# my library for ICPC

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# Contents

T	mis	${f c}$
	$\frac{1.1}{1.2}$	environment.sh
2	dat	a structure
	2.1	data-structure/binary-indexed-tree.inc.cpp
	2.2	data-structure/segment-tree.inc.cpp
	2.3	data-structure/dual-segment-tree.inc.cpp
	2.4	data-structure/lazy-propagation-segment-tree.inc.cpp
	2.5	data-structure/dynamic-segment-tree.inc.cpp
	2.6	data-structure/union-find-tree.inc.cpp
	2.7	data-structure/treap.inc.cpp
	2.8	data-structure/sparse-table.inc.cpp
	2.9	data-structure/sliding-window.inc.cpp
3	gra	ph ,
	$\bar{3}.1$	graph/ford-fulkerson.inc.cpp
	3.2	graph/dinic.inc.cpp
	3.3	graph/minimum-cost-flow.inc.cpp
	3.4	graph/two-edge-connected-components.inc.cpp
4	con	binatorics
		combinatorics/powmod.inc.cpp
	4.2	combinatorics/extgcd.inc.cpp
5	nun	nber1
		$\frac{1}{10}$
	5.2	number/primes.inc.cpp
6	stri	$_{ m ng}$
	6.1	string/palindrome.inc.cpp
7	util	$\mathbf{s}$
	7.1	utils/binsearch.inc.cpp
	7.2	utils/convex-hull-trick.inc.cpp
	7.3	utils/longest-increasing-subsequence.inc.cpp
	7.4	utils/dice.inc.cpp
	7.5	utils/subset.inc.cpp

# 1 misc

#### 1.1 environment.sh

```
1 #!/bin/bash
2
2
3 cat <<EOF > "/.vimrc
4 syntax on
5 set smartindent
6 set tabstop=4
8 set shiftwidth=4
8 set expandtab
9 set relativenumber
10 EOF
11
12 setxkbmap -option ctrl:swapcaps
13
14 alias e=vim
15 alias cxx="$CXX_u-std=c++14_u-Wall_u-O2',
16 alias cxx="$CXX_u-std=c++14_u-Wall_u-G3_u-mtune=native_u-march=native',
17 alias cxx="$CXX_u-std=c++14_u-Wall_u-g_u-fsanitize=undefined_u-D_GLIBCXX_DEBUG',
18
19 judge() { for f in test/*.in ; do ; echo $f ; diff <(./a.out < $f$) $ff%.in}.out ; done ; }</pre>
```

#### 1.2 template.cpp

#### 2 data structure

# 2.1 data-structure/binary-indexed-tree.inc.cpp

```
template <typename Monoid>
struct binary_indexed_tree { // on monoid}

typedef typename Monoid:underlying_type underlying_type;

vector<underlying_type> data;

Monoid mon;

binary_indexed_tree(size_t n, Monoid const & a_mon = Monoid()): mon(a_mon) {
    data.resize(n, mon.unit());
}

void point_append(size_t i, underlying_type z) { // data[i] += z
    for (size_t j = i + 1; j <= data.size(); j += j & -j) data[j - 1] = mon.append(data[j - 1], z);
}

underlying_type initial_range_concat(size_t i) { // sum [0, i)}

underlying_type acc = mon.unit();
for (size_t j = i; 0 < j; j -= j & -j) acc = mon.append(data[j - 1], acc);
    return acc;
}

for (size_t j = i; 0 < j; j -= j & -j) acc = mon.append(data[j - 1], acc);
    return acc;
}

unittest {
    binary_indexed_tree <plus_t> bit(8);
    bit.point_append(3, 4);
    bit.point_append(4, 3);
    bit.point_append(4, 3);
    bit.point_append(4, 3);
    bit.point_append(4, 3);
    bit.point_append(4, 3);
    bit.point_append(4, 2);
    assert (bit.initial_range_concat(3) == 0);
    assert (bit.initial_range_concat(6) == 8);
    bit.point_append(4, 2);
    assert (bit.initial_range_concat(5) == 9);
    assert (bit.initial_range_concat(6) == 10);
}
```

#### 2.2 data-structure/segment-tree.inc.cpp

```
% Obrief a segment tree, or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object of the segment tree or a fenwick tree
% Object or a fenwick tree
% Object
```

# 2.3 data-structure/dual-segment-tree.inc.cpp

```
template <class OperatorMonoid>
struct dual_segment_tree {
   typedef OperatorMonoid monoid_type;
   typedef typename OperatorMonoid::underlying_type operator_type;
   typedef typename OperatorMonoid::target_type underlying_type;
   int n;
   vector<operator_type> f;
   vector<operator_type> a:
                                                           vector < underlying_type > a;
                                                      vector<underlying_type> a;
OperatorMonoid op;
dual_segment_tree() = default;
dual_segment_tree(int a_n, underlying_type initial_value, OperatorMonoid const & a_op = OperatorMonoid()) : op(a_op) {
    n = 1; while (n < a_n) n *= 2;
    a.resize(n, initial_value);
    f.resize(n-1, op.unit());
}</pre>
10
11
12
13
14
15
16
17
                                                        underlying_type point_get(int i) { // O-based
underlying_type acc = a[i];
for (i = (i+n).2; i > 0; i /= 2) { // 1-based
acc = op.apply(f[i-1], acc);
\begin{array}{c} 188 \\ 199 \\ 201 \\ 212 \\ 222 \\ 244 \\ 255 \\ 260 \\ 300 \\ 330 \\ 333 \\ 333 \\ 344 \\ 444 \\ 445 \\ 646 \\ 448 \\ 489 \\ 900 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 666 \\ 667 \\ 701 \\ 702 \\ 703 \\ 703 \\ 704 \\ 705 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\ 707 \\
                                                      rvoid range_apply(int 1, int r, operator_type z) { // 0-based, [l, r)
    assert (0 <= 1 and 1 <= r and r <= n);
    range_apply(0, 0, n, 1, r, z);
}</pre>
                                                         [1] = op.append(z, f[i]);
} else {
    a[i-n+1] = op.apply(z, a[i-n+1]);
}
                                                                             lae {
   range_apply(2*i+1, il, (il+ir)/2, 0, n, f[i]);
   range_apply(2*i+2, (il+ir)/2, ir, 0, n, f[i]);
   f[i] = op.unit();
   range_apply(2*i+1, il, (il+ir)/2, l, r, z);
   range_apply(2*i+2, (il+ir)/2, ir, l, r, z);
                               struct plus_operator_monoid
                                                      typedef int underlying_type;
typedef int target_type;
int unit() const { return 0; }
                                                        int append(int a, int b) const { return a + b; }
int apply(int a, int b) const { return a + b; }
                                 };
struct min_operator_monoid {
   typedef int underlying_type;
   typedef int target_type;
   int unit() const { return INT_MAX; }
   int append(int a, int b) const { return min(a, b); }
   int apply(int a, int b) const { return min(a, b); }
}.
                               unittest {
    dual_segment_tree < min_operator_monoid > segtree (12, 100);
                                                   dual_segment_tree < min_operator_monoid >
segtree.range_apply(2, 7, 50);
segtree.range_apply(5, 9, 30);
segtree.range_apply(1, 11, 80);
sestree.range_apply(1, 11, 80);
assert (segtree.point_get( 0) == 100);
assert (segtree.point_get( 2) == 50);
assert (segtree.point_get( 2) == 50;
assert (segtree.point_get( 3) == 50);
assert (segtree.point_get( 4) == 50);
assert (segtree.point_get( 5) == 30);
assert (segtree.point_get( 6) == 30);
assert (segtree.point_get( 7) == 30);
assert (segtree.point_get( 9) == 80);
assert (segtree.point_get( 9) == 80);
assert (segtree.point_get( 10) == 80);
assert (segtree.point_get( 10) == 80);
assert (segtree.point_get( 11) == 100);
```

