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Project

Statistical Inference, Fall 2022

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Note:

In the R code I used couple of libraries that are not installed by default. If you want to run the code, please check and uncomment the install.pakges("") in my code.

Question 0:

A) Airbnb is a service that helps house owners to rent out their properties to people who need a temporary place to stay. Airbnb does not own any of these houses, it profits by receiving a commission from each booking. This service has grown larger every year since 2008. This dataset contains these data:

Field	Type	Description
Id	Integer	Airbnb's unique identifier for the listing.
Name	Text	The property name.
Host id	Integer	Airbnb's unique identifier for the owners.
Host identify verified	Text or Boolean(t=true; f=false)	Airbnb hosts will have the option of requiring that all their guests verify their identification before booking a reservation. Hosts who choose this option will be required to verify their own identification as well.
Host name	Text	Name of the host. Usually just the first name(s).
Neighborhood group	Text	The neighborhood group as geocoded using the latitude and longitude against neighborhoods as defined by open or public digital shapefiles.
Neighborhood	Text	The neighborhood as geocoded using the latitude and longitude against neighborhoods as defined by open or public digital shapefiles.
Lat (latitude)	Numeric	Uses the World Geodetic System (WGS84) projection for latitude and longitude.
Long (longitude)	numeric	Uses the World Geodetic System (WGS84) projection for latitude and longitude.
Country	Text	The country where the house is located.
Instant bookable	boolean	[t=true; f=false]. Whether the guest can automatically book the listing without the host requiring to accept their booking request. An indicator of a commercial listing.
cancellation_policy	Text	There are 10 cancellation policies as followed: Flexible Moderate Firm Strict Strict Long term Flexible Long term Non-refundable option Super Strict 30 days Super Strict 60 days Special cases However, this dataset only contains 3 of these policies:

		Flexible: Guests can cancel until 24 hours before check-in for a full refund, and you won't be paid. If they cancel after that, you'll be paid for each night they stay, plus 1 additional night. Moderate: Guests can cancel until 5 days before check-in for a full refund, and you won't be paid. If they cancel after that, you'll be paid for each night they stay, plus 1 additional night, plus 50% for all unspent nights. Strict: To receive a full refund, guests must cancel within 48 hours of booking, and the cancellation must occur at least 14 days before check-in. If they cancel between 7 and 14 days before check-in, you'll be paid 50% for all nights. If they cancel after that, you'll be paid 100% for all nights.
Room type	Text	
		All homes are grouped into the following three room types: Entire place Private room Shared room
		Entire place: Entire places are best if you're seeking a home away from home. With an entire place, you'll have the whole space to yourself. This usually includes a bedroom, a bathroom, a kitchen, and a separate, dedicated entrance. Hosts should note in the description if they'll be on the property or not (ex: "Host occupies first floor of the home"), and provide further details on the listing.
		Private rooms: Private rooms are great for when you prefer a little privacy, and still value a local connection. When you book a private room, you'll have your own private room for sleeping and may share some spaces with others. You might need to walk through indoor spaces that another host or guest may occupy to get to your room.
		Shared rooms: Shared rooms are for when you don't mind sharing a space with others. When you book a shared room, you'll be sleeping in a space that is shared with others and share the entire space with other people. Shared rooms are popular among flexible travelers looking for new friends and budget-friendly stays.
Construction year	Integer	The year the house was constructed.
Price	Integer	daily price in local currency. (\$ sign may be used despite local.)
service fee	Integer	To help Airbnb run smoothly and to cover the cost of services like 24/7 customer support, Airbnb charges a service fee when a booking is confirmed.
minimum nights	Integer	minimum number of night stay for the listing (calendar rules may be different).
number of reviews	Integer	The number of reviews the listing has over the lifetime of the listing.

reviews per month	Numeric	The average number of reviews that the listing get in each month.		
review rate	Integer	Average rating of the location.		
number				
calculated host	integer	The number of listings the host has in the current scrape, in the		
listings count		city/region geography.		
availability 365	integer	avaliability_x. The availability of the listing x days in the future as		
	-	determined by the calendar. (listing may be available because it has		
		been booked by a guest or blocked by the host)		

Why studying the Airbnb dataset can be interesting?

This dataset can give various insights in matters such as:

- What features are more important for people to choose their preferred house?
 - O Does neighborhood play a role in choosing houses?
 - Are some Neighborhoods cheaper?
 - Are neighborhoods that are close to tourist attractions more popular?
 - Do houses located in some neighborhoods get more visitors? And Which neighborhoods are more popular?
 - What range or price is more acceptable for people?
 - Do people prefer to go to cheaper houses or rating matters most?
 - Do people care about service fees and if it is expensive is it a deal breaker?
 - •
 - o Does house rating affect people's decisions?
 - Do more expensive houses get a better rating?
 - Does the number of previous visitors and their rating matter to people?
 - _
 - What kind of house do people prefer to stay in?
 - Does the Construction year matter?
 - What kind of Room type is more popular among renters? Do people prefer to get a more expensive house to get more privacy?
 - What kind of policies drive people away?
 - Does Instance booking matter?
 - Does availability 365 matter?
 - Are people ok with strict cancellation policies?
- Property owners prefer to provide what kind of services?
 - o Do property owners prefer to be strict on their policies?
 - o Do property owners prefer to verify their identification? And does it affects their visitors?
 - o Do people in more poor Neighborhoods tend to rent part of their home?
 - What is the range of price preferred for property owners of each area?

Also, we can use these data in combination whit users' data to provide a good house recommendation for them.

