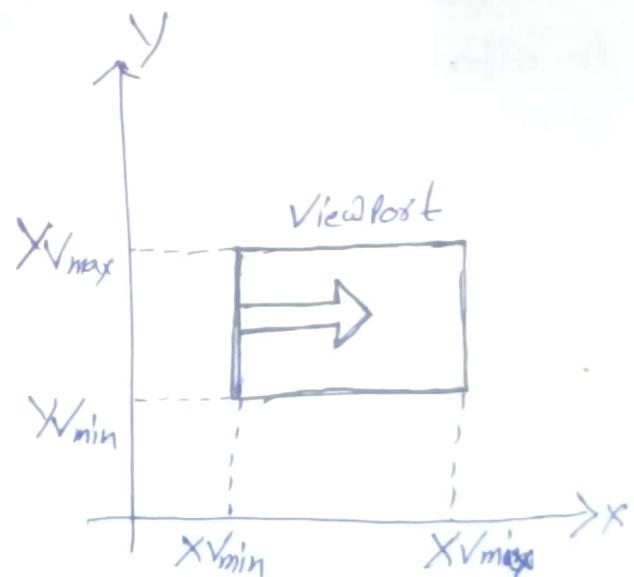
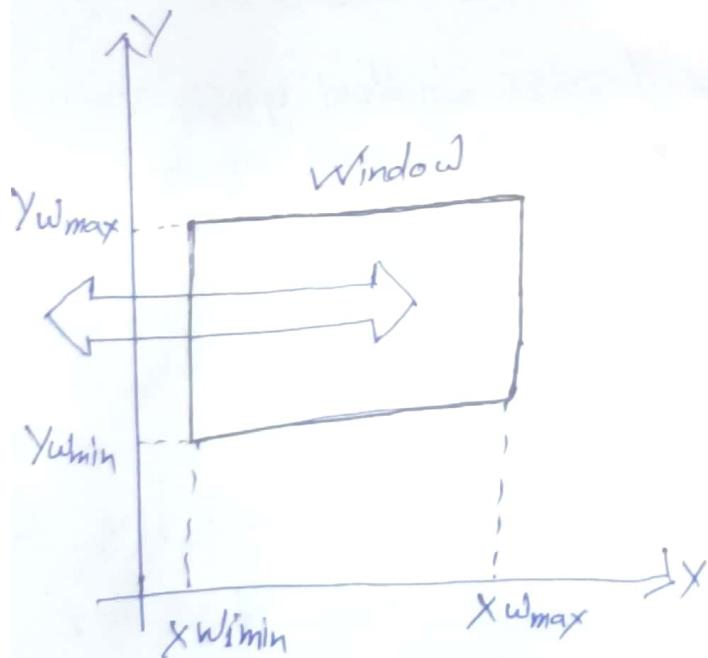


