

# Antenna Array Processing

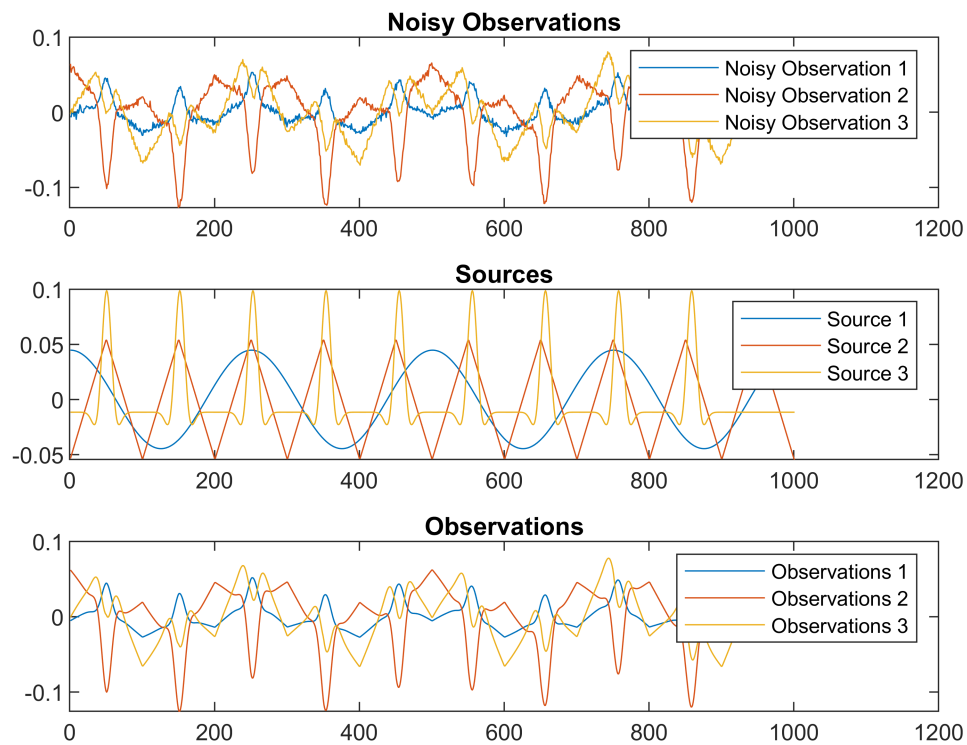
## HW10-S2

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1402/03/21

```
clear; clc; close all;
% Load Data:
Data = load("hw10.mat");
A     = Data.A;      S = Data.S;  Noise = Data.Noise;
X     = A*S+Noise;  X_Noiseless = A*S;
% Depict X:
figure()
subplot(3,1,1)
plot(X(1,:)); hold on; plot(X(2,:)); plot(X(3,:)); hold off;
title("Noisy Observations")
legend("Noisy Observation 1","Noisy Observation 2","Noisy Observation 3")
subplot(3,1,2)
plot(S(1,:)); hold on; plot(S(2,:)); plot(S(3,:)); hold off;
title("Sources")
legend("Source 1","Source 2","Source 3")

subplot(3,1,3)
plot(X_Noiseless(1,:)); hold on; plot(X_Noiseless(2,:)); plot(X_Noiseless(3,:)); hold off;
title("Observations")
legend("Observations 1","Observations 2","Observations 3")
```



```
% WHitening theData:
```

```
[U , Gamma] = eig(X*X');
```

```
W = Gamma^(-0.5);
```

```
Z = W*U'*X; % Whiten Data
```

```
R_z = Z*Z';
```

```
disp(R_z); % We can see that Rz equals to I where all elements are zero excepts those 1s on the
```

```
1.0000    0.0000   -0.0000
0.0000    1.0000    0.0000
-0.0000    0.0000    1.0000
```

```
B = generate_orthonormal_matrix(size(A,1)) ; % Because B and A are in the same size due to the
```

```
mu = 1e-02;
```

```
Max_Iter = 2e+3;
```

```
thresh_cntr = 1e-1;
```

```
thresh_B = 1e-10;
```

```
Error_Iter_deflate = zeros(1,Max_Iter)+inf;
```

```

cntr = 1;

y_hat = B*Z;
MIN_ERR = inf;

Utility = zeros(3,1);
while(true)
    B_prev = B;

    % Update B:
    for i=1:length(B) % Each Row

        % Update Based on Fixed Point Method
        B(i,:) = ((Z*(B(i,:)*Z)'.^3)'/length(Z) -3*B(i,:) );;%B(i,:) + mu*StepSize ;
        B(i,:) = B(i,:)/norm(B(i,:)); % Normalization
        B(i,:) = ( eye(size(B)) - B(1:i-1,:)'*B(1:i-1,:) ) * B(i,:); % Orthogonality

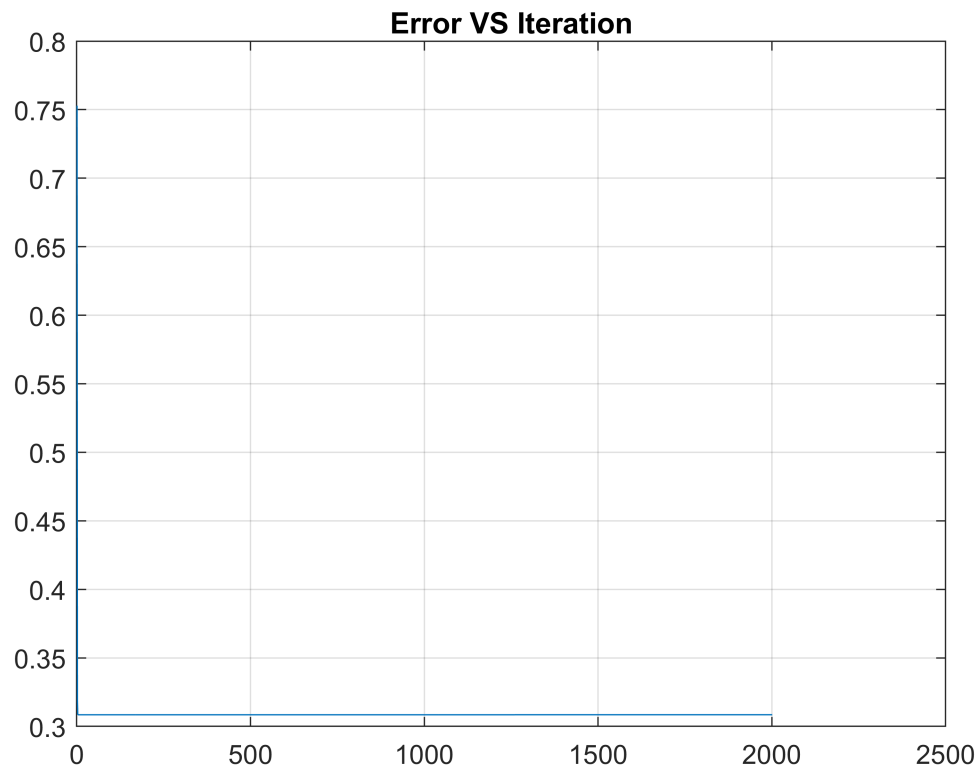
    end

    [Error_Perm,y_Hat_Chosen,B] = Perm_AMP_Disamb(B,S,Z);
    Error_Iter_deflate(cntr) = min(Error_Perm);
    y_hat = B*Z;
    New_Utility = [kurtosis(y_hat(1,:)) ; kurtosis(y_hat(2,:)) ; kurtosis(y_hat(3,:)) ];
    Utility = [Utility, New_Utility];
    % Check Convergence:
    if( (abs(Error_Iter_deflate(1,cntr))<thresh_cntr) || (cntr>Max_Iter) || ( norm(B_prev - B,
        break;
    end
    if ( Error_Iter_deflate(cntr)<MIN_ERR )
        y_hat_best = y_Hat_Chosen;
        B_hat_best = B;
        Index_Best = cntr;
        MIN_ERR = Error_Iter_deflate(cntr);
    end
    cntr = cntr +1;

end

figure()
plot(Error_Iter_deflate)
grid on
title("Error VS Iteration")