B) This dataset has 23 columns. Six of these columns are useless and do not have any practical application. These columns are the entry's id, name of the place, name of the owner, the host id, id of the place, and the country (All of the houses are in America, obviously). Therefore, we have 17 features and 30000 cases.

```
> df <- read.csv(file = 'Airbnb_Open_Data.csv')
> df <- df[ , ! names(df) %in% c("X","NAME","id","host.id","host.name","country")]
> n_col<- ncol(df)
> n_row<- nrow(df)
> n_col
[1] 17
> n_row
[1] 30000
```

It should be mentioned that there are some duplicate data in this dataset after deleting them we will have 29957 cases.

```
> df<-df[!duplicated(df), ]
> n_row<- nrow(df)
> n_row
[1] 29957
```

C) First off, we need to analyze if the values are correct in each feature:

It is obvious in the above figure. There are some values that are inherently wrong:

- The minimum nights feature is inherently positive and should not have a case with a negative value.
- For the minimum nights feature great values, such as 5645 are highly unlikely. (It does not make sense to rent the house for 5645 days on minimum)
- Availability 365 is inherently positive and should not have a case with a negative value.
- Availability 365 means the availability of the listing 365 days in the future as determined by the calendar. Cases with values more than 365 are unlikely to be the correct values.
- For reviews per month features, cases with a value of more than 30 do not really make any sense. Because it means more than 30 people have stayed there in 30 days. Which is not possible. However, it is possible that people stayed there in groups of more than 1 person. But it is still unlikely that every person who stayed there wrote a review. (I checked the actual place on the Airbnb website that had 65.74 reviews per month and it only has 973 reviews as of right now. Which, confirms that the data is incorrect or it was just a temporary spike.). I am suspecting most of the cases with more than 10 reviews per month are incorrect but I keep these data for sake of having some outliers for future parts of this project.

For correction of the incorrect values, we can give them Nan values and fix them with other Nan values later, or we can just guess what was the correct value. We use the first approach:

• The minimum nights:

Most of the data is between 1 and 30. However, Some of the values of more than 30 can make sense. For example, People might want to rent their house for the whole summer to go on vacation (There is a spike in 90 days which might be caused by the explained theory).

Nevertheless, we exclude the values outside this range by replacing them with Nans.

```
> df['minimum.nights'][df['minimum.nights'] < 0]=NA
> df['minimum.nights'][df['minimum.nights'] >31]=NA
```

• Availability 365:

Most of the data is between 1 and 365. we exclude the values outside this range by replacing them with Nans.

Reviews per month:

we exclude the values outside the range of 0 to 30 by replacing them with Nans.

```
> df['reviews.per.month'][df['reviews.per.month'] >31]=NA
```

In addition to the above problems. Some features that are in text format have some incorrect or missing values.

• The neighborhood group:

In this feature, there are 13 cases with missing values (because it is in text format df summary did not show this). Also, in some cases, Manhattan is misspelled.

• The neighborhood:

In this feature, there are 5 cases with missing values.

```
> table(df$neighbourhood)[0:5]
```

```
Allerton Arden Heights Arrochar Arverne 5 25 5 14 73
```

• cancellation_policy:

In this feature, there are 26 cases with missing values.

host_identity_verified:

In this feature, there are 92 cases with missing values.

instant bookable:

In this feature, there are 39 cases with missing values.

```
> table(df$instant_bookable)
    False True
    39 15099 14819
> df['instant_bookable'][df['instant_bookable']== '']=NA
```

After deleting incorrect data our dataset would look like this:

```
> summary(df)
Nost_identity_verified neighbourhood.group length:29957
Mode :character
Mode :
```

There are missing data in 14 features.

The construction year has 66 nulls which represent 0.2203158% of the total rows. The price has 76 nulls which represent 0.2536970% of the total rows. The service fee has 93 nulls which represent 0.3104450% of the total rows. Minimum nights has 487 nulls which represent 1.6256635% of the total rows. The number of reviews has 58 nulls which represent 0. 1936108% of the total rows. Reviews per month has 4641 nulls which represent 15.49220549% of the total rows. The review rate number has 102 nulls which represent 0.34048803% of the total rows. The calculated host listings count has 100 nulls which represent 0.3338118% of the total rows. Availability 365 has 1025 nulls which represent 3.4215709% of the total rows. The neighborhood group has 14 nulls which represent 0.04339553% of the total rows. The neighborhood has 5 nulls which represent 0.01669059% of the total rows. The instant bookable has 39 nulls which represent 0.13018660% of the total rows. The cancellation policy has 26 nulls which represent 0.08679107% of the total rows. The host_identity_verified has 92 nulls which represent 0.30710685% of the total rows.

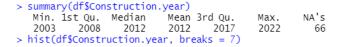
Other features do not have any missing data.

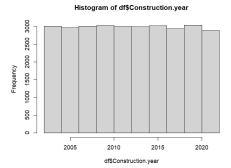
The portion of missing values for each variable is as followed:

```
> na_count <-sapply(df, function(y) sum(length(which(is.na(y)))))/n_row*100
        host_identity_verified
0.30710685
                                              neighbourhood.group
                                                                                       neiahbourhood
                                                        0.04339553
                                                                                           0.01669059
                                                                                                                             0.00000000
                                                                                cancellation_policy
0.08679107
                                              instant_bookable
                     long
0.00000000
                                                                                                                               room.tvpe
                                                        0.13018660
                                                                                                                             0.00000000
                                                                                service.fee
              construction.year
                                                                                                                        minimum.nights
                                                       price
0.25369697
                                                                                 0.31044497 1.0250007.7 review.rate.number calculated.host.listings.count
                     0 22031579
              number.of.reviews
                                                reviews.per.month
                      0.19361084
                                                       15.49220549
               availability.365
3.42157092
```

For handling missing values in each column we should analyze the column based on its real-world meaning. We can replace these nan values with an educated guess or we can just dispose of any case with a nan value. but the second option is not a good choice because in such a way we lose the information. Here, we use the first approach and replace these data:

• Construction year:

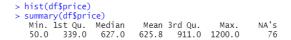


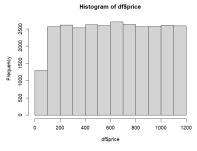


The construction year feature has an almost even distribution in the span of 2022 to 2003 and we can simply replace any nan values in this variable with the median of this feature.

```
> df$Construction.year[is.na(df$Construction.year)]<-median(df$Construction.year,na.rm=TRUE)
> # Price Nan values
> summary(df$price)
Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
50.0 339.0 627.0 625.8 911.0 1200.0 76
```

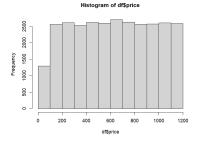
Price:





The price feature has an almost even distribution between 50 to 1200 and there are not many outliers to skew our mean. Therefore, we can simply replace any nan values in this variable with the mean or median of this feature.

