable to evaluate the product — for instance, if a component of the Hessian is undefined at x — the user need not alter u, but should then set <code>eval_status</code> to a non-zero value. • 23. The user should follow the instructions for 2 and 3 above before returning. • 25. The user should follow the instructions for 2 and 5 above before returning. • 35. The user should follow the instructions for 3 and 5 above before returning. • 235. The user should follow the instructions for 2, 3 and 5 above before returning. |
| <i>in, out</i> | <i>eval_status</i> | is a scalar variable of type <code>int</code> , that is used to indicate if objective function/gradient/Hessian values can be provided (see above) |
| <i>in</i> | <i>n</i> | is a scalar variable of type <code>int</code> , that holds the number of variables |
| <i>in, out</i> | <i>x</i> | is a one-dimensional array of size n and type <code>double</code> , that holds the values x of the optimization variables. The j -th component of x , $j = 0, \dots, n-1$, contains x_j . |

Parameters

| | | |
|---------|-------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| in | <i>f</i> | is a scalar variable pointer of type double, that holds the value of the objective function. |
| in, out | <i>g</i> | is a one-dimensional array of size n and type double, that holds the gradient $g = \nabla_x f(x)$ of the objective function. The j-th component of g, $j = 0, \dots, n-1$, contains g_j . |
| in, out | <i>u</i> | is a one-dimensional array of size n and type double, that is used for reverse communication (see status=5,6,7 above for details) |
| in, out | <i>v</i> | is a one-dimensional array of size n and type double, that is used for reverse communication (see status=5,6,7 above for details) |
| in, out | <i>index_nz↔ _v</i> | is a one-dimensional array of size n and type int, that is used for reverse communication (see status=7 above for details) |
| in, out | <i>nnz_v</i> | is a scalar variable of type int, that is used for reverse communication (see status=7 above for details) |
| in | <i>index_nz↔ _u</i> | is a one-dimensional array of size n and type int, that is used for reverse communication (see status=7 above for details) |
| in | <i>nnz_u</i> | is a scalar variable of type int, that is used for reverse communication (see status=7 above for details). On initial (status=1) entry, nnz_u should be set to an (arbitrary) nonzero value, and nnz_u=0 is recommended |

Examples

[bgot.c](#), and [bgotf.c](#).

3.1.2.9 bgo_information()

```
void bgo_information (
    void ** data,
    struct bgo_inform_type * inform,
    int * status )
```

Provides output information

Parameters

| | | |
|---------|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| in, out | <i>data</i> | holds private internal data |
| out | <i>inform</i> | is a struct containing output information (see bgo_inform_type) |
| out | <i>status</i> | is a scalar variable of type int, that gives the exit status from the package. Possible values are (currently): <ul style="list-style-type: none"> • 0. The values were recorded succesfully |

Examples

[bgot.c](#), and [bgotf.c](#).

3.1.2.10 bgo_terminate()

```
void bgo_terminate (
    void ** data,
    struct bgo\_control\_type * control,
    struct bgo\_inform\_type * inform )
```

Deallocate all internal private storage

Parameters

| | | |
|---------|----------------|------------------------------------------------------------------------------------|
| in, out | <i>data</i> | holds private internal data |
| out | <i>control</i> | is a struct containing control information (see bgo_control_type) |
| out | <i>inform</i> | is a struct containing output information (see bgo_inform_type) |

Examples

[bgot.c](#), and [bgotf.c](#).

Chapter 4

Example Documentation

4.1 bgot.c

This is an example of how to use the package to find an approximation to the global minimum of a given function within a bounded region. A variety of supported Hessian and constraint matrix storage formats are shown.

Notice that C-style indexing is used, and that this is flagged by setting `control.f_indexing` to `false`.

```
/* bgot.c */
/* Full test for the BGO C interface using C sparse matrix indexing */
#include <stdio.h>
#include <math.h>
#include "bgo.h"
// Custom userdata struct
struct userdata_type {
    double p;
    double freq;
    double mag;
};
// Function prototypes
int fun( int n, const double x[], double *f, const void * );
int grad( int n, const double x[], double g[], const void * );
int hess( int n, int ne, const double x[], double hval[], const void * );
int hess_dense( int n, int ne, const double x[], double hval[], const void * );
int hessprod( int n, const double x[], double u[], const double v[],
    bool got_h, const void * );
int shessprod( int n, const double x[], int nnz_v, const int index_nz_v[],
    const double v[], int *nnz_u, int index_nz_u[], double u[],
    bool got_h, const void * );
int prec( int n, const double x[], double u[], const double v[], const void * );
int fun_diag( int n, const double x[], double *f, const void * );
int grad_diag( int n, const double x[], double g[], const void * );
int hess_diag( int n, int ne, const double x[], double hval[], const void * );
int hessprod_diag( int n, const double x[], double u[], const double v[],
    bool got_h, const void * );
int shessprod_diag( int n, const double x[], int nnz_v, const int index_nz_v[],
    const double v[], int *nnz_u, int index_nz_u[],
    double u[], bool got_h, const void * );

int main(void) {
    // Derived types
    void *data;
    struct bgo_control_type control;
    struct bgo_inform_type inform;
    // Set user data
    struct userdata_type userdata;
    userdata.p = 4.0;
    userdata.freq = 10;
    userdata.mag = 1000;
    // Set problem data
    int n = 3; // dimension
    int ne = 5; // Hesssian elements
    double x_l[] = {-10,-10,-10};
    double x_u[] = {0.5,0.5,0.5};
    int H_row[] = {0, 1, 2, 2, 2}; // Hessian H
    int H_col[] = {0, 1, 0, 1, 2}; // NB lower triangle
```

```

int H_ptr[] = {0, 1, 2, 5};    // row pointers
// Set storage
double g[n]; // gradient
char st;
int status;
printf(" C sparse matrix indexing\n\n");
printf(" tests options for all-in-one storage format\n\n");
for(int d=1; d <= 5; d++){
    // Initialize BGO
    bgo_initialize( &data, &control, &status );
    // Set user-defined control options
    control.f_indexing = false; // C sparse matrix indexing
    control.attempts_max = 10000;
    control.max_evals = 20000;
    control.sampling_strategy = 3;
    control.trb_control.maxit = 100;
    //control.print_level = 1;
    // Start from 0
    double x[] = {0,0,0};
    switch(d){
        case 1: // sparse co-ordinate storage
            st = 'C';
            bgo_import( &control, &data, &status, n, x_l, x_u,
                        "coordinate", ne, H_row, H_col, NULL );
            bgo_solve_with_mat( &data, &userdata, &status, n, x, g,
                                ne, fun, grad, hess, hessprod, prec );
            break;
        case 2: // sparse by rows
            st = 'R';
            bgo_import( &control, &data, &status, n, x_l, x_u,
                        "sparse_by_rows", ne, NULL, H_col, H_ptr );
            bgo_solve_with_mat( &data, &userdata, &status, n, x, g,
                                ne, fun, grad, hess, hessprod, prec );
            break;
        case 3: // dense
            st = 'D';
            bgo_import( &control, &data, &status, n, x_l, x_u,
                        "dense", ne, NULL, NULL, NULL );
            bgo_solve_with_mat( &data, &userdata, &status, n, x, g,
                                ne, fun, grad, hess_dense, hessprod, prec );
            break;
        case 4: // diagonal
            st = 'I';
            bgo_import( &control, &data, &status, n, x_l, x_u,
                        "diagonal", ne, NULL, NULL, NULL );
            bgo_solve_with_mat( &data, &userdata, &status, n, x, g,
                                ne, fun_diag, grad_diag, hess_diag,
                                hessprod_diag, prec );
            break;
        case 5: // access by products
            st = 'P';
            bgo_import( &control, &data, &status, n, x_l, x_u,
                        "absent", ne, NULL, NULL, NULL );
            bgo_solve_without_mat( &data, &userdata, &status, n, x, g,
                                   fun, grad, hessprod, shessprod, prec );
            break;
    }
    // Record solution information
    bgo_information( &data, &inform, &status );
    if(inform.status == 0){
        printf("c:%6i evaluations. Optimal objective value = %5.2f"
               " status = %1i\n", st, inform.f_eval, inform.obj, inform.status);
    }else{
        printf("c: BGO_solve exit status = %1i\n", st, inform.status);
    }
    //printf("x: ");
    //for(int i = 0; i < n; i++) printf("%f ", x[i]);
    //printf("\n");
    //printf("gradient: ");
    //for(int i = 0; i < n; i++) printf("%f ", g[i]);
    //printf("\n");
    // Delete internal workspace
    bgo_terminate( &data, &control, &inform );
}
printf("\n tests reverse-communication options\n\n");
// reverse-communication input/output
int eval_status, nnz_u, nnz_v;
double f = 0.0;
double u[n], v[n];
int index_nz_u[n], index_nz_v[n];
double H_val[ne], H_dense[n*(n+1)/2], H_diag[n];

for(int d=1; d <= 5; d++){
    // Initialize BGO
    bgo_initialize( &data, &control, &status );
    // Set user-defined control options
    control.f_indexing = false; // C sparse matrix indexing

```



```

control.attempts_max = 10000;
control.max_evals = 20000;
control.sampling_strategy = 3;
control.trb_control.maxit = 100;
//control.print_level = 1;
// Start from 0
double x[] = {0,0,0};
switch(d) {
    case 1: // sparse co-ordinate storage
        st = 'C';
        bgo_import( &control, &data, &status, n, x_l, x_u,
                    "coordinate", ne, H_row, H_col, NULL );
        while(true){ // reverse-communication loop
            bgo_solve_reverse_with_mat( &data, &status, &eval_status,
                                        n, x, f, g, ne, H_val, u, v );
            if(status == 0){ // successful termination
                break;
            }else if(status < 0){ // error exit
                break;
            }else if(status == 2){ // evaluate f
                eval_status = fun( n, x, &f, &userdata );
            }else if(status == 3){ // evaluate g
                eval_status = grad( n, x, g, &userdata );
            }else if(status == 4){ // evaluate H
                eval_status = hess( n, ne, x, H_val, &userdata );
            }else if(status == 5){ // evaluate Hv product
                eval_status = hessprod( n, x, u, v, false, &userdata );
            }else if(status == 6){ // evaluate the product with P
                eval_status = prec( n, x, u, v, &userdata );
            }else if(status == 23){ // evaluate f and g
                eval_status = fun( n, x, &f, &userdata );
                eval_status = grad( n, x, g, &userdata );
            }else if(status == 25){ // evaluate f and Hv product
                eval_status = fun( n, x, &f, &userdata );
                eval_status = hessprod( n, x, u, v, false, &userdata );
            }else if(status == 35){ // evaluate g and Hv product
                eval_status = grad( n, x, g, &userdata );
                eval_status = hessprod( n, x, u, v, false, &userdata );
            }else if(status == 235){ // evaluate f, g and Hv product
                eval_status = fun( n, x, &f, &userdata );
                eval_status = grad( n, x, g, &userdata );
                eval_status = hessprod( n, x, u, v, false, &userdata );
            }else{
                printf(" the value %li of status should not occur\n",
                       status );
                break;
            }
        }
        break;
    case 2: // sparse by rows
        st = 'R';
        bgo_import( &control, &data, &status, n, x_l, x_u,
                    "sparse_by_rows", ne, NULL, H_col, H_ptr );
        while(true){ // reverse-communication loop
            bgo_solve_reverse_with_mat( &data, &status, &eval_status,
                                        n, x, f, g, ne, H_val, u, v );
            if(status == 0){ // successful termination
                break;
            }else if(status < 0){ // error exit
                break;
            }else if(status == 2){ // evaluate f
                eval_status = fun( n, x, &f, &userdata );
            }else if(status == 3){ // evaluate g
                eval_status = grad( n, x, g, &userdata );
            }else if(status == 4){ // evaluate H
                eval_status = hess( n, ne, x, H_val, &userdata );
            }else if(status == 5){ // evaluate Hv product
                eval_status = hessprod( n, x, u, v, false, &userdata );
            }else if(status == 6){ // evaluate the product with P
                eval_status = prec( n, x, u, v, &userdata );
            }else if(status == 23){ // evaluate f and g
                eval_status = fun( n, x, &f, &userdata );
                eval_status = grad( n, x, g, &userdata );
            }else if(status == 25){ // evaluate f and Hv product
                eval_status = fun( n, x, &f, &userdata );
                eval_status = hessprod( n, x, u, v, false, &userdata );
            }else if(status == 35){ // evaluate g and Hv product
                eval_status = grad( n, x, g, &userdata );
                eval_status = hessprod( n, x, u, v, false, &userdata );
            }else if(status == 235){ // evaluate f, g and Hv product
                eval_status = fun( n, x, &f, &userdata );
                eval_status = grad( n, x, g, &userdata );
                eval_status = hessprod( n, x, u, v, false, &userdata );
            }else{
                printf(" the value %li of status should not occur\n",
                       status);
                break;
            }
        }

```

```

    }
    break;
case 3: // dense
    st = 'D';
    bgo_import( &control, &data, &status, n, x_l, x_u,
               "dense", ne, NULL, NULL, NULL );
    while(true){ // reverse-communication loop
        bgo_solve_reverse_with_mat( &data, &status, &eval_status,
                                   n, x, f, g, n*(n+1)/2,
                                   H_dense, u, v );

        if(status == 0){ // successful termination
            break;
        }else if(status < 0){ // error exit
            break;
        }else if(status == 2){ // evaluate f
            eval_status = fun( n, x, &f, &userdata );
        }else if(status == 3){ // evaluate g
            eval_status = grad( n, x, g, &userdata );
        }else if(status == 4){ // evaluate H
            eval_status = hess_dense( n, n*(n+1)/2, x, H_dense,
                                     &userdata );
        }else if(status == 5){ // evaluate Hv product
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 6){ // evaluate the product with P
            eval_status = prec( n, x, u, v, &userdata );
        }else if(status == 23){ // evaluate f and g
            eval_status = fun( n, x, &f, &userdata );
            eval_status = grad( n, x, g, &userdata );
        }else if(status == 25){ // evaluate f and Hv product
            eval_status = fun( n, x, &f, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 35){ // evaluate g and Hv product
            eval_status = grad( n, x, g, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 235){ // evaluate f, g and Hv product
            eval_status = fun( n, x, &f, &userdata );
            eval_status = grad( n, x, g, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else{
            printf(" the value %li of status should not occur\n",
                  status);
            break;
        }
    }
    break;
case 4: // diagonal
    st = 'I';
    bgo_import( &control, &data, &status, n, x_l, x_u,
               "diagonal", ne, NULL, NULL, NULL );
    while(true){ // reverse-communication loop
        bgo_solve_reverse_with_mat( &data, &status, &eval_status,
                                   n, x, f, g, n, H_diag, u, v );

        if(status == 0){ // successful termination
            break;
        }else if(status < 0){ // error exit
            break;
        }else if(status == 2){ // evaluate f
            eval_status = fun_diag( n, x, &f, &userdata );
        }else if(status == 3){ // evaluate g
            eval_status = grad_diag( n, x, g, &userdata );
        }else if(status == 4){ // evaluate H
            eval_status = hess_diag( n, n, x, H_diag, &userdata );
        }else if(status == 5){ // evaluate Hv product
            eval_status = hessprod_diag( n, x, u, v, false,
                                         &userdata );
        }else if(status == 6){ // evaluate the product with P
            eval_status = prec( n, x, u, v, &userdata );
        }else if(status == 23){ // evaluate f and g
            eval_status = fun_diag( n, x, &f, &userdata );
            eval_status = grad_diag( n, x, g, &userdata );
        }else if(status == 25){ // evaluate f and Hv product
            eval_status = fun_diag( n, x, &f, &userdata );
            eval_status = hessprod_diag( n, x, u, v, false,
                                         &userdata );
        }else if(status == 35){ // evaluate g and Hv product
            eval_status = grad_diag( n, x, g, &userdata );
            eval_status = hessprod_diag( n, x, u, v, false,
                                         &userdata );
        }else if(status == 235){ // evaluate f, g and Hv product
            eval_status = fun_diag( n, x, &f, &userdata );
            eval_status = grad_diag( n, x, g, &userdata );
            eval_status = hessprod_diag( n, x, u, v, false,
                                         &userdata );
        }else{
            printf(" the value %li of status should not occur\n",
                  status);
        }
    }

```

```

        break;
    }
}
break;
case 5: // access by products
    st = 'P';
    bgo_import( &control, &data, &status, n, x_l, x_u,
               "absent", ne, NULL, NULL, NULL );
    nnz_u = 0;
    while(true){ // reverse-communication loop
        bgo_solve_reverse_without_mat( &data, &status, &eval_status,
                                       n, x, f, g, u, v, index_nz_v,
                                       &nnz_v, index_nz_u, nnz_u );

        if(status == 0){ // successful termination
            break;
        }else if(status < 0){ // error exit
            break;
        }else if(status == 2){ // evaluate f
            eval_status = fun( n, x, &f, &userdata );
        }else if(status == 3){ // evaluate g
            eval_status = grad( n, x, g, &userdata );
        }else if(status == 5){ // evaluate Hv product
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 6){ // evaluate the product with P
            eval_status = prec( n, x, u, v, &userdata );
        }else if(status == 7){ // evaluate sparse Hess-vect product
            eval_status = shessprod( n, x, nnz_v, index_nz_v, v,
                                    &nnz_u, index_nz_u, u,
                                    false, &userdata );
        }else if(status == 23){ // evaluate f and g
            eval_status = fun( n, x, &f, &userdata );
            eval_status = grad( n, x, g, &userdata );
        }else if(status == 25){ // evaluate f and Hv product
            eval_status = fun( n, x, &f, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 35){ // evaluate g and Hv product
            eval_status = grad( n, x, g, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 235){ // evaluate f, g and Hv product
            eval_status = fun( n, x, &f, &userdata );
            eval_status = grad( n, x, g, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else{
            printf(" the value %li of status should not occur\n",
                   status);
            break;
        }
    }
    break;
}
// Record solution information
bgo_information( &data, &inform, &status );
if(inform.status == 0){
    printf("%c:%6i evaluations. Optimal objective value = %5.2f"
          " status = %li\n", st, inform.f_eval, inform.obj, inform.status);
}else{
    printf("%c: BGO_solve exit status = %li\n", st, inform.status);
}
//printf("x: ");
//for(int i = 0; i < n; i++) printf("%f ", x[i]);
//printf("\n");
//printf("gradient: ");
//for(int i = 0; i < n; i++) printf("%f ", g[i]);
//printf("\n");
// Delete internal workspace
bgo_terminate( &data, &control, &inform );
}
}
// Objective function
int fun( int n,
        const double x[],
        double *f,
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double p = myuserdata->p;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    *f = pow(x[0] + x[2] + p, 2) + pow(x[1] + x[2], 2) + mag * cos(freq*x[0])
        + x[0] + x[1] + x[2];
    return 0;
}
// Gradient of the objective
int grad( int n,
        const double x[],
        double g[],
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;

```

```

double p = myuserdata->p;
double freq = myuserdata->freq;
double mag = myuserdata->mag;
g[0] = 2.0 * ( x[0] + x[2] + p ) - mag * freq * sin(freq*x[0]) + 1;
g[1] = 2.0 * ( x[1] + x[2] ) + 1;
g[2] = 2.0 * ( x[0] + x[2] + p ) + 2.0 * ( x[1] + x[2] ) + 1;
return 0;
}
// Hessian of the objective
int hess( int n,
         int ne,
         const double x[],
         double hval[],
         const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;

    hval[0] = 2.0 - mag * freq * freq * cos(freq*x[0]);
    hval[1] = 2.0;
    hval[2] = 2.0;
    hval[3] = 2.0;
    hval[4] = 4.0;
    return 0;
}
// Dense Hessian
int hess_dense( int n,
               int ne,
               const double x[],
               double hval[],
               const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;

    hval[0] = 2.0 - mag * freq * freq * cos(freq*x[0]);
    hval[1] = 0.0;
    hval[2] = 2.0;
    hval[3] = 2.0;
    hval[4] = 2.0;
    hval[5] = 4.0;
    return 0;
}
// Hessian-vector product
int hessprod( int n,
             const double x[],
             double u[],
             const double v[],
             bool got_h,
             const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;

    u[0] = u[0] + 2.0 * ( v[0] + v[2] )
           - mag * freq * freq * cos(freq*x[0]) * v[0];
    u[1] = u[1] + 2.0 * ( v[1] + v[2] );
    u[2] = u[2] + 2.0 * ( v[0] + v[1] + 2.0 * v[2] );
    return 0;
}
// Sparse Hessian-vector product
int shessprod( int n,
              const double x[],
              int nnz_v,
              const int index_nz_v[],
              const double v[],
              int *nnz_u,
              int index_nz_u[],
              double u[],
              bool got_h,
              const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    double p[] = {0., 0., 0.};
    bool used[] = {false, false, false};
    for(int i = 0; i < nnz_v; i++){
        int j = index_nz_v[i];
        switch(j){
            case 0:
                p[0] = p[0] + 2.0 * v[0] - mag * freq * freq * cos(freq*x[0]) * v[0];
                used[0] = true;
                p[2] = p[2] + 2.0 * v[0];
                used[2] = true;
                break;
            case 1:
                p[1] = p[1] + 2.0 * v[1];

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```

        used[1] = true;
        p[2] = p[2] + 2.0 * v[1];
        used[2] = true;
        break;
    case 2:
        p[0] = p[0] + 2.0 * v[2];
        used[0] = true;
        p[1] = p[1] + 2.0 * v[2];
        used[1] = true;
        p[2] = p[2] + 4.0 * v[2];
        used[2] = true;
        break;
    }
}
*nnz_u = 0;
for(int j = 0; j < 3; j++){
    if(used[j]){
        u[j] = p[j];
        *nnz_u = *nnz_u + 1;
        index_nz_u[*nnz_u-1] = j;
    }
}
return 0;
}
// Apply preconditioner
int prec( int n,
        const double x[],
        double u[],
        const double v[],
        const void *userdata ){
    u[0] = 0.5 * v[0];
    u[1] = 0.5 * v[1];
    u[2] = 0.25 * v[2];
    return 0;
}
// Objective function
int fun_diag( int n,
        const double x[],
        double *f,
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double p = myuserdata->p;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    *f = pow(x[2] + p, 2) + pow(x[1], 2) + mag * cos(freq*x[0])
        + x[0] + x[1] + x[2];
    return 0;
}
// Gradient of the objective
int grad_diag( int n,
        const double x[],
        double g[],
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double p = myuserdata->p;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    g[0] = -mag * freq * sin(freq*x[0]) + 1;
    g[1] = 2.0 * x[1] + 1;
    g[2] = 2.0 * ( x[2] + p ) + 1;
    return 0;
}
// Hessian of the objective
int hess_diag( int n,
        int ne,
        const double x[],
        double hval[],
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    hval[0] = -mag * freq * freq * cos(freq*x[0]);
    hval[1] = 2.0;
    hval[2] = 2.0;
    return 0;
}
// Hessian-vector product
int hessprod_diag( int n,
        const double x[],
        double u[],
        const double v[],
        bool got_h,
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    u[0] = u[0] + -mag * freq * freq * cos(freq*x[0]) * v[0];

