

# Computational Electromagnetics

## Hw6-Q4

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1401/09/30

```
clear; clc; close all;
```

```
a = 1/2;  
W = 0.125:0.25:1.125;  
d = 0.375;  
eps0 = 8.854*1e-12 ; % F/m
```

```
Sweep_N = [ 9 , 16 , 25 , 36 , 49 , 64 , 81 , 100];
```

```
C = zeros( length(W) , length(Sweep_N));  
C_plate = zeros( length(W),1);
```

```
A = (2*a)^2;
```

```
Alpha_t = cell(1,length(W)) ;
```

```
for i=1:length(W)  
    for j=1:length(Sweep_N)
```

```
        [C(i,j) , Alpha_t{i}] = Find_C(W(i) , Sweep_N(j),a ,d );
```

```
    end
```

```
    C_plate(i,1) = 2*(eps0*A/W(i) + eps0*A/d + eps0*A/ sqrt( W(i)^2 + d^2 ) ) ;
```

```
end
```

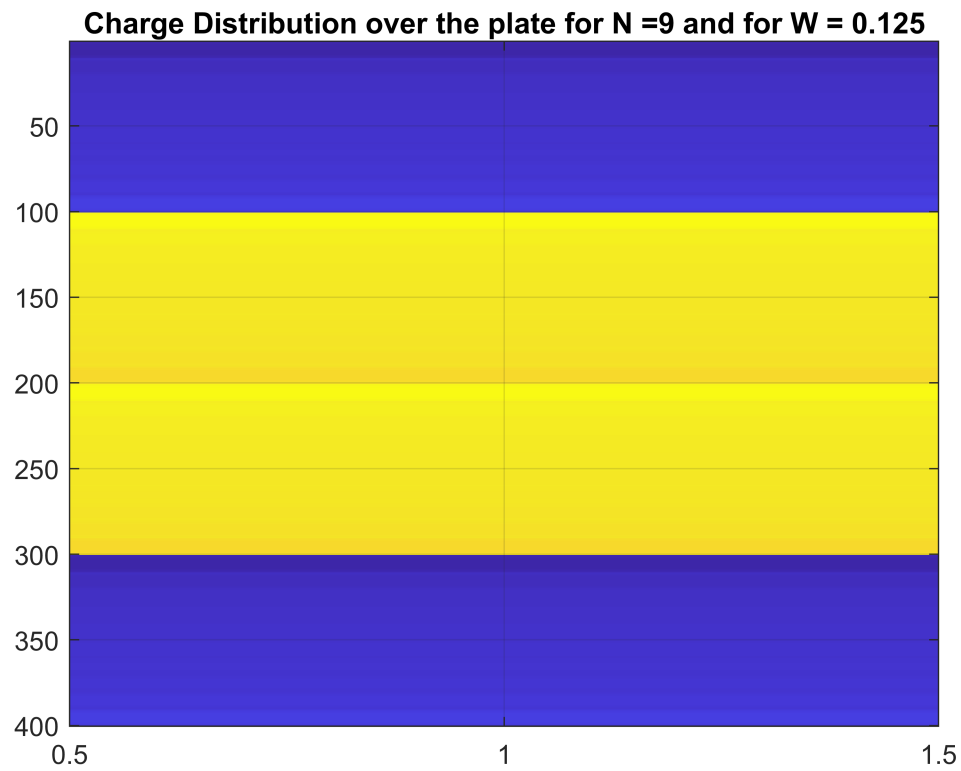
```
Charge_Distribution = Alpha_t{1};
```

```
figure(4)
```

```
imagesc(Charge_Distribution)
```

```
title("Charge Distribution over the plate for N =" + num2str(Sweep_N(1))+ " and for W =" + num2str(W(1)))
```

```
grid on
```



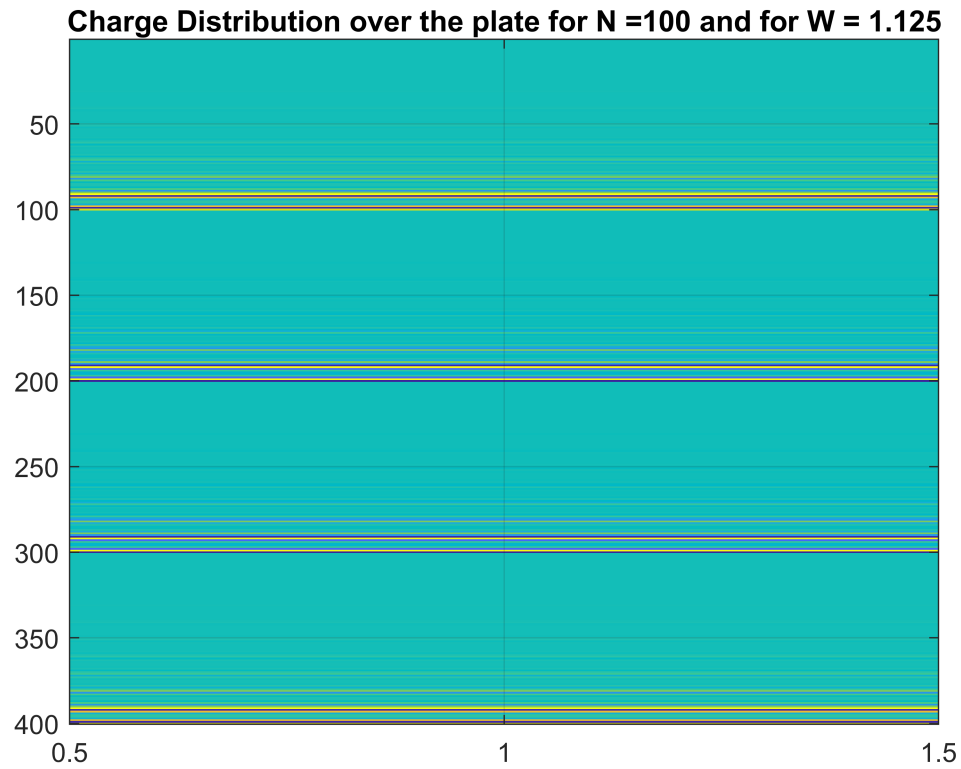
```
Charge_Distribution_end = Alpha_t{end};
```

```
figure(5)
```

```
imagesc(Charge_Distribution_end)
```

```
title("Charge Distribution over the plate for N =" + num2str(Sweep_N(end))+ " and for W = "+num2str(W))
```

```
grid on
```



```
function X_pos = Find_Cordx(m , N )
```

```
    if(m > sqrt(N) )
```

```
        Rem = m - sqrt(N);
```

```
        X_pos = Find_Cordx(Rem , N);
```

```
    else
```

```
        X_pos = ( m - 1/2);
```

```
    end
```

```
end
```

```
function Y_pos = Find_Cordy(m , N )
```

```
    Y_pos = floor(m/sqrt(N+1)+1)*1 - 1/2;
```

```
end
```

```
function R = R_finder(m,n,delta_X,delta_Y,N, reside,W)
```

```
    if(reside ==0 )
```

```
        R = abs( delta_X*Find_Cordx(m , N ) - delta_X*Find_Cordx(n , N ) )^2 +  
            abs( delta_Y*Find_Cordy(m , N ) - delta_Y*Find_Cordy(n , N ) )^2 ;
```

```
    else
```

```
        R = abs( delta_X*Find_Cordx(m , N ) - delta_X*Find_Cordx(n , N ) )^2 +
```

```

abs( delta_Y*Find_Cordy(m , N ) - delta_Y*(W+Find_Cordy(n , N )) )^2

end
end

function lmn = lmn_tt(m, n , delta_Sn , delta_X , delta_Y , N )
    eps0 = 8.854*1e-12 ; % F/m

    if(m==n)
        lmn = (sqrt(delta_Sn)/eps0)*0.2806;
    else
        lmn = delta_Sn/(4*pi*eps0*sqrt( R_finder(m,n,delta_X,delta_Y,N,0,0)) ) ;
    end
end

function lmn = lmn_rl(m, n , delta_Sn , delta_X , delta_Y , N , W)
    eps0 = 8.854*1e-12 ; % F/m
    % aeq = sqrt(delta_Sn/pi) ;
    residue =1;

    lmn = delta_Sn/(4*pi*eps0* sqrt( R_finder(m,n,delta_X,delta_Y,N, residue,W) )) ;
end

function lmn = lmn_tb(m, n , delta_Sn , delta_X , delta_Y , N , d)
    eps0 = 8.854*1e-12 ; % F/m
    aeq = sqrt(delta_Sn/pi) ;

    if(m==n)
        lmn = 1/(2*eps0) * (sqrt(aeq^2+d^2) - d ) ;
    else
        lmn = delta_Sn/(4*pi*eps0* sqrt(R_finder(m,n,delta_X,delta_Y,N,0,0)+d^2) ) ;
    end
end

function lmn = lmn_diag(m,n,delta_Sn , delta_X, delta_Y , N , W , d)

    eps0 = 8.854*1e-12 ; % F/m
    % aeq = sqrt(delta_Sn/pi) ;
    residue =1;

    lmn = delta_Sn/(4*pi*eps0* sqrt( d^2 + R_finder(m,n,delta_X,delta_Y,N, residue,W) )) ;
end

```

```

function [C , Alpha_t] = Find_C(W, N,a ,d)

    L11 = zeros(N,N);

    L13 = zeros(N,N);
    L14 = L13;
    L12 = L13;

    V =1;
    b = a / sqrt(N);
    delta_Sn = (2*b)^2 ;
    % eps0 = 8.854*1e-12 ; % F/m
    delta_X = 2*b;
    delta_Y = 2*b;

    for i=1:N
        for j=1:N
            L11(i,j) = lmn_tt(i, j , delta_Sn , delta_X , delta_Y , N );
            L13(i,j) = lmn_rl(i, j , delta_Sn , delta_X , delta_Y , N , W);
            L14(i,j) = lmn_diag(i,j,delta_Sn , delta_X, delta_Y , N , W , d);
            L12(i,j) = lmn_tb(i, j , delta_Sn , delta_X , delta_Y , N , d);
        end
    end

    L = [L11 , L12 , L13 , L14 ; L12 , L11 , L14, L13 ; L13 , L14 , L11 , L12 ; L14 , L13 , L12 , L11];

    Alpha_t = inv( L ) * [V*ones(N,1) ; -V*ones(N,1); -V*ones(N,1); V*ones(N,1) ];

    C = 1/(V) * sum([Alpha_t(1:N,:) ; Alpha_t(end-N+1,end) ],'all')*delta_Sn;

end

```