

(1) (1 points) Convert the following numbers from decimal to binary

$$217.75 = 0111 \ 1111 . 11$$

$$-14.125 = 1000 \ 1110 . 001$$

(2) (1 points) Convert the following numbers from binary to decimal

$$11011.0011 = 27 + 2^{-3} + 2^{-4} = 27.1875$$

$$-0.0101 = -(2^{-2} + 2^{-4}) = -0.3125$$

(3) (2 points) Following the IEEE 754 standard for floating point numbers, represent the following binary real number as a single-precision floating point number (32-bits)

$$11011.0011 = 0 \ 10000011 \ 101100110000000000000000$$

(4) (6 points) Use the figure below to answer the following questions

a. Represent the vector $\mathbf{a} = \mathbf{AB}$ in Cartesian representation

$$(2)\mathbf{i} + (-2)\mathbf{j}$$

b. Compute the angle between \mathbf{AB} and the positive x-axis

$$0.7853981633974484 = \frac{\pi}{4} = 45^\circ$$

c. Compute the angle between \mathbf{BD} and the positive x-axis

$$0.7853981633974484 = \frac{\pi}{4} = 45^\circ$$

d. Compute the angle between \mathbf{AB} and \mathbf{BD}

$$1.5707963267948966 = \frac{\pi}{2} = 90^\circ$$

e. Compute the cross product $\mathbf{AB} \times \mathbf{BD}$ in two different ways

$$\mathbf{AB}_x * \mathbf{BD}_y - \mathbf{AB}_y * \mathbf{BD}_x = 8$$

$$\mathbf{DB}_x * \mathbf{AB}_y - \mathbf{DB}_y * \mathbf{AB}_x = ||\mathbf{AB}|| \times ||\mathbf{BD}|| \times \cos(90^\circ) = 8$$

f. Compute the dot product $\mathbf{AB} \cdot \mathbf{BD}$ in two different ways

$$\mathbf{AB}_x * \mathbf{BD}_x + \mathbf{AB}_y * \mathbf{BD}_y = 0$$

$$||\mathbf{AB}|| \times ||\mathbf{BD}|| \times \cos(90^\circ) = 0$$

g. Compute the coordinates of the intersection of the two line segments $\mathbf{BD'}$ and $\mathbf{AC'}$

$$(1.333333, 3.333333) \approx \left(\frac{4}{3}, \frac{10}{3}\right)$$

In []: