

InvertedIndexReport

December 17, 2016

1 INVERTED INDEX SEARCH ENGINE

source code at [my github repo](#)

2 1. Report

2.1 Early Plan

first, I was trying to write the whole project in python3.5 and with the aid of the Wiley book, Algorithm and > Data structure in python, and I read the book up to end of chapter 8: trees, and I have built my code on that book basic, many expertise of python programming like annotation and decorator which supports in python3.5.2 had been used in this period and code developed practical, clean, designed, but snails, which takes about 2 weeks to complete, and are stored in [my github repo: DataStructure_Python](#), in implementing TST and TrieST I have used the another famous book, Algorithm.4ed published by Addison-Wesley, which was written java friendly, I used its algorithm to developed my code.

2.2 Middle Plan

in middle of the project I decided to write the whole project in Jupyter notebook, it was challenging and also fun. but if you (like me) don't have a reliable memory for remembering all of the methods for a class or variables, interacting with Jupyter gets hard.

2.3 Final Product

after the backend of the project completed, I should begin to implement the Graphical user interface (GUI), first I started to learn basic of Tkinter layout manager, but after a day or two, I gave up and search for something like swing in python, so I found Jython (an extinct project !!!!!) unfortunately Jython just support python2.7, but that was not a bad news because python2.7 was my first programming language that I learned. I translate all of my code in python2.7 and start coding in Jython with Jython compiler. after a while I faced with some frightening exception like "instance error" or "null pointer exception" or "java.lang.Runnable exception". But fortunately I overcame them finally and the whole project survive.

2.3.1 dependencies:

to run the project you need jython compiler, you can install this via this command:

```
'sudo apt-get install Jython'
```

to open jupyter notebook you should download this packages:

```
'sudo apt-get install anaconda3'
```

```
'sudo apt-get install ipython-notebook'
```

```
'sudo apt-get install jupyter'
```

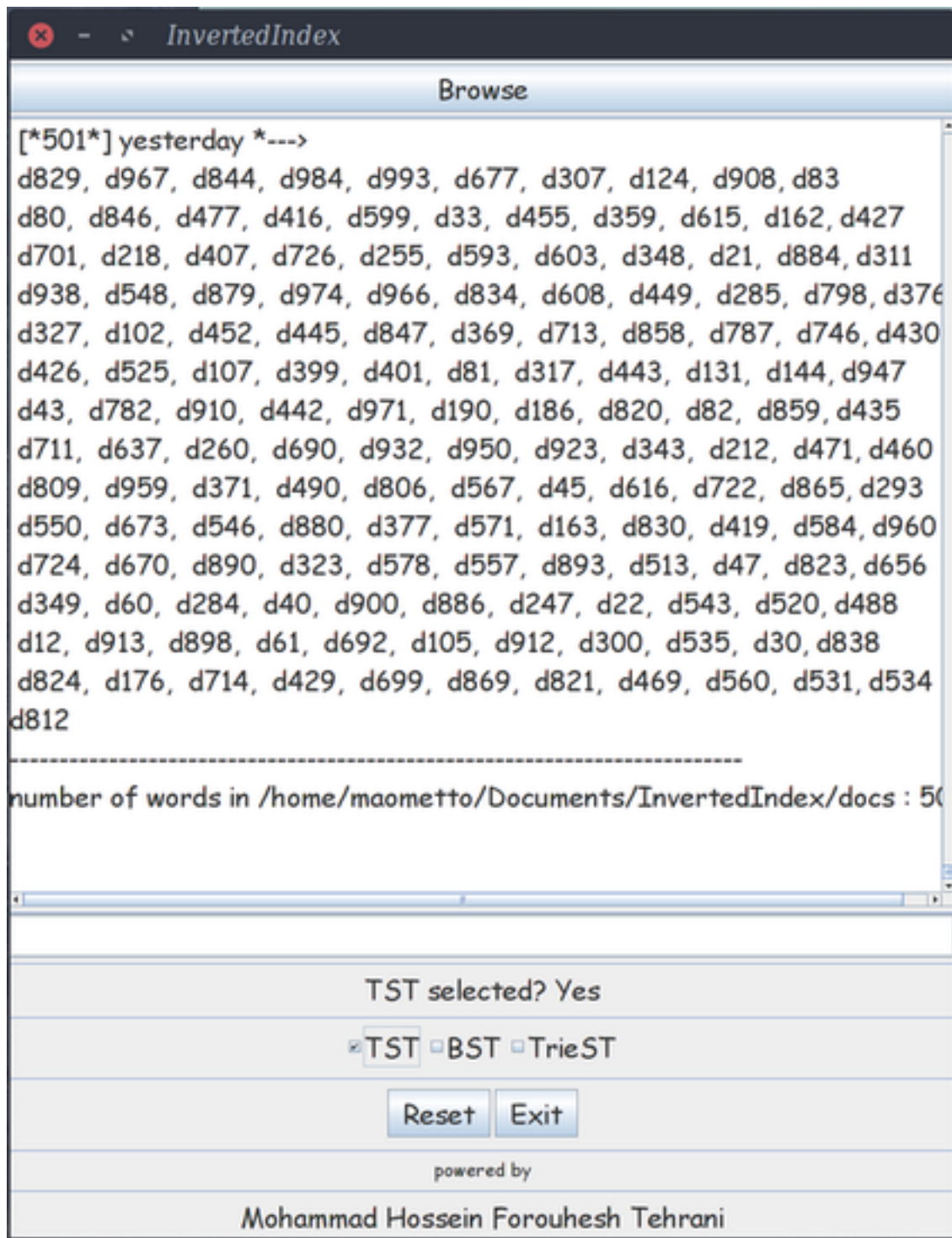
**2.4 here are some screenshots of the project:
description:**

this window will open when you run the program.



