

Chinese Remainder Theorem

We are given two arrays `num[0..k-1]` and `rem[0..k-1]`. In `num[0..k-1]`, every pair is coprime (gcd for every pair is 1).

```
// A C++ program to demonstrate
// working of Chinese remainder
// Theorem
#include <bits/stdc++.h>
using namespace std;
// Returns modulo inverse of a
// with respect to m using
// extended Euclid Algorithm.
// Refer below post for details:
// https://www.geeksforgeeks.org/
// multiplicative-inverse-under-modulo-m/
int inv(int a, int m)
{
    int m0 = m, t, q;
    int x0 = 0, x1 = 1;
    if (m == 1)
        return 0;
    // Apply extended Euclid Algorithm
    while (a > 1) {
        // q is quotient
        q = a / m;
        t = m;
        // m is remainder now, process same as
        // euclid's algo
        m = a % m, a = t;
        t = x0;
        x0 = x1 - q * x0;
        x1 = t;
    }
    // Make x1 positive
    if (x1 < 0)
        x1 += m0;
    return x1;
}
```

```

}
// k is size of num[] and rem[]. Returns the smallest
// number x such that:
// x % num[0] = rem[0],
// x % num[1] = rem[1],
// .....
// x % num[k-2] = rem[k-1]
// Assumption: Numbers in num[] are pairwise coprime
// (gcd for every pair is 1)
int findMinX(int num[], int rem[], int k)
{
    // Compute product of all numbers
    int prod = 1;
    for (int i = 0; i < k; i++)
        prod *= num[i];
    // Initialize result
    int result = 0;
    // Apply above formula
    for (int i = 0; i < k; i++) {
        int pp = prod / num[i];
        result += rem[i] * inv(pp, num[i]) * pp;
    }

    return result % prod;
}

// Driver method
int main(void)
{
    int num[] = { 3, 4, 5 };
    int rem[] = { 2, 3, 1 };
    int k = sizeof(num) / sizeof(num[0]);
    cout << "x is " << findMinX(num, rem, k);
    return 0;
}

```