```



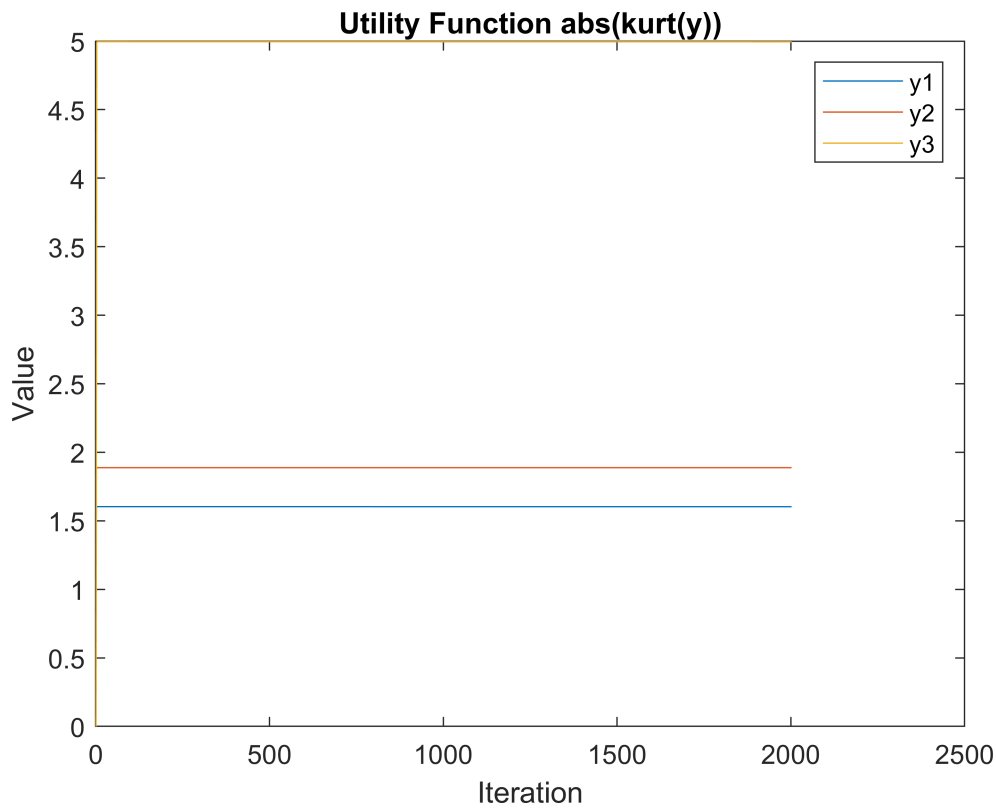
```
disp("calculated Error Equals to: "+min(Error_Iter_deflate))
```

calculated Error Equals to: 0.30849

```
disp(abs(B_hat_best*W*U'*A))
```

0.9895	0.0259	0.0689
0.0204	1.0942	0.2385
0.0440	0.3701	1.1142

```
figure()
plot(Utility')
title("Utility Function abs(kurt(y))")
xlabel("Iteration")
ylabel("Value")
legend("y1", "y2", "y3")
```



## Signal Illustration:

```
% Recovered S_hat:
y = y_Hat_Chosen;

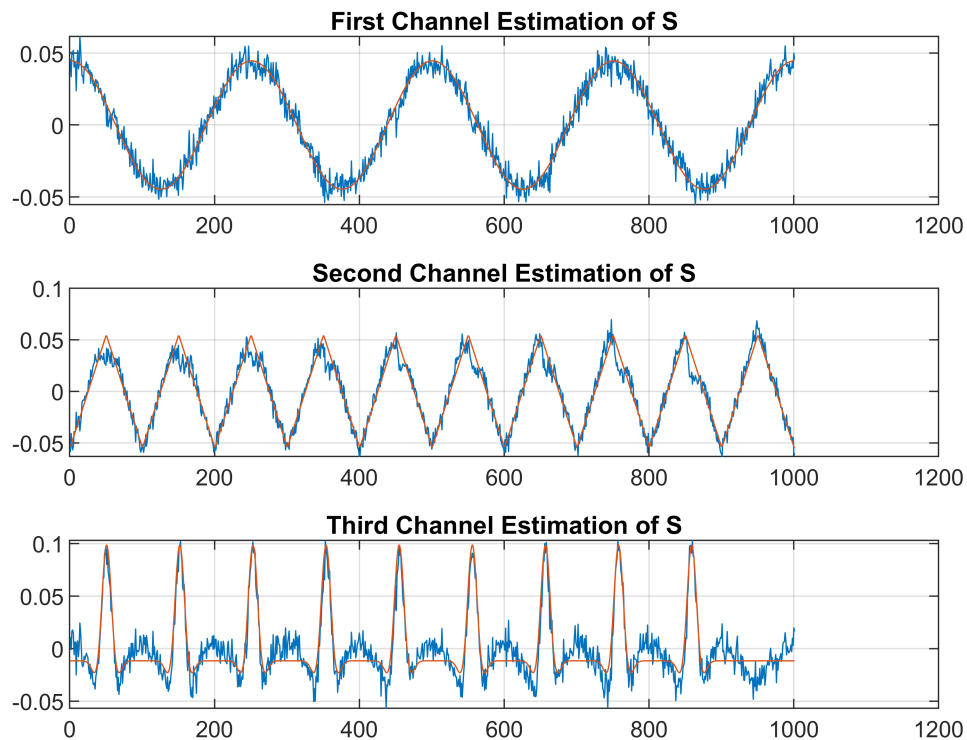
figure()
subplot(3,1,1)
plot(y(1,:))% Permutaion
hold on
plot(S(1,:))
hold off
grid on
title("First Channel Estimation of S")

subplot(3,1,2)
plot(y(2,:))
hold on
plot(S(2,:))
hold off
grid on
title("Second Channel Estimation of S")
```

```

subplot(3,1,3)
plot(y(3,:))
hold on
plot(S(3,:))
hold off
grid on
title("Third Channel Estimation of S")

```



## Functions:

```

function matrix = generate_orthonormal_matrix(size)
    % Step 1: Generate a random matrix
    matrix = randn(size, size);

    % Step 2: Apply the Gram-Schmidt process
    for i = 1:size
        for j = 1:i-1
            matrix(:, i) = matrix(:, i) - dot(matrix(:, j), matrix(:, i)) * matrix(:, j);
        end
    end

    % Step 3: Normalize each column
    norms = vecnorm(matrix);

```

```

matrix = matrix ./ norms;
end
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
function [Error_Perm,S_Hat_Chosen,B] = Perm_AMP_Disamb(B,S,Z) %% Perm_AMP_Disamb

    Final_Result_S_hat = calculate_permutations_and_Signs(B);
    % Calc the Error:
    L3 = size(Final_Result_S_hat,3);
    Error_Perm = zeros(1,L3);
    for i=1:L3
        S_hat_temp = Final_Result_S_hat(:,:,i)*Z;
        Error_Perm(1,i) = norm(S_hat_temp-S,"fro")/norm(S,"fro");
    end
    [~, idx ] = min(Error_Perm);
    S_Hat_Chosen = Final_Result_S_hat(:,:,idx)*Z;
    B = Final_Result_S_hat(:,:,idx);
end

function Final_Result = calculate_permutations_and_Signs(matrix)
    num_of_columns_matrix = size(matrix,2);
    variations = calculate_variations(matrix);
    cntr =1;
    %Temp = zeros(size(variations(:,:,1)));
    Final_Result = zeros([size(matrix), (2^num_of_columns_matrix)*factorial(num_of_columns_matrix)],3);
    for j=1:size(variations,3)
        Temp = variations(:,:,j);

        num_of_columns = size(Temp,2);
        Different_Col_Arranges = perms(1:num_of_columns);
        for i=1:size(Different_Col_Arranges,1)
            Final_Result(:,:,cntr) = Temp(:,Different_Col_Arranges(i,:)) ;
            cntr = cntr +1;
        end
    end
end

end

function variations = calculate_variations(matrix)
    % Get the size of the matrix
    [num_rows, num_cols] = size(matrix);

    % Generate all possible combinations of signs
    sign_combinations = cell(1, num_rows);
    [sign_combinations{:}] = ndgrid([-1, 1]);
    sign_combinations = cellfun(@(x) x(:), sign_combinations, 'UniformOutput', false);
    sign_combinations = cat(2, sign_combinations{:});

    % Calculate the number of variations

```

```
num_variations = size(sign_combinations, 1);

% Initialize the variations array
variations = zeros(num_rows, num_cols, num_variations);

% Generate the variations
for i = 1:num_variations
    % Apply the sign variations to each row
    variations( :, :, i) = matrix .* reshape(sign_combinations(i, :), 1, num_rows, 1);
end
end
```