

61A Lecture 5

Friday, January 30

Announcements

- Quiz 1 scores will be posted eventually, but you already know what you'll get
- 0/3: Please talk to your TA for advice on how to proceed
- 1/3: Make sure to spend time understanding all lab & discussion questions
- 2/3: Practice is extremely helpful in learning how to solve CS problems
- Guerrilla Section 1 on higher-order functions is on Saturday 1/31 in 271 Soda
 - Optional discussion to promote mastery of core concepts (prepares you for midterms)
 - 2pm – 4pm is the vanguard section (you commit to helping teach the main section)
 - 4pm – 6pm is the main section
- Please do not bring questions about homework or projects to guerrilla sections
- Small-group tutoring begins next week! Apply online by Sunday if you want a (free) tutor
- Homework 2 (which is *small*) is due Monday 2/2 at 11:59pm
- Project 1 (which is **BIG**) is due Thursday 2/5 at 11:59pm

Environments for Higher-Order Functions

Names can be Bound to Functional Arguments

```
1 def apply_twice(f, x):
2   return f(f(x))
3
4 def square(x):
5   return x * x
6
7 result = apply_twice(square, 2)
```

Global frame

- func apply_twice(f, x) [parent=Global]
- func square(x) [parent=Global]

Applying a user-defined function:

- Create a new frame
- Bind formal parameters (f & x) to arguments
- Execute the body: return f(f(x))

Interactive Diagram

Environments for Nested Definitions

(Demo)

Environment Diagrams for Nested Def Statements

```
1 def make_adder(n):
2   def adder(k):
3     return k + n
4   return adder
5
6 add_three = make_adder(3)
7 add_three(4)
```

Nested def

Global frame

- func make_adder(n) [parent=Global]
- func adder(k) [parent=f1]
- f1: make_adder [parent=Global]
- adder
- Return value
- f2: adder [parent=f1]
- k: 4
- Return value: 7

- Every user-defined function has a parent frame (often global)
- The parent of a function is the frame in which it was defined
- Every local frame has a parent frame (often global)
- The parent of a frame is the parent of the function called

Interactive Diagram

How to Draw an Environment Diagram

When a function is defined:

Create a function value: func <name>(<formal parameters>) [parent=<label>]

Its parent is the current frame.

```
f1: make_adder    func adder(k) [parent=f1]
```

Bind <name> to the function value in the current frame

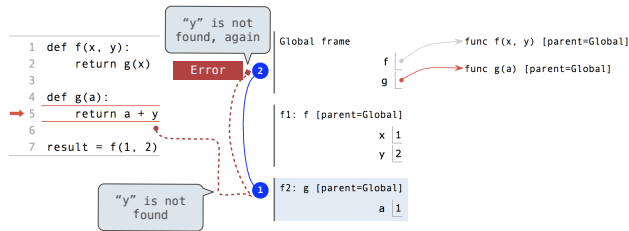
When a function is called:

1. Add a local frame, titled with the <name> of the function being called.
- ★ 2. Copy the parent of the function to the local frame: [parent=<label>]
3. Bind the <formal parameters> to the arguments in the local frame.
4. Execute the body of the function in the environment that starts with the local frame.

Local Names

(Demo)

Local Names are not Visible to Other (Non-Nested) Functions



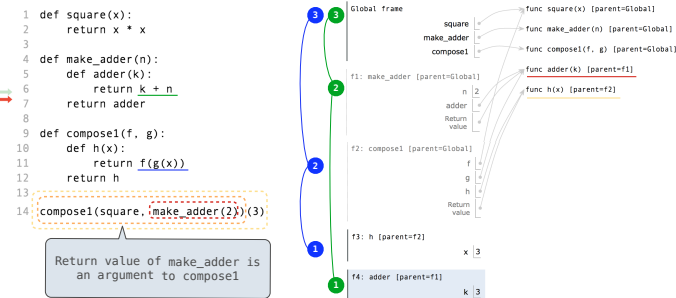
- An environment is a sequence of frames.
- The environment created by calling a top-level function (no def within def) consists of one local frame, followed by the global frame.

Interactive Diagram

Function Composition

(Demo)

The Environment Diagram for Function Composition



Interactive Diagram

Lambda Expressions

(Demo)

Lambda Expressions

```
>>> x = 10
>>> square = x * x
>>> square = lambda x: x * x
>>> square(4)
16
```

An expression: this one evaluates to a number

Also an expression: evaluates to a function

Important: No "return" keyword!

A function with formal parameter x that returns the value of "x * x"

Must be a single expression

Lambda expressions are not common in Python, but important in general
Lambda expressions in Python cannot contain statements at all!

Lambda Expressions Versus Def Statements

square = lambda x: x * x VS def square(x): return x * x

- Both create a function with the same domain, range, and behavior.
- Both functions have as their parent the frame in which they were defined.
- Both bind that function to the name square.
- Only the def statement gives the function an intrinsic name.



Currying

Function Currying

```
def make_adder(n):
    return lambda k: n + k
```

```
>>> make_adder(2)(3)
5
>>> add(2, 3)
5
```

There's a general relationship between these functions

(Demo)

Curry: Transform a multi-argument function into a single-argument, higher-order function