

C interfaces to GALAHAD ULS

Jari Fowkes and Nick Gould STFC Rutherford Appleton Laboratory Fri Mar 18 2022

| 1 GALAHAD C package uls | 1 |
|---|----|
| 1.1 Introduction | 1 |
| 1.1.1 Purpose | 1 |
| 1.1.2 Authors | 1 |
| 1.1.3 Originally released | 1 |
| 1.1.4 Terminology | 1 |
| 1.1.5 Method | 2 |
| 1.1.6 Reference | 2 |
| 1.1.7 Call order | 2 |
| 1.1.8 Unsymmetric matrix storage formats | 2 |
| 1.1.8.1 Dense storage format | 3 |
| 1.1.8.2 Sparse co-ordinate storage format | 3 |
| 1.1.8.3 Sparse row-wise storage format | 3 |
| 2 File Index | 5 |
| 2.1 File List | 5 |
| 3 File Documentation | 7 |
| 3.1 uls.h File Reference | 7 |
| 3.1.1 Data Structure Documentation | 7 |
| 3.1.1.1 struct uls_control_type | 7 |
| 3.1.1.2 struct uls_inform_type | 8 |
| 3.1.2 Function Documentation | 10 |
| 3.1.2.1 uls_initialize() | 10 |
| 3.1.2.2 uls_read_specfile() | 10 |
| 3.1.2.3 uls_factorize_matrix() | 11 |
| 3.1.2.4 uls_reset_control() | 12 |
| 3.1.2.5 uls_solve_system() | 13 |
| 3.1.2.6 uls_information() | 13 |
| 3.1.2.7 uls_terminate() | 14 |
| 4 Example Documentation | 15 |
| 4.1 ulst.c | 15 |
| 4.2 ulstf.c | 17 |
| Index | 19 |

Chapter 1

GALAHAD C package uls

1.1 Introduction

1.1.1 Purpose

This package solves dense or sparse unsymmetric systems of linear equations using variants of Gaussian elimination. Given a sparse symmetric $m \times n$ matrix $A = a_{ij}$, and an m-vector b, this subroutine solves the system Ax = b. If b is an n-vector, the package may solve instead the system $A^Tx = b$. Both square (m = n) and rectangular ($m \neq n$) matrices are handled; one of an infinite class of solutions for consistent systems will be returned whenever A is not of full rank.

The method provides a common interface to a variety of well-known solvers from HSL. Currently supported solvers include MA28/GLS and HSL_MA48. Note that **the solvers themselves do not form part of this package and must be obtained separately.** Dummy instances are provided for solvers that are unavailable. Also note that additional flexibility may be obtained by calling the solvers directly rather that via this package.

1.1.2 Authors

N. I. M. Gould, STFC-Rutherford Appleton Laboratory, England.

C interface, additionally J. Fowkes, STFC-Rutherford Appleton Laboratory.

1.1.3 Originally released

August 2009, C interface December 2021.

1.1.4 Terminology

The solvers used each produce an P_RLUP_C factorization of A, where L and U are lower and upper triangular matrices, and P_R and P_C are row and column permutation matrices respectively.

1.1.5 Method

Variants of sparse Gaussian elimination are used.

The solver GLS is available as part of GALAHAD and relies on the HSL Archive packages MA33. To obtain HSL Archive packages, see

```
http://hsl.rl.ac.uk/archive/.
```

The solver HSL MA48 is part of HSL 2007. To obtain HSL 2007 packages, see

```
http://hsl.rl.ac.uk/hsl2007/.
```

1.1.6 Reference

The methods used are described in the user-documentation for

HSL 2007, A collection of {F}ortran codes for large-scale scientific computation (2007).

```
http://www.cse.clrc.ac.uk/nag/hsl
```

1.1.7 Call order

To solve a given problem, functions from the uls package must be called in the following order:

- uls_initialize provide default control parameters and set up initial data structures
- uls_read_specfile (optional) override control values by reading replacement values from a file
- uls_factorize_matrix set up matrix data structures, analyse the structure to choose a suitable order for factorization, and then factorize the matrix A
- uls_reset_control (optional) possibly change control parameters if a sequence of problems are being solved
- uls_solve_system solve the linear system of equations Ax=b or $A^Tx=b$
- uls_information (optional) recover information about the solution and solution process
- uls_terminate deallocate data structures

See Section 4.1 for examples of use.