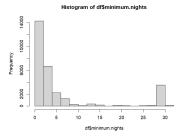
Service fee:



The service fee has an almost even distribution between 10 to 240 and there are not many outliers to skew our mean. Therefore, we can simply replace any nan values in this variable with the mean or median of this feature.

```
> df$service.fee[is.na(df$service.fee)]<-median(df$service.fee,na.rm=TRUE)
> summary(df$service.fee)
   Min. 1st Qu. Median Mean 3rd Qu. Max.
   10.0 68.0 125.0 125.2 182.0 240.0
```

Minimum nights



The minimum nights feature is extremely skewed to right. For handling the nan values for this feature. We know that 1 night is the most repeated number so we replace all the nan values with 1. Which, makes sense people need to stay at least one night.

> summary(df\$number.of.reviews)

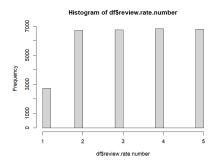
• Number of reviews:

```
Min. 1st Qu.
                               Median
                                               Mean 3rd Qu.
                                                                         Max.
        0.00
                     1.00
                                  7.00
                                              27.52
                                                           31.00
                                                                     884.00
            Histogram of df$number.of.reviews
  25000
  20000
  15000
Frequi
  10000
  2000
                                            > table(df$number.of.reviews)[0:5]
                                                           2
                                               Λ
                                                     1
                 df$number.of.reviews
                                            4650 3033 2042 1572 1215
```

The Number of reviews is extremely skewed to right. For handling the nan values for this feature. We know that 0 reviews is the most common number so we replace all the nan values with 0.

```
> df$number.of.reviews[is.na(df$number.of.reviews)]<-0
> summary(df$number.of.reviews)
   Min. 1st Qu. Median Mean 3rd Qu. Max.
   0.00   1.00   7.00   27.52   31.00   884.00
```

• Review rate number:

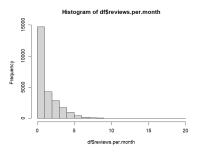


The rating has an almost even distribution. Therefore, we can simply replace any nan values in this variable with the median of this feature.

```
> df$review.rate.number[is.na(df$review.rate.number)]<-median(df$review.rate.number,na.rm=TRUE)
> summary(df$review.rate.number)
Min. 1st Qu. Median Mean 3rd Qu. Max.
1.000 2.000 3.000 3.275 4.000 5.000
```

• Reviews per month:

```
> summary(df$reviews.per.month)
   Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
   0.010   0.220   0.750   1.372   2.020   19.750   4644
> hist(df$reviews.per.month)
```

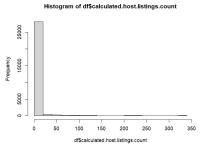


The Reviews per month feature is extremely skewed to right. For handling the nan values for this feature. We replace the Nan values with the median of this variable.

```
> df$reviews.per.month[is.na(df$reviews.per.month)]<-median(df$reviews.per.month,na.rm=TRUE)
> summary(df$reviews.per.month)
   Min. 1st Qu. Median Mean 3rd Qu. Max.
   0.010  0.280  0.750  1.276  1.730  19.750
```

• Calculated host listings count:

```
> summary(df$calculated.host.listings.count)
   Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
1.000 1.000 1.000 7.843 2.000 332.000 100
> hist(df$calculated.host.listings.count)
```

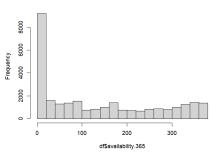


The calculated host listing count month feature is extremely skewed to right. For handling the nan values for this feature. We replace the Nan values with the median of this variable.

• Availability 365:

```
> summary(df$availability.365)
   Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
   0.0   3.0   90.0  133.4  249.0  366.0  1025
> hist(df$availability.365)
```

Histogram of df\$availability.365



The availability 365 feature has a spike around 0 and has an almost even distribution in other bins. We know that 0 is the most common number. Therefore, we replace all the nan values with 0.

```
> summary(df$availability.365)
  Min. 1st Qu. Median Mean 3rd Qu. Max.
    0.0    0.0    87.0    128.9    245.0    366.0
```

For the below categorical variables we choose the most common category for each variable to replace the nan values.

• host_identity_verified:

```
Unconfirmed is the most common status.
```

```
> tail(names(sort(table(df$host_identity_verified))), 1)
[1] "unconfirmed"
> df$host_identity_verified[is.na(df$host_identity_verified)]<-tail(names(sort(table(df$host_identity_verified))), 1)</pre>
```

neighborhood.group:

Manhattan is the most common neighborhood group.

```
> tail(names(sort(table(df$neighbourhood.group))), 1)
[1] "Manhattan"
> df$neighbourhood.group[is.na(df$neighbourhood.group)]<-tail(names(sort(table(df$neighbourhood.group))), 1)</pre>
```

neighbourhood:

Bedford-Stuyvesant is the most common neighborhood.

```
> tail(names(sort(table(df$neighbourhood))), 1)
[1] "Bedford-Stuyvesant"
> df$neighbourhood[is.na(df$neighbourhood)]<-tail(names(sort(table(df$neighbourhood))), 1)</pre>
```

cancellation_policy:

The moderate is the most common cancellation policy.

```
> tail(names(sort(table(df$cancellation_policy))), 1)
[1] "moderate"
> df$cancellation_policy[is.na(df$cancellation_policy)]<-tail(names(sort(table(df$cancellation_policy))), 1)</pre>
```

• instant bookable:

```
False is the most common Status.
```

```
> tail(names(sort(table(df$instant_bookable))), 1)
[1] "False"
> df$instant_bookable[is.na(df$instant_bookable)]<-tail(names(sort(table(df$instant_bookable))), 1)</pre>
```

D) I believe the sum of price and service fee will have the main role in this dataset. Because normally people decide based on their budget and they will have some exaptation based on the price of the house. Therefore, the price of a house defiantly has an impact on what people thought of the house

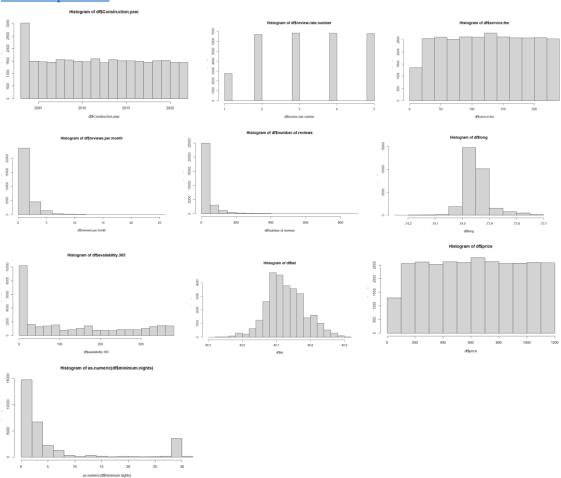
and as a result, their rating. Also, based on the range of price it can be guessed what neighborhood this house is located and what is its' room type.