#### 2.4 data-structure/lazy-propagation-segment-tree.inc.cpp

```
* Onote lazy_propagation_segment_tree<maz_monoid, plus_operator_monoid> is the starry sky tree

* Onote verified https://www.hackerrank.com/contests/world-codesprint-12/challenges/factorial-array/submissions/code/1304452669

* Onote verified https://www.hackerrank.com/contests/world-codesprint-12/challenges/animal-transport/submissions/code/1304454860

* One the verified https://www.hackerrank.com/contests/world-codesprint-12/challenges/animal-transport/submissions/code/1304454860

* One template <class Monoid, class OperatorMonoid>
* Struct lazy_propagation_segment_tree { // on monoids

* Static_assert (is_same<typename Monoid:underlying_type, typename OperatorMonoid::target_type>::value, "");

* typedef typename Monoid::underlying_type underlying_type;

* Monoid mon;

* OperatorMonoid op;

* int n;

* vector<underlying_type> a;

* vector<operator_type> f;

* lazy_propagation_segment_tree() = default;
```

```
lazy_propagation_segment_tree(int a_n, underlying_type initial_value = Monoid().unit(), Monoid const & a_mon = Monoid(), OperatorMonoid const & a_op = OperatorMonoid
                                     ())
: mon(a_mon), op(a_op) {
n = 1; while (n <= a_n) n *= 2;
a.resize(2 * n - 1, mon.unit());
fill(a.begin() + (n - 1), a.begin() + ((n - 1) + a_n), initial_value); // set initial_values
REP_R (i, n - 1) a[i] = mon.append(a[2 * i + 1], a[2 * i + 2]); // propagate initial_values
f.resize(max(0, (2 * n - 1) - n), op.identity());
   19
   20
   ryoid point_set(int i, underlying_type z) {
   assert (0 <= i and i < n);
   point_set(0, 0, n, i, z);
}</pre>
                           }
void point_set(int i, int il, int ir, int j, underlying_type z) {
   if (i == n + j - 1) { // O-based
        a[i] = z;
} else if (ir <= j or j+1 <= il) {
        // nop
} else {</pre>
                                                lse {
    range_apply(2 * i + 1, il, (il + ir) / 2, 0, n, f[i]);
    range_apply(2 * i + 2, (il + ir) / 2, ir, 0, n, f[i]);
    f[i] = op.identity();
    point_set(2 * i + 1, il, (il + ir) / 2, j, z);
    point_set(2 * i + 2, (il + ir) / 2, ir, j, z);
    a[i] = mon.append(a[2 * i + 1], a[2 * i + 2]);
                                    }
                           roid range_apply(int 1, int r, operator_type z) {
    assert (0 <= 1 and 1 <= r and r <= n);
    range_apply(0, 0, n, 1, r, z);
}</pre>
                          \begin{array}{c} 58\\ 59\\ 60\\ 61\\ 66\\ 66\\ 66\\ 66\\ 66\\ 66\\ 66\\ 70\\ 71\\ 72\\ 73\\ 75\\ 76\\ 77\\ 78\\ 81\\ 82\\ 83\\ 84\\ 85\\ 88\\ 90\\ 91\\ 92\\ 93\\ 49\\ 5 \end{array}
                                    }
                           runderlying_type range_concat(int 1, int r) {
   assert (0 <= 1 and 1 <= r and r <= n);
   return range_concat(0, 0, n, 1, r);</pre>
                           Junderlying_type range_concat(int i, int il, int ir, int l, int r) {
    if (l <= il and ir <= r) { // O-based
        return a[i];
    } else if (ir <= l or r <= il) {
        return mon.unit();
    }
}</pre>
                                      } else {
                                                }
                 struct max_monoid {
   typedef int underlying_type;
   int unit() const { return 0; }
   int append(int a, int b) const { return min(a, b); }
}.
                  struct plus_operator_monoid {
                           ict plus_operator_monoid {
   typedef int underlying_type;
   typedef int target_type;
   int identity() const { return 0; }
   int apply(underlying_type a, target_type b) const { return a + b; }
   int compose(underlying_type a, underlying_type b) const { return a + b; }
                1:
                 struct min_monoid {
   typedef int underlying_type;
   int unit() const { return INT_MAX; }
   int append(int a, int b) const { return min(a, b); }
   96
97
                 f;
struct plus_with_int_max_operator_monoid {
   typedef int underlying_type;
   typedef int target_type;
   int identity() const { return 0; }
   int apply(underlying_type a, target_type b) const { return b == INT_MAX ? INT_MAX : a + b; }
   int compose(underlying_type a, underlying_type b) const { return a + b; }
}.
98
99
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                 typedef lazy_propagation_segment_tree<max_monoid, plus_operator_monoid> starry_sky_tree;
105
105
106
107
108
109
110
                           ttest {
lazy_propagation_segment_tree<min_monoid, plus_with_int_max_operator_monoid> segtree(9);
segtree.point_set(2, 2);
segtree.point_set(3, 3);
segtree.point_set(4, 4);
segtree.point_set(6, 6);
111
                           segtree.point_set(6, 6);
assert (segtree.range_concat(2, 3) == 2);
assert (segtree.range_concat(5, 8) == 6);
segtree.range_apply(1, 4, 9);
assert (segtree.range_concat(3, 6) == 4);
assert (segtree.range_concat(0, 3) == 11);
112
113
114
115
116
118
                template <int N>
struct count_monoid {
  typedef array<int, N> underlying_type;
  underlying_type unit() const { return underlying_type(); }
  underlying_type append(underlying_type a, underlying_type b) const {
    underlying_type c = {};
    REP (i, N) c[i] = a[i] + b[i];
    return c;
}
119
120 \\ 121 \\ 122 \\ 123 \\ 124 \\ 125
126
                         }
128
                 };
template <int N>
struct increment_operator_monoid {
   typedef int underlying_type;
   typedef array<int, N> target_type;
   underlying_type identity() const { return 0; }
   target_type apply(underlying_type a, target_type b) const {
      if (a == 0) return b;
      target_type c = {};
   REP (i, N - a) c[i + a] = b[i];
      return c;
}
129
130
131
132
133
134
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137
138
139
```

