Assignment 4

	Section-A
A1)(a)(a)	input image size = 15 x 15 x 4
	kerneli = hxwxIx0
TO STATE OF THE PARTY OF THE PA	Dutput after fout conv layer - (kernel: 5 x 5 x 4 x 1)
	input image size: 15 x 15 x 4 kerneli = hx w x I x 0 Dutput after finit conv layer - (kernel: 5 x 5 x 4 x 1) nize = (15 + 2x1 - 5 + 1) x (15 + 2x1 - 5 + 1)
v	= 13x13, and no of output channels=1,
	So, image size=13x13x1
	Dutput after maxpooling layer - (kernel = 3x3)
	$sige = \left(\frac{13-3}{2}+1\right) \times \left(\frac{13-3+1}{2}\right) = 0$
	= 6 x 6
	So, image size = 6x6x1 (it doesn't affect no of hanny
	Output image after second convlayer-(kernel=5+3x4x)
	$size = \left(\frac{6+2x^2-5}{2}+1\right) \times \left(\frac{6+2x^2-5}{2}+1\right)$
	= 4 × 4 (rounding off)
F	Tence, output image size = 4x4x1

(h)	Pooling helps to reduce the dimensionality
-	of the image with the lace the strange
36	of the image without loosing features the
	making it more computationally efficient. It
- 54	also helps in making the model learn its
177	features no to their introducing translational
-1711	equivariance property to it, making it more
	robert. It also holps in combat solving
	the peoplem of vanishing gradient which may
	& layers.
	& layers.
<u> </u>	The total no of learnable parametery are-
	First Can laure T. T.
	A manpooling layer doesn't brave learnable
	A marpooling layer doesn't have learnable parameters.
	Second Conv Panen: 5x3x4 = \$60
	Second Conv layer: 5x3x4 = \$60 Thut, total parameters = 150 (without bear)
	(methode play)
(b)	No. If the k-monny alasith ment
	No. If the k-means algorithm requite a particular configuration then it won't will form a loop as it will visit the
	will love a fact as it i'll out
	at the continuation of the
	stops configurations after them too they making
7	it jun indefinitely. The k-means algo can't
	result a configuration before because of the
	nature of objective junction defined on it. It states that minimize the intra-cluster
	states that minimize the intra-cluster
	distance while maximizing the inter-cluster
	distance which has is essentially a hill-
	climking algorithm, to They, it can't requisit
	a provious soulinus ation and it amon the
	a previous configuration which quarantees
	îte convergence.

(c)	Linear filters can detect simple linear patterns like edger, lines, etc. Thus, it can be used to extract low-level feature.
- A	byttorns like edger, lines, etc. Thur, it
T ett	can be used to extract low-level feature
	Non-linear letters can countify more
E Time of	complex patterns too in the data thus
1 14 150	making it more usable to excract high
8.5.0	level features too. It increases the
	expressive power of CNNs.

Section B

Convolution:

All the necessary functions were implemented for it -

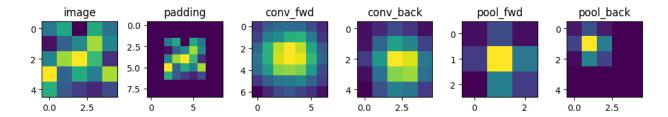
- Forward Convolution Pass: This involves sliding the kernel over the input image.
 At each position, an element-wise multiplication is performed between the kernel
 and the section of the image it currently covers, followed by summing up the
 results to get a single output pixel. This process is repeated for all positions that
 the kernel can slide to, resulting in a new image.
- Backward Convolution Pass: This was a part of the backpropagation process in training a Convolutional Neural Network model. This function calculates the gradient of the loss function with respect to the parameters of the convolution layer (the kernel values), and with respect to its input. This involves applying the chain rule to propagate the gradients backward through the network.
- **Windowing:** A small window of the input image is extracted for processing. This window is the section of the image that the kernel covers at a particular position. The size of the window is the same as the size of the kernel.
- **Zero-Padding:** This was achieved by adding zeros around the border of the input image.

