



Robotics Project

3 DOF Robot Arm

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This document explains a procedure for getting models of robot kinematics that are appropriate for robot control design. The procedure consists of the following steps:

- 1- derivation of robot kinematic models and establishing correctness of their structures
- 2- experimental estimation of the model parameters
- 3- model validation

Motors calculations:

Robotics Project

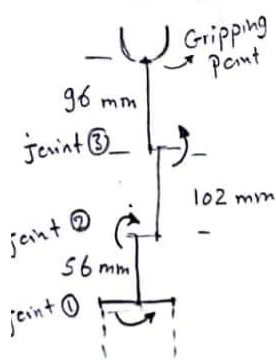


Diagram labels: joint ③, 96 mm, Gripping Point, joint ②, 102 mm, 56 mm, joint ①, motor, 35.31 mm

* Gripping Point

$$\therefore F * 0.035 = T$$

$$= 0.13$$

$F = 3.7 \text{ N} \rightarrow \text{Assuming } \mu = 0.2$

max Weight gripper can hold = $3.7 * 0.2 = 0.74 \text{ N}$

= 74 gram Force

* joint ③ $0.74 * 0.096 = 0.071 \text{ N-m}$

$T_3 = 0.71 \text{ Kg-cm}$ # weight of 3.2 kg servo

* joint ② $T_2 = (0.102 + 0.096) * 0.74 + 0.36 * (0.102)$

$= 0.183 \text{ N-m} = \text{1.8 Kg-cm}$

* joint ① \rightarrow the load on this joint as (Torque) is due to acceleration in movements

So assuming all links are horizontal $L = 0.102 + 0.096 = 0.198 \text{ m}$

With $m = (36 * 2 + 74) = 150 \text{ gram}$

$\therefore T = 3.2 \text{ Kg-cm} = 0.32 \text{ N-m} \Rightarrow 0.32 = 0.198 * 0.15 * a$

$a = 10.77 \text{ m/s}^2$
max

- ABS 40 MPa

- PLA 65 MPa

- motor torque 3.2 Kg-cm = 0.32 N-m

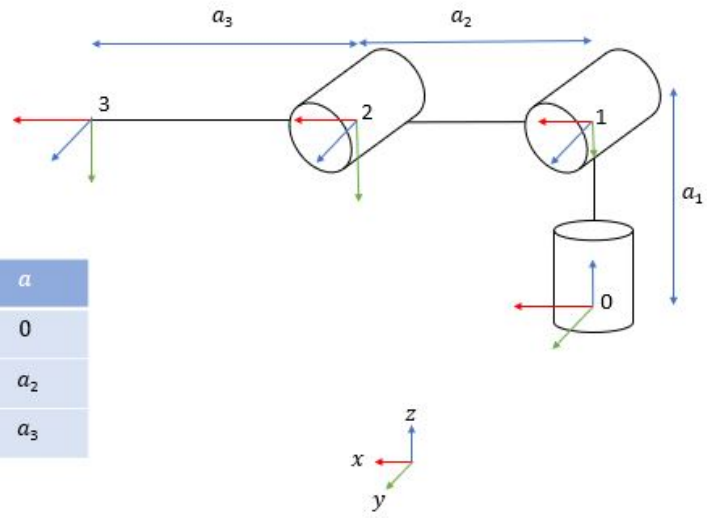
neglecting links inertia

\Rightarrow Final Notes

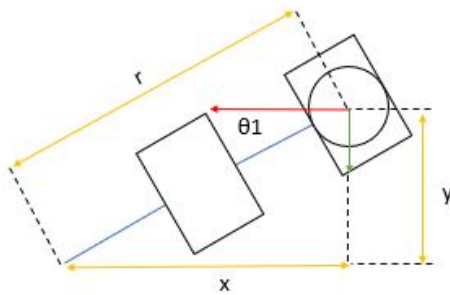
* Fixations of motors & Load on shafts by pending