1.1.8 Unsymmetric matrix storage formats

The unsymmetric m by n matrix A may be presented and stored in a variety of convenient input formats.

Both C-style (0 based) and fortran-style (1-based) indexing is allowed. Choose control.f_indexing as false for C style and true for fortran style; the discussion below presumes C style, but add 1 to indices for the corresponding fortran version.

Wrappers will automatically convert between 0-based (C) and 1-based (fortran) array indexing, so may be used transparently from C. This conversion involves both time and memory overheads that may be avoided by supplying data that is already stored using 1-based indexing.

1.1 Introduction 3

1.1.8.1 Dense storage format

The matrix A is stored as a compact dense matrix by rows, that is, the values of the entries of each row in turn are stored in order within an appropriate real one-dimensional array. In this case, component n*i+j of the storage array A_val will hold the value A_{ij} for $0 \le i \le m-1$, $0 \le j \le n-1$.

1.1.8.2 Sparse co-ordinate storage format

Only the nonzero entries of the matrices are stored. For the l-th entry, $0 \le l \le ne-1$, of A, its row index i, column index j and value A_{ij} , $0 \le i \le m-1$, $0 \le j \le n-1$, are stored as the l-th components of the integer arrays A_row and A_col and real array A_val, respectively, while the number of nonzeros is recorded as A_ne = ne.

1.1.8.3 Sparse row-wise storage format

Again only the nonzero entries are stored, but this time they are ordered so that those in row i appear directly before those in row i+1. For the i-th row of A the i-th component of the integer array A_ptr holds the position of the first entry in this row, while A_ptr(m) holds the total number of entries plus one. The column indices j, $0 \le j \le n-1$, and values A_{ij} of the nonzero entries in the i-th row are stored in components I = A_ptr(i), ..., A_ptr(i+1)-1, $0 \le i \le m-1$, of the integer array A_col, and real array A_val, respectively. For sparse matrices, this scheme almost always requires less storage than its predecessor.

Chapter 2

File Index

2.1 File List

| Here is a list of all files with brief descriptions: | | |
|--|--|--|
| uls.h | | |

6 File Index

Chapter 3

File Documentation

3.1 uls.h File Reference

```
#include <stdbool.h>
#include "galahad_precision.h"
#include "gls.h"
#include "ma48.h"
```

Data Structures

- struct uls control type
- struct uls_inform_type

Functions

- void uls initialize (const char solver[], void **data, struct uls control type *control, int *status)
- void uls_read_specfile (struct uls_control_type *control, const char specfile[])
- void uls_factorize_matrix (struct uls_control_type *control, void **data, int *status, int m, int n, const char type[], int ne, const real_wp_ val[], const int row[], const int col[], const int ptr[])
- void uls_reset_control (struct uls_control_type *control, void **data, int *status)
- void uls_solve_system (void **data, int *status, int m, int n, real_wp_sol[], bool trans)
- void uls information (void **data, struct uls inform type *inform, int *status)
- void uls_terminate (void **data, struct uls_control_type *control, struct uls_inform_type *inform)

3.1.1 Data Structure Documentation

3.1.1.1 struct uls_control_type

control derived type as a C struct

Examples

ulst.c, and ulstf.c.

8 File Documentation

Data Fields

| bool | f_indexing | use C or Fortran sparse matrix indexing |
|----------|------------------------------|---|
| int | error | unit for error messages |
| int | warning | unit for warning messages |
| int | out | unit for monitor output |
| int | print_level | controls level of diagnostic output |
| int | print_level_solver | controls level of diagnostic output from external solver |
| int | initial_fill_in_factor | prediction of factor by which the fill-in will exceed the initial number of nonzeros in ${\cal A}$ |
| int | min_real_factor_size | initial size for real array for the factors and other data |
| int | min_integer_factor_size | initial size for integer array for the factors and other data |
| int | max_factor_size | maximum size for real array for the factors and other data |
| int | blas_block_size_factorize | level 3 blocking in factorize |
| int | blas_block_size_solve | level 2 and 3 blocking in solve |
| int | pivot control | pivot control: |
| | _ | 1 Threshold Partial Pivoting is desired |
| | | 2 Threshold Rook Pivoting is desired |
| | | 3 Threshold Complete Pivoting is desired |
| | | 4 Threshold Symmetric Pivoting is desired |
| | | 5 Threshold Diagonal Pivoting is desired |
| int | pivot_search_limit | number of rows/columns pivot selection restricted to (0 = no restriction) |
| int | minimum_size_for_btf | the minimum permitted size of blocks within the block-triangular form |
| int | max_iterative_refinements | maximum number of iterative refinements allowed |
| bool | stop_if_singular | stop if the matrix is found to be structurally singular |
| real_wp_ | array_increase_factor | factor by which arrays sizes are to be increased if they are too small |
| real_wp_ | switch_to_full_code_density | switch to full code when the density exceeds this factor |
| real_wp_ | array_decrease_factor | if previously allocated internal workspace arrays are greater than array_decrease_factor times the currently required sizes, they are reset to current requirements |
| real_wp_ | relative_pivot_tolerance | pivot threshold |
| real_wp_ | absolute_pivot_tolerance | any pivot small than this is considered zero |
| real_wp_ | zero_tolerance | any entry smaller than this in modulus is reset to zero |
| real_wp_ | acceptable_residual_relative | refinement will cease as soon as the residual $\ Ax-b\ $ falls below max(acceptable_residual_relative $*\ \ b\ $, acceptable_residual_absolute) |
| real_wp_ | acceptable_residual_absolute | see acceptable_residual_relative |
| char | prefix[31] | all output lines will be prefixed by prefix(2:LEN(TRIM(.prefix))-1) where prefix contains the required string enclosed in quotes, e.g. "string" or 'string' |

3.1.1.2 struct uls_inform_type

inform derived type as a C struct

3.1 uls.h File Reference 9

Examples

ulst.c, and ulstf.c.

Data Fields

| Data Ficias | | |
|-------------------|-----------------------|---|
| int | status | reported return status: |
| | | • 0 success |
| | | -1 allocation error |
| | | -2 deallocation error |
| | | -3 matrix data faulty (m < 1, n < 1, ne < 0) |
| | | • -26 unknown solver |
| | | • -29 unavailable option |
| | | -31 input order is not a permutation or is faulty in some other way |
| | | -32 error with integer workspace |
| | | -33 error with real workspace |
| | | -50 solver-specific error; see the solver's info parameter |
| int | alloc_status | STAT value after allocate failure. |
| char | bad_alloc[81] | name of array which provoked an allocate failure |
| int | more_info | further information on failure |
| int | out_of_range | number of indices out-of-range |
| int | duplicates | number of duplicates |
| int | entries_dropped | number of entries dropped during the factorization |
| int | workspace_factors | predicted or actual number of reals and integers to hold factors |
| int | compresses | number of compresses of data required |
| int | entries_in_factors | number of entries in factors |
| int | rank | estimated rank of the matrix |
| int | structural_rank | structural rank of the matrix |
| int | pivot_control | pivot control: |
| | | 1 Threshold Partial Pivoting has been used |
| | | 2 Threshold Rook Pivoting has been used |
| | | 3 Threshold Complete Pivoting has been desired |
| | | 4 Threshold Symmetric Pivoting has been desired |
| | | 5 Threshold Diagonal Pivoting has been desired |
| int | iterative_refinements | number of iterative refinements performed |
| bool | alternative | has an "alternative" y: $A^T y = 0$ and yT b > 0 been found when trying to solve A x = b ? |
| struct gls_ainfo | gls_ainfo | the output arrays from GLS |
| struct gls_finfo | gls_finfo | see gls_ainfo |
| struct gls_sinfo | gls_sinfo | see gls_ainfo |
| struct ma48_ainfo | ma48_ainfo | the output arrays from MA48 |
| struct ma48_finfo | ma48_finfo | see ma48_ainfo |
| struct ma48_sinfo | ma48_sinfo | see ma48_ainfo |
| - | | |

10 File Documentation

3.1.2 Function Documentation

3.1.2.1 uls_initialize()

Set default control values and initialize private data

Select solver, set default control values and initialize private data

Parameters

| in | solver | is a one-dimensional array of type char that specifies the solver package that should be used to factorize the matrix A . It should be one of 'gls', 'ma28' or 'ma48; lower or upper |
|--------|---------|--|
| | | case variants are allowed. |
| in,out | data | holds private internal data |
| out | control | is a struct containing control information (see uls_control_type) |
| out | status | is a scalar variable of type int, that gives the exit status from the package. Possible values are: |
| | | 0. The import was succesful. |
| | | -26. The requested solver is not available. |

Examples

ulst.c, and ulstf.c.

3.1.2.2 uls_read_specfile()

Read the content of a specification file, and assign values associated with given keywords to the corresponding control parameters

Parameters

| i | ln,out | control | is a struct containing control information (see uls_control_type) |
|---|--------|----------|---|
| i | Ln | specfile | is a character string containing the name of the specification file |

3.1 uls.h File Reference

3.1.2.3 uls_factorize_matrix()

Import matrix data into internal storage prior to solution, analyse the sparsity patern, and subsequently factorize the matrix

Parameters

| in | control | is a struct whose members provide control paramters for the remaining prcedures (see |
|--------|---------|--|
| | | uls_control_type) |
| in,out | data | holds private internal data |
| out | status | is a scalar variable of type int, that gives the exit status from the package. Possible values are: |
| | | 0. The import, analysis and factorization were conducted succesfully. |
| | | -1. An allocation error occurred. A message indicating the offending array is written on unit control.error, and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. |
| | | -2. A deallocation error occurred. A message indicating the offending array is written on unit control.error and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. |
| | | -3. The restrictions n > 0 and m> 0 or requirement that the matrix type must contain the relevant string 'dense', 'coordinate' or 'sparse_by_rows has been violated. |
| | | -26. The requested solver is not available. |
| | | -29. This option is not available with this solver. |
| | | -32. More than control.max integer factor size words of internal integer storage are required for in-core factorization. |
| | | -50. A solver-specific error occurred; check the solver-specific information component of inform along with the solver's documentation for more details. |
| in | m | is a scalar variable of type int, that holds the number of rows in the unsymmetric matrix A . |
| in | n | is a scalar variable of type int, that holds the number of columns in the unsymmetric matrix A . |

12 File Documentation

Parameters

| in | type | is a one-dimensional array of type char that specifies the unsymmetric storage scheme used for the matrix A . It should be one of 'coordinate', 'sparse_by_rows' or 'dense'; lower or upper case variants are allowed. |
|----|------|---|
| in | ne | is a scalar variable of type int, that holds the number of entries in A in the sparse co-ordinate storage scheme. It need not be set for any of the other schemes. |
| in | val | is a one-dimensional array of size ne and type double, that holds the values of the entries of the matrix A in any of the supported storage schemes. |
| in | row | is a one-dimensional array of size ne and type int, that holds the row indices of the matrix A in the sparse co-ordinate storage scheme. It need not be set for any of the other three schemes, and in this case can be NULL. |
| in | col | is a one-dimensional array of size ne and type int, that holds the column indices of the matrix A in either the sparse co-ordinate, or the sparse row-wise storage scheme. It need not be set when the dense storage schemes is used, and in this case can be NULL. |
| in | ptr | is a one-dimensional array of size $m+1$ and type int, that holds the starting position of each row of the matrix A , as well as the total number of entries plus one, in the sparse row-wise storage scheme. It need not be set when the other schemes are used, and in this case can be NULL. |

Examples

ulst.c, and ulstf.c.

3.1.2.4 uls_reset_control()

Reset control parameters after import if required.

Parameters

| in | control | is a struct whose members provide control paramters for the remaining prcedures (see uls_control_type) |
|--------|---------|--|
| in,out | data | holds private internal data |
| in,out | status | is a scalar variable of type int, that gives the exit status from the package. Possible values are: |
| | | 0. The import was succesful. |

Examples

ulst.c, and ulstf.c.

3.1 uls.h File Reference

3.1.2.5 uls_solve_system()

Solve the linear system Ax = b or $A^Tx = b$.

Parameters

| in,out | data | holds private internal data |
|---------|--------|--|
| in, out | status | is a scalar variable of type int, that gives the exit status from the package. Possible values are: 0. The required solution was obtained. -1. An allocation error occurred. A message indicating the offending array is written on unit control.error, and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. -2. A deallocation error occurred. A message indicating the offending array is written on unit control.error and the returned allocation status and a string containing the name of the offending array are held in inform.alloc_status and inform.bad_alloc respectively. -34. The package PARDISO failed; check the solver-specific information components inform.pardiso iparm and inform.pardiso_dparm along with PARDISO's documentation for more details. -35. The package WSMP failed; check the solver-specific information components inform.wsmp_iparm and inform.wsmp dparm along with WSMP's documentation for more details. |
| in | m | is a scalar variable of type int, that holds the number of rows in the unsymmetric matrix ${\cal A}.$ |
| in | n | is a scalar variable of type int, that holds the number of columns in the unsymmetric matrix ${\cal A}.$ |
| in,out | sol | is a one-dimensional array of size n and type double. On entry, it must hold the vector b . On a successful exit, its contains the solution x . |
| in | trans | is a scalar variable of type bool, that specifies whether to solve the equation $A^Tx=b$ (trans=true) or $Ax=b$ (trans=false). |

Examples

ulst.c, and ulstf.c.