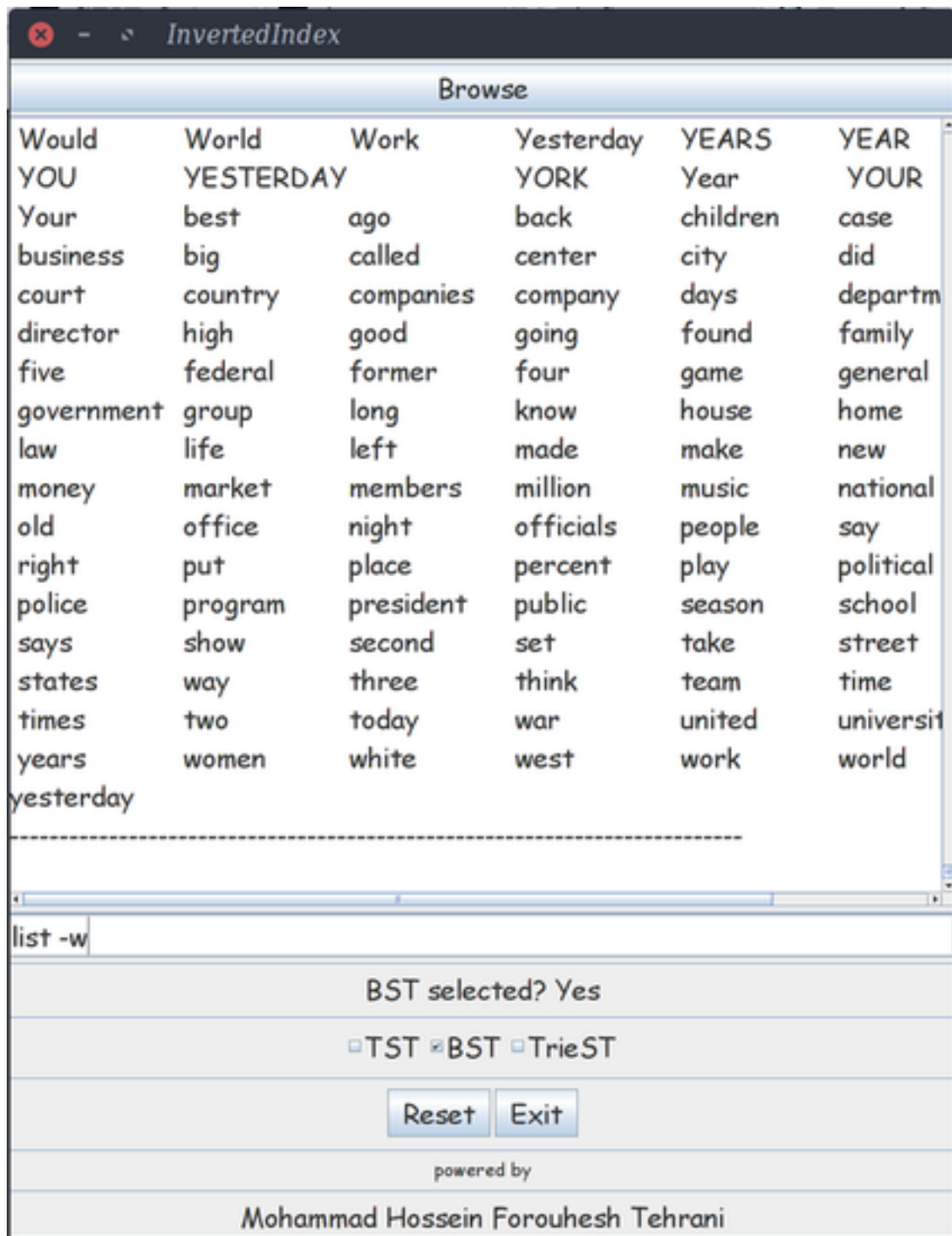
describtion:

when you hit the TST checkbox after a while, this will be shown to you.



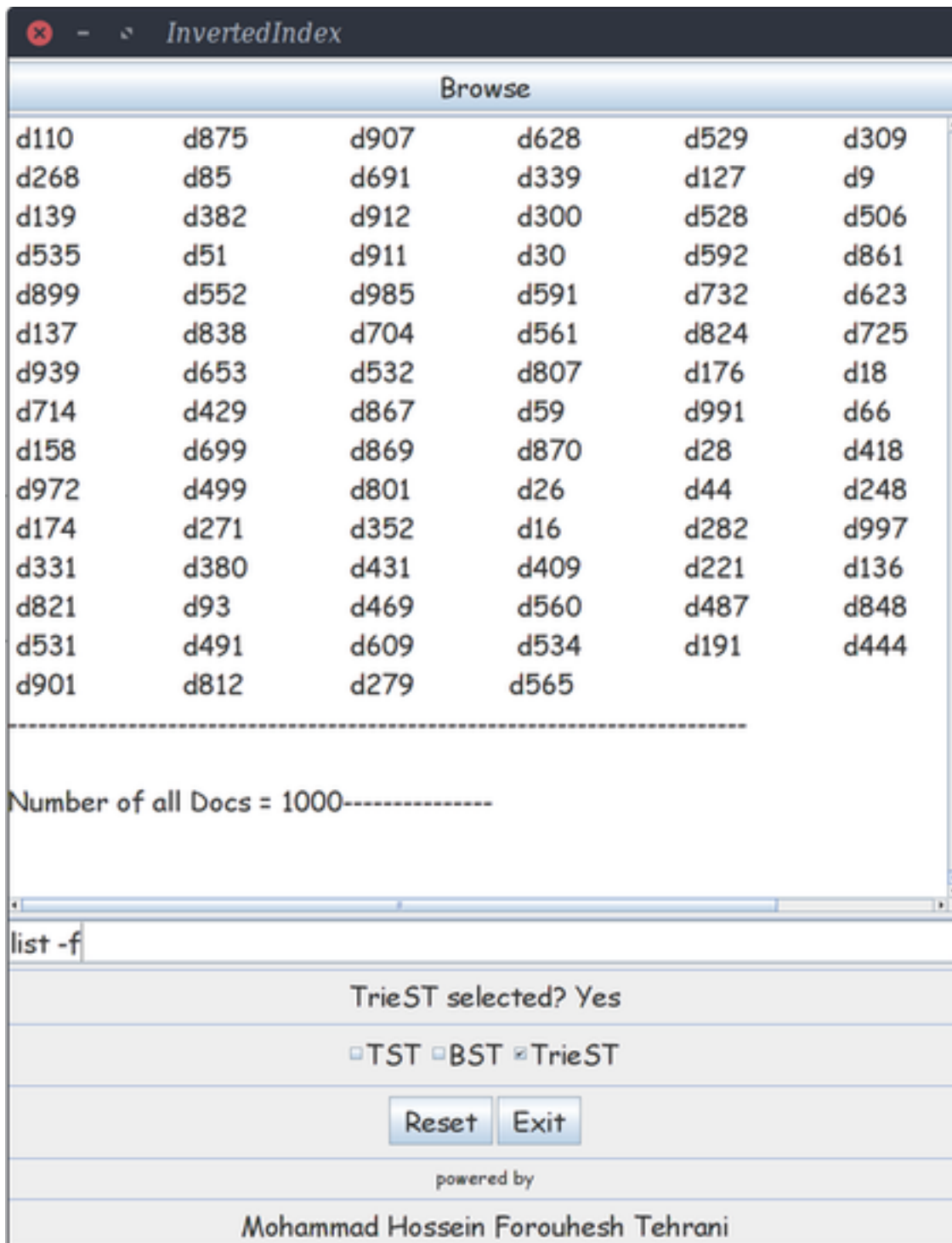
describition:

you may want just your words.



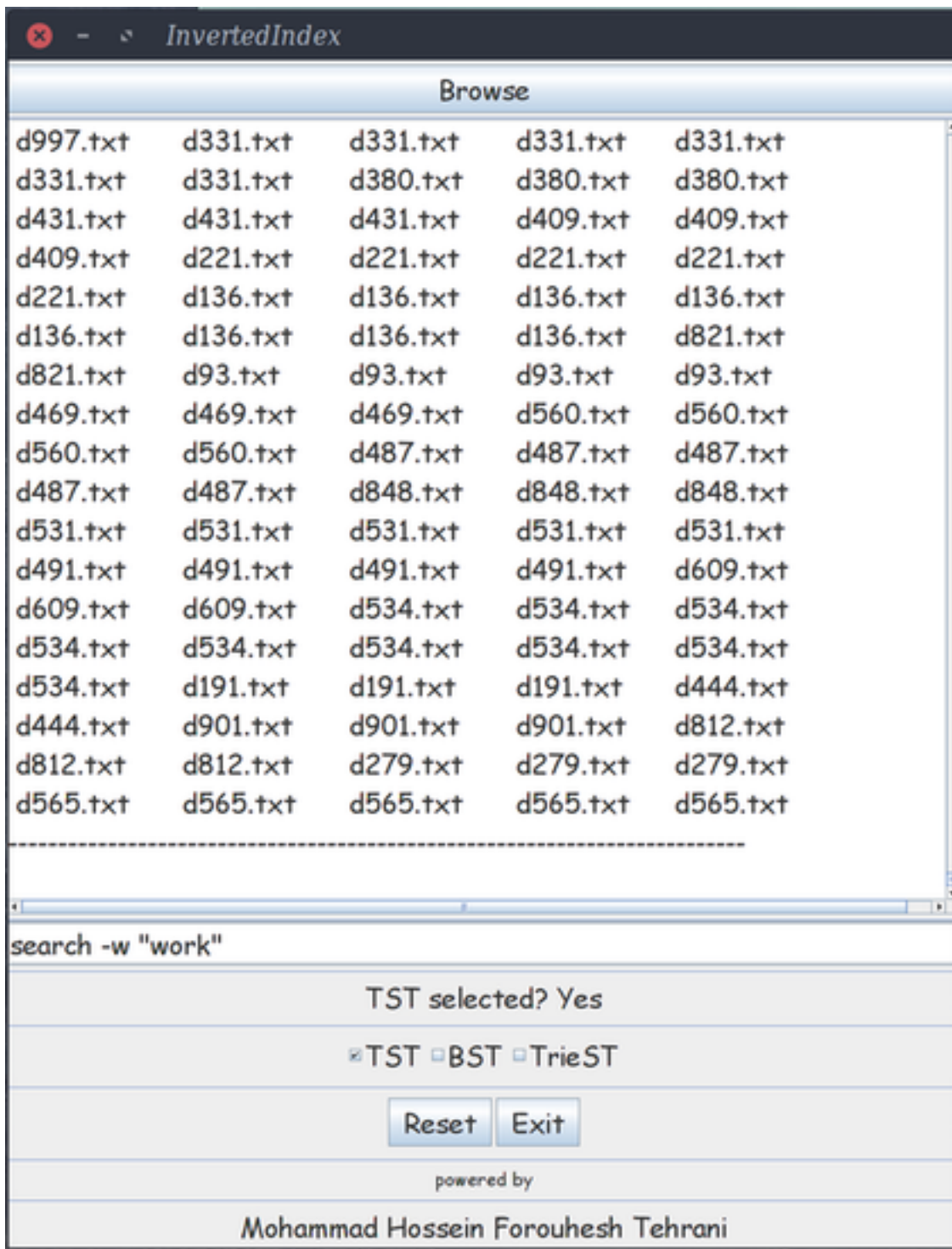
describition:

with this command you can see the files in the directory.



describtion:

you can search the words.



3 2. Here is a short description of the data structure code:

3.1 DynamicArray

3.1.1 preview :

dynamic cpython array instead of python list


```
In [1]: import ctypes
```

```
class DynamicArray:
    """
    dynamic python array instead of python list
    """
    def __init__(self):
        """
        create an empty array
        """
        self._number_of_actual_elements = 0
        self._capacity = 1
        self._low_level_array = self._make_array(self._capacity)

    def __len__(self) -> int:
        """
        :return: the length of array
        """
        return self._number_of_actual_elements

    def __getitem__(self, index: int) -> object:
        """
        :type index: int
        :param index: the index of desired item in the array.
        :return: return the item.
        """
        if not 0 <= index < self._number_of_actual_elements:
            raise IndexError("index out of range")
        return self._low_level_array[index]

    def is_empty(self):
        if self._number_of_actual_elements == 0:
            return True
        return False

    def pop(self):
        if self.is_empty():
            raise Exception("empty array")
        var = self._low_level_array[self._number_of_actual_elements - 1]
        self._number_of_actual_elements -= 1
        return var

    def append(self, item: object):
        """
        add object to the end of array
        :param item: desired object
        """
        if self._number_of_actual_elements == self._capacity:
            self._resize(2 * self._capacity)
        self._low_level_array[self._number_of_actual_elements] = item
        self._number_of_actual_elements += 1
```



```

def _resize(self, new_size: int):
    """
    resize the internal array to capacity new_size
    :param new_size: desired capacity
    """
    new_array = self._make_array(new_size)
    for k in range(self._number_of_actual_elements):
        new_array[k] = self._low_level_array[k]
    self._low_level_array = new_array
    self._capacity = new_size

def _make_array(self, capacity: int) -> object:
    """
    return new array with fixed capacity.
    :param capacity: the desired capacity
    :return: return ctypes array
    """
    return (capacity * ctypes.py_object)()

```

3.2 LinkedList

3.2.1 preview:

this is my linked list class which supports many feature like adding first and last and between, it

In [2]: class LinkedList:

```

class Node:
    """
    Lightweight, nonpublic class for storing a doubly linked node.
    """
    __slots__ = 'element', 'prev', 'after', 'upside_arrow', 'downside_arrow' # streamline

    def __init__(self, element, prev, after): # initialize node's fields
        self.element = element # user's element
        self.prev = prev # previous node reference
        self.after = after

def __init__(self):
    """
    Create an empty list.
    """
    self.header = self.Node(None, None, None)
    self.trailer = self.Node(None, None, None)
    self.header.after = self.trailer # trailer is after header
    self.trailer.prev = self.header # header is before trailer
    self.size = 0

def __len__(self):
    return self.size

def __iter__(self):
    if self.is_empty():
        yield self.Node(None, None, None)
    current = self.header