Note:

As you can see in the below histograms.

Most of the important features have an uniform distribution and only longitude and latitude have a close to normal distribution. Therefore, in the following questions you can see there is little to no relationship between variables, and we can not infer anything based on this dataset.

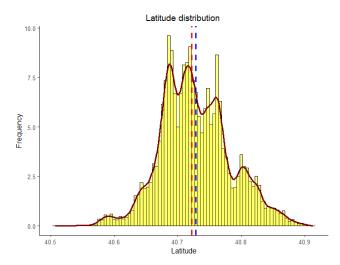
I have answered all the questions based on this dataset. But, I need to mention that this dataset is not correct and has been changed by someone (it is obvious just by looking at the price distribution that it should be skewed toward zero like real world data). The correct dataset is in New York City Airbnb Open Data.



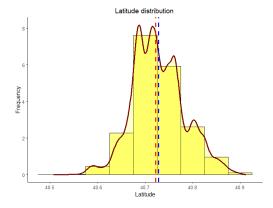
Question 1:

I will answer this question for two variables one of them is longitude which has a better distribution. The second one is price which is more important for this dataset.

- 1- Longitude:
- A) The distribution for this variable can be approximated as normal.



For choosing the bin size we used Freedman-Diaconis. However, because our chased variable is longitude, we can consider a bin size that is aligned with our data. For example, bin size=0.05 makes sense. Because, we can understand the frequency of rental houses in distances of 5 km, and our hisogram would look like this:



B) The distribution is skewed to right. In the figure above you can see the difference of mean and median. The histogram is also unimodal.

C)

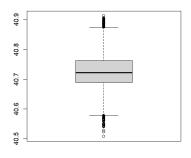
• The upper whisker reach: min(max(x), Q3 + 1.5 * IQR) = 40.79976

• The lower whisker reach: max(min(x), Q1 - 1.5 * IQR) = 40.57818

• IQR=Q3-Q1= 0.07386

• The upper quartile: 40.76283

• The lower quartile: 40.68897

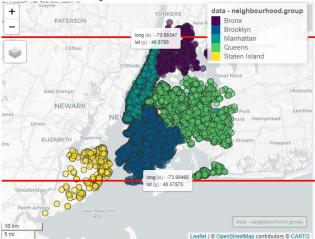


D) Cases with longitudes more than 40.79976 and less than 40.57818 are considered outliers

```
> PC_plotSut [11] 40.88107 40.88165 40.89600 40.88393 40.89702 40.88805 40.56033 40.57556 40.88526 40.87618 40.57773 40.57753 [12] 40.87828 40.89245 40.54106 40.56614 40.88985 40.88746 40.87993 40.57476 40.88796 40.88796 40.88467 40.88377 40.8823 40.89601 40.87297 40.87821 40.86688 40.87491 40.9948 40.87910 40.87340 40.8834 40.57636 40.88996 40.87666 40.88393 40.88933 40.88931 40.87866 40.87491 40.88297 40.87895 40.88948 40.57629 40.88939 40.92814 40.87933 40.88016 40.87866 40.87829 40.87896 40.87869 40.87869 40.8793 40.88016 40.87866 40.87829 40.87896 40.87896 40.87896 40.88939 40.88948 40.87820 40.87864 40.87820 40.88914 40.88211 40.88216 40.87391 40.88016 40.87394 40.87939 40.87896 40.87866 40.87820 40.87866 40.88217 40.88217 40.88217 40.88217 40.88217 40.88217 40.88217 40.88217 40.88217 40.88217 40.88217 40.88218 40.87218 40.88218 40.57762 40.88218 40.87821 40.88217 40.88218 40.87821 40.88218 40.57821 40.88218 40.87821 40.88218 40.88218 40.87821 40.88218 40.87821 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40.88218 40
```

We have 235 outliers in our data:

These data will look like this in the map:



Based on the above figure it is obvious that these cases are far away from the center of New York City. Therefore, they are considered outliers.

E)

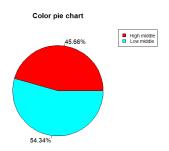
- Mean=40.72828
- Median=40.72224
- Variance=0.00309331
- Standard deviation=0.05561753

```
> mean(df$1at)
[1] 40.72828
> median(df$lat)
[1] 40.72224
> var(df$1at)
[1] 0.00309331
> sd(df$lat)
[1] 0.05561753
```

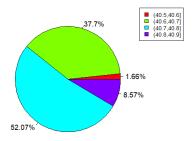
As it is understandable from the map. Our data is not much spread out from the mean. Which caused the low variance and low standard deviation, and because our data is not much skewed, the mean and median are close.

- F) It is not obvious what is the meaning of this question. I will answer for two possible meanings:
 - 1- Splitting data into 4 categories:
 - a. Lower than half of mean
 - b. Bigger than half of the mean and lower than mean
 - c. Bigger than mean and lower than 1.5*mean
 - d. Bigger than 1.5*mean

As mentioned in past parts of this project. Our data is very dense around the mean. Therefore, there is no data present in categories of d and a.

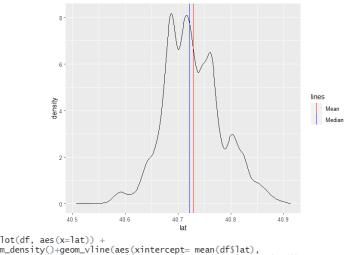


2- Splitting our data into 4 groups using cut:



```
> dat=cut(df$lat,breaks=4)
> pie(table(dat),labels = paste0(round(100 *table(dat)/sum(table(dat)), 2), "%"),col=rainbow(length(levels(dat))))
> legend("topright", levels(dat), cex = 0.8,fill = rainbow(length(levels(dat))))
```

G) The density plot will be as followed:



Based on the plot we understand that Mean>Median

Density has a spike near the mean. Which means, most of the data are around the mean.

Price:

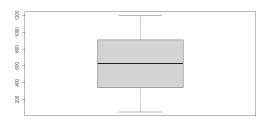


For this variable, the distribution is not normal and it is almost uniform.