3.1.2.6 uls_information()

```
void uls_information (
     void ** data,
```

14 File Documentation

```
struct uls_inform_type * inform,
int * status )
```

Provides output information

Parameters

| in,out | data | holds private internal data |
|--------|--------|---|
| out | inform | is a struct containing output information (see uls_inform_type) |
| out | status | is a scalar variable of type int, that gives the exit status from the package. Possible values are (currently): |
| | | 0. The values were recorded succesfully |

Examples

ulst.c, and ulstf.c.

3.1.2.7 uls_terminate()

Deallocate all internal private storage

Parameters

| in,ou | ıt data | holds private internal data |
|-------|----------------|---|
| out | control | is a struct containing control information (see uls_control_type) |
| out | inform | is a struct containing output information (see uls_inform_type) |

Examples

ulst.c, and ulstf.c.

Chapter 4

Example Documentation

4.1 ulst.c

This is an example of how to use the package in conjunction with the sparse linear solver sils. A variety of supported matrix storage formats are illustrated.

Notice that C-style indexing is used, and that this is flaggeed by setting control.f_indexing to false.

```
/* ulst.c */
/\star Full test for the ULS C interface using C sparse matrix indexing \star/
#include <stdio.h>
#include <math.h>
#include <stdlib.h>
#include <float.h>
#include "uls.h"
int maxabsarray(double a[],int n, double *maxabs);
int main (void)
     // Derived types
     void *data;
     struct uls_control_type control;
     struct uls_inform_type inform;
     // Set problem data
     int m = 5; // column dimension of A
     int n = 5; // column dimension of A
     int ne = 7; // number of entries of A
     int dense_ne = 25; // number of elements of A as a dense matrix
     int row[] = {0, 1, 1, 2, 2, 3, 4}; // row indices int col[] = {0, 0, 4, 1, 2, 2, 3}; // column indices int ptr[] = {0, 1, 3, 5, 6, 7}; // pointers to indices double val[] = {2.0, 3.0, 6.0, 4.0, 1.0, 5.0, 1.0}; // values
     double dense[] = {2.0, 0.0, 0.0, 0.0, 0.0, 3.0, 0.0, 0.0, 6.0,
                             0.0, 4.0, 1.0, 0.0, 0.0, 0.0, 0.0, 5.0, 0.0, 0.0,
    0.0, 0.0, 0.0, 1.0, 0.0);

double rhs[] = {2.0, 33.0, 11.0, 15.0, 4.0};

double rhst[] = {8.0, 12.0, 23.0, 5.0, 12.0};

double sol[] = {1.0, 2.0, 3.0, 4.0, 5.0};
     int i, status;
     double x[n];
     double error[n];
     Bool trans:
     double norm_residual;
     double good_x = pow(DBL_EPSILON, 0.3333);
     printf(" C sparse matrix indexing\n\n");
     RHST refine\n");
     for( int d=1; d <= 3; d++){
    // Initialize ULS - use the gls solver
    uls_initialize( "gls", &data, &control, &status );</pre>
           // Set user-defined control options
          control.f_indexing = false; // Fortran sparse matrix indexing
switch(d) { // import matrix data and factorize
    case 1: // sparse co-ordinate storage
    printf(" coordinate ");
                     uls_factorize_matrix( &control, &data, &status, m, n,
                                                 "coordinate", ne, val, row, col, NULL );
```

}

```
break;
    case 2: // sparse by rows
    printf(" sparse by rows ");
         break:
    case 3: // dense
        printf(" dense
         uls_factorize_matrix( &control, &data, &status, m, n, "dense",
                                 dense_ne, dense, NULL, NULL, NULL );
// Set right-hand side and solve the system A x = b
for(i=0; i<n; i++) x[i] = rhs[i];
trans = false;
uls_solve_system( &data, &status, m, n, x, trans );
uls_information( &data, &inform, &status );
if(inform.status == 0){
  for(i=0; i<n; i++) error[i] = x[i]-sol[i];</pre>
  status = maxabsarray( error, n, &norm_residual );
  if(norm_residual < good_x){
  printf(" ok ");</pre>
  lelse(
    printf(" fail ");
}else{
    printf(" ULS_solve exit status = %li\n", inform.status);
// printf("sol: ");
// for( int i = 0; i < n; i++) printf("%f ", x[i]);
// resolve, this time using iterative refinement
control.max_iterative_refinements = 1;
uls_reset_control( &control, &data, &status );
for(i=0; i<n; i++) x[i] = rhs[i];</pre>
uls_solve_system( &data, &status, m, n, x, trans );
uls_information( &data, &inform, &status );
if(inform.status == 0){
  for (i=0; i<n; i++) error[i] = x[i]-sol[i];</pre>
  status = maxabsarray( error, n, &norm_residual );
  if(norm_residual < good_x){
  printf(" ok ");</pre>
    printf("
  lelse(
   printf(" fail ");
    printf(" ULS_solve exit status = %1i\n", inform.status);
// Set right-hand side and solve the system A^T x = b
for(i=0; i<n; i++) x[i] = rhst[i];</pre>
trans = true;
uls_solve_system( &data, &status, m, n, x, trans );
uls_information( &data, &inform, &status );
if(inform.status == 0){
  for(i=0; i<n; i++) error[i] = x[i]-sol[i];</pre>
  status = maxabsarray( error, n, &norm_residual );
  if(norm_residual < good_x){
  printf(" ok ");</pre>
   printf("
   printf(" fail ");
lelsef
    printf(" ULS_solve exit status = %1i\n", inform.status);
// for( int i = 0; i < n; i++) printf("%f ", x[i]);
// resolve, this time using iterative refinement
control.max_iterative_refinements = 1;
uls_reset_control( &control, &data, &status );
for(i=0; i<n; i++) x[i] = rhst[i];</pre>
uls_solve_system( &data, &status, m, n, x, trans );
uls_information( &data, &inform, &status );
if(inform.status == 0){
  for(i=0; i<n; i++) error[i] = x[i]-sol[i];
status = maxabsarray( error, n, &norm_residual );</pre>
  if(norm_residual < good_x){
  printf(" ok ");</pre>
   printf(" fail ");
lelse(
   printf(" ULS_solve exit status = %1i\n", inform.status);
// Delete internal workspace
uls_terminate( &data, &control, &inform );
printf("\n");
```

4.2 ulstf.c 17

```
int maxabsarray(double a[],int n, double *maxabs)
{
    int i;
    double b,max;
    max=abs(a[0]);
    for(i=1; i<n; i++)
    {
        b = abs(a[i]);
    if(max<b)
        max=b;
    }
    *maxabs=max;
}</pre>
```

