



C interfaces to GALAHAD SCU

Jari Fowkes and Nick Gould
STFC Rutherford Appleton Laboratory
Wed Feb 2 2022

1 GALAHAD C package scu	1
1.1 Introduction	1
1.1.1 Purpose	1
1.1.2 Authors	1
1.1.3 Originally released	1
1.1.4 Method	2
2 File Index	3
2.1 File List	3
3 File Documentation	5
3.1 scu.h File Reference	5
3.1.1 Data Structure Documentation	5
3.1.1.1 struct sha_control_type	5
3.1.1.2 struct scu_inform_type	5
Index	7

Chapter 1

GALAHAD C package scu

1.1 Introduction

1.1.1 Purpose

Compute the the **solution to an extended system of $n + m$ sparse real linear equations in $n + m$ unknowns**,

$$(1) \begin{pmatrix} A & B \\ C & D \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} b_1 \\ b_2 \end{pmatrix}$$

in the case where the n by n matrix A is nonsingular and solutions to the systems

$$Ax = b \text{ and } A^T y = c$$

may be obtained from an external source, such as an existing factorization. The subroutine uses reverse communication to obtain the solution to such smaller systems. The method makes use of the Schur complement matrix

$$S = D - CA^{-1}B.$$

The Schur complement is stored and factorized as a dense matrix and the subroutine is thus appropriate only if there is sufficient storage for this matrix. Special advantage is taken of symmetry and definiteness in the coefficient matrices. Provision is made for introducing additional rows and columns to, and removing existing rows and columns from, the extended matrix.

Currently, only the control and inform parameters are exposed; these are provided and used by other GALAHAD packages with C interfaces.

1.1.2 Authors

N. I. M. Gould, STFC-Rutherford Appleton Laboratory, England.

C interface, additionally J. Fowkes, STFC-Rutherford Appleton Laboratory.

1.1.3 Originally released

March 2005, C interface January 2022.

1.1.4 Method

The subroutine `galahad_factorize` forms the Schur complement $S = D - CA^{-1}B$ of A in the extended matrix by repeated reverse communication to obtain the columns of $A^{-1}B$. The Schur complement or its negative is then factorized into its QR or, if possible, Cholesky factors.

The subroutine `galahad_solve` solves the extended system using the following well-known scheme:

1. Compute the solution to $Au = b_1$;
2. Compute x_2 from $Sx_2 = b_2 - Cu$;
3. Compute the solution to $Av = Bx_2$; and
4. Compute $x_1 = u - v$.

The subroutines `galahad_append` and `galahad_delete` compute the factorization of the Schur complement after a row and column have been appended to, and removed from, the extended matrix, respectively. The existing factorization is updated to obtain the new one; this is normally more efficient than forming the factorization from scratch.

Chapter 2

File Index

2.1 File List

Here is a list of all files with brief descriptions:

scu.h	5
---------------------------------	---

Chapter 3

File Documentation

3.1 scu.h File Reference

```
#include <stdbool.h>
#include "galahad_precision.h"
```

Data Structures

- struct [sha_control_type](#)
- struct [scu_inform_type](#)

3.1.1 Data Structure Documentation

3.1.1.1 struct sha_control_type

control derived type as a C struct

Data Fields

bool	f_indexing	use C or Fortran sparse matrix indexing
------	------------	---

3.1.1.2 struct scu_inform_type

inform derived type as a C struct

Data Fields

int	alloc_status	the return status from the last attempted internal workspace array allocation or deallocation. A non-zero value indicates that the allocation or deallocation was unsuccessful, and corresponds to the fortran STAT= value on the user's system.
int	inertia[3]	the inertia of S when the extended matrix is symmetric. Specifically, inertia(i), i=0,1,2 give the number of positive, negative and zero eigenvalues of S respectively.

Index

scu.h, [5](#)
scu_inform_type, [5](#)
sha_control_type, [5](#)