B) the distribution modality is uniform. It is almost symmetric and there is no skewness.

C)

- The upper whisker reach: min(max(x), Q3 + 1.5 * IQR) = 1200
- The lower whisker reach: max(min(x), Q1 1.5 * IQR) = 50
- IQR=Q3-Q1= 569
- The upper quartile: 910
- The lower quartile: 341



```
PC_plot$stats
     [,1]
                > IQR(df$price)
       50
                [1] 569
[2,]
      341
                > quantile(df$price)
      627
[3,]
                  0% 25% 50%
                                75% 100%
[4,]
      910
                  50
                      341 627
                                 910 1200
[5,] 1200
```

D) As it is seen in the boxplot there is no outliers.

E)

The distribution is uniform from 50 to 1200. Therefore, it makes sense for the mean and the median to be almost exactly in the middle of our range. Also, we have a big range that has an almost distribution. Hence, the large value of variance and standard deviation is valid.

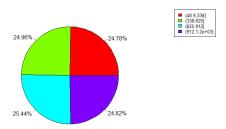
- F) It is not obvious what is the meaning of this question. I will answer for two possible meanings:
 - 3- Splitting data into 4 categories:

- a. Lower than half of mean
- b. Bigger than half of the mean and lower than mean
- c. Bigger than mean and lower than 1.5*mean
- d. Bigger than 1.5*mean

As mentioned in past parts of this project. Our data is very dense around the mean. Therefore, there is no data present in categories of d and a.

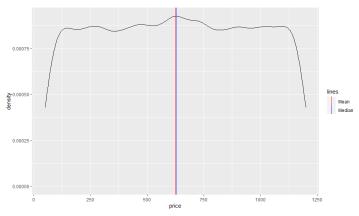


4- Splitting our data into 4 groups using cut:



```
> dat=cut(dfŚprice,breaks=4)
> pie(table(dat),labels = paste0(round(100 *table(dat)/sum(table(dat)), 2), "%"),col=rainbow(length(levels(dat))))
> legend("topright", levels(dat), cex = 0.8,fill = rainbow(length(levels(dat))))
```

G)



Mean and median are almost equal.

Question 2:

I chose the neighborhood group variable:

A) The table is like this:

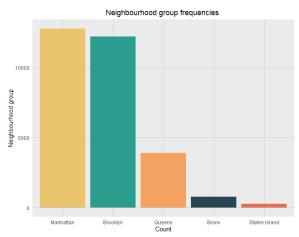
Neighborhood Group	Bronx	Brooklyn	Manhattan	Queens	Staten Island
Frequency	797	12201	12784	3897	278

In R:

> table(df\$neighbourhood.group)

Bronx Brooklyn Manhattan Queens Staten Island 797 12201 12784 3897 278

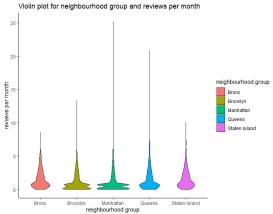
B)



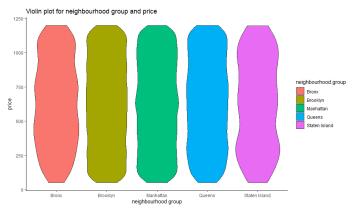
C)

Barplot of neighbourhood group 100 Frequency of neighbourhood group 8 90 40 2 Bronx Staten Island Brooklyn Manhattan Queens neighbourhood group xlab="neighbourhood group", ylab="Frequency of neighbourhood group",) text(bp, 0, paste(round(meds, 2), "%", sep=""), cex=1, pos=3)

D) We chose reviews per month as the second numerical variable. The violin plot is as followed:



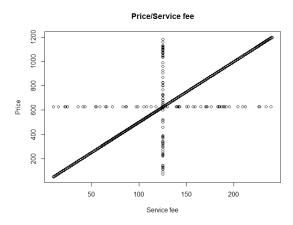
I will show this plot for price/neighborhood too to prove my point about this dataset having incorrect data:



As you can see here. The price distribution in all the neighborhood groups are almost equal. This obviously is not usual because in every city some neighborhood groups are more expensive than others. In this scenario, Manhattan and Brooklyn are two of the most renowned neighborhood and most expensive neighborhood in NYC. But here all the neighborhood have almost the same price.

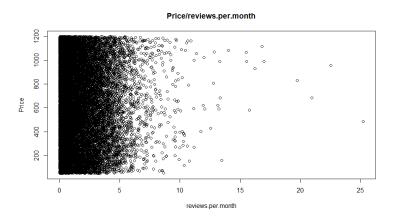
Question 3:

A) For price and service fee the scatter plot would look like this:



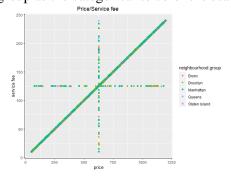
In most cases, there is a positive linear relationship between price and service fee. as one increases, the other increases.

We can draw scatter plot for other variables too for example:



There is not really a relationship between these two variables. But, It is understandable that most of the houses get under the 10 reviews. Per month which is valid.

B) We chose the neighborhood group as the categorical to color the scatter plot.

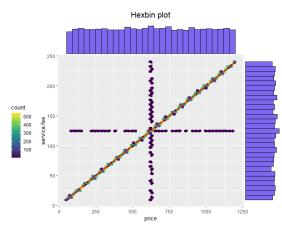


The relation between price and service fee still holds for different categories.

C) They are highly correlated:

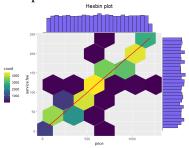
A p-value is a probability that the null hypothesis is true. In our case, it represents the probability that the correlation between price and service fee in the sample data occurred by chance. A p-value of 2.2e-16 means that there is only $2.2 \times 10^{-14}\%$ chance that results from our sample occurred due to chance.

D)

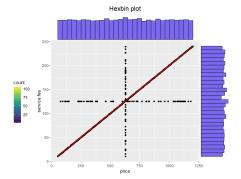


Based on the above figure, we understand that most of the cases abide by the relationship between price and service fee. Meaning that only small amount cases have a high price while having low service fees and vice versa.

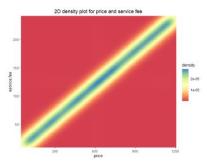
If the bin size is really small, The concentration of the data will not be clear, and a large range may be presented as the data concentration point.



If the bin size is really big, the Hexbin plot does not differ from a simple scatter plot and will not give us any useful additional information.



E)



Hexibin plot shows data in more accurate way. In general it leaves room for interpretation, we can find the exact outliers and their density. A data is a dot on a specific spot. However, 2d density plots shows some specific information in more understandable way. In addition, if the data set is so large that you literally can't make sense of a scatter plot due to overdrawing/occlusion, then we have to start looking for solutions like the chart on the left. Hexagon bin plots are another good option. Also, determining the number of bins in the Hexibin plot is something that should be discussed.

Question 4:

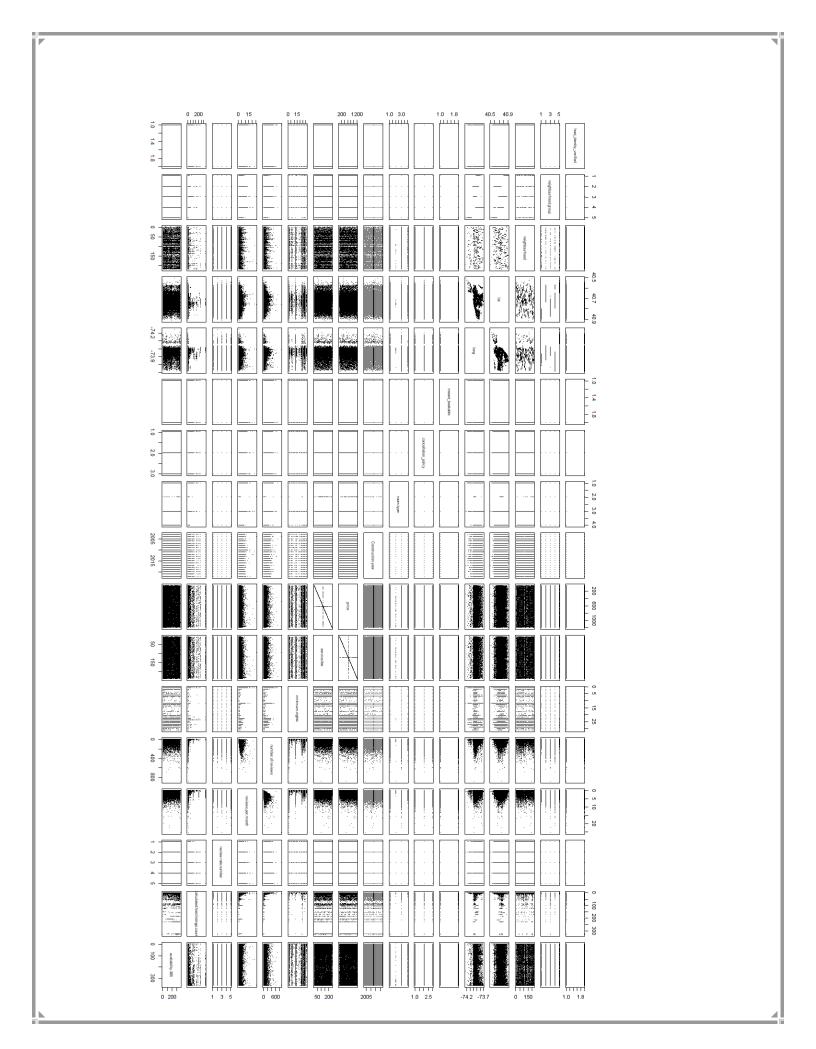
A) The heatmap correlograms for our variable will be like this (containing p-value and Pearson's correlation coefficients). The significant correlation is highlighted with the color red.

```
ed.host.listings.count 0.83 -0.3 🕱 🕱 🕱 -0.08 -0.03 0.82 🐽 0.07
                                            <mark>0.960.78</mark>0.590.590.510.480.72<mark>0.86</mark>0.62
                                              0 67 0 57 0 57 0 97 0 84 0 74 0 32 0 93
                               uction.year 0.78 0.67 0.67 0.67 0.6 0.56 0.79 0.78 0.62
                                   price 0.59 0.57 0.67
                                                           0.56 0.5 0.570.64 0.5
                                                                                                                                                   NE NE 0387 0343 0381 -051 0388
                                 ervice.fee 0.59 0.57 0.67
                                                           0.56 0.5 0.570.64 0.5
                         number.of.reviews 0.510.97 0.6 0.560.56
                                                                   0.620.350.95
                         reviews.per.month 0.48 0.84 0.56 0.5 0.5
                                                                   0.710.420.97
                        review.rate.number 0.72 0.74 0.79 0.57 0.57 0.62 0.71 0.86 0.71
                 calculated.host.listings.count 0.86 0.32 0.78 0.64 0.64 0.35 0.42 0.86
                           availability.365 0.62 0.93 0.62 0.5 0.5 0.95 0.97 0.71 0.57
> airbnb_cor <- df[, sapply(df, is.numeric)]
> airbnb_cor <- airbnb_cor[complete.cases(airbnb_cor), ]
> correlation_matrix <- cor(airbnb_cor)</pre>
  p.mat <- cor_pmat(correlation_matrix)</pre>
```

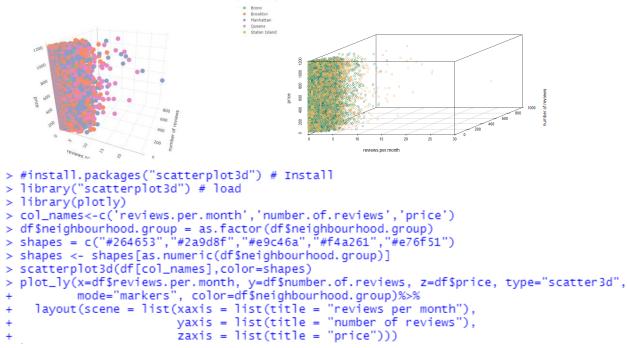
B) The correlogram is on the next page:

In most variables, there is no meaningful pattern between features. In other words, cases are distributed almost even in every class. Here I mention a couple of these patterns that I could spot:

- In most cases, there is a positive linear relationship between price and service fee. as one increases, the other increases.
- Based on the latitude and longitude(in addition to information from previous parts of this project). It is understandable these houses are concentrated around the center of NYC.
- The listing with the most number of reviews has the most number of reviews per month. Which makes sense. Also, most cases have reviews per month<15. (I explained why this is logical in Question 0.)



