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INSTITUTE OF TECHNOLOGY
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DEPARTMENT OF COMPUTER ENGINEERING

Subject : Competitive Programming Lab

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Expt. No. :13

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Title : Priest Mathematician Problem

Remark

Signature

Language: C++

// Priest Mathematician Problem by Meraj 32 T2

#include <iostream>

#include <vector>

#include <string>

#include <algorithm>

using namespace std;

// Add two non-negative decimal integers (as strings), both passed by value

string addStr(string a, string b) {

int i = a.size() - 1, j = b.size() - 1, carry = 0;

string res;

while (i >= 0 || j >= 0 || carry) {

int sum = carry;

if (i >= 0) { sum += (a[i] - '0'); --i; }

if (j >= 0) { sum += (b[j] - '0'); --j; }

carry = sum / 10;

res.push_back(char('0' + (sum % 10)));

}

reverse(res.begin(), res.end());

// strip leading zeros

size_t p = res.find_first_not_of('0');

return (p == string::npos ? "0" : res.substr(p));

}

// Subtract exactly 1 from a positive decimal string

```
string decOne(string s) {  
    int i = s.size() - 1;  
    while (i >= 0) {  
        if (s[i] > '0') {  
            s[i] = char(s[i] - 1);  
            break;  
        }  
        s[i] = '9';  
        --i;  
    }  
    size_t p = s.find_first_not_of('0');  
    return (p == string::npos ? "0" : s.substr(p));  
}
```

// Return true if a < b, both non-negative decimal strings

```
bool lessStr(string a, string b) {  
    if (a.size() != b.size())  
        return a.size() < b.size();  
    return a < b;  
}
```

// Solve for one N using DP + Frame–Stewart

```
string solveOne(int N) {  
    if (N <= 1) return (N == 0 ? "0" : "1");  
  
    // build powers of two up to N  
    vector<string> pow2(N+1);  
    pow2[0] = "1";  
    for (int i = 1; i <= N; ++i) {  
        pow2[i] = addStr(pow2[i-1], pow2[i-1]);  
    }  
}
```

// dp[i] = best moves for i disks on 4 pegs

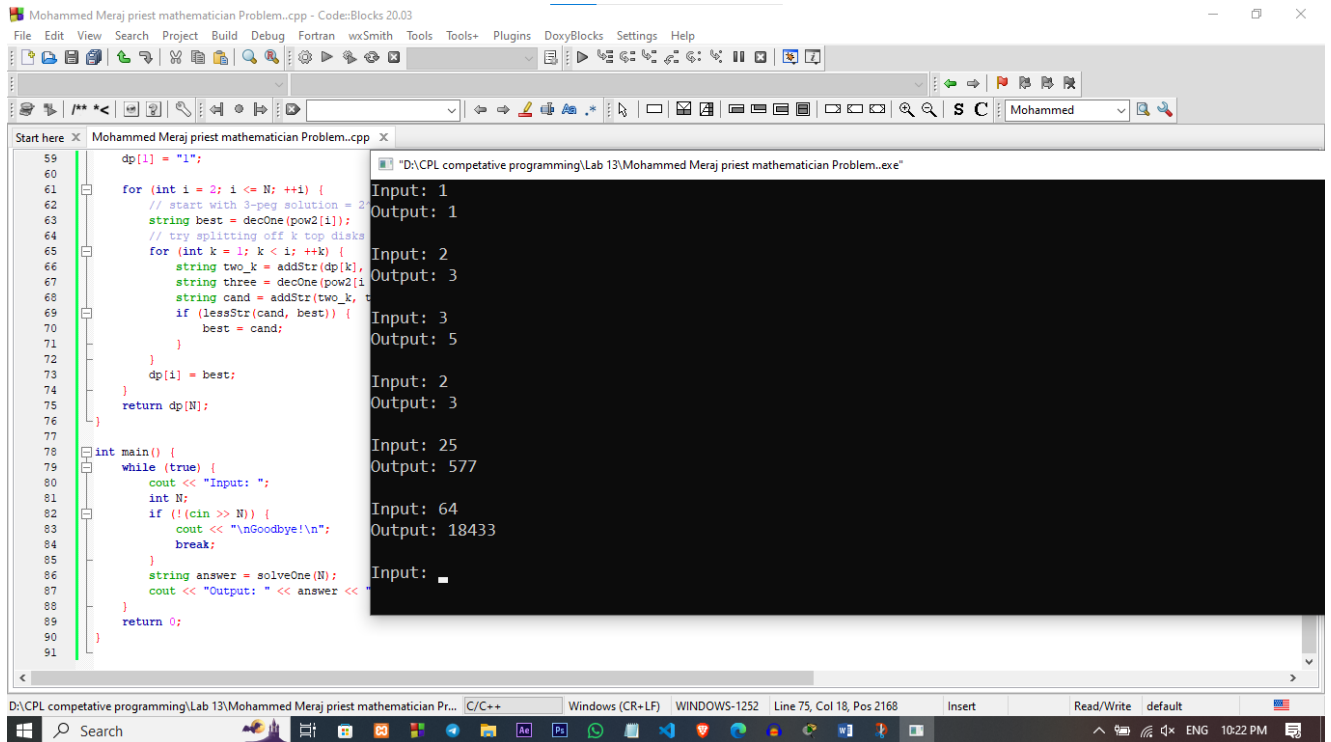
```
vector<string> dp(N+1, "0");  
dp[1] = "1";
```

```
for (int i = 2; i <= N; ++i) {  
    // start with 3-peg solution =  $2^i - 1$   
    string best = decOne(pow2[i]);  
    // try splitting off k top disks  
    for (int k = 1; k < i; ++k) {
```

```
        string two_k = addStr(dp[k], dp[k]);
        string three = decOne(pow2[i - k]);
        string cand = addStr(two_k, three);
        if (lessStr(cand, best)) {
            best = cand;
        }
    }
    dp[i] = best;
}
return dp[N];
}

int main() {
    while (true) {
        cout << "Input: ";
        int N;
        if (!(cin >> N)) {
            cout << "\nGoodbye!\n";
            break;
        }
        string answer = solveOne(N);
        cout << "Output: " << answer << "\n\n";
    }
    return 0;
}
```

Output :



```
59 dp[1] = "1";
60
61 for (int i = 2; i <= N; ++i) {
62     // start with 3-peg solution = 2
63     string best = decOne(pow2[i]);
64     // try splitting off k top disks
65     for (int k = 1; k < i; ++k) {
66         string two_k = addStr(dp[k],
67         string three = decOne(pow2[i-k]);
68         string cand = addStr(two_k, three);
69         if (lessStr(cand, best)) {
70             best = cand;
71         }
72     }
73     dp[i] = best;
74 }
75 return dp[N];
76 }
77
78 int main() {
79     while (true) {
80         cout << "Input: ";
81         int N;
82         if (!(cin >> N)) {
83             cout << "\nGoodbye!\n";
84             break;
85         }
86         string answer = solveOne(N);
87         cout << "Output: " << answer << "\n";
88     }
89     return 0;
90 }
91 }
```

Input: 1
Output: 1

Input: 2
Output: 3

Input: 3
Output: 5

Input: 2
Output: 3

Input: 25
Output: 577

Input: 64
Output: 18433

Input: