

# National University of Computer & Emerging Sciences, Karachi Spring -2017 CS-Department



MidTerm 2

29th March 2017, 11:00 am - 12pm

Course Name: Numerical Methods Course Code: MT-207 Instructor Name: Syed M. Fahad Riaz Section No: Student Roll No:

## Instructions (Can vary according to requirements):

- Return the question paper.
- Read each question completely before answering it. There are 3 questions and 1 page.
- In case of any ambiguity, you may make assumption. But your assumption should not contradict any statement in the question paper.
- All the answers must be solved according to the sequence given in the question paper.
- This paper is subjective

Time: 60 minutes.

Max Marks: 30 points

#### Question 1:

Use the Adam-Bashforth-Moulton method, the three starting points and the step size h=0.05 to calculate [10] the next two values, y4 and y5 for the IVP given below:

$$y' = t^2 - y, y(0) = 1 \text{ over } [0,5]$$
  
 $y_1 = 0.9513$   
 $y_2 = 0.9052$   
 $y_3 = 0.8618$ 

### Question 2:

Consider the non-linear system

[5+5]

$$x^{2} - 2x - y + 0.5 = 0$$
$$x^{2} + 4y^{2} - 4 = 0$$

with the starting value  $(p_0, q_0) = (2.00, 0.25)$ 

- (a) Compute the Jacobian matrix and check whether the Jacobian matrix is invertible.
- (b) Use newton's method to compute  $(p_1, q_1)$ ,  $(p_2, q_2)$  and  $(p_3, q_3)$

#### Question 3:

- a) Write an algorithm of LU decomposition for 4x4 system and also state the number of equations and number of unknowns when LU decomposition method is applied.
- b) Use LU decomposition and Doolittle's method to solve the following linear system: [5]

$$x + y + z = 5$$
  
 $x + 2y + 2z = 6$   
 $x + 2y + 3z = 8$ 

BEST OF LUCK!