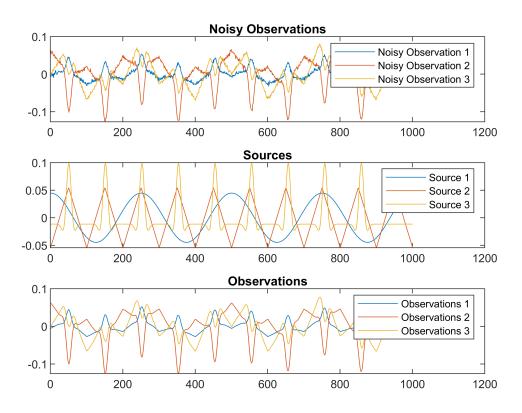
Antenna Array Processing

HW10-S4

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```
clear; clc; close all;
% Load Data:
Data = load("hw10.mat");
                    S = Data.S; Noise = Data.Noise;
Α
      = Data.A;
      = A*S+Noise; X Noiseless = A*S;
Χ
% Depict X:
figure()
subplot(3,1,1)
plot(X(1,:)); hold on; plot(X(2,:)); plot(X(3,:)); hold off;
title("Noisy Observations")
legend("Noisy Observation 1", "Noisy Observation 2", "Noisy Observation 3")
subplot(3,1,2)
plot(S(1,:)); hold on; plot(S(2,:)); plot(S(3,:)); hold off;
title("Sources")
legend("Source 1", "Source 2", "Source 3")
subplot(3,1,3)
plot(X_Noiseless(1,:)); hold on; plot(X_Noiseless(2,:)); plot(X_Noiseless(3,:)); hold off;
title("Observations")
legend("Observations 1", "Observations 2", "Observations 3")
```

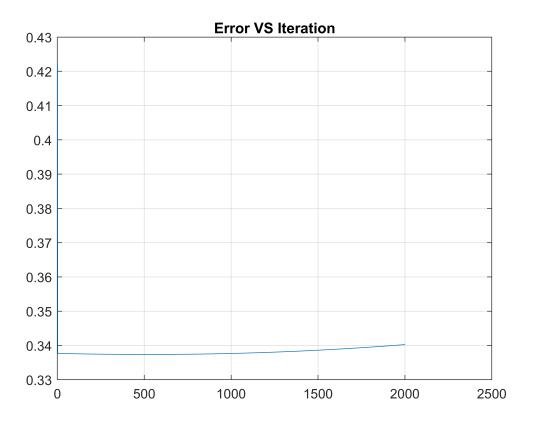


```
% WHitening theData:
[U , Gamma] = eig(X*X');
W = Gamma^(-0.5);
Z = W*U'*X; % Whitened Data

R_z = Z*Z';
disp(R_z); % We can see that Rz equals to I where all elements are zero excepts those 1s on the
    1.0000    0.0000    -0.0000
    0.0000    1.0000    0.0000
    -0.0000    0.0000    1.0000
```

```
B = generate_orthonormal_matrix(size(A,1)) ; % Because B and A are in the same size due to the
mu = 1e-02;
Max_Iter = 2e+3;
thresh_cntr = 1e-1;
thresh_B = 1e-10;
Error_Iter_deflate = zeros(1,Max_Iter)+inf;
```

```
cntr = 1;
y hat = B*Z;
MIN_ERR = inf;
Utility = zeros(3,1);
while(true)
    B_prev = B;
   % Update B:
   for i=1:length(B) % Each Row
        % Update Based on FIxed Point Method
        %StepSize
        Term_1
                      = mean( Z*((B(i,:)*Z)*exp(-(B(i,:)*Z).^2/2)')/length(Z),2);
                      = ((B(i,:)*Z).^2*exp(-(B(i,:)*Z).^2/2)'/length(Z))*B(i,:);
        Term 2
        B(i,:)
                     = Term_1 - Term_2'; %B(i,:) + mu*StepSize' ;
        B(i,:)
                     = B(i,:)/norm(B(i,:)); % Normalization
        B(i,:)
                     = (eye(size(B)) - B(1:i-1,:)'*B(1:i-1,:))* B(i,:)'; % Orthogonali
    end
    [Error_Perm,y_Hat_Chosen,B] = Perm_AMP_Disamb(B,S,Z);
    Error Iter deflate(cntr) = min(Error Perm);
    y_hat = B*Z;
    New_Utility = [F1\_Mine(y\_hat(1,:)); F1\_Mine(y\_hat(2,:)); F1\_Mine(y\_hat(2,:))];
   Utility = [Utility, New_Utility];
   % Check Convergence:
    if( (abs(Error_Iter_deflate(1,cntr))<thresh_cntr) || (cntr>Max_Iter) || ( norm(B_prev - B,
        break;
    end
    if ( Error_Iter_deflate(cntr)<MIN_ERR )</pre>
       y_hat_best = y_Hat_Chosen;
       B_hat_best = B;
       Index_Best = cntr;
       MIN_ERR = Error_Iter_deflate(cntr);
    end
    cntr = cntr +1;
end
figure()
plot(Error_Iter_deflate)
grid on
title("Error VS Iteration")
```



```
disp("calculated Error Equals to: "+min(Error_Iter_deflate))
```

calculated Error Equals to: 0.33736

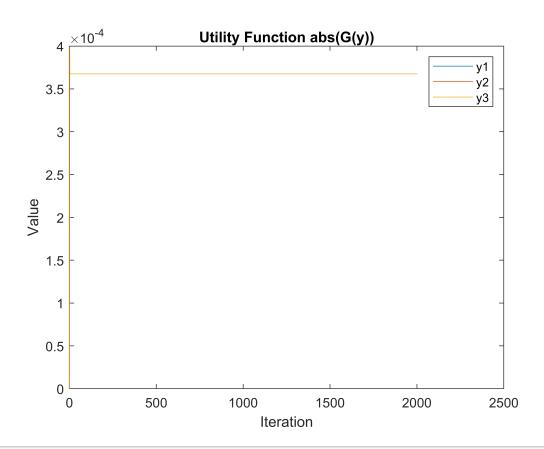
```
disp(abs(B_hat_best*W*U'*A))
```

```
      0.9707
      0.1861
      0.2479

      0.0952
      1.1132
      0.3289

      0.1742
      0.2469
      1.0646
```

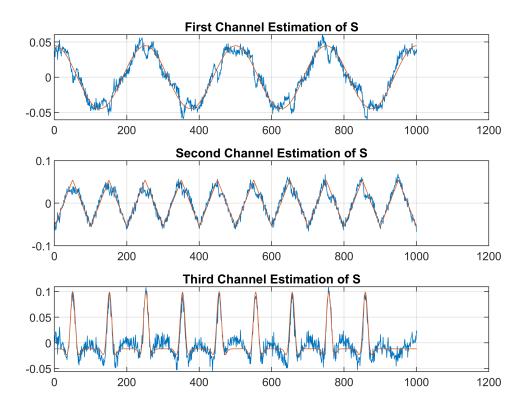
```
figure()
plot(Utility')
title("Utility Function abs(G(y))")
xlabel("Iteration")
ylabel("Value")
legend("y1","y2","y3")
```



Signal Illustration:

```
% Recovered S_hat:
y = y_Hat_Chosen;
figure()
subplot(3,1,1)
plot(y(1,:))% Permutaion
hold on
plot(S(1,:))
hold off
grid on
title("First Channel Estimation of S")
subplot(3,1,2)
plot(y(2,:))
hold on
plot(S(2,:))
hold off
grid on
title("Second Channel Estimation of S")
```

```
subplot(3,1,3)
plot(y(3,:))
hold on
plot(S(3,:))
hold off
grid on
title("Third Channel Estimation of S")
```



Functions:

```
function matrix = generate_orthonormal_matrix(size)
    % Step 1: Generate a random matrix
    matrix = randn(size, size);

% Step 2: Apply the Gram-Schmidt process
    for i = 1:size
        for j = 1:i-1
            matrix(:, i) = matrix(:, i) - dot(matrix(:, j), matrix(:, i)) * matrix(:, j);
        end
    end
end

% Step 3: Normalize each column
```

```
norms = vecnorm(matrix);
   matrix = matrix ./ norms;
end
function [Error_Perm,S_Hat_Chosen,B] = Perm_AMP_Disamb(B,S,Z) %% Perm_AMP_Disamb
       Final_Result_S_hat = calculate_permutations_and_Signs(B);
       % Calc the Error:
       L3 = size(Final_Result_S_hat,3);
       Error Perm = zeros(1,L3);
       for i=1:L3
           S_hat_temp = Final_Result_S_hat(:,:,i)*Z;
           Error_Perm(1,i) = norm(S_hat_temp-S, "fro")/norm(S, "fro");
       end
       [~ , idx ] = min(Error_Perm);
       S_Hat_Chosen = Final_Result_S_hat(:,:,idx)*Z;
       B = Final_Result_S_hat(:,:,idx);
    end
   function
               Final_Result = calculate_permutations_and_Signs(matrix)
       num_of_columns_matrix = size(matrix,2);
       variations = calculate_variations(matrix);
       cntr =1;
       %Temp = zeros(size(variations(:,:,1)));
       Final_Result = zeros([size(matrix), (2^num_of_columns_matrix)*factorial(num_of_columns_matrix)
       for j=1:size(variations,3)
           Temp = variations(:,:,j);
            num_of_columns = size(Temp,2);
            Different_Col_Arranges = perms(1:num_of_columns);
           for i=1:size(Different_Col_Arranges,1)
               Final Result(:,:,cntr) = Temp(:,Different_Col_Arranges(i,:)) ;
               cntr = cntr +1;
           end
       end
   end
   function variations = calculate_variations(matrix)
       % Get the size of the matrix
       [num rows, num cols] = size(matrix);
       % Generate all possible combinations of signs
       sign_combinations = cell(1, num_rows);
       [sign_combinations{:}] = ndgrid([-1, 1]);
       sign\_combinations = cellfun(@(x) x(:), sign\_combinations, 'UniformOutput', false);
       sign_combinations = cat(2, sign_combinations{:});
```