```

```

        while current is not None:
            yield current
            current = current.after

def is_empty(self) -> bool:
    return self.size == 0

def insert_between(self, element, predecessor: Node, successor: Node) -> Node:
    newest = self.Node(element, predecessor, successor) # linked to neighbors
    predecessor.after = newest
    successor.prev = newest
    self.size += 1
    return newest

def delete_node(self, node: Node) -> type(Node.element):
    predecessor = node.prev
    successor = node.after
    predecessor.after = successor
    successor.prev = predecessor
    self.size -= 1
    element = node.element # record deleted element
    node.prev = node.after = node.element = None # deprecate node
    return element

# -----

def add_first(self, element: type(Node.element)) -> Node:
    return self.insert_between(element, self.header, self.header.after)

def add_last(self, element: type(Node.element)) -> Node:
    return self.insert_between(element, self.trailer.prev, self.trailer)

def add_before(self, prevElement: type(Node.element), element: type(Node.element)) -> Node:
    original = self.search(prevElement)
    return self.insert_between(element, original.prev, original)

def add_after(self, nextElement: type(Node.element), element: type(Node.element)) -> Node:
    original = self.search(nextElement)
    return self.insert_between(element, original, original.after)

# -----

def delete(self, undesireElement) -> type(Node.element):
    original = self.search(undesireElement)
    if original is None:
        return
    return self.delete_node(original)

def search(self, desireElement: type(Node.element)) -> Node:
    head = self.header
    while head.after is not None:
        head = head.after
        if head.element == desireElement:
            return head

```

```
return None
```

3.3 LinkedStack

```
In [3]: class LinkedStack():
```

```
# ----- Nested Class -----
class Node:

    __slots__ = 'element', 'next' # streamline memory usage

    def __init__(self, element, next): # initialize node field
        self.element = element # reference to current element
        self.next = next # reference to the next node

# ----- Stack Methods -----
def __init__(self):
    self.head = self.Node(None, None) # head is a kind of node
    self.size = 0

def __len__(self) -> int:
    return self.size

def __iter__(self):
    if self.is_empty():
        yield
    current = self.head
    while current is not None:
        yield current
        current = current.next

def is_empty(self) -> bool:
    return self.size == 0

def push(self, element: type(Node.element)):
    self.head = self.Node(element, self.head) # created and linked a new node
    self.size += 1 # size is incremented

def top(self) -> type(Node.element):
    if self.is_empty():
        raise Exception("stack is empty")
    return self.head.element

def pop(self) -> Node:
    if self.is_empty():
        raise Exception("stack is empty")
    answer = self.head.element
    self.head = self.head.next # bypass the former node :)
    self.size -= 1 # size decremented
    return answer

def query(self):
    """
    for TTD and debugging.
```

```

    """
    for k in self:
        print(k.element)

```

3.4 LinkedQueue

In [4]: class LinkedQueue:

```

    """
    FIFO implementation of queue with using linked list as internal storage
    """

    # ----- Nested Class -----
    class Node:
        "light weight class for storing linked node"
        __slots__ = 'element', 'next'                # streamline memory usage

        def __init__(self, element, next):           # initialize node field
            self.element = element                   # reference to current element
            self.next = next                         # reference to the next node

    # ----- Stack Methods -----
    def __init__(self):
        self._head = self.Node(None, None)
        self._tail = self.Node(None, None)
        self._size = 0

    def __len__(self) -> int:
        """
        return the number of elements in the linked list
        :return: integer
        """
        return self._size

    def __iter__(self):
        """
        iterate thorough the linked list
        """
        if self.is_empty():
            yield
        current = self._head
        while current is not None:
            yield current
            current = current.next

    def is_empty(self) -> bool:
        """
        :return: bool True if list is empty and False otherwise
        """
        return self._size == 0

    def first(self):
        """
        just Return the first element in the queue

```

```

        """
        if self.is_empty():
            raise Exception("empty Error")
        return self._head.element

def dequeue(self):
    """
    remove and return the first element
    """
    if self.is_empty():
        raise Exception("empty Error")
    var = self._head.element
    self._head = self._head.next
    self._size -= 1
    if self.is_empty():
        self._tail = None
    return var

def enqueue(self, element):
    newest = self.Node(element, None)
    if self.is_empty():
        self._head = newest
    else:
        self._tail.next = newest
    self._tail = newest
    self._size += 1

def query(self):
    """
    for TTD and debugging.
    """
    for k in self:
        print(k.element)

```

3.5 Binary Search Tree

3.5.1 preview:

my BST class is implemented with aim of inner node class and an abstract meta class which provide the

```

In [5]: from abc import ABCMeta, abstractmethod
import os
import re

```

```

class ABCNode(metaclass=ABCMeta):
    @abstractmethod
    def insert(self, key, NodeType):
        pass

    @abstractmethod
    def find(self, key):
        pass

    @abstractmethod

```

```

def minimum(self):
    pass

@abstractmethod
def successor(self):
    pass

@abstractmethod
def delete(self):
    pass

class BST(object):
    class Node(ABCNode):
        __slots__ = "key", "parent", "left", "right", "size", "repetition"

        # -----

        def __init__(self, parent, key):
            """Create a new leaf with key t."""
            self.key = key
            self.parent = parent
            self.left = None
            self.right = None
            self.size = 1
            self.repetition = 1

        # -----

        def update_stats(self):
            """Updates this node's size based on its children's sizes."""
            self.size = (0 if self.left is None else self.left.size) \
                + (0 if self.right is None else self.right.size)

        # -----

        def insert(self, key, NodeType) -> ABCNode:
            self.size += 1
            if key < self.key:
                if self.left is None:
                    self.left = NodeType(self, key)
                    return self.left
                else:
                    return self.left.insert(key, NodeType)
            elif key == self.key:
                self.repetition += 1
                return
            else:
                if self.right is None:
                    self.right = NodeType(self, key)
                    return self.right
                else:
                    return self.right.insert(key, NodeType)