DH parameter:

	θ	α	d	a
1	θ_1	$-\pi/2$	a_1	0
2	θ_2	0	0	a_2
3	θ_3	0	0	a_3

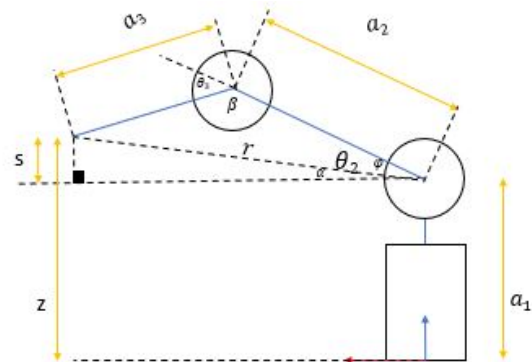


Inverse Kinematics:



$$r = \sqrt{x^2 + y^2}$$

$$\theta_1 = \tan^{-1} \frac{y}{x}$$



$$s = z - a_1$$

$$\alpha = \sin^{-1} \frac{s}{r}, \theta_2 = \alpha + \varphi, \theta_3 = \pi - \beta$$

$$a_3^2 = a_2^2 + r^2 - 2a_2r \cos \varphi$$

$$\varphi = \cos^{-1} \frac{a_2^2 + r^2 - a_3^2}{2a_2r}$$

$$\theta_2 = \alpha + \cos^{-1} \frac{a_2^2 + r^2 - a_3^2}{2a_2r}$$

$$r^2 = a_2^2 + a_3^2 - 2a_2a_3 \cos \beta$$

$$\theta_3 = \pi - \cos^{-1} \frac{a_2^2 + a_3^2 - r^2}{2a_2a_3}$$

CAD model:



The Arduino code for controlling the robot arm using FK and IK by a joystick with a simulation of its moves in V-rep using ROS for IK:

1- Forward Kinematics With PS4 Controller :

```
#include <PS4USB.h>

#ifdef dobogusinclude
#include <spi4teensy3.h>
#endif

#include <SPI.h>

USB Usb;

PS4USB PS4(&Usb);
```

```
bool printAngle, printTouch;  
uint8_t oldL2Value, oldR2Value;
```

```
int ix_axis_left;  
int ix_left;  
int iy_axis_left;  
int iy_left;  
int ix_axis_right;  
int ix_right;
```

```
int g_angle = 90 ;  
int b_angle = 90 ;  
int s_angle = 90 ;  
int e_angle = 90 ;
```

```
int vrep_b_angle;  
int vrep_s_angle;  
int vrep_e_angle;  
int vrep_g_angle;
```

```
#include <VarSpeedServo.h>
```

```
VarSpeedServo servo1, servo2, servo3, servo4;
```

```
void setup() {  
  //Serial.begin(115200);  
  Serial.begin(115200);
```

```

#if !defined(__MIPSEL__)

    while (!Serial); // Wait for serial port to connect
#endif

    if (Usb.Init() == -1) {
        //Serial.print(F("\r\nOSC did not start"));
        while (1); // Halt

    }

    // Serial.print(F("\r\nPS4 USB Library Started"));

    servo1.attach(4);
    servo2.attach(5);
    servo3.attach(6);
    servo4.attach(7);

}

void loop() {

    //V-REP joint values

    vrep_b_angle = map ( b_angle , 10, 180, -45, 125);
    vrep_s_angle = map ( s_angle, 10, 180, -100, 70);
    vrep_e_angle = map ( e_angle, 0, 180, 10, -170);
    vrep_g_angle = map ( g_angle, 80, 170, -20, 80);

    //serial_senddata();

    Usb.Task();

```

```
if (PS4.connected()) {
```

```
// base servo control by left x axis pad on PS4 Controller
```

```
if (PS4.getAnalogHat(LeftHatX) && PS4.getAnalogHat(LeftHatX) < 100) {
```

```
  // Serial.print(F("\r\nLeft_X: "));
```

```
  // Serial.print(PS4.getAnalogHat(LeftHatX));
```

```
  // Serial.print(F("\r\nbase angle: "));
```

```
  // Serial.print(b_angle);
```

```
  ix_axis_left = map (PS4.getAnalogHat(LeftHatX), 0, 100, 30, 0);
```

```
  b_angle++;
```

```
  delay(40);
```

```
  if ( b_angle >= 10 || b_angle <= 180 ){
```

```
    b_angle++;
```

```
  }
```

```
  if ( b_angle < 10) {
```

```
    b_angle = 10;
```

```
  }
```

```
  if (b_angle > 180) {
```

```
    b_angle = 180;
```

```
  }
```

```
servo1.write(b_angle, ix_axis_left);
```

```
serial_senddata();  
}
```

```
if (PS4.getAnalogHat(LeftHatX) && PS4.getAnalogHat(LeftHatX) > 150){  
    // Serial.print(F("\r\nLeft_X: "));  
    // Serial.print(PS4.getAnalogHat(LeftHatX));  
    // Serial.print(F("\r\nbase angle: "));  
    // Serial.print(b_angle);  
    ix_left = map(PS4.getAnalogHat(LeftHatX), 150, 255, 0, 30);
```

```
    b_angle--;  
    delay(40);  
    if ( b_angle >= 10 || b_angle <= 180 ){  
        b_angle--;  
    }  
    if ( b_angle < 10) {  
        b_angle = 10;  
    }  
    if (b_angle > 180) {  
        b_angle = 180;  
    }  
    servo1.write(b_angle, ix_left);  
    serial_senddata();  
}
```

```
// shoulder servo control by left Y axis PS4 controller
```

```
if (PS4.getAnalogHat(LeftHatY) && PS4.getAnalogHat(LeftHatY) < 100) { // These are the only analog  
buttons on the PS4 controller
```



```

// Serial.print(F("\r\nLeft_Y: "));
// Serial.print(PS4.getAnalogHat(LeftHatY));
// Serial.print(F("\r\nshoulder angle: "));
// Serial.print(s_angle);
iy_axis_left = map (PS4.getAnalogHat(LeftHatY), 0, 100, 30, 0);
s_angle++;
delay(40);
if ( s_angle >= 10 || s_angle <= 180 ){
    s_angle++;
}
if ( s_angle < 10) {
    s_angle = 10;
}
if (s_angle > 180) {
    s_angle = 180;
}
servo2.write(s_angle, iy_axis_left);
serial_senddata();
}

if (PS4.getAnalogHat(LeftHatY) && PS4.getAnalogHat(LeftHatY) > 150){
    // Serial.print(F("\r\nLeft_Y: "));
    // Serial.print(PS4.getAnalogHat(LeftHatY));
    // Serial.print(F("\r\nshoulder angle: "));
    // Serial.print(s_angle);
    iy_left = map (PS4.getAnalogHat(LeftHatY), 150, 225, 0, 30);

    s_angle--;
    delay(40);
}

```

```

if ( s_angle >= 10 || s_angle <= 180 ){
    s_angle--;
}
if ( s_angle < 10) {
    s_angle = 10;
}
if (s_angle > 180) {
    s_angle = 180;
}
servo2.write(s_angle, iy_left);
serial_senddata();
}

```

// ELBOW SERVO CONTROL BY PS4 RIGHT X AXIS on PS4 controller

```

if (PS4.getAnalogHat(RightHatY) && PS4.getAnalogHat(RightHatY) < 100) { // These are the only
analog buttons on the PS4 controller

```

```

    // Serial.print(F("\r\nRight_X: "));

```

```

    // Serial.print(PS4.getAnalogHat(RightHatX));

```

```

    // Serial.print(F("\r\nelbow angle: "));

```

```

    // Serial.print(e_angle);

```

```

    ix_axis_right = map (PS4.getAnalogHat(RightHatY), 0, 100, 30, 0);

```

```

    // Serial.print(F("\r\nRight_X inverse: "));

```

```

    // Serial.print(ix_axis_right);

```

```

    e_angle++;

```

```

    delay(40);

```

```

if ( e_angle >= 0 || e_angle <= 180 ){
    e_angle++;
}
if ( e_angle < 0 ) {
    e_angle = 0;
}
if (e_angle > 180) {
    e_angle = 180;
}
servo3.write(e_angle, ix_axis_right);
serial_senddata();
}

```

```

if (PS4.getAnalogHat(RightHatY) && PS4.getAnalogHat(RightHatY) > 150){
    //// Serial.print(F("\r\nRight_X: "));
    // Serial.print(PS4.getAnalogHat(RightHatX));
    // Serial.print(F("\r\nelbow angle: "));
    // Serial.print(e_angle);
    ix_right = map ( PS4.getAnalogHat(RightHatY), 150, 255, 0, 30);

    e_angle--;
    delay(40);
    if ( e_angle >= 0 || e_angle <= 180 ){
        e_angle--;
    }
    if ( e_angle < 0 ) {
        e_angle = 0;
    }
    if (e_angle > 180) {

```

```
    e_angle = 180;
  }

  servo3.write(e_angle, ix_right);
  serial_senddata();
}
```

// gripper control by R2 & L2 analog buttons on PS4 controller

```
if (PS4.getAnalogButton(L2)) { // These are the only analog buttons on the PS4 controller
  //Serial.print(F("\r\nL2: "));
  // Serial.print(PS4.getAnalogButton(L2));
  // Serial.print(F("\r\ngripper angle: "));
  // Serial.print(g_angle);
  g_angle++;
  delay(40);
  if ( g_angle >= 80 || g_angle <= 175 ){
    g_angle++;
  }
  if ( g_angle < 80) {
    g_angle = 80;
  }
  if (g_angle > 175) {
    g_angle = 175;
  }

  servo4.write(g_angle, PS4.getAnalogButton(L2));
  serial_senddata();
}
```

```

if (PS4.getAnalogButton(R2)){
    //Serial.print(F("\r\nR2: "));
    // Serial.print(PS4.getAnalogButton(R2));
    // Serial.print(F("\r\ngribber angle: "));
    // Serial.print(g_angle);

    g_angle--;
    delay(40);
    if ( g_angle >= 80 || g_angle <= 175 ){
        g_angle--;
    }
    if ( g_angle < 80) {
        g_angle = 80;
    }
    if (g_angle > 175) {
        g_angle = 175;
    }
    servo4.write(g_angle, PS4.getAnalogButton(R2));
    serial_senddata();
}

if (PS4.getButtonClick(CIRCLE)) {
    Position_1();
    Serial.print(35);
    Serial.print(",");
    Serial.print(-20);
    Serial.print(",");
    Serial.print(-80);
    Serial.print(",");

```

```
    Serial.println(-20);  
    delay(40);  
}  
if (PS4.getButtonClick(CROSS)) {  
    Position_2();  
    Serial.print(-45);  
    Serial.print(",");  
    Serial.print(-100);  
    Serial.print(",");  
    Serial.print(-170);  
    Serial.print(",");  
    Serial.println(80);  
    delay(40);  
}  
if (PS4.getButtonClick(SQUARE)) {  
    Position_3();  
    Serial.print(125);  
    Serial.print(",");  
    Serial.print(-100);  
    Serial.print(",");  
    Serial.print(10);  
    Serial.print(",");  
    Serial.println(47);  
    delay(40);  
}  
if (PS4.getButtonClick(TRIANGLE)) {  
    Position_4();
```

```
Serial.print(50);  
Serial.print(",");  
Serial.print(-35);  
Serial.print(",");  
Serial.print(-155);  
Serial.print(",");  
Serial.println(-20);  
delay(40);  
}  
}  
  
// delay(1000);  
  
}
```

```
void serial_senddata(){  
  
Serial.print(vrep_b_angle);  
Serial.print(",");  
Serial.print(vrep_s_angle);  
Serial.print(",");  
Serial.print(vrep_e_angle);  
Serial.print(",");  
Serial.println(vrep_g_angle);  
  
delay(40);
```

```
    return;  
}
```

```
void Position_1(){  
    servo1.write(90, 35);  
    servo2.write(90, 35);  
    servo3.write(90, 35);  
    servo4.write(80, 35);
```

```
    servo1.wait();  
    servo2.wait();  
    servo3.wait();  
    servo4.wait();
```

```
    delay(300);  
}
```

```
void Position_2(){  
    servo1.write(10, 35);  
    servo2.write(10, 35);  
    servo3.write(180, 35);  
    servo4.write(170, 35);
```

```
    servo1.wait();  
    servo2.wait();  
    servo3.wait();  
    servo4.wait();
```



```
delay(300);
```

```
}
```

```
void Position_3(){
```

```
servo1.write(180, 35);
```

```
servo2.write(10, 35);
```

```
servo3.write(0, 35);
```

```
servo4.write(140, 35);
```

```
servo1.wait();
```

```
servo2.wait();
```

```
servo3.wait();
```

```
servo4.wait();
```

```
delay(300);
```

```
}
```

```
void Position_4(){
```

```
servo1.write(105, 35);
```

```
servo2.write(75, 35);
```

```
servo3.write(165, 35);
```

```
servo4.write(80, 35);
```

```
servo1.wait();
```

```
servo2.wait();
```

```
servo3.wait();
```

```
servo4.wait();
```

```
delay(300);
```

```
}
```

2- Inverse Kinematics Arduino Code :

```
#include <VarSpeedServo.h>

#include <math.h>

/* Arm dimensions( mm ) */
#define a1 55 //a1 = base to 2# joint length arm
#define a2 111 //a2 = length arm from joint 2 to 3
#define a3 140 //a3 = length arm from joint #3 to gripper

#define base_servo 4

/* Using Servo 3.2 Kg.cm */
#define shoulder_servo 5

/* Using Servo 3.2 Kg.cm */
#define elbow_servo 6

/* Using Micro servo 1.3 Kg.cm */
#define Gripper_servo 7

/*Using Micro servo 1.3 Kg.cm */

float x_coord;    // X coordinate of the end point
float y_coord;    // Y coordinate of the end point
float z_coord;    // Z coordinate of the end point
float gripper_angle; //gripper angle

#define speed1 30
#define speed2 100
```

```
#define speed3 170
```

```
//Some Values to be used
```

```
#define pi 3.141592654
```

```
VarSpeedServo servo1,servo2,servo3,servo4;
```

```
void setup()
```

```
{
```

```
servo1.attach( base_servo, 544, 2400 ); //setting min and max values in microseconds,default min is 544,  
max is 2400
```

```
servo2.attach( shoulder_servo, 544, 2400 );
```

```
servo3.attach( elbow_servo, 544, 2400 );
```

```
servo4.attach( Gripper_servo, 544, 2400 );
```

```
//servos.start(); //Start the servo shield
```

```
servo_park();
```

```
delay( 2000 );
```

```
Serial.begin( 9600 );
```

```
Serial.println("Start");
```

```
}
```

```

void loop()
{
// test fixed positions

//set_arm ( 20, 20, 0, 90, 10);
//delay(1000);
//set_arm ( 20, 50, 0, 150, 10);
//delay(1000);
//set_arm ( 20, 70, 0, 150, 10);
//delay(3000);


if(Serial.available()>0){

char data = Serial.read();

switch(data) {

case 'x' : x_coord++; //adjust x position up
break;

case 'u' : x_coord--; // adjust x position down
break;


case 'y' : y_coord++; // adjust y position up
break;

case 'v' : y_coord--; // adjust y position down
break;

```

```
case 'z' : z_coord++; // adjust z position up
```

```
break;
```

```
case 'w' : z_coord--; // adjust z position down
```

```
break;
```

```
case 'r' : gripper_angle++; //adjust gripper wider
```

```
    // set boundaries to the gripper
```

```
    if( gripper_angle > 150 ) {
```

```
        gripper_angle = 120;
```

```
    }
```

```
    break;
```

```
case 's' : gripper_angle--; // adjust gripper narrower
```

```
    // set boundaries to the gripper
```

```
    if( gripper_angle < 70 ) {
```

```
        gripper_angle = 170;
```

```
    }
```

```
    break;
```

```
case 'm' : arm_park();
```

```
break;
```

```
case 'n' : servo_park();
```

```
break;
```

```
}
```

```
set_arm(x_coord, y_coord, z_coord, gripper_angle, speed2);
```

```
}
```

```
}
```

```
// XYZ Positioning using the base, shoulder, elbow joints
```

```
void set_arm( float x, float y, float z, float gripper, int servospeed){
```

```
float theta1_r = atan2( x, y ); // in radian value
```

```
float theta1_d = ((theta1_r*180)/pi);
```

```
if(theta1_d >= 10 || theta1_d <= 180 ){
```

```
    theta1_d = theta1_d;
```

```
}
```

```
if( theta1_d <=9){
```

```
    theta1_d =10;
```

```
}
```

```
if ( theta1_d >= 181 ){
```

```
    theta1_d = 180;
```

```
}
```

```
float r_distance = sqrt(( x * x ) + ( y * y ));
```

```
float s = z -a1 ; // length in mm
```

```
float alpha_r = asin(s/r_distance); // s must always be less than R distance
```

```
float alpha_d = ((alpha_r*180)/pi);
```

```
float theta2_r = alpha_r + acos((sq(a2)+sq(r_distance)-sq(a3))/(2*a2*r_distance));
```

```
float theta2_d = ((theta2_r*180)/pi);
```

```
if(theta2_d >= 10 || theta2_d <= 180 ){
```

```
    theta2_d = theta2_d;
```

```
}
```

```
if( theta2_d <=9 ){
```

```
    theta2_d = 10;
```

```
}
```

```
if (theta2_d >= 181 ) {
```

```
    theta2_d = 180;
```

```
}
```

```
float theta3_r = pi - acos((sq(a1)+sq(a3)-sq(r_distance))/(2*a2*a3));
```

```
float theta3_d = ((theta3_r*180)/pi);
```

```
if(theta3_d >= 0 || theta3_d <= 180 ){
```



```
        theta3_d = theta3_d;  
    }  
    if( theta3_d <=0 ){  
        theta3_d = 0;  
    }
```

```
    if( theta3_d > 180) {  
        theta3_d = 180 ;  
    }
```

```
servo1.write ( theta1_d, servospeed);  
servo2.write ( theta2_d, servospeed);  
servo3.write ( theta3_d, servospeed);  
servo4.write ( gripper, servospeed);  
servo1.wait();  
servo2.wait();  
servo3.wait();  
servo4.wait();  
Serial.print("T1:");  
Serial.print(theta1_d);  
Serial.print("    T2:");  
Serial.print(theta2_d);  
Serial.print("    T3:");  
Serial.println(theta3_d);  
  
Serial.print("X:");  
Serial.print(x);  
Serial.print("    Y:");
```

```

Serial.print(y);
Serial.print("    Z:");
Serial.println(z);

delay(100); // delay to give the robot time to perform the required position

}