```

```

    u[1] = u[1] + 2.0 * v[1];
    u[2] = u[2] + 2.0 * v[2];
    return 0;
}
// Sparse Hessian-vector product
int shessprod_diag( int n,
                    const double x[],
                    int nnz_v,
                    const int index_nz_v[],
                    const double v[],
                    int *nnz_u,
                    int index_nz_u[],
                    double u[],
                    bool got_h,
                    const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    double p[] = {0., 0., 0.};
    bool used[] = {false, false, false};
    for(int i = 0; i < nnz_v; i++){
        int j = index_nz_v[i];
        switch(j){
            case 0:
                p[0] = p[0] - mag * freq * freq * cos(freq*x[0]) * v[0];
                used[0] = true;
                break;
            case 1:
                p[1] = p[1] + 2.0 * v[1];
                used[1] = true;
                break;
            case 2:
                p[2] = p[2] + 2.0 * v[2];
                used[2] = true;
                break;
        }
    }
    *nnz_u = 0;
    for(int j = 0; j < 3; j++){
        if(used[j]){
            u[j] = p[j];
            *nnz_u = *nnz_u + 1;
            index_nz_u[*nnz_u-1] = j;
        }
    }
    return 0;
}

```

4.2 bgotf.c

This is the same example, but now fortran-style indexing is used.

```

/* bgot2.c */
/* Full test for the BGO C interface using Fortran sparse matrix indexing */
#include <stdio.h>
#include <math.h>
#include "bgo.h"
// Custom userdata struct
struct userdata_type {
    double p;
    double freq;
    double mag;
};
// Function prototypes
int fun( int n, const double x[], double *f, const void * );
int grad( int n, const double x[], double g[], const void * );
int hess( int n, int ne, const double x[], double hval[], const void * );
int hess_dense( int n, int ne, const double x[], double hval[], const void * );
int hessprod( int n, const double x[], double u[], const double v[],
              bool got_h, const void * );
int shessprod( int n, const double x[], int nnz_v, const int index_nz_v[],
               const double v[], int *nnz_u, int index_nz_u[], double u[],
               bool got_h, const void * );
int prec(int n, const double x[], double u[], const double v[], const void * );
int fun_diag(int n, const double x[], double *f, const void * );
int grad_diag(int n, const double x[], double g[], const void * );
int hess_diag(int n, int ne, const double x[], double hval[], const void * );
int hessprod_diag( int n, const double x[], double u[], const double v[],
                  bool got_h, const void * );
int shessprod_diag( int n, const double x[], int nnz_v, const int index_nz_v[],
                   const double v[], int *nnz_u, int index_nz_u[],

```

```

double u[], bool got_h, const void * );

int main(void) {
    // Derived types
    void *data;
    struct bgo_control_type control;
    struct bgo_inform_type inform;
    // Set user data
    struct userdata_type userdata;
    userdata.p = 4.0;
    userdata.freq = 10;
    userdata.mag = 1000;
    // Set problem data
    int n = 3; // dimension
    int ne = 5; // Hesssian elements
    double x_l[] = {-10,-10,-10};
    double x_u[] = {0.5,0.5,0.5};
    int H_row[] = {1, 2, 3, 3, 3}; // Hessian H
    int H_col[] = {1, 2, 1, 2, 3}; // NB lower triangle
    int H_ptr[] = {1, 2, 3, 6}; // row pointers
    // Set storage
    double g[n]; // gradient
    char st;
    int status;
    printf(" Fortran sparse matrix indexing\n\n");
    printf(" tests options for all-in-one storage format\n\n");
    for(int d=1; d <= 5; d++){
        // Initialize BGO
        bgo_initialize( &data, &control, &status );
        // Set user-defined control options
        control.f_indexing = true; // Fortran sparse matrix indexing
        control.attempts_max = 10000;
        control.max_evals = 20000;
        control.sampling_strategy = 3;
        control.trb_control.maxit = 100;
        //control.print_level = 1;
        // Start from 0
        double x[] = {0,0,0};
        switch(d) {
            case 1: // sparse co-ordinate storage
                st = 'C';
                bgo_import( &control, &data, &status, n, x_l, x_u,
                           "coordinate", ne, H_row, H_col, NULL );
                bgo_solve_with_mat( &data, &userdata, &status, n, x, g,
                                   ne, fun, grad, hess, hessprod, prec );
                break;
            case 2: // sparse by rows
                st = 'R';
                bgo_import( &control, &data, &status, n, x_l, x_u,
                           "sparse_by_rows", ne, NULL, H_col, H_ptr );
                bgo_solve_with_mat( &data, &userdata, &status, n, x, g,
                                   ne, fun, grad, hess, hessprod, prec );
                break;
            case 3: // dense
                st = 'D';
                bgo_import( &control, &data, &status, n, x_l, x_u,
                           "dense", ne, NULL, NULL, NULL );
                bgo_solve_with_mat( &data, &userdata, &status, n, x, g,
                                   ne, fun, grad, hess_dense, hessprod, prec );
                break;
            case 4: // diagonal
                st = 'I';
                bgo_import( &control, &data, &status, n, x_l, x_u,
                           "diagonal", ne, NULL, NULL, NULL );
                bgo_solve_with_mat( &data, &userdata, &status, n, x, g,
                                   ne, fun_diag, grad_diag, hess_diag,
                                   hessprod_diag, prec );
                break;
            case 5: // access by products
                st = 'P';
                bgo_import( &control, &data, &status, n, x_l, x_u,
                           "absent", ne, NULL, NULL, NULL );
                bgo_solve_without_mat( &data, &userdata, &status, n, x, g,
                                      fun, grad, hessprod, shessprod, prec );
                break;
        }
        // Record solution information
        bgo_information( &data, &inform, &status );
        if(inform.status == 0){
            printf("%c:%6i evaluations. Optimal objective value = %5.2f"
                  " status = %1i\n", st, inform.f_eval, inform.obj, inform.status);
        }else{
            printf("%c: BGO_solve exit status = %1i\n", st, inform.status);
        }
        //printf("x: ");
        //for(int i = 0; i < n; i++) printf("%f ", x[i]);
        //printf("\n");
        //printf("gradient: ");
    }
}