```

```

# -----

def find(self, key) -> ABCNode:
    """Return the node for key if it is in this tree, or None otherwise."""
    if key == self.key:
        return self
    elif key < self.key:
        if self.left is None:
            return None
        else:
            return self.left.find(key)
    else:
        if self.right is None:
            return None
        else:
            return self.right.find(key)

# -----

def rank(self, key) -> int:
    """Return the number of keys <= key in the subtree rooted at this node."""
    left_size = 0 if self.left is None else self.left.size
    if key == self.key:
        return left_size + 1
    elif key < self.key:
        if self.left is None:
            return 0
        else:
            return self.left.rank(key)
    else:
        if self.right is None:
            return left_size + 1
        else:
            return self.right.rank(key) + left_size + 1

def minimum(self) -> ABCNode:
    """Returns the node with the smallest key in the subtree rooted by this node."""
    current = self
    while current.left is not None:
        current = current.left
    return current

def successor(self) -> ABCNode:
    """
    Returns the node with the smallest key larger than this node's key,
    or None if this has the largest key in the tree.
    """
    if self.right is not None:
        return self.right.minimum()
    current = self
    while current.parent is not None and current.parent.right is current:
        current = current.parent
    return current.parent

```



```

# -----

def delete(self) -> ABCNode:
    """Delete this node from the tree."""
    if self.left is None or self.right is None:
        if self is self.parent.left:
            self.parent.left = self.left or self.right
            if self.parent.left is not None:
                self.parent.left.parent = self.parent
        else:
            self.parent.right = self.left or self.right
            if self.parent.right is not None:
                self.parent.right.parent = self.parent
        current = self.parent
        while current.key is not None:
            current.update_stats()
            current = current.parent
        return self
    else:
        s = self.successor()
        self.key, s.key = s.key, self.key
        return s.delete()

# -----check for error-----

def check(self, lower_key, higher_key):
    """
    Checks that the subtree rooted at key is a valid BST
    and all keys are between (lower_key, higher_key).
    """
    if lower_key is not None and self.key <= lower_key:
        raise Exception("BST RI violation")
    if higher_key is not None and self.key >= higher_key:
        raise Exception("BST RI violation")
    if self.left is not None:
        if self.left.parent is not self:
            raise Exception("BST RI violation")
        self.left.check(lower_key, self.key)
    if self.right is not None:
        if self.right.parent is not self:
            raise Exception("BST RI violation")
        self.right.check(self.key, higher_key)
    if self.size != 1 + (0 if self.left is None else self.left.size) + (
        0 if self.right is None else self.right.size):
        raise Exception("BST RI violation")

def __repr__(self) -> str:
    return "<BST Node, key:" + str(self.key) + ">"

def __init__(self, NodeType=Node):
    self.root = None
    self.NodeType = NodeType
    self.proot = self.NodeType(None, None)

```

```

        self.content = DynamicArray()
        self.docs = DynamicArray()

# -----
def reroot(self):
    self.root = self.psroot.left

def insert(self, key) -> Node:
    """Insert key into this BST, modifying it in-place."""
    if self.root is None:
        self.psroot.left = self.NodeType(self.psroot, key)
        self.reroot()
        self.root.update_stats()
        return self.root
    else:
        return self.root.insert(key, self.NodeType)

def add_doc(self, doc_name: str):
    self.docs.append(doc_name)

# -----

def find(self, key) -> Node:
    """Return the node for key if is in the tree, or None otherwise."""
    if self.root is None:
        return None
    else:
        return self.root.find(key)

def rank(self, key) -> int:
    """The number of keys <= key in the tree."""
    if self.root is None:
        return 0
    else:
        return self.root.rank(key)

def traverse(self, node: Node = None) -> list:
    if node is None:
        node = self.root

    self.content.append(node)
    if node.left is not None:
        self.traverse(node=node.left)
    if node.right is not None:
        self.traverse(node=node.right)

def delete(self, key) -> Node:
    node = self.find(key)
    if node is None:
        raise Exception("nadari in klid ro")
    deleted = node.delete()
    self.reroot()
    return deleted

```

```

# -----

def check(self):
    if self.root is not None:
        self.root.check(None, None) # check in the Node class

def __str__(self) -> str:
    if self.root is None:
        return '<empty tree>'

    def recurse(node):
        if node is None: return [], 0, 0
        label = str(node.key)
        left_lines, left_pos, left_width = recurse(node.left)
        right_lines, right_pos, right_width = recurse(node.right)
        middle = max(right_pos + left_width - left_pos + 1, len(label), 2)
        pos = left_pos + middle // 2
        width = left_pos + middle + right_width - right_pos
        while len(left_lines) < len(right_lines):
            left_lines.append(' ' * left_width)
        while len(right_lines) < len(left_lines):
            right_lines.append(' ' * right_width)
        if (middle - len(label)) % 2 == 1 and node.parent is not None and \
            node is node.parent.left and len(label) < middle:
            label += '.'
        label = label.center(middle, '.')
        if label[0] == '.': label = ' ' + label[1:]
        if label[-1] == '.': label = label[:-1] + ' '
        lines = [' ' * left_pos + label + ' ' * (right_width - right_pos),
            ' ' * left_pos + '/' + ' ' * (middle - 2) +
            '\\ ' + ' ' * (right_width - right_pos)] + \
            [left_line + ' ' * (width - left_width - right_width) + right_line

            for left_line, right_line in zip(left_lines, right_lines)]
        return lines, pos, width

    return '\n'.join(recurse(self.root)[0])