. underlying\_type compose(underlying\_type a, underlying\_type b) const { return a + b; }

117

127

140 141

# 2.5 data-structure/dynamic-segment-tree.inc.cpp

```
/**  
* Onote verified http://arc054.contest.atcoder.jp/submissions/1335245  
*/
                         */
template <class Monoid>
struct dynamic_segment_tree { // on monoid
typedef Monoid monoid_type;
typedef typename Monoid:type underlying_type;
                                           struct node_t {
   int left, right; // indices on pool underlying_type value;
 10
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12
13
14
15
16
17
                                           Monoid mon;
dynamic_segment_tree(Monoid const & a_mon = Monoid()) : mon(a_mon) {
   node_t node = { -1, -1, mon.unit() };
   pool.push_back(node);
   root = 0;
   width = 1;
   size = 1;
}
\begin{array}{c} 188 \\ 190 \\ 201 \\ 222 \\ 233 \\ 304 \\ 335 \\ 363 \\ 333 \\ 333 \\ 334 \\ 344 \\ 444 \\ 456 \\ 663 \\ 664 \\ 666 \\ 667 \\ 707 \\ 777 \\ 734 \\ 776 \\ 767 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\ 777 \\
                         protected:
                                        int create_node(int parent, bool is_right) {
    // make a new node
    int i = pool.size();
    node_t node = { -1, -1, mon.unit() };
    pool.push_back(node);
    // link from the parent
    assert (parent! = -1);
    int & ptr = is_right ? pool[parent].right : pool[parent].left;
    assert (ptr == -1);
    ptr = i;
    return i;
}
                                          int get_value(int i) {
   return i == -1 ? mon.unit() : pool[i].value;
                                            ic:
    void point_set(int i, underlying_type z) {
        assert (0 <= i);
        while (width <= i) {
            node_t node = { root, -1, pool[root].value };
            root = pool.size();
            pool.push_back(node);
            width *= 2;
}</pre>
                                                              point_set(root, -1, false, 0, width, i, z);
                                          }
pool[i].value = z;
} else if (ir <= j or j+1 <= il) {
    // nop
} else {
    if (i == -1) i = create_node(pi)</pre>
                                                                                lse {
   if (i == -1) i = create_node(parent, is_right);
   point_set(pool[i].left, i, false, il, (il+ir)/2, j, z);
   point_set(pool[i].right, i, true, (il+ir)/2, ir, j, z);
   pool[i].value = mon.append(get_value(pool[i].left), get_value(pool[i].right));
                                           underlying_type range_concat(int 1, int r) {
   assert (0 <= 1 and 1 <= r);
   if (width <= 1) return mon.unit();
   return range_concat(root, 0, width, 1, min(width, r));</pre>

}
underlying_type range_concat(int i, int il, int ir, int l, int r) {
    if (i == -1) return mon.unit();
    if (1 <= il and ir <= r) { // 0-based
        return pool[i].value;
    } else if (ir <= l or r <= il) {
        return mon.unit();
    } else f
}</pre>
                                                             } else {
                                                                                lse {
    return mon.append(
        range_concat(pool[i].left, i1, (i1+ir)/2, 1, r),
        range_concat(pool[i].right, (i1+ir)/2, ir, 1, r));
                                           ftemplate <class Func>
void traverse_leaves(Func func) {
    return traverse_leaves(root, 0, width, func);
}
                                            }
template <class Func>
void traverse_leaves(int i, int il, int ir, Func func) {
   if (i == -1) return;
   if (ir - il == 1) {
      func(il, pool[i].value);
   }
}
                                                             funt(1, pr...)
else {
  traverse_leaves(pool[i].left, il, (il+ir)/2, func);
  traverse_leaves(pool[i].right, (il+ir)/2, ir, func);
```