4.2 ulstf.c

This is the same example, but now fortran-style indexing is used.

```
/* ulstf.c */
/\star Full test for the ULS C interface using Fortran sparse matrix indexing \star/
#include <stdio.h>
#include <math.h>
#include <stdlib.h>
#include <float.h>
#include "uls.h"
int maxabsarray(double a[],int n, double *maxabs);
int main(void) {
   // Derived types
    void *data;
    struct uls_control_type control;
    struct uls_inform_type inform;
    // Set problem data
    int m = 5; // column dimension of A
    int n = 5; // column dimension of A
    int ne = 7; // number of entries of A
    int dense_ne = 25; // number of elements of A as a dense matrix
   0.0, 0.0, 0.0, 1.0, 0.0};
    double rhs[] = {2.0, 33.0, 11.0, 15.0, 4.0};
double rhst[] = {8.0, 12.0, 23.0, 5.0, 12.0};
double sol[] = {1.0, 2.0, 3.0, 4.0, 5.0};
    int i, status;
double x[n];
    double error[n];
    _Bool trans;
    double norm_residual;
    double good_x = pow(DBL_EPSILON, 0.3333);
    printf(" storage
                              RHS refine
                                             RHST refine\n");
    for( int d=1; d <= 3; d++){
        // Initialize ULS - use the gls solver
        uls_initialize( "gls", &data, &control, &status );
       // Set user-defined control options
control.f_indexing = true; // Fortran sparse matrix indexing
        switch(d) { // import matrix data and factorize
           case 1: // sparse co-ordinate storage
                                        ");
                printf(" coordinate
                uls_factorize_matrix( &control, &data, &status, m, n,
                                     "coordinate", ne, val, row, col, NULL);
            case 2: // sparse by rows
                printf(" sparse by rows ");
                uls_factorize_matrix( &control, &data, &status, m, n,
                                    "sparse_by_rows", ne, val, NULL, col, ptr );
            case 3: // dense
                printf(" dense
                                        ");
                uls_factorize_matrix( &control, &data, &status, m, n,
                                     "dense", dense_ne, dense, NULL, NULL, NULL);
        // Set right-hand side and solve the system A x = b
        for(i=0; i<n; i++) x[i] = rhs[i];
        trans = false;
        uls_solve_system( &data, &status, m, n, x, trans );
```

```
uls_information( &data, &inform, &status );
          if(inform.status == 0){
             for (i=0; i<n; i++) error[i] = x[i]-sol[i];</pre>
            status = maxabsarray( error, n, &norm_residual );
            if(norm_residual < good_x){
  printf(" ok ");</pre>
             }else{
              printf(" fail ");
          }else{
              printf(" ULS_solve exit status = %1i\n", inform.status);
          // printf("sol: ");
          // for( int i = 0; i < n; i++) printf("%f ", x[i]);
          // resolve, this time using iterative refinement
          control.max_iterative_refinements = 1;
          uls_reset_control( &control, &data, &status );
for(i=0; i<n; i++) x[i] = rhs[i];
uls_solve_system( &data, &status, m, n, x, trans );</pre>
          uls_information( &data, &inform, &status );
          if(inform.status == 0){
             for (i=0; i< n; i++) error[i] = x[i]-sol[i];
            status = maxabsarray( error, n, &norm_residual );
if(norm_residual < good_x) {
  printf(" ok ");</pre>
             }else{
              printf(" fail ");
          }else{
              printf(" ULS_solve exit status = %1i\n", inform.status);
          // Set right-hand side and solve the system A^T x = b
          for(i=0; i<n; i++) x[i] = rhst[i];</pre>
          trans = true;
          uls_solve_system( &data, &status, m, n, x, trans );
uls_information( &data, &inform, &status );
if(inform.status == 0){
            for (i=0; i<n; i++) error[i] = x[i]-sol[i];</pre>
            status = maxabsarray( error, n, &norm_residual );
            if(norm_residual < good_x){
  printf(" ok ");</pre>
              printf("
            lelse(
              printf(" fail ");
          }else{
              printf(" ULS_solve exit status = %1i\n", inform.status);
          // printf("sol: ");
// for( int i = 0; i < n; i++) printf("%f ", x[i]);
// resolve, this time using iterative refinement</pre>
          control.max_iterative_refinements = 1;
          uls_reset_control( &control, &data, &status );
         for(i=0; i<n; i++) x[i] = rhst[i];
uls_solve_system( &data, &status, m, n, x, trans );
uls_information( &data, &inform, &status );
if(inform.status == 0){</pre>
            for (i=0; i<n; i++) error[i] = x[i]-sol[i];</pre>
            status = maxabsarray( error, n, &norm_residual );
            if(norm_residual < good_x){
  printf(" ok ");</pre>
              printf("
             lelse(
              printf(" fail ");
              printf(" ULS_solve exit status = %1i\n", inform.status);
          // Delete internal workspace
          uls_terminate( &data, &control, &inform );
          printf("\n");
int maxabsarray(double a[],int n, double *maxabs)
     int i:
     double b, max;
     max=abs(a[0]);
     for (i=1; i<n; i++)</pre>
         b = abs(a[i]);
     if (max<b)
           max=b;
     *maxabs=max;
```

Index

```
uls.h, 7
     uls_factorize_matrix, 11
     uls_information, 13
     uls_initialize, 10
    uls_read_specfile, 10
    uls_reset_control, 12
     uls_solve_system, 12
    uls_terminate, 14
uls_control_type, 7
uls_factorize_matrix
    uls.h, 11
uls_inform_type, 8
uls_information
    uls.h, 13
uls_initialize
    uls.h, 10
uls_read_specfile
    uls.h, 10
uls_reset_control
    uls.h, 12
uls_solve_system
    uls.h, 12
uls_terminate
    uls.h, 14
```