Pooling:

All the necessary functions were implemented for it -

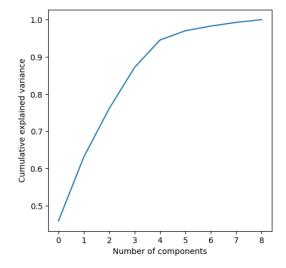
- Forward Pooling Function: This function applies a max pooling operation over the input image. It involved sliding a pooling kernel over the input, and for each position, taking the maximum value within the window was taken for creating the output image thus reducing image dimensionality.
- Mask Creation: This function helped in creating the mask during the forward pooling process to remember the location of the maximum value within each window. This mask was the same size as the window and has a value of 1 at the position of the maximum value and 0 elsewhere. This mask is used in the backward pooling function to distribute gradients back to the input.
- Backward Pooling Function: This function distributes the gradient from the
 output of the pooling layer back to its input, based on the masks created during
 the forward pooling function. The gradient is passed back only to the input value
 that was the maximum within its window. It is an essential part of the
 backpropagation process in training the CNN.
- Value Distribution: This is a step in the backward pooling function where the
 gradient is distributed back to the input. The way the gradient is distributed
 depends on the type of pooling operation. For max pooling, the gradient is
 passed back only to the position of the maximum value within each window (as
 indicated by the mask). For average pooling, the gradient is distributed evenly to
 all values within the window.

A random image and kernel was created of specified size. The result of each step was observed as follows -



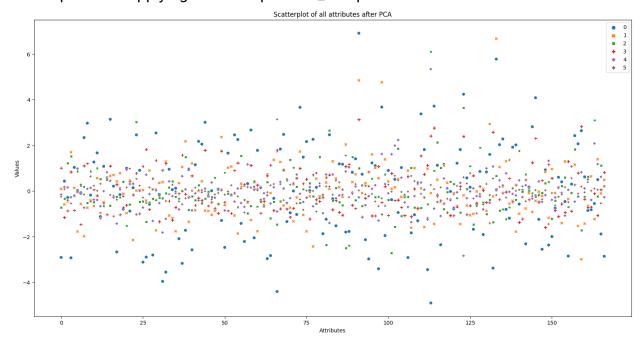
Section C

To standardize the data StandardScaler() was used. After applying PCA for varying number of components, we got the following graph -

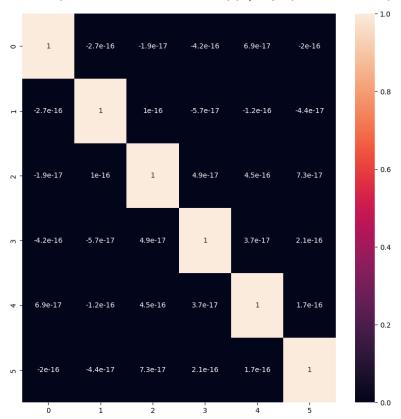


Thus, from here, we could determine that the number of components for optimal PCA would be 6. This was also cross verified using PCA with 'mle' as the number of components, and the results matched with it.

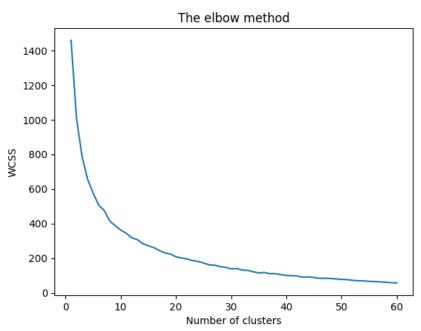
Scatterplot after applying PCA for optimal n_components -



Heatmap for the dataset after applying optimal n_components in PCA -



K-Means Clustering Algorithm -



SIlhouette Method -

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Optimal number of clusters with threshold 0.001: 3 0.29637364602520705
```

The second line denotes the score.

The first array denotes the labeling of each data point. The second array denotes the centroids of each data point. The third line denotes the wcss score from kmeans.inertia_ and the fourth line denotes the number of iterations.