C) I Choose the price, reviews per month, and number of reviews for numerical variables and the neighborhood group as the categorical variables.



The price, reviews per month, and the number of reviews distribution is almost even in a different neighborhood group. However, there is a slight increase in price for houses with a larger number of reviews. Also, a larger number of reviews per month caused a slight increase in the number of reviews.

Ouestion 5:

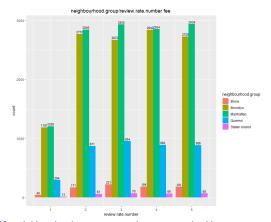
A) The Contingency table for the neighborhood group and review rate number is like this:

neighborhood group / review rate number	1	2	3	4	5	Total
Bronx	40	171	221	184	181	797
Brooklyn	1187	2772	2672	2842	2728	12201
Manhattan	1208	2848	2935	2854	2939	12784
Queens	294	871	954	892	886	3897
Staten Island	13	61	70	66	68	278
Total	2742	6723	6852	6838	6802	29957

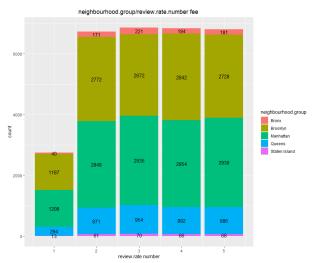
In R:

> addmargins(table(df\$neighbourhood.group,df\$review.rate.number))

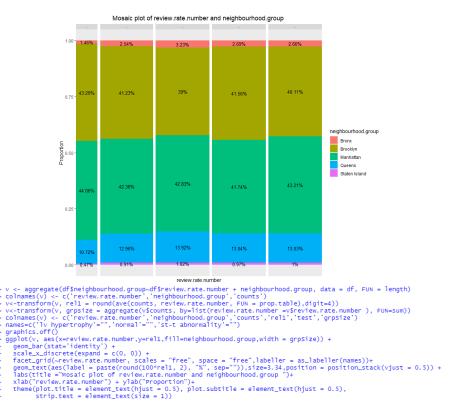
	1	2	3	4	5	Sum
Bronx	40	171	221	184	181	797
Brooklyn	1187	2772	2672	2842	2728	12201
Manhattan	1208	2848	2935	2854	2939	12784
Queens	294	871	954	892	886	3897
Staten Island	13	61	70	66	68	278
Sum	2742	6723	6852	6838	6802	29957



C)



D)

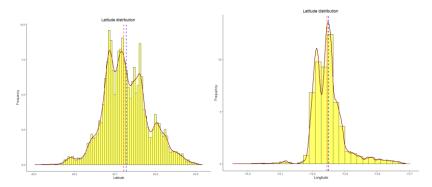


Question 6:

In this dataset, there are no numerical variables that have a close to the normal distribution, except longitude and latitude. But, these two variables both have outliers which, prevents us from using the CLT-based test. Also, these two variables are unimportant for our research. However, for the sake of doing the tests, and showing the process of t-test and CLT I assume there are no outliers and ignore them in these two variables and I will do the test. It should be mentioned that, because these variables do not met conditions of test. The result of these test might be incorrect.

I answer this question for two possibilities:

- 1- Two completely different numerical values:
- A) I chose the latitude and longitude as our numerical values
 For choosing between the t-test and the z-test we need to check the conditions:
 - Our observations are independent.
 - We chose 25 samples which are less than 10% of the whole population.
 - The population distribution is not extremely skewed.
 - O However, we have chosen 25 samples which are less than 30
 - There are outliers and therefore we can not use CLT but for the sake of doing the test we assume, there are no outliers.



Based on the above explanation, we need to use t-test.

B)

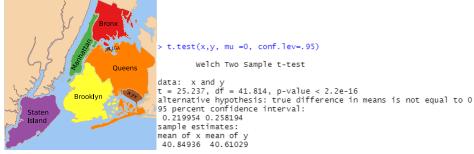
Difference = 40.73893 - (-73.95599) = 114.67068

 $p-value < \alpha = 0.05$. Therefore, We reject H_0 meaning that there is a significant difference between the mean of our variables.

As I mentioned in the beginning CLT based tests should not be used for this variable because of the presence of outliers. Here, we got a wrong answer for our hypothesis. The difference value is in our confidence interval. The confidence interval does not support rejecting the H_0 . Which is wrong and the result of the t-test and CLT should be the same.

2- One numerical variable and two different groups:

For example, I chose to check if there is a significant difference between the mean latitude of two neighborhoods.



Difference = 40.84936 - (40.61029) = 0.23907

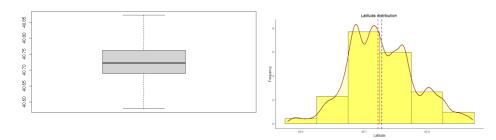
 $p-value < \alpha = 0.05$. Therefore, We reject H_0 meaning that there is a significant difference between the mean of our variables.

As I mentioned in the beginning CLT based tests should not be used for this variable because of the presence of outliers. Here, we got a wrong answer for our hypothesis. The difference value is in our confidence interval. The confidence interval does not support rejecting the H_0 . Which is wrong and based on the map above it is clearly obvious that the means should be different.

Question 7:

Based on the variables of this dataset, I can not answer this question. Because None of the variables met the condition to use CLT.

However, for the sake of doing this task, I assume there are no outliers for the latitude variable and I will delete them to use CLT.

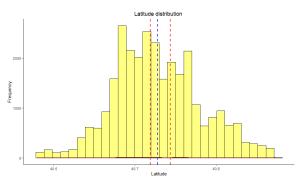


```
> IQR <- IQR(data_no_outlier$lat)
> quartiles <- quantile(data_no_outlier$lat, probs=c(.25, .75), na.rm = FALSE)
> Lower <- quartiles[1] - 1.5*IQR
> Upper <- quartiles[2] + 1.5*IQR
> data_no_outlier <- subset(data_no_outlier, data_no_outlier$lat > Lower & data_no_outlier$lat < Upper)
> boxplot(data_no_outlier$lat)
```

A) We calculate the interval using the below formula:

B) We are 98% confident that rental houses in NYC on average are located between 40.71879 to 40.74338.