#### 2.6 data-structure/union-find-tree.inc.cpp

#### 2.7 data-structure/treap.inc.cpp

63

```
// https://www.hackerrank.com/contests/zalando-codesprint/challenges/give-me-the-order/submissions/code/6004391
template <typename T>
struct treap {
    typedef T value_type;
    typedef double key_type;
    value_type v;
    key_type k;
    shared_ptr<treap> 1, r;
    size t m size:
                  size_t m_size;
                  treap(value_type v)
: v(v)
: v(v)
, k(generate())
, 1()
                                 , m_size(1) {
                 static size_t size(shared_ptr<treap> const & t) {
   return t ? t->m_size : 0;
                  , static shared_ptr<treap> merge(shared_ptr<treap> const & a, shared_ptr<treap> const & b) { // destructive
                        itic shared_ptr<treap> merge
if (not a) return b;
if (not b) return a;
if (a->k > b->k) {
    a->r = merge(a->r, b);
    return update(a);
} else {
    b->1 = merge(a, b->1);
    return update(b);
}
                 static pair<shared_ptr<treap>, shared_ptr<treap> > split(shared_ptr<treap> const & t, size_t i) { // [0, i) [i, n), destructive
if (not t) return { shared_ptr<treap>(), shared_ptr<treap>() };
if (i <= size(t->1)) {
            shared_ptr<treap> u; tie(u, t->1) = split(t->1, i);
                                 shared_ptr<treap> u; tie
return { u, update(t) };
                        retuin t u, upacott...,
} else {
    shared_ptr<treap> u; tie(t->r, u) = split(t->r, i - size(t->l) - 1);
    return { update(t), u };
                  static shared_ptr<treap> insert(shared_ptr<treap> const & t, size_t i, value_type v) { // destructive
    shared_ptr<treap> 1, r; tie(1, r) = split(t, i);
    shared_ptr<treap> u = make_shared<treap>(v);
    return merge(aerge(1, u), r);
                  , static pair<shared_ptr<treap>, shared_ptr<treap> > erase(shared_ptr<treap> const & t, size_t i) \{\ //\ (t \setminus t\_i,\ t\_i),\ destructive
                         shared_ptr<treap> 1, u, r;
tie(1, r) = split(t, i + 1);
tie(1, u) = split(1, i);
return { merge(1, r), u };
                  static shared_ptr<treap> update(shared_ptr<treap> const & t) {
                          if (t) {
    t->m_size = 1 + size(t->1) + size(t->r);
                          return t;
                 static key_type generate() {
    static random_device device;
    static default_random_engine engine(device());
    static uniform_real_distribution<double> dist;
                          return dist(engine);
```

#### 2.8 data-structure/sparse-table.inc.cpp

```
1 /**
2 * @brief sparse table on a monoid
3 * @note space: O(N log N)
```

#### 2.9 data-structure/sliding-window.inc.cpp

```
1  // http://poj.org/problem?id=2823
2  // http://cf16-tournament-round3-open.contest.atcoder.jp/tasks/asaporo_d
template <typename T>
4  struct sliding_window {
    deque<pair<int, T> data;
    function<bool (T const &, T const &) cmp;
    template <typename F>
    sliding_window { a_lt) : cmp(a_lt) {}
    T front() { return data.front().second; } // smallest
    void push_back(int i, T a) { while (not data.empty() and cmp(a, data.back().second)) data.pop_back(); data.emplace_back(i, a); }
    void push_front(int i) { if (data.front().first == i) data.pop_front(); }
    void push_front(int i, T a) { if (data.empty() or not cmp(data.front().second, a)) data.emplace_front(i, a); }
};
```

# 3 graph

## 3.1 graph/ford-fulkerson.inc.cpp

```
struct edge_t { int to, cap, rev; };
int maximum_flow_destructive(int s, int t, vector<vector<edge_t>> & g) { // ford fulkerson, O(EF)
   int n = g.size();
   vector<bool' used(n);
   function<int (int, int)> dfs = [&](int i, int f) {
        if (i == t) return f;
        used[i] = true;
        for (edge_t & e : g[i]) {
            if (used[e.to] or e.cap <= 0) continue;
        }
}</pre>
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                               (eage_t & e : g[1]) f
if (used[e.to] or e.cap <= 0) continue;
int nf = dfs(e.to, min(f, e.cap));
if (nf > 0) {
    e.cap -= nf;
    g[e.to][e.rev].cap += nf;
    return nf;
}
                       return 0;
                  int result = 0;
                 int result = 0;
while (true) {
    used.clear(); used.resize(n);
    int f = dfs(s, numeric_limits<int>::max());
    if (f == 0) break;
    result += f;
                 return result;
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           int maximum_flow(int s, int t, vector<vector<edge_t> > g /* adjacency list */) { // ford fulkerson, O(FE) return maximum_flow_destructive(s, t, g);
\begin{array}{c} 33\\ 34\\ 35\\ 36\\ 37\\ 38\\ 39\\ 40\\ 41\\ 42\\ 43\\ 445\\ 46\\ 47\\ 48\\ 49\\ 50\\ 51\\ 52\\ 53\\ 54\\ 55\\ 60\\ 61\\ \end{array}
         if (b.count(i)) {
   add_edge(i, dst, 1);
                       }
                 fmaximum_flow_destructive(src, dst, h);
vector<pair<int,int> > ans;
for (int from : a) {
    for (edge_t e : h[from]) if (b.count(e.to) and e.cap == 0) {
        ans.emplace_back(from, e.to);
    }
}
62
                 return ans;
```

#### 3.2 graph/dinic.inc.cpp

```
// https://kimiyuki.net/blog/2016/01/16/arc-031-d/
double maximum_flow(int s, int t, vector<vector<double> > const & capacity /* adjacency matrix */) { // dinic, O(V^2E)
    int n = capacity.size();
    vector<vector<double> > flow(n, vector<double>(n));
    auto residue = [&](int i, int j) { return capacity[i][j] - flow[i][j]; };
    vector<vector<int> > g(n); repeat (i,n) repeat (j,n) if (capacity[i][j] or capacity[j][i]) g[i].push_back(j); // adjacency list
    double recult = 0.
                          vector<vector<int> > g(n); repeat (i,n) repeat (j,n) if (capacity[i][j
double result = 0;
while (true) {
    vector<int> level(n, -1); level[s] = 0;
    queue<int> q; q.push(s);
    for (int d = n; not q.empty() and level[q.front()] < d; ) {
        int i = q.front(); q.pop();
        if (i == t) d = level[i];
        for (int j : g[i]) if (level[j] == -1 and residue(i,j) > 0) {
            level[j] = level[i] + 1;
            q.push(j);
        }
}
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fy
vector<bool> finished(n);
function<double (int, double)> augmenting_path = [&](int i, double cur) -> double {
   if (i == t or cur == 0) return cur;
   if (finished[i]) return 0;
                                                  if (inished[i]) fetune;
for (int j : g[i]) if (level[i] < level[j]) {
    double f = augmenting_path(j, min(cur, residue(i,j)));
    if (f > 0) {
        flow[i][j] += f;
        flow[j][i] -= f;
        finished[i] = false;
        return f
                                                                         return f;
                                                           }
                                                  return 0;
                                        ;;
hool cont = false;
                                       bool cont = false;
while (true) {
    double f = augmenting_path(s, numeric_limits<double>::max());
    if (f == 0) break;
    result += f;
    cont = true;
                                       if (not cont) break;
                // https://kimiyuki.net/blog/2017/10/22/kupc-2017-h/
               uint64_t pack(int i, int j) {
    return (uint64_t(i) << 32) | j;</pre>
               }

Il maximum_flow(int s, int t, int n, unordered_map<uint64_t, 1l> & capacity /* adjacency matrix */) { // dinic, O(V^2E) auto residue = [&](int i, int j) { auto key = pack(i, j); return capacity.count(key) ? capacity[key] : 0; }; vector<vector<int> > g(n); repeat (i,n) repeat (j,n) if (residue(i, j) or residue(j, i)) g[i].push_back(j); // adjacency list
                          while (true) {
                                     le (true) {
vector<int> level(n, -1); level[s] = 0;
queue<int> q; q.push(s);
for (int d = n; not q.empty() and level[q.front()] < d; ) {
   int i = q.front(); q.pop();
   if (i == t) d = level[i];
   for (int j : g[i]) if (level[j] == -1 and residue(i,j) > 0) {
        level[j] = level[i] + 1;
        q.push(j);
   }
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                                                 }
                                       ir (inissaedil) return v;
finished[i] = true;
for (int j : g[i]) if (level[i] < level[j]) {
    ll f = augmenting_path(j, min(cur, residue(i,j)));
    if (f > 0) {
        capacity[pack(i, j)] -= f;
        capacity[pack(j, i)] += f;
        finished[i] = false;
        return f:
                                                                          return f;
                                                           }
                                                  return 0;
                                       };
bool cont = false;
while (true) {
    ll f = augmenting_path(s, numeric_limits<ll>::max());
    if (f == 0) break;
    result += f;
    cont = true;
}
                                        if (not cont) break;
```