```

```

    //for(int i = 0; i < n; i++) printf("%f ", g[i]);
    //printf("\n");
    // Delete internal workspace
    bgo_terminate( &data, &control, &inform );
}
printf("\n tests reverse-communication options\n\n");
// reverse-communication input/output
int eval_status, nnz_u, nnz_v;
double f = 0.0;
double u[n], v[n];
int index_nz_u[n], index_nz_v[n];
double H_val[ne], H_dense[n*(n+1)/2], H_diag[n];

for(int d=1; d <= 5; d++){
    // Initialize BGO
    bgo_initialize( &data, &control, &status );
    // Set user-defined control options
    control.f_indexing = true; // Fortran sparse matrix indexing
    control.attempts_max = 10000;
    control.max_evals = 20000;
    control.sampling_strategy = 3;
    control.trb_control.maxit = 100;
    //control.print_level = 1;
    // Start from 0
    double x[] = {0,0,0};
    switch(d){
        case 1: // sparse co-ordinate storage
            st = 'C';
            bgo_import( &control, &data, &status, n, x_l, x_u,
                        "coordinate", ne, H_row, H_col, NULL );
            while(true){ // reverse-communication loop
                bgo_solve_reverse_with_mat( &data, &status, &eval_status,
                                            n, x, f, g, ne, H_val, u, v );
                if(status == 0){ // successful termination
                    break;
                }else if(status < 0){ // error exit
                    break;
                }else if(status == 2){ // evaluate f
                    eval_status = fun( n, x, &f, &userdata );
                }else if(status == 3){ // evaluate g
                    eval_status = grad( n, x, g, &userdata );
                }else if(status == 4){ // evaluate H
                    eval_status = hess( n, ne, x, H_val, &userdata );
                }else if(status == 5){ // evaluate Hv product
                    eval_status = hessprod( n, x, u, v, false, &userdata );
                }else if(status == 6){ // evaluate the product with P
                    eval_status = prec( n, x, u, v, &userdata );
                }else if(status == 23){ // evaluate f and g
                    eval_status = fun( n, x, &f, &userdata );
                    eval_status = grad( n, x, g, &userdata );
                }else if(status == 25){ // evaluate f and Hv product
                    eval_status = fun( n, x, &f, &userdata );
                    eval_status = hessprod( n, x, u, v, false, &userdata );
                }else if(status == 35){ // evaluate g and Hv product
                    eval_status = grad( n, x, g, &userdata );
                    eval_status = hessprod( n, x, u, v, false, &userdata );
                }else if(status == 235){ // evaluate f, g and Hv product
                    eval_status = fun( n, x, &f, &userdata );
                    eval_status = grad( n, x, g, &userdata );
                    eval_status = hessprod( n, x, u, v, false, &userdata );
                }else{
                    printf(" the value %li of status should not occur\n",
                           status );
                    break;
                }
            }
            break;
        case 2: // sparse by rows
            st = 'R';
            bgo_import( &control, &data, &status, n, x_l, x_u,
                        "sparse_by_rows", ne, NULL, H_col, H_ptr );
            while(true){ // reverse-communication loop
                bgo_solve_reverse_with_mat( &data, &status, &eval_status,
                                            n, x, f, g, ne, H_val, u, v );
                if(status == 0){ // successful termination
                    break;
                }else if(status < 0){ // error exit
                    break;
                }else if(status == 2){ // evaluate f
                    eval_status = fun( n, x, &f, &userdata );
                }else if(status == 3){ // evaluate g
                    eval_status = grad( n, x, g, &userdata );
                }else if(status == 4){ // evaluate H
                    eval_status = hess( n, ne, x, H_val, &userdata );
                }else if(status == 5){ // evaluate Hv product
                    eval_status = hessprod( n, x, u, v, false, &userdata );
                }else if(status == 6){ // evaluate the product with P

```



```

        eval_status = prec( n, x, u, v, &userdata );
    }else if(status == 23){ // evaluate f and g
        eval_status = fun( n, x, &f, &userdata );
        eval_status = grad( n, x, g, &userdata );
    }else if(status == 25){ // evaluate f and Hv product
        eval_status = fun( n, x, &f, &userdata );
        eval_status = hessprod( n, x, u, v, false, &userdata );
    }else if(status == 35){ // evaluate g and Hv product
        eval_status = grad( n, x, g, &userdata );
        eval_status = hessprod( n, x, u, v, false, &userdata );
    }else if(status == 235){ // evaluate f, g and Hv product
        eval_status = fun( n, x, &f, &userdata );
        eval_status = grad( n, x, g, &userdata );
        eval_status = hessprod( n, x, u, v, false, &userdata );
    }else{
        printf(" the value %li of status should not occur\n",
            status);
        break;
    }
}
break;
case 3: // dense
st = 'D';
bgo_import( &control, &data, &status, n, x_l, x_u,
    "dense", ne, NULL, NULL, NULL );
while(true){ // reverse-communication loop
    bgo_solve_reverse_with_mat( &data, &status, &eval_status,
        n, x, f, g, n*(n+1)/2,
        H_dense, u, v );

    if(status == 0){ // successful termination
        break;
    }else if(status < 0){ // error exit
        break;
    }else if(status == 2){ // evaluate f
        eval_status = fun( n, x, &f, &userdata );
    }else if(status == 3){ // evaluate g
        eval_status = grad( n, x, g, &userdata );
    }else if(status == 4){ // evaluate H
        eval_status = hess_dense( n, n*(n+1)/2, x, H_dense,
            &userdata );
    }else if(status == 5){ // evaluate Hv product
        eval_status = hessprod( n, x, u, v, false, &userdata );
    }else if(status == 6){ // evaluate the product with P
        eval_status = prec( n, x, u, v, &userdata );
    }else if(status == 23){ // evaluate f and g
        eval_status = fun( n, x, &f, &userdata );
        eval_status = grad( n, x, g, &userdata );
    }else if(status == 25){ // evaluate f and Hv product
        eval_status = fun( n, x, &f, &userdata );
        eval_status = hessprod( n, x, u, v, false, &userdata );
    }else if(status == 35){ // evaluate g and Hv product
        eval_status = grad( n, x, g, &userdata );
        eval_status = hessprod( n, x, u, v, false, &userdata );
    }else if(status == 235){ // evaluate f, g and Hv product
        eval_status = fun( n, x, &f, &userdata );
        eval_status = grad( n, x, g, &userdata );
        eval_status = hessprod( n, x, u, v, false, &userdata );
    }else{
        printf(" the value %li of status should not occur\n",
            status);
        break;
    }
}
break;
case 4: // diagonal
st = 'I';
bgo_import( &control, &data, &status, n, x_l, x_u,
    "diagonal", ne, NULL, NULL, NULL );
while(true){ // reverse-communication loop
    bgo_solve_reverse_with_mat( &data, &status, &eval_status,
        n, x, f, g, n, H_diag, u, v );

    if(status == 0){ // successful termination
        break;
    }else if(status < 0){ // error exit
        break;
    }else if(status == 2){ // evaluate f
        eval_status = fun_diag( n, x, &f, &userdata );
    }else if(status == 3){ // evaluate g
        eval_status = grad_diag( n, x, g, &userdata );
    }else if(status == 4){ // evaluate H
        eval_status = hess_diag( n, n, x, H_diag, &userdata );
    }else if(status == 5){ // evaluate Hv product
        eval_status = hessprod_diag( n, x, u, v, false,
            &userdata );
    }else if(status == 6){ // evaluate the product with P
        eval_status = prec( n, x, u, v, &userdata );
    }else if(status == 23){ // evaluate f and g

```

```

        eval_status = fun_diag( n, x, &f, &userdata );
        eval_status = grad_diag( n, x, g, &userdata );
    }else if(status == 25){ // evaluate f and Hv product
        eval_status = fun_diag( n, x, &f, &userdata );
        eval_status = hessprod_diag( n, x, u, v, false,
                                     &userdata );
    }else if(status == 35){ // evaluate g and Hv product
        eval_status = grad_diag( n, x, g, &userdata );
        eval_status = hessprod_diag( n, x, u, v, false,
                                     &userdata );
    }else if(status == 235){ // evaluate f, g and Hv product
        eval_status = fun_diag( n, x, &f, &userdata );
        eval_status = grad_diag( n, x, g, &userdata );
        eval_status = hessprod_diag( n, x, u, v, false,
                                     &userdata );
    }else{
        printf(" the value %li of status should not occur\n",
               status);
        break;
    }
}
break;
case 5: // access by products
    st = 'P';
    bgo_import( &control, &data, &status, n, x_l, x_u,
               "absent", ne, NULL, NULL, NULL );
    nnz_u = 0;
    while(true){ // reverse-communication loop
        bgo_solve_reverse_without_mat( &data, &status, &eval_status,
                                     n, x, f, g, u, v, index_nz_v,
                                     &nnz_v, index_nz_u, nnz_u );

        if(status == 0){ // successful termination
            break;
        }else if(status < 0){ // error exit
            break;
        }else if(status == 2){ // evaluate f
            eval_status = fun( n, x, &f, &userdata );
        }else if(status == 3){ // evaluate g
            eval_status = grad( n, x, g, &userdata );
        }else if(status == 5){ // evaluate Hv product
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 6){ // evaluate the product with P
            eval_status = prec( n, x, u, v, &userdata );
        }else if(status == 7){ // evaluate sparse Hess-vect product
            eval_status = shessprod( n, x, nnz_v, index_nz_v, v,
                                   &nnz_u, index_nz_u, u,
                                   false, &userdata );
        }else if(status == 23){ // evaluate f and g
            eval_status = fun( n, x, &f, &userdata );
            eval_status = grad( n, x, g, &userdata );
        }else if(status == 25){ // evaluate f and Hv product
            eval_status = fun( n, x, &f, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 35){ // evaluate g and Hv product
            eval_status = grad( n, x, g, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else if(status == 235){ // evaluate f, g and Hv product
            eval_status = fun( n, x, &f, &userdata );
            eval_status = grad( n, x, g, &userdata );
            eval_status = hessprod( n, x, u, v, false, &userdata );
        }else{
            printf(" the value %li of status should not occur\n",
                   status);
            break;
        }
    }
    break;
}
// Record solution information
bgo_information( &data, &inform, &status );
if(inform.status == 0){
    printf("%c:%6i evaluations. Optimal objective value = %5.2f"
           " status = %li\n", st, inform.f_eval, inform.obj, inform.status);
}else{
    printf("%c: BGO_solve exit status = %li\n", st, inform.status);
}
//printf("x: ");
//for(int i = 0; i < n; i++) printf("%f ", x[i]);
//printf("\n");
//printf("gradient: ");
//for(int i = 0; i < n; i++) printf("%f ", g[i]);
//printf("\n");
// Delete internal workspace
bgo_terminate( &data, &control, &inform );
}
// Objective function

```

```

int fun( int n,
        const double x[],
        double *f,
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double p = myuserdata->p;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    *f = pow(x[0] + x[2] + p, 2) + pow(x[1] + x[2], 2) + mag * cos(freq*x[0])
        + x[0] + x[1] + x[2];
    return 0;
}
// Gradient of the objective
int grad( int n,
        const double x[],
        double g[],
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double p = myuserdata->p;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    g[0] = 2.0 * ( x[0] + x[2] + p ) - mag * freq * sin(freq*x[0]) + 1;
    g[1] = 2.0 * ( x[1] + x[2] ) + 1;
    g[2] = 2.0 * ( x[0] + x[2] + p ) + 2.0 * ( x[1] + x[2] ) + 1;
    return 0;
}
// Hessian of the objective
int hess( int n,
        int ne,
        const double x[],
        double hval[],
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;

    hval[0] = 2.0 - mag * freq * freq * cos(freq*x[0]);
    hval[1] = 2.0;
    hval[2] = 2.0;
    hval[3] = 2.0;
    hval[4] = 4.0;
    return 0;
}
// Dense Hessian
int hess_dense( int n,
        int ne,
        const double x[],
        double hval[],
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;

    hval[0] = 2.0 - mag * freq * freq * cos(freq*x[0]);
    hval[1] = 0.0;
    hval[2] = 2.0;
    hval[3] = 2.0;
    hval[4] = 2.0;
    hval[5] = 4.0;
    return 0;
}
// Hessian-vector product
int hessprod( int n,
        const double x[],
        double u[],
        const double v[],
        bool got_h,
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;

    u[0] = u[0] + 2.0 * ( v[0] + v[2] )
        - mag * freq * freq * cos(freq*x[0]) * v[0];
    u[1] = u[1] + 2.0 * ( v[1] + v[2] );
    u[2] = u[2] + 2.0 * ( v[0] + v[1] + 2.0 * v[2] );
    return 0;
}
// Sparse Hessian-vector product
int shessprod( int n,
        const double x[],
        int nnz_v,
        const int index_nz_v[],
        const double v[],
        int *nnz_u,
        int index_nz_u[],
        double u[],

```

```

        bool got_h,
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    double p[] = {0., 0., 0.};
    bool used[] = {false, false, false};
    for(int i = 0; i < nnz_v; i++){
        int j = index_nz_v[i];
        switch(j){
            case 1:
                p[0] = p[0] + 2.0 * v[0]
                    - mag * freq * freq * cos(freq*x[0]) * v[0];
                used[0] = true;
                p[2] = p[2] + 2.0 * v[0];
                used[2] = true;
                break;
            case 2:
                p[1] = p[1] + 2.0 * v[1];
                used[1] = true;
                p[2] = p[2] + 2.0 * v[1];
                used[2] = true;
                break;
            case 3:
                p[0] = p[0] + 2.0 * v[2];
                used[0] = true;
                p[1] = p[1] + 2.0 * v[2];
                used[1] = true;
                p[2] = p[2] + 4.0 * v[2];
                used[2] = true;
                break;
        }
    }
    *nnz_u = 0;
    for(int j = 0; j < 3; j++){
        if(used[j]){
            u[j] = p[j];
            *nnz_u = *nnz_u + 1;
            index_nz_u[*nnz_u-1] = j+1;
        }
    }
    return 0;
}

// Apply preconditioner
int prec( int n,
        const double x[],
        double u[],
        const double v[],
        const void *userdata ){
    u[0] = 0.5 * v[0];
    u[1] = 0.5 * v[1];
    u[2] = 0.25 * v[2];
    return 0;
}

// Objective function
int fun_diag( int n,
        const double x[],
        double *f,
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double p = myuserdata->p;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    *f = pow(x[2] + p, 2) + pow(x[1], 2) + mag * cos(freq*x[0])
        + x[0] + x[1] + x[2];
    return 0;
}

// Gradient of the objective
int grad_diag( int n,
        const double x[],
        double g[],
        const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double p = myuserdata->p;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    g[0] = -mag * freq * sin(freq*x[0]) + 1;
    g[1] = 2.0 * x[1] + 1;
    g[2] = 2.0 * ( x[2] + p ) + 1;
    return 0;
}

// Hessian of the objective
int hess_diag( int n,
        int ne,
        const double x[],
        double hval[],
        const void *userdata ){

```

```

    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    hval[0] = -mag * freq * freq * cos(freq*x[0]);
    hval[1] = 2.0;
    hval[2] = 2.0;
    return 0;
}
// Hessian-vector product
int hessprod_diag( int n,
                  const double x[],
                  double u[],
                  const double v[],
                  bool got_h,
                  const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    u[0] = u[0] + -mag * freq * freq * cos(freq*x[0]) * v[0];
    u[1] = u[1] + 2.0 * v[1];
    u[2] = u[2] + 2.0 * v[2];
    return 0;
}
// Sparse Hessian-vector product
int shessprod_diag( int n,
                  const double x[],
                  int nnz_v,
                  const int index_nz_v[],
                  const double v[],
                  int *nnz_u,
                  int index_nz_u[],
                  double u[],
                  bool got_h,
                  const void *userdata ){
    struct userdata_type *myuserdata = (struct userdata_type *) userdata;
    double freq = myuserdata->freq;
    double mag = myuserdata->mag;
    double p[] = {0., 0., 0.};
    bool used[] = {false, false, false};
    for(int i = 0; i < nnz_v; i++){
        int j = index_nz_v[i];
        switch(j){
            case 1:
                p[0] = p[0] - mag * freq * freq * cos(freq*x[0]) * v[0];
                used[0] = true;
                break;
            case 2:
                p[1] = p[1] + 2.0 * v[1];
                used[1] = true;
                break;
            case 3:
                p[2] = p[2] + 2.0 * v[2];
                used[2] = true;
                break;
        }
    }
    *nnz_u = 0;
    for(int j = 0; j < 3; j++){
        if(used[j]){
            u[j] = p[j];
            *nnz_u = *nnz_u + 1;
            index_nz_u[*nnz_u-1] = j+1;
        }
    }
    return 0;
}

```


Index

- bgo.h, [7](#)
 - bgo_import, [10](#)
 - bgo_information, [24](#)
 - bgo_initialize, [10](#)
 - bgo_read_specfile, [10](#)
 - bgo_reset_control, [12](#)
 - bgo_solve_reverse_with_mat, [17](#)
 - bgo_solve_reverse_without_mat, [21](#)
 - bgo_solve_with_mat, [12](#)
 - bgo_solve_without_mat, [14](#)
 - bgo_terminate, [24](#)
- bgo_control_type, [8](#)
- bgo_import
 - bgo.h, [10](#)
- bgo_inform_type, [9](#)
- bgo_information
 - bgo.h, [24](#)
- bgo_initialize
 - bgo.h, [10](#)
- bgo_read_specfile
 - bgo.h, [10](#)
- bgo_reset_control
 - bgo.h, [12](#)
- bgo_solve_reverse_with_mat
 - bgo.h, [17](#)
- bgo_solve_reverse_without_mat
 - bgo.h, [21](#)
- bgo_solve_with_mat
 - bgo.h, [12](#)
- bgo_solve_without_mat
 - bgo.h, [14](#)
- bgo_terminate
 - bgo.h, [24](#)
- bgo_time_type, [9](#)