

Q1)

node 0

Home tree = $\{0\}$

$d(0) = 0$

Guest nodes = $\{1, 2, 3, 4, 5, 6, 7, 8\}$, $d(\cdot) = \infty$

Distance to node 1 is 6

Distance to node 2 is 2

Update distance label: $d(1) = 6$, $d(2) = 2$

Find the closest guest node 2, because $d(2) = 2 < d(1) = 6$

Add node 2 and link $(0 \rightarrow 2)$ into home tree

node 2

Home tree = $\{0, 2\}$ $d(\cdot) = \infty$

Guest nodes = $\{1, 3, 4, 7, 5, 6, 8\}$

Determine the distance to guest nodes connected to node 2:

Distance to node 3 = $2 + 8 = 10$

Distance to node 4 = $2 + 10 = 12$

Distance to node 7 = $2 + 20 = 22$

Updated $d(3) = 10$, $d(4) = 12$, $d(7) = 22$

node 1 Home tree = $\{0, 1\}$, $d(0) = 0$, $d(1) = 6$

Guest nodes = $\{2, 3, 4, 7, 5, 6, 8\}$ $d(\cdot) = \infty$

Distance 1-2 = $5 + 6 = 11$

Distance 1-3 = $2 + 6 = 8$

Updated $d(2) = 2$, $d(3) = 8$

node 3

Home tree: $\{0, 1, 2, 3\}$, $d(0)=0$ $d(1)=6$ $d(2)=2$ $d(3)=8$

Guest nodes: $\{4, 5, 6, 7, 8\}$ $d(\cdot)=\infty$

Distance: $3-4 = 3+8 = 11$

Distance $3-5 = 8+7 = 15$

Updated $d(4)=11$ $d(5)=15$

node 4

Home tree: $\{0, 1, 2, 3, 4\}$, $d(0)=0$ $d(1)=6$ $d(2)=2$ $d(3)=8$ $d(4)=11$

Guest nodes: $\{5, 6, 7, 8\}$ $d(\cdot)=\infty$

Distance: $4-5 = 11+2 = 13$

Distance: $4-7 = 11+6 = 17$

Updated $d(5)=13$, $d(7)=17$

node 7

Home tree: $\{0, 1, 2, 3, 4, 7\}$, $d(0)=0$ $d(1)=6$ $d(2)=2$ $d(3)=8$ $d(4)=11$ $d(7)=17$

Guest nodes: $\{5, 6, 8\}$ $d(\cdot)=\infty$

Distance $7-8 = 17+3 = 20$

Updated $d(8)=20$

Node 5

Home tree: $\{0, 1, 2, 3, 4, 5\}$, $d(0)=0$, $d(1)=6$ $d(2)=2$ $d(3)=8$ $d(4)=11$ $d(5)=13$

Guest nodes: $\{6, 7, 8\}$, $d(\cdot)=\infty$

Distance $5-7 = 13+7 = 20$

Distance $5-6 = 13+5 = 18$

Updated $d(7)=17$, $d(6)=18$

Node 6

Home tree: $\{0, 1, 2, 3, 4, 5, 6, 7\}$, $d(0)=0$, $d(1)=6$, $d(2)=2$, $d(3)=8$, $d(4)=11$ $d(5)=13$

Guest nodes: $\{8\}$

$d(6)=18$ $d(7)=17$

Distance $6-8 = 18+4 = 22$

Updated

$d(8)=20$

Home tree = $\{0, 1, 2, 3, 4, 5, 6, 7, 8\}$

Guest nodes = $\{ \}$

The shortest path:

0-1-3-4-7-8