#### 3.3 graph/minimum-cost-flow.inc.cpp

```
template <class T>
struct edge { int to; T cap, cost; int rev; };

template <class T>

void add_edge(vector<vector<edge<T> > & graph, int from, int to, T cap, T cost) {
    graph[from].push_back((edge<T>) { to, cap, cost, int(graph[ to].size()) });

    graph[ to].push_back((edge<T>) { from, 0, - cost, int(graph[from].size()) - 1 });

} /**

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```

```
if (not updated) break;
}

while (0 < flow) {
// update potential using dishstre
vector(T) distance(graph.size(0); // constitute a single-linked-list represents the flow-path
vector(int) prev.v(graph.size(0); // constitute a single-linked-list represents the flow-path
vector(int) prev.v(graph.size(0); // constitute a single-linked-list represents the flow-path
vector(int) prev.e(graph.size(0); // constitute a single-linked-list represents the flow-path
vector(int) prev.e(graph.size(0); // constitute a single-linked-list represents the flow-path
vector(int) prev.e(graph.size(0); // single-linked-list represents the flow-path
vector(int) represents the flow-path
vec
```

# 3.4 graph/two-edge-connected-components.inc.cpp

#### 4 combinatorics

 $\begin{array}{c} 28 \\ 290 \\ 311 \\ 322 \\ 334 \\ 456 \\ 474 \\ 489 \\ 501 \\ 555 \\ 556 \\ 666 \\ 666 \\ 669 \\ 701 \\ 727 \\ 757 \\ 789 \\ \end{array}$ 

## 4.1 combinatorics/powmod.inc.cpp

#### 4.2 combinatorics/extgcd.inc.cpp

#### 5 number

# 5.1 number/gcd.inc.cpp

# 5.2 number/primes.inc.cpp

# 6 string

# 6.1 string/palindrome.inc.cpp

```
vector<int> even_palindrome_length(string const & s) {
    int n = s.length();
    string t(2*n*1, '\0');
    repeat (i,n) t[2*i+1] = s[i];
    vector<int> r = manacher(t);
    vector<int> (in);
    repeat (i,n) if (r[2*i+2] >= 3) l[i-r[2*i+2]/2+1] = r[2*i+2]-1;
    repeat (i,n-1) setmax(l[i+1], l[i]-2);
    return l;
}
```

#### 7 utils

 $\frac{22}{23}$ 

#### 7.1 utils/binsearch.inc.cpp

# 7.2 utils/convex-hull-trick.inc.cpp

