

# Multiple Linear Regression Analysis Report

## 1. Introduction

Multiple Linear Regression is a statistical method used to predict the value of a **dependent variable (target)** based on two or more **independent variables (predictors)**. This report explains the steps taken to build and evaluate the model, compares different regression techniques, and provides recommendations for best performance.

## 2. Methodology

### 2.1 Model Equation

The model follows the equation:

$$Y = b_0 + b_1X_1 + b_2X_2 + \dots + b_nX_n$$

- **Y** = Target variable (what we want to predict).
- **X<sub>1</sub>, X<sub>2</sub>, ..., X<sub>n</sub>** = Predictor variables (features).
- **b<sub>0</sub>** = Intercept (starting value when all predictors are zero).
- **b<sub>1</sub>, b<sub>2</sub>, ..., b<sub>n</sub>** = Coefficients (how much each predictor affects the target).

### 2.2 Steps Taken

#### Step 1: Data Preprocessing

- **Missing Values Check:** Ensured no empty data points.
- **Exploratory Data Analysis (EDA):** Studied how features relate to each other.
- **Categorical Encoding:** Converted text categories into numbers (if needed).
- **Train-Test Split:** Divided data into:
  - **70% Training set** (to train the model).
  - **30% Testing set** (to evaluate performance).

#### Step 2: Model Training

- Used **LinearRegression()** from sklearn.
- Checked **coefficients** to see which features matter most.

#### Step 3: Performance Evaluation

Measured using:

- **R<sup>2</sup> Score (0-1):** How well the model explains the data (closer to 1 = better).
- **Mean Absolute Error (MAE):** Average prediction error.
- **Mean Squared Error (MSE):** Larger errors penalized more.

3. Model Comparison & Results

Model Type	Key Settings	R <sup>2</sup> Score	Notes
Standard Linear Regression	fit_intercept=True	0.9358	Works well when intercept is included.
	fit_intercept=False	0.7389	Much worse without intercept.
	normalize=True	-19,155,898,675	Normalization breaks the model.
	n_jobs=-1 (parallel)	-21,724,334,601	Using multiple CPUs gives bad results.
Ridge Regression (L2)	alpha=1.0	0.9357 ≈ Same	Helps prevent overfitting.
	solver='saga'	0.9353 ≈ Same	Slightly lower but stable.
Lasso Regression (L1)	max_iter=1000	0.9357 ≈ Same	Good for feature selection.
Elastic Net (L1 + L2)	l1_ratio=0.5	0.9355 ≈ Same	Balanced regularization.
Feature Scaled Regression	with_mean=True, with_std=True	0.9355 ≈ Same	Scaling doesn't help much here.

Key Findings:

- Standard Linear Regression works best when fit\_intercept=True (R<sup>2</sup> = 0.9358).
- Normalization & n\_jobs cause huge errors—avoid them.
- Ridge, Lasso, and Elastic Net perform almost the same as standard regression.
- Feature Scaling doesn't improve results in this case.

4. Recommendations

Best Model Choice:

Standard Linear Regression (with fit\_intercept=True)

- Simple and performs best.
- Avoid normalize and n\_jobs—they ruin performance.

Alternative Models (If Needed):

Ridge or Lasso Regression

- Almost as good as standard regression.

- Helps prevent overfitting.

### Elastic Net Regression

- Good if you want both L1 & L2 regularization.

### General Tips:

✓ **Always check if intercept is needed** (fit\_intercept=True is usually better).

✓ **Avoid normalization** unless necessary (it caused extreme errors here).

✓ **Feature scaling is good practice**, but it didn't help much in this case.

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## 5. Conclusion

The best model is **Standard Linear Regression** with fit\_intercept=True. Other models (Ridge, Lasso, Elastic Net) are also good but don't improve results significantly. Avoid normalization and multi-CPU settings (n\_jobs) as they cause errors. Feature scaling is safe but not necessary here.

For future work:

- Try more datasets to confirm findings.
- Test other advanced models if needed.

**Final Decision:** Use **Standard Linear Regression** for best performance.