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COMPUTER SCIENCE 61A

January 29, 2015

1 Control

Control structures direct the flow of logic in a program. For example, conditionals allow a program to skip sections of code, while iteration allows a program to repeat a section.

1.1 Conditional Statements

Conditional statements let programs execute different lines of code depending on certain conditions. In Python, we can use the if-elif-else block:

Some notes:

- The else and elif statements are optional.
- You can have any number of elif statements.
- A **conditional expression** is a Python expression. All that matters for control is whether its value is a true value or a false value.
- The code that is executed is the **suite** that is indented under the first if/elif that has a true **conditional expression**. If none are true, then the else suite is executed.
- Once one suite is executed, the rest are skipped.

Note: in Python, there are a few things that are treated as false values:

- The boolean False
- The integer 0
- The value None
- And more...

Python also includes **boolean operators** and, or, and not. These operators are used to combine and manipulate boolean values.

- not True evaluates to False, and not False evaluates to True.
- True and True evaluates to True, but a false value on either side makes it False.
- False or False evaluates to False, but a true value on either side makes it True.

1.2 Iteration

Iteration lets a program repeat statements multiple times. A common iterative block of code is the **while loop**:

This block of code states: "while the conditional clause is still True, continue executing the indented body of statements." Here is an example:

1.3 Questions

1. Fill in the is_prime function, which returns True if n is a prime number and False otherwise.

Hint: use the % operator: x % y returns the remainder of x when divided by y.

def is_prime(n):

```
Solution:
    if n == 1:
        return False
    k = 2
    while k < n:
        if n % k == 0:
            return False
        k += 1
    return True</pre>
```

1.4 Extra Questions

1. Fill in the choose function, which returns the number of ways to choose k items from n items. Mathematically, choose (n, k) is defined as:

$$\frac{n \times (n-1) \times (n-2) \times \cdots \times (n-k+1)}{k \times (k-1) \times (k-2) \times \cdots \times 2 \times 1}$$

```
def choose(n, k):
    """Returns the number of ways to choose K items from
    N items.

>>> choose(5, 2)
10
>>> choose(20, 6)
38760
"""
```

```
Solution:
    total = 1
    i = 0
    while i < k:
       total = total * (n - i) // (i + 1)
       i += 1
    return total</pre>
```

2 Higher Order Functions

A function that manipulates other functions is called a **higher order function** (HOF), which is a function that takes functions as arguments, returns a function, or both.

2.1 Functions as Argument Values

Suppose we want to square or double every integer from 1 to n and print the result as we go. Fill in the functions square_ints and double_ints by using the square and double functions we have defined.

```
def square(x):
    return x * x

def square_ints(n):
    """Print out the square of every integer from 1 to n.
    >>> square_ints(3)
    1
    4
    9
    """
```

```
Solution:
    i = 1
    while i <= n:
        print(square(i))
        i += 1</pre>
```

```
def double(x):
    return 2 * x

def double_ints(n):
    """Print out the double of every integer from 1 to n.
    >>> double_ints(3)
    2
    4
    6
    """
```

```
i = 1
while i <= n:
    print(double(i))
    i += 1</pre>
```

The only difference between square_ints and double_ints is the function called before printing (either square or double).

It would be nice to have a generalized function, transform_ints, that took care of the while loop and the incrementing for us. That way, we could triple_ints or cube_ints without repeating so much code:

```
def square_ints(n):
    transform_ints(square, n)

def double_ints(n):
    transform_ints(double, n)

def cube(x):
    return x * x * x

def cube_ints(n):
    transform_ints(cube, n)
```

2.2 Questions

1. Implement the function transform_ints that takes in a function func and a number n and prints the result of applying that function to each of the first n natural numbers.

```
def transform_ints(func, n):
    """Print out all integers from 1 to n with func applied
    on them.

>>> def square(x):
    ... return x * x
>>> transform_ints(square, 3)
1
4
9
"""
```

```
Solution:
    i = 1
    while i <= n:
        print(func(i))
        i += 1</pre>
```

2.3 Functions as Return Values

Often, we will need to write a function that returns another function. One way to do this is to define a function inside of a function:

```
def outer(x):
    def inner(y):
        ...
    return inner
```

Note two things:

- 1. The return value of the outer function is inner. This is where a function returns a function.
- 2. In this case, the inner function is defined inside of the outer function. This is a common pattern, but it is not necessary; we could have defined inner outside of the outer and still use the same return statement.

2.4 Questions

1. Write a function and add that takes a function f (such that f is a function of one argument) and a number n as arguments. It should return a function that takes one argument, and does the same thing as the function f, except also adds n to the result.

```
def and_add(f, n):
    """Return a new function. This new function takes an
    argument x and returns f(x) + n.

>>> def square(x):
    ... return x * x

>>> new_square = and_add(square, 3)

>>> new_square(4) # 4 * 4 + 3

19
"""
```

```
Solution:

def g(x):
    return f(x) + n
return g
```

2. Draw the environment diagram that results from running the following code:

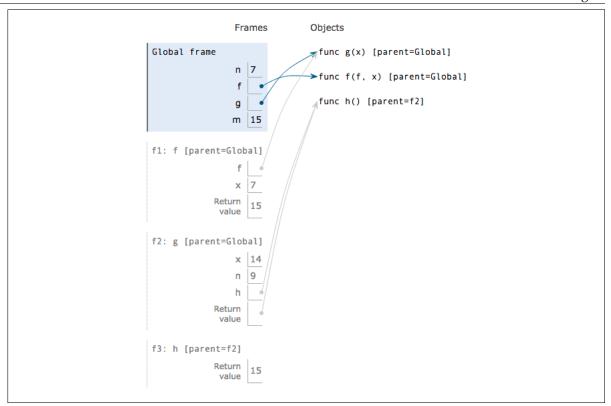
```
n = 7

def f(x):
    n = 8
    return x + 1

def g(x):
    n = 9
    def h():
        return x + 1
    return h

def f(f, x):
    return f(x + n)()

m = f(g, n)
```