```
// http://d.hatena.ne.jp/sune2/20140310/1394440369
              // http://d.hatena.ne.jp/sune2/20140310/1394440369
// http://techtipshoge.blogspot.jp/2013/06/convex-hull-trickdequepop-back.html
// http://satanic0238.hatenablog.com/entry/2016/08/16/181331
// http://wcipeg.com/wiki/Convex_hull_trick
// vernified: http://codeforces.com/contest/631/submission/31828502
struct line_t { 11 a, b; };
bool operator < (line_t lhs, line_t rhs) { return make_pair(- lhs.a, lhs.b) < make_pair(- rhs.a, rhs.b); }
struct rational_t { 11 num, den; };
rational_t make_rational(11 num, 11 den = 1) {
    if (den < 0) { num *= -1; den *= -1; }
    return { num, den };
}</pre>
                properator < (rational_t lhs, rational_t rhs) {
    if (lhs.num == LLONG_MAX or rhs.num == - LLONG_MAX) return false;
    if (lhs.num == - LLONG_MAX or rhs.num == LLONG_MAX) return true;
    return lhs.num * rhs.den < rhs.num * lhs.den;</pre>
16
                struct convex_hull_trick {
\begin{array}{c} 18 \\ 19 \\ 20 \\ 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 27 \\ 28 \\ 29 \\ 30 \\ 31 \\ 32 \\ 33 \\ 34 \\ 35 \\ 36 \\ 37 \\ 38 \\ 40 \\ 41 \\ 42 \\ 43 \\ 44 \\ 44 \\ 45 \\ 47 \\ \end{array}
                          convex_hull_trick() {
   lines.insert({ + LLONG_MAX, 0 });   // sentinels
   lines.insert({ - LLONG_MAX, 0 });
   cross.emplace(make_rational(- LLONG_MAX), (line_t) { - LLONG_MAX, 0 });
                          }
void add_line(ll a, ll b) {
   auto it = lines.insert({ a, b }).first;
   if (not is_required(*prev(it), { a, b }, *next(it))) {
      lines.erase(it);
      return;
   }
}
                                     }
{ // remove left lines
  auto ju = next(it);
  while(next(ju) != lines.end() and not is_required({ a, b }, *ju, *next(ju))) ++ ju;
  cross_erase(++ it, ju);
  it = prev(lines.erase(it, ju));
}
                                     cross.emplace(cross_point(*prev(it), *it), *it);
cross.emplace(cross_point(*it, *next(it)), *next(it));
                          ll get_min(ll x) const {
                                    line_t f = prev(cross.lower_bound(make_rational(x)))->second;
return f.a * x + f.b;
\begin{array}{c} 48 \\ 49 \\ 50 \\ 51 \\ 52 \\ 53 \\ 54 \\ 55 \\ 56 \\ 67 \\ 58 \\ 60 \\ 62 \\ 63 \\ 66 \\ 66 \\ 67 \\ 71 \\ 72 \\ 73 \\ 74 \\ 75 \end{array}
            rational_t cross_point(line_t f1, line_t f2) const {
   if (f1.a == LLONG_MAX) return make_rational(- LLONG_MAX);
   if (f2.a == - LLONG_MAX) return make_rational( LLONG_MAX);
   return make_rational(f1.b - f2.b, f2.a - f1.a);
                          fequired(line_t f1, line_t f2, line_t f3) const {
    if (f1.a == f2.a and f1.b <= f2.b) return false;
    if (f1.a == LLONG_MAX or f3.a == - LLONG_MAX) return true;
    return (f2.a - f1.a) * (f3.b - f2.b) < (f2.b - f1.b) * (f3.a - f2.a);</pre>
                          ttest {
    default_random_engine gen;
    repeat (iteration, 1000) {
        vector(pair(int, int> > lines;
        convex_hull_trick cht;
        repeat (i, 100) {
```

```
int a = uniform_int_distribution<int>(- 30, 30)(gen);
    int b = uniform_int_distribution<int>(- 30, 30)(gen);
    lines.emplace_back(a, b);
    cht.add_line(a, b);
}
repeat (i, 10) {
    int x = uniform_int_distribution<int>(- 100, 100)(gen);
    int y = INT_MAX;
    for (auto line : lines) {
        int a, b; tie(a, b) = line;
        setmin(y, a * x + b);
    }
    assert (cht.get_min(x) == y);
}
}
struct inverted_convex_hull_trick {
    convex_hull_trick data;
    void add_line(l a, ll b) { data.add_line(- a, - b); }
ll get_max(ll x) { return - data.get_min(x); }
};
```

#### 7.3 utils/longest-increasing-subsequence.inc.cpp

#### 7.4 utils/dice.inc.cpp

# 7.5 utils/subset.inc.cpp