```

```

void servo_park(){          // park position using servo angles
    servo1.write ( 150, speed1);
    //servo.setposition(base_servo ): (Angle, Speed)
    servo2.write ( 105, speed1);
    //servo.setposition( shoulder_servo )
    servo3.write ( 170, speed1);
    //servo.setposition( elbow_servo )
    servo4.write ( 80, speed1);
    //servo.setposition( Gripper_servo )
    servo1.wait();
    servo2.wait();
    servo3.wait();
    servo4.wait();
    delay(500);

    return;
}

```

```

void arm_park(){ // park position using XYZ Co-Ordinates

```

```
set_arm(x_coord = 70, y_coord = 0, z_coord = 0, gripper_angle= 140, speed1);  
delay (500);  
}
```

```
void zero_x() //fixed y axis movement  
{  
for( double yaxis = 250.0; yaxis < 400.0; yaxis += 1 ) {  
    Serial.print(" Y axis = ");  
    Serial.println(yaxis);  
    set_arm( 0, yaxis, 200.0, 0 ,10);  
    delay( 10 );  
}  
    delay(1000);  
for( double yaxis = 400.0; yaxis > 250.0; yaxis -= 1 ) {  
    Serial.print(" Y axis = ");  
    Serial.println(yaxis);  
    set_arm( 0, yaxis, 200.0, 0 ,10);  
    delay( 10 );  
}  
}
```

3- LUA Code On V_REP:

```
function sysCall_threadmain()

sim.setThreadSwitchTiming(2) -- Default timing for automatic thread switching
simDelegateChildScriptExecution()

--defining the serial port number
-- port=sim.getScriptSimulationParameter(sim.handle_self,'serialPortNumber')
portNumber="\\\\.\\COM8"
--could be defined as followed
--portNumber=[\\.\COM21]
baudrate=115200
serial=sim.serialOpen(portNumber,baudrate)


jointHandles={-1,-1,-1,-1}

jointHandles[1]=sim.getObjectHandle('first_link')
jointHandles[2]=sim.getObjectHandle('second_link')
jointHandles[3]=sim.getObjectHandle('Third_link')
jointHandles[4]=sim.getObjectHandle('Gripper_link')


-- Set-up some of the RML vectors:
vel=120
accel=40
```

```

jerk=80
currentVel={0,0,0,0}
currentAccel={0,0,0,0}
maxVel={vel*math.pi/180,vel*math.pi/180,vel*math.pi/180,vel*math.pi/180}
maxAccel={accel*math.pi/180,accel*math.pi/180,accel*math.pi/180,accel*math.pi/180}
maxJerk={jerk*math.pi/180,jerk*math.pi/180,jerk*math.pi/180,jerk*math.pi/180}
targetVel={0,0,0,0}
--sim.serialSend(serial,'D')
while true do

--read a full line
str=sim.serialRead(serial,250,true,'\n',0)

if str~= nil then
    print(str)
    --sending next reading request
    -- sim.serialSend(serial,'D')

    local token

    val={}

    cpt=0

    --extracting the values in str separated by a ,
    for token in string.gmatch( str, "[^,]+") do
        cpt=cpt+1
        val[cpt]=tonumber(token)
    end

end

end

targetPos={val[1]*math.pi/180,val[2]*math.pi/180,val[3]*math.pi/180,val[4]*math.pi/180}

```

```
    sim.rmlMoveToJointPositions(jointHandles,-
1,currentVel,currentAccel,maxVel,maxAccel,maxJerk,targetPos,targetVel)

    -- targetPos2={-90*math.pi/180,45*math.pi/180,-45*math.pi/180,135*math.pi/180}

    -- sim.rmlMoveToJointPositions(jointHandles,-
1,currentVel,currentAccel,maxVel,maxAccel,maxJerk,targetPos2,targetVel)

    -- targetPos3={0,0,0,0,0,0}

    --sim.rmlMoveToJointPositions(jointHandles,-
1,currentVel,currentAccel,maxVel,maxAccel,maxJerk,targetPos3,targetVel)

    sim.switchThread()

end

end
```