C)



D) We suppose that house in NYC are located on average in latitude of 40.7 and we test if based on our sample this assumption is true or not.

$$H_0$$
: $lat = 40.7$
 H_A : $lat > 40.7$

If we consider $\alpha=0.02$. The p-value is very small therefore, we reject the null hypothesis. This means, our sample do not provide enough evidence to prove houses in NYC are located on average in 40.7

in our cases, p-value is the probability of the location of housed on average be in 40.7 and considering observation of our sample.

E) Yes the confidence interval supports our p-value result. The latitude of 40.7 is outside of the range of CI. Therefore, CI rejects the null hypothesis too.

F)

Power = 1 - Type II error =
$$1 - \beta = 1 - p(z \le z_a - \frac{40.72866 - 40.7}{0.005089511}) \Rightarrow power = 1 - p(z \le 1.96 - \frac{40.72866 - 40.7}{0.005089511}) = 1 - p(z \le 2.326348) = 1 - 0.6535786$$

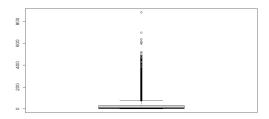
= 0.01

Type II error = 0.99

G) The magnitude of an effect size greatly impacts statistical power. Large effect sizes increase statistical power and small effect sizes decrease power.

Question 8:

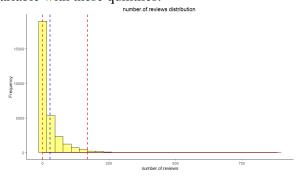
I used the number of reviews for this question:



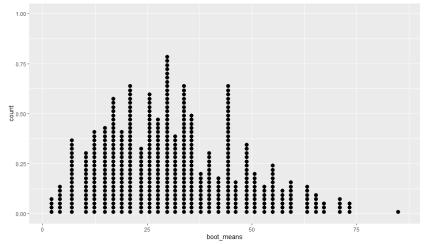
A) The 95% confidential interval using the quintiles of this variable are as followed:



The histogram of this variable with these quintiles:



- B) Now we take 20 samples from the original data and we will resample from this sample for 500 times with replacement to build the bootstrap distribution.
 - The bootstrap distribution is as followed:



Now for this distribution we calculate the CI:

$$\overline{x} - z^*SE < \mu < \overline{x} + z^*SE$$
Latitude distribution

C) Yes, there is noticeable difference between two methods. The quintile method is used on the original population and is not the correct method for estimating the mean. However, with bootstrapping we can calculate a correct confidence interval to estimate the mean value.

Question 9:

Again, we do not have any variables to that meet our conditions. However, for the sake of doing the tests, and showing the process of ANOVA I will show the process. It should be mentioned that, because these variables do not met conditions of test. The result might be incorrect.

I will use neighborhood group and latitude as my categorical and numerical variable. We check if latitude is different in different neighborhood groups. (It obviously is)

I also check for the price and neighborhood group variable. Because, price is a more important variable for this dataset.

1- Latitude:

A)

Hypothesis

H₀: The mean latitude is the same across all the mentioned neighborhood group.

$$\mu_1 = \mu_2 = \mu_3 = \mu_4 = \mu_5$$

H_A: The mean latitude differs between at least one pair of the mentioned neighborhood group.

```
Df Sum Sq Mean Sq F value Pr(>F)
neighbourhood.group 4 50.84 12.710 10796 <2e-16 ***
Residuals 29680 34.94 0.001
---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' '1
> df$neighbourhood.group <- factor(df$neighbourhood.group)
> result <- aov( lat~neighbourhood.group, data = data_no_outlier)
> summary(result)

B)
```

Based on the calculated $p - value < \alpha = 0.05$. We reject the null hypothesis. In other words, we conclude that there is at least one group that has a different mean latitude from others.

Now we need to do a pairwise comparison to find this group.

Our hypothesis for each pair wise comparison would be like:

 H_0 : The mean latitude in neighborhood group i and neighborhood group j is the same.

$$\mu_i - \mu_i = 0$$

H_A: The mean latitude in neighborhood group i and neighborhood group j is not the same.

$$\mu_i - \mu_i \neq 0$$

For the above pairwise test, we need to modify α based on Bonferroni correction therefore we have:

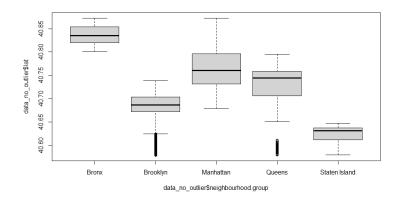
$$\alpha^* = \frac{\alpha}{5} = 0.01$$

However we could just use the bulletin Bonferroni correction like this:

Our test would be like this:

Based on the p-value in the pairwise comparison of each group, because in all the comparison $p - value < \alpha$. We reject the null hypothesis for each pair. Therefore, we conclude that the mean latitude is not equal in any of the groups.

The boxplot for this variable supports our findings too:



2- Price:

A)

Hypothesis

H₀: The mean price is the same across all the mentioned neighborhood group.

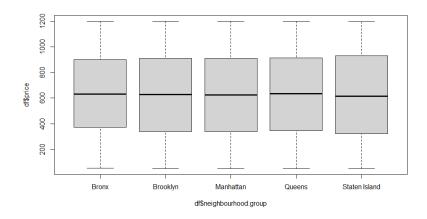
$$\mu_1 = \mu_2 = \mu_3 = \mu_4 = \mu_5$$

H_A: The mean price differs between at least one pair of the mentioned neighborhood group.

Our test would look like this:

Based on the calculated $p-value>\alpha=0.05$. We reject the H_A hypothesis. In other words, we conclude that the data suggests that the mean price of all the neighborhood group are equal.

This result is supported based on the boxplot too:



We can to a pairwise comparison. But because ANOVA test resulted in means being equal we expect the same result in each test.

Our hypothesis for each pair wise comparison would be like:

H₀: The mean price in neighborhood group i and neighborhood group j is the same.

$$\mu_i - \mu_j = 0$$

H_A: The mean price in neighborhood group i and neighborhood group j is not the same.

$$\mu_i - \mu_i \neq 0$$

For the above pairwise test, we need to modify α based on Bonferroni correction therefore we have:

$$\alpha^* = \frac{\alpha}{5} = 0.01$$

However we could just use the bulletin Bonferroni correction like this:

Our test would be like this:

Based on the p-value in the pairwise comparison of each group, because in all the comparison $p-value > \alpha$. We reject the null hypothesis for each pair. Therefore, we conclude, this data suggests that the mean price in all the groups are equal.