2.5 Extra Questions

1. Implement a function keep_ints, which takes in a function cond and a number n, and only prints a number from 1 to n if calling cond on that number returns True:

```
def keep_ints(cond, n):
    """Print out all integers 1..i..n where cond(i) is true

>>> def is_even(x):
    ...  # Even numbers have remainder 0 when divided by 2.
    ...  return x % 2 == 0
>>> keep_ints(is_even, 5)
2
4
"""
```

```
Solution:
    i = 1
    while i <= n:</pre>
```

```
if cond(i):
    print(i)
i += 1
```

2. The following code has been loaded into the Python interpreter:

```
def skipped(f):
    def g():
        return f
    return q
def composed(f, g):
    def h(x):
        return f(g(x))
    return h
def added(f, q):
    def h(x):
        return f(x) + g(x)
    return h
def square(x):
    return x*x
def two(x):
    return 2
```

What will Python output when the following lines are evaluated?

>>> composed(square, two)(7)

```
Solution:
4
```

>>> skipped(added(square, two))()(3)

```
Solution:
11
```

>>> composed(two, square)(2)

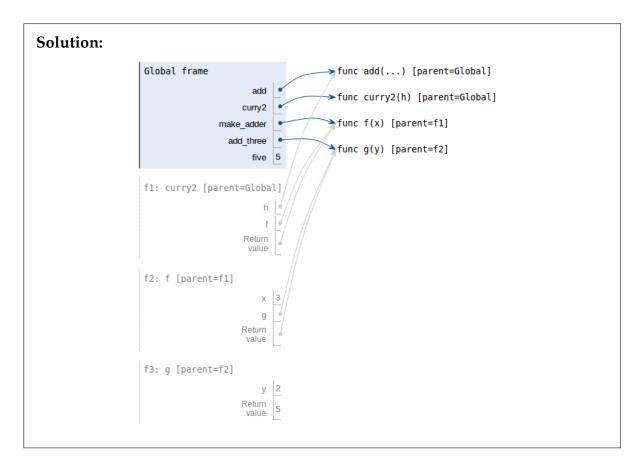
Solution:

2

3. Draw the environment diagram for the following code:

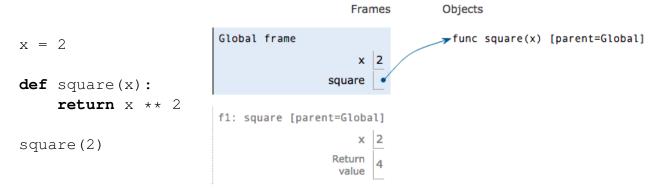
```
from operator import add
def curry2(h):
    def f(x):
    def g(y):
        return h(x, y)
    return f

make_adder = curry2(add)
add_three = make_adder(3)
five = add_three(2)
```



3 Addendum: Environment Diagrams

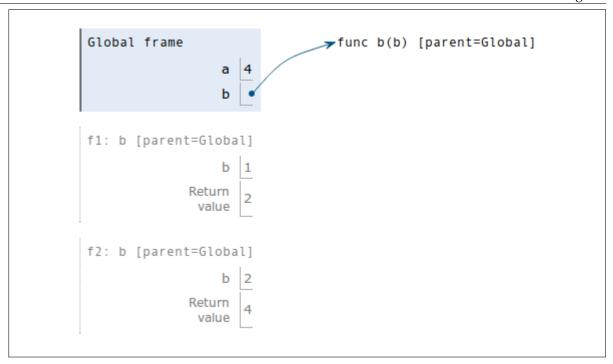
An **environment diagram** helps visualize the Python environment when a program is executed. The environment consists of a stack of frames, which contain variables and the values bound to them.



3.1 Questions

1. Draw the environment diagram that results from running the following code.

```
a = 1
def b(b):
    return a + b
a = b(a)
a = b(a)
```

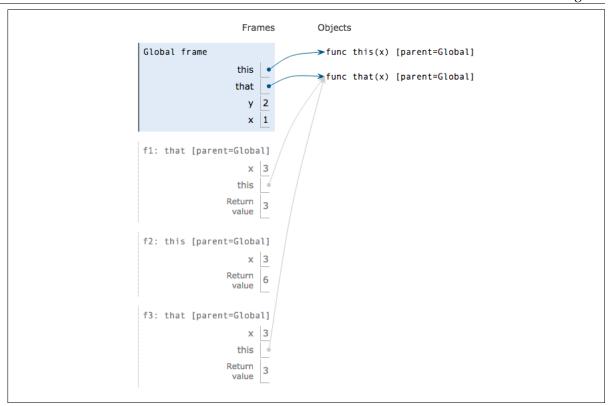


2. Draw the environment diagram that results from executing the code below.

```
def this(x):
    return 2*that(x)

def that(x):
    x = y + 1
    this = that
    return x

x, y = 1, 2
this(that(y))
```



3.2 Extra Questions

1. Draw the environment diagram that results from executing the code below.

```
from operator import add, mul
six = 2

def ty(one, a):
    spring = one(a, six)
    return spring

def fif(teen):
    return teen ** 2

six = ty(add, mul(six, six))
spring = fif(six)
```