```

3.6 Ternary Search Tree

3.6.1 preview :

based on string searching method and functionality.

```

In [6]: class TST:
        __slots__ = 'size', 'root', 'valid_words', 'docs'

        # ----- inner class -----

        class Node:
            __slots__ = 'key_char', 'left', 'mid', 'right', 'value'

            def __init__(self, key_char: str):
                self.key_char = key_char
                self.left = None

```

```

        self.mid = None
        self.right = None
        self.value = str()

# ----- end of inner class -----

def __init__(self):
    self.root = TST.Node(" ")
    self.size = 0
    self.valid_words = LinkedQueue()
    self.docs = DynamicArray()

def __sizeof__(self) -> int:
    return self.size

def __contains__(self, item: str) -> bool:
    if item is None:
        raise Exception("nothing to be contained!!!")
    return self.__getitem__(item) is not None

def __getitem__(self, item: str) -> str:
    if item is None:
        raise Exception("call __getitem__ with None argument")
    if len(item) == 0:
        raise Exception("item must have length >= 1")
    x = self.get(self.root, item, 0)
    if x is None:
        return None
    return x.value

def intable(self, stream: object) -> tuple:
    try:
        integer = int(stream)
        return True, integer
    except Exception as err:
        return False, err

def get(self, x: Node, item: str, d: int) -> Node:
    """
    return sub-trie corresponding to given key
    """
    if x is None:
        return None
    if len(item) == 0:
        raise Exception("item must have length >= 1")
    char = item[d]
    if char < x.key_char:
        return self.get(x.left, item, d)
    elif char > x.key_char:
        return self.get(x.right, item, d)
    elif d < len(item) - 1:
        return self.get(x.mid, item, d + 1)
    else:
        return x

```

```

def put(self, item: str, value: int) -> None:
    """
    Inserts the key-value pair into the symbol table
    """
    if item is None:
        raise Exception("call __setitem__ with None argument")
    else:
        self.size += 1
        self.root = self.set(self.root, item, value, 0)

def set(self, x: Node, item: str, value: int, d: int) -> Node:
    char = item[d]
    if x is None:
        x = TST.Node(char)
        # self.size += 1
    if char < x.key_char:
        x.left = self.set(x.left, item, value, d)
    elif char > x.key_char:
        x.right = self.set(x.right, item, value, d)
    elif d < len(item) - 1:
        x.mid = self.set(x.mid, item, value, d + 1)
    else:
        x.value = value
    return x

def longestPrefixOf(self, query: str) -> str:
    if query is None:
        raise Exception("call longestPrefixOf() with None argument")
    if len(query) == 0:
        return None
    length = int(0)
    x = self.root
    i = 0
    while x is not None and i < len(query):
        char = query[i]
        if char < x.key_char:
            x = x.left
        elif char > x.key_char:
            x = x.right
        else:
            i += 1
            if x.value is not None:
                length = i
            x = x.mid

    return query[0:length]          # testing required

def keys(self) -> LinkedQueue:
    queue = LinkedQueue()
    self.collect(self.root, str(), queue)
    return queue                    # queue is iterable?

```

```

def keysWithPrefix(self, prefix: str) -> LinkedQueue:

    if prefix is None:
        raise Exception("call keysWithPrefix() with None argument")
    queue = LinkedQueue()
    x = self.root
    x = self.get(x, prefix, 0)
    if x is None:
        return queue
    if x.value is not None:
        queue.enqueue(prefix)
    self.collect(x.mid, str(prefix), queue)
    return queue

def collect(self, x: Node, prefix: str, queue: LinkedQueue) -> None:
    if x is None:
        return None
    self.collect(x.left, prefix, queue)
    if x.value is not None:
        queue.enqueue(str(prefix) + x.key_char)
    # self.collect(x.mid, str(prefix) + str(x.key_char), queue)
    prefix = prefix[:-1]
    self.collect(x.right, prefix, queue)

def keysThatMatch(self, pattern: str) -> LinkedQueue:
    queue = LinkedQueue()
    self.patternMatching(self.root, str(), 0, pattern, queue)
    return queue

def patternMatching(self, x: Node, prefix: str, i: int, pattern: str, queue: LinkedQueue):
    """
    some kind of collector
    """
    if x is None:
        return
    char = pattern[i]
    if char == '.' or char < x.key_char:
        self.patternMatching(x.left, prefix, i, pattern, queue)
    if char == '.' or char == x.key_char:
        if i == len(pattern) - 1 and x.value is not None:
            queue.enqueue(str(prefix) + str(x.key_char))
        if i < len(pattern) - 1:
            self.patternMatching(x.mid, str(prefix) + str(x.key_char), i + 1, pattern, queue)
        prefix = prefix[:-1]

    if char == '.' or char > x.key_char:
        self.patternMatching(x.right, prefix, i, pattern, queue)

def add_doc(self, doc_name: str):
    self.docs.append(doc_name)

def traverse(self):
    if self.size == 0:

```

```

        raise Exception("empty tst can't be traversed")
    for q in self.keys():
        if self[q.element] is not None and self[q.element] is not "":
            yield q.element

def validation(self):
    for v in self.traverse():

        self.valid_words.enqueue(v)

```

3.7 TrieST

3.7.1 previwe :

this class is based on a light weight inner Node class, it can supports all 256 ascii character :))

In [7]: class TrieST:

```

    R = 256
    __slots__ = 'root', 'number_of_keys', 'valid_words', 'docs'

```

```

    # -----

```

```

class Node:
    __slots__ = 'value', 'next'

    def __init__(self):
        self.value = str()
        self.next = [None] * TrieST.R

```

```

def __init__(self):
    self.root = self.Node()
    self.number_of_keys = 0
    self.valid_words = LinkedQueue()
    self.docs = DynamicArray()

```

```

def __sizeof__(self) -> int:
    return self.number_of_keys

```

```

def __len__(self) -> int:
    return self.__sizeof__()

```

```

def is_empty(self) -> bool:
    return self.__sizeof__() == 0

```

```

def __getitem__(self, key: str) -> str:
    x = self.get(self.root, key, 0)
    if x is None:
        return None
    return str(x.value)

```

```

def __contains__(self, key: str) -> bool:
    return self.__getitem__(key) is not None

```

```

def get(self, x: Node, key: str, d: int) -> Node:
    if x is None:

```



```

        return None
    if d == len(key):
        return x
    char = key[d]
    return self.get(x.next[int(ord(char))], key, d + 1)

def put(self, key: str, value: int):
    if value is None:
        del key
    else:
        self.root = self.set(self.root, key, value, 0)

def set(self, x: Node, key: str, value: int, d: int) -> Node:
    if x is None:
        x = self.Node()
    if d == len(key):
        if x.value is None:
            self.number_of_keys += 1
        x.value = value
        return x
    char = key[d]
    x.next[int(ord(char))] = self.set(x.next[int(ord(char))], key, value, d + 1)
    return x

def keys(self) -> LinkedQueue:
    return self.keysWithPrefix("")

def keysWithPrefix(self, prefix: str) -> LinkedQueue:
    result = LinkedQueue()
    x = self.get(self.root, prefix, 0)
    self.collect(x, str(prefix), result)
    return result

def collect(self, x: Node, prefix: str, result: LinkedQueue) -> None:
    if x is None:
        return
    if x.value is not None:
        result.enqueue(str(prefix))
    for i in range(self.R):
        prefix += chr(i)
        self.collect(x.next[i], prefix, result)
    prefix = prefix[:-1]

def keysThatMatch(self, pattern: str) -> LinkedQueue:
    result = LinkedQueue()
    self.patternMatching(self.root, str(), pattern, result)
    return result

def patternMatching(self, x: Node, prefix: str, pattern: str, result: LinkedQueue) -> None:
    if x is None:
        return
    d = len(prefix)
    if d == len(pattern) and x.value is not None:
        result.enqueue(str(prefix))

```

```

    if d == len(pattern):
        return

    char = pattern[d]
    if char == '.':
        for i in range(self.R):
            prefix += str(i)
            self.patternMatching(x.next[i], prefix, pattern, result)
            prefix = prefix[:-1]
    else:
        prefix += str(char)
        self.patternMatching(x.next[int(ord(char))], prefix, pattern, result)
        prefix = prefix[:-1]

def longestPrefix(self, query: str) -> str:
    length = self.longestPrefixOf(self.root, query, 0, -1)
    if length == -1:
        return None
    else:
        return query[:length]

def longestPrefixOf(self, x: Node, query: str, d: int, length: int) -> int:
    if x is None:
        return length
    if x.value is not None:
        length = d
    if d == len(query):
        return length
    char = query[d]
    return self.longestPrefixOf(x.next[int(ord(char))], query, d + 1, length)

def add_doc(self, doc_name: str):
    self.docs.append(doc_name)

def traverse(self):
    query = self.keys()
    for q in query:
        if self[q.element] is not "":
            yield(q.element)

def validation(self):
    for v in self.traverse():
        self.valid_words.enqueue(v)

def delete(self, key: str, x: Node=None, d: int=None) -> Node:
    if x is None and d is None:
        self.root = self.delete(key, x=self.root, d=0)
    if x is None:
        return None
    if d == len(key):
        if x.value is not None:
            self.number_of_keys -= 1
        x.value = None
    else:

```

```

        char = key[d]
        x.next[int(ord(char))] = self.delete(x.next[int(ord(char))], key, d + 1)

# remove subtree rooted at x if it is completely empty
        if x.value is not None:
            return x
        for i in range(self.R):
            if x.next[i] is not None:
                return x
        return None

```