### 61A Lecture 7 Wednesday, February 4

### Announcements -Project 1 is due Thursday 2/5 @ 11:59pm; Early bonus point for submitting on Wednesday! -Extra tutor office hours on Wednesday 2/4 (See Piazza for details) -Midterm 1 is on Monday 2/9 from 7pm to 9pm! -Review session on Saturday 2/7 -HKN review session on Sunday 2/8 -Includes topics up to and including this lecture -Closed book/note exam, except for one page (2 sides) of hand-written notes & study guide -Cannot attend? Fill out the conflict form by Wednesday 2/4! http://goo.gl/2P5fKq -Optional Hog strategy contest ends Wednesday 2/18 @ 11:59pm

### Hog Contest Rules Fall 2011 Winners Up to two people submit one entry; Max of one entry per person Kaylee Mann Yan Duan & Ziming Li Brian Prike & Zhenghao Qian Parker Schuh & Robert Chatham $\bullet$ Your score is the number of entries against which you win more than 50% of the time Fall 2012 Winners All strategies must be deterministic, pure functions of the current player scores Chenyang Yuan Joseph Hui Fall 2013 Winners • All winning entries will receive 2 points of extra credit Paul Bramsen Sam Kumar & Kangsik Lee Kevin Chen • The real prize: honor and glory Fall 2014 Winners Alan Tong & Elaine Zhao Zhenyang Zhang Adam Robert Villaflor & Joany Gao Zhen Qin & Dian Chen Zizheng Tai & Yihe Li Spring 2015 Winners YOUR NAME COULD BE HERE... FOREVER!

Order of Recursive Calls

```
The Cascade Function
                                                      (Demo)
                                       Global frame
          def cascade(n):
                                                                         > func cascade(n) [parent=Global]
               if n < 10:
                                                        cascade 
               print(n)
else:
print(n)
                                       f1: cascade [parent=Global]
                   cascade(n//10)
                  print(n)
                                       f2: cascade [parent=Global]

    Each cascade frame is from a
different call to cascade.

                                                        n 12
        9 cascade(123)
                                                                     • Until the Return value appears, that call has not completed.
                                                      Return None
    Program output:
    • Any statement can appear before or after the recursive call.
                                           Interactive Diagram
```

```
(Demo)

def cascade(n):
    if n < 10:
        print(n)
    else:
        print(n)
    cascade(n/10)
    print(n)

    cascade(n/10)
    print(n)

    cascade(n/10)
    print(n)

    cascade(n/10)
    print(n)

If two implementations are equally clear, then shorter is usually better

In this case, the longer implementation is more clear (at least to me)

When learning to write recursive functions, put the base cases first

Both are recursive functions, even though only the first has typical structure
```

```
Example: Inverse Cascade
```

# Tree Recursion

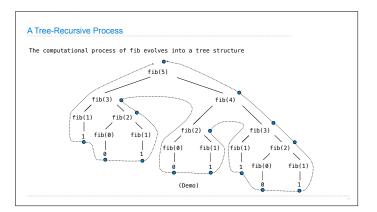
```
Tree Recursion

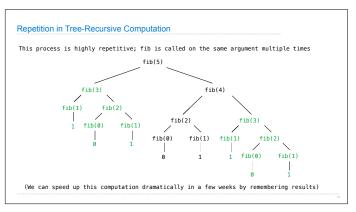
Tree-shaped processes arise whenever executing the body of a recursive function makes more than one recursive call

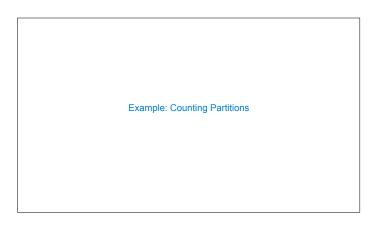
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35

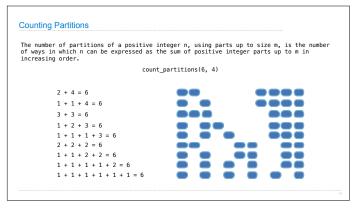
fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465

def fib(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return fib(n-2) + fib(n-1)
```









## Counting Partitions The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order. Count\_partitions(6, 4) Recursive decomposition: finding simpler instances of the problem. Explore two possibilities: -Use at least one 4 -Don't use any 4 -Solve two simpler problems: -count\_partitions(2, 4)---count\_partitions(6, 3) -Tree recursion often involves exploring different choices.

```
Counting Partitions

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

Recursive decomposition: finding simpler instances of the problem.
Explore two possibilities:
Use at least one 4
Don't use any 4
Solve two simpler problems:
Count_partitions(2, 4)
Count_partitions(2, 4)
Count_partitions(6, 3)
Count_partitions(1, m-1)
Count_partitions(1, m-
```