

C interfaces to GALAHAD FDC

Jari Fowkes and Nick Gould STFC Rutherford Appleton Laboratory Fri Mar 18 2022

1 GALAHAD C package fdc	1
1.1 Introduction	1
1.1.1 Purpose	1
1.1.2 Authors	1
1.1.3 Originally released	1
1.1.4 Method	1
1.1.5 Call order	2
1.1.6 Array indexing	2
2 File Index	3
2.1 File List	3
3 File Documentation	5
3.1 fdc.h File Reference	5
3.1.1 Data Structure Documentation	5
3.1.1.1 struct fdc_control_type	5
3.1.1.2 struct fdc_time_type	6
3.1.1.3 struct fdc_inform_type	6
3.1.2 Function Documentation	7
3.1.2.1 fdc_initialize()	7
3.1.2.2 fdc_read_specfile()	7
3.1.2.3 fdc_find_dependent_rows()	8
3.1.2.4 fdc_terminate()	9
4 Example Documentation	13
4.1 fdct.c	13
4.2 fdctf.c	14
Index	15

GALAHAD C package fdc

1.1 Introduction

1.1.1 Purpose

Given an under-determined set of linear equations/constraints $a_i^Tx = b_i$, $i = 1, \ldots, m$ involving $n \ge m$ unknowns x, this package **determines whether the constraints are consistent, and if so how many of the constraints are dependent**; a list of dependent constraints, that is, those which may be removed without changing the solution set, will be found and the remaining a_i will be linearly independent. Full advantage is taken of any zero coefficients in the vectors a_i .

1.1.2 Authors

N. I. M. Gould, STFC-Rutherford Appleton Laboratory, England.

C interface, additionally J. Fowkes, STFC-Rutherford Appleton Laboratory.

1.1.3 Originally released

August 2006, C interface January 2021

1.1.4 Method

A choice of two methods is available. In the first, the matrix

$$K = \left(\begin{array}{cc} \alpha I & A^T \\ A & 0 \end{array}\right)$$

is formed and factorized for some small $\alpha>0$ using the GALAHAD package SLS—the factors $K=PLDL^TP^T$ are used to determine whether A has dependent rows. In particular, in exact arithmetic dependencies in A will correspond to zero pivots in the block diagonal matrix D.

The second choice of method finds factors A=PLUQ of the rectangular matrix A using the GALAHAD package ULS. In this case, dependencies in A will be reflected in zero diagonal entries in U in exact arithmetic.

The factorization in either case may also be used to determine whether the system is consistent.

1.1.5 Call order

To solve a given problem, functions from the fdc package must be called in the following order:

- fdc_initialize provide default control parameters and set up initial data structures
- fdc_read_specfile (optional) override control values by reading replacement values from a file
- fdc_find_dependent_rows find the number of dependent rows and, if there are any, whether the constraints are independent
- fdc_terminate deallocate data structures

See Section 4.1 for examples of use.

1.1.6 Array indexing

Both C-style (0 based) and fortran-style (1-based) indexing is allowed. Choose <code>control.f_indexing</code> as <code>false</code> for C style and <code>true</code> for fortran style; add 1 to input integer arrays if fortran-style indexing is used, and beware that return integer arrays will adhere to this.

File Index

2 1	Fi	le	l i	et
Z . I	ГΙ	ıe	L	ЭL

Here is a list of all files with brief descriptions:	
fdc.h	5

4 File Index

File Documentation

3.1 fdc.h File Reference

```
#include <stdbool.h>
#include "galahad_precision.h"
#include "sls.h"
#include "uls.h"
```

Data Structures

- struct fdc_control_type
- struct fdc_time_type
- struct fdc_inform_type

Functions

- void fdc_initialize (void **data, struct fdc_control_type *control, int *status)
- void fdc_read_specfile (struct fdc_control_type *control, const char specfile[])
- void fdc_find_dependent_rows (struct fdc_control_type *control, void **data, struct fdc_inform_type *inform, int *status, int m, int n, int A_ne, const int A_col[], const int A_ptr[], const real_wp_ A_val[], const real_wp_ b[], int *n_depen, int depen[])
- void fdc_terminate (void **data, struct fdc_control_type *control, struct fdc_inform_type *inform)

3.1.1 Data Structure Documentation

3.1.1.1 struct fdc_control_type

control derived type as a C struct

Examples

fdct.c, and fdctf.c.

Data Fields

bool	f_indexing	use C or Fortran sparse matrix indexing
int	error	unit for error messages
int	out	unit for monitor output
int	print_level	controls level of diagnostic output
int	indmin	initial estimate of integer workspace for sls (obsolete)
int	valmin	initial estimate of real workspace for sls (obsolete)
real_wp_	pivot_tol	the relative pivot tolerance (obsolete)
real_wp_	zero_pivot	the absolute pivot tolerance used (obsolete)
real_wp_	max_infeas	the largest permitted residual
bool	use_sls	choose whether SLS or ULS is used to determine dependencies
bool	scale	should the rows of A be scaled to have unit infinity norm or should no scaling be applied
bool	space_critical	if space is critical, ensure allocated arrays are no bigger than needed
bool	deallocate_error_fatal	exit if any deallocation fails
char	symmetric_linear_solver[31]	symmetric (indefinite) linear equation solver
char	unsymmetric_linear_solver[31]	unsymmetric linear equation solver
char	prefix[31]	all output lines will be prefixed by prefix(2:LEN(TRIM(.prefix))-1) where prefix contains the required string enclosed in quotes, e.g. "string" or 'string'
struct sls_control_type	sls_control	control parameters for SLS
struct uls_control_type	uls_control	control parameters for ULS

3.1.1.2 struct fdc_time_type

time derived type as a C struct

Data Fields

real_wp_	total	the total CPU time spent in the package
real_wp_	analyse	the CPU time spent analysing the required matrices prior to factorizatio
real_wp_	factorize	the CPU time spent factorizing the required matrices
real_wp_	clock_total	the total clock time spent in the package
real_wp_	clock_analyse	the clock time spent analysing the required matrices prior to factorizat
real_wp_	clock_factorize	the clock time spent factorizing the required matrices

3.1.1.3 struct fdc_inform_type

inform derived type as a C struct

Examples

fdct.c, and fdctf.c.

3.1 fdc.h File Reference 7

Data Fields

int	status	return status. See FDC_find_dependent for details
int	alloc_status	the status of the last attempted allocation/deallocation
char	bad_alloc[81]	the name of the array for which an allocation/deallocation error ocurred
int	factorization_status	the return status from the factorization
int	factorization_integer	the total integer workspace required for the factorization
int	factorization_real	the total real workspace required for the factorization
real_wp_	non_negligible_pivot	the smallest pivot which was not judged to be zero when detecting linear dependent constraints
struct fdc_time_type	time	timings (see above)
struct sls_inform_type	sls_inform	SLS inform type.
struct uls_inform_type	uls_inform	ULS inform type.

3.1.2 Function Documentation

3.1.2.1 fdc_initialize()

Set default control values and initialize private data

Parameters

in,out	data	holds private internal data	
out	control	is a struct containing control information (see fdc_control_type)	
out	status	is a scalar variable of type int, that gives the exit status from the package. Possible values are (currently):	
		0. The import was succesful.	

Examples

fdct.c, and fdctf.c.

3.1.2.2 fdc_read_specfile()

C interfaces to GALAHAD FDC GALAHAD 4.0

Read the content of a specification file, and assign values associated with given keywords to the corresponding control parameters

Parameters

in,out	control	is a struct containing control information (see fdc_control_type)	
in	specfile	is a character string containing the name of the specification file	

3.1.2.3 fdc_find_dependent_rows()

Find dependent rows and, if any, check if $\boldsymbol{A}\boldsymbol{x}=\boldsymbol{b}$ is consistent

Parameters

	in	control	is a struct containing control information (see fdc_control_type)	
	in,out	data	nolds private internal data	
Ī	out	inform	is a struct containing output information (see fdc_inform_type)	

3.1 fdc.h File Reference 9

Parameters

in,out	status	is a scalar variable of type int, that gives the entry and exit status from the package. Possible exit are:
		0. The run was succesful.
		 -1. An allocation error occurred. A message indicating the offending array is written on unit control.error, and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively.
		 -2. A deallocation error occurred. A message indicating the offending array is written on unit control.error and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively.
		 -3. The restrictions n > 0 and m > 0 or requirement that a type contains its relevant string 'dense', 'coordinate', 'sparse_by_rows', 'diagonal', 'scaled_identity', 'identity', 'zero' or 'none' has been violated.
		-5. The constraints appear to be inconsistent.
		 -9. The analysis phase of the factorization failed; the return status from the factorization package is given in the component inform.factor_status
		 -10. The factorization failed; the return status from the factorization package is given in the component inform.factor_status.
in	m	is a scalar variable of type int, that holds the number of rows of A .
in	n	is a scalar variable of type int, that holds the number of columns of A .
in	A_ne	is a scalar variable of type int, that holds the number of nonzero entries in ${\cal A}.$
in	A_col	is a one-dimensional array of size A_ne and type int, that holds the column indices of A in a row-wise storage scheme. The nonzeros must be ordered so that those in row i appear directly before those in row i+1, the order within each row is unimportant.
in	A_ptr	is a one-dimensional array of size $n+1$ and type int, that holds the starting position of each row of A , as well as the total number of entries plus one.
in	A_val	is a one-dimensional array of size a_ne and type double, that holds the values of the entries of the $\cal A$ ordered as in A_col and A_ptr.
in	b	is a one-dimensional array of size m and type double, that holds the linear term b in the constraints. The i-th component of b, i = 0,, m-1, contains b_i .
out	n_depen	is a scalar variable of type int, that holds the number of dependent constraints, if any.
out	depen	is a one-dimensional array of size m and type int, whose first n_depen components contain the indices of dependent constraints.

Examples

fdct.c, and fdctf.c.

3.1.2.4 fdc_terminate()

```
void fdc_terminate (
     void ** data,
```

C interfaces to GALAHAD FDC GALAHAD 4.0

```
struct fdc_control_type * control,
struct fdc_inform_type * inform )
```

Deallocate all internal private storage

3.1 fdc.h File Reference

Parameters

in,out	data	holds private internal data
out	control	is a struct containing control information (see fdc_control_type)
out	inform	is a struct containing output information (see fdc_inform_type)

Examples

fdct.c, and fdctf.c.

C interfaces to GALAHAD FDC GALAHAD 4.0

Example Documentation

4.1 fdct.c

This is an example of how to use the package to solve a quadratic program. A variety of supported Hessian and constraint matrix storage formats are shown.

Notice that C-style indexing is used, and that this is flaggeed by setting control.f_indexing to false.

```
/\star Full test for the FDC C interface using C sparse matrix indexing \star/
#include <stdio.h>
#include <math.h>
#include "fdc.h
int main(void) {
    // Derived types
    void *data;
    struct fdc_control_type control;
    struct fdc_inform_type inform;
    // Set problem data
    int m = 3; // number of rows
int n = 4; // number of columns
    int A_ne = 10; // number of nonzeros
    int A_col[] = {0, 1, 2, 3, 0, 1, 2, 3, 1, 3}; // column indices
int A_ptr[] = {0, 4, 8, 10}; // row pointers
double A_val[] = {1.0, 2.0, 3.0, 4.0, 2.0, -4.0, 6.0, -8.0, 5.0, 10.0};
    double b[] = \{5.0, 10.0, 0.0\};
    // Set output storage
    int depen[m]; // dependencies, if any
    int n_depen;
    int status;
    printf(" C sparse matrix indexing\n");
     // Initialize FDC
    fdc_initialize( &data, &control, &status );
    // Set user-defined control options
    control.f_indexing = false; // C sparse matrix indexing
    // Start from 0
    fdc_find_dependent_rows( &control, &data, &inform, &status, m, n, A_ne,
                                 A_col, A_ptr, A_val, b, &n_depen, depen );
      if (n_depen == 0) {
        printf("FDC_find_dependent - no dependent rows, status = 1in",
                 status);
        printf("FDC_find_dependent - dependent rows(s):");
        for( int i = 0; i < n_depen; i++) printf(" %i", depen[i]);
printf(", status = %i\n", status);</pre>
    }else{
        printf("FDC_find_dependent - exit status = %li\n", status);
     // Delete internal workspace
    fdc_terminate( &data, &control, &inform );
```

4.2 fdctf.c

This is the same example, but now fortran-style indexing is used.

```
/\star Full test for the FDC C interface using Fortran sparse matrix indexing \star/
#include <stdio.h>
#include <math.h>
#include "fdc.h"
int main(void) {
    // Derived types
    void *data;
    struct fdc_control_type control;
struct fdc_inform_type inform;
     // Set problem data
     int m = 3; // number of rows
     int n = 4; // number of columns
     int A_ne = 10; // number of nonzeros
    int A_ne = 10; // humber of honzeros
int A_col[] = {1, 2, 3, 4, 1, 2, 3, 4, 2, 4}; // column indices
int A_ptr[] = {1, 5, 9, 11}; // row pointers
double A_val[] = {1.0, 2.0, 3.0, 4.0, 2.0, -4.0, 6.0, -8.0, 5.0, 10.0};
double b[] = {5.0, 10.0, 0.0};
     // Set output storage
     int depen[m]; // dependencies, if any
     int n_depen;
     int status:
     printf(" Fortran sparse matrix indexing\n");
     // Initialize FDC
     fdc_initialize( &data, &control, &status );
     // Set user-defined control options
     control.f_indexing = true; // Fortran sparse matrix indexing
     // Start from 0
     fdc_find_dependent_rows( &control, &data, &inform, &status, m, n, A_ne, A_col, A_ptr, A_val, b, &n_depen, depen);
       if(n_depen == 0){
    printf("FDC_find_dependent - no dependent rows, status = %i\n",
                   status);
       lelse(
         printf("FDC_find_dependent - dependent rows(s):");
         for( int i = 0; i < n_depen; i++) printf(" %i", depen[i]);
printf(", status = %i\n", status);</pre>
     }else{
         printf("FDC_find_dependent - exit status = %li\n", status);
     // Delete internal workspace
     fdc_terminate( &data, &control, &inform );
```

Index

```
fdc.h, 5
     fdc_find_dependent_rows, 8
    fdc_initialize, 7
    fdc_read_specfile, 7
    fdc_terminate, 9
fdc_control_type, 5
fdc\_find\_dependent\_rows
    fdc.h, 8
fdc_inform_type, 6
fdc_initialize
    fdc.h, 7
fdc_read_specfile
    fdc.h, 7
fdc_terminate
    fdc.h, 9
fdc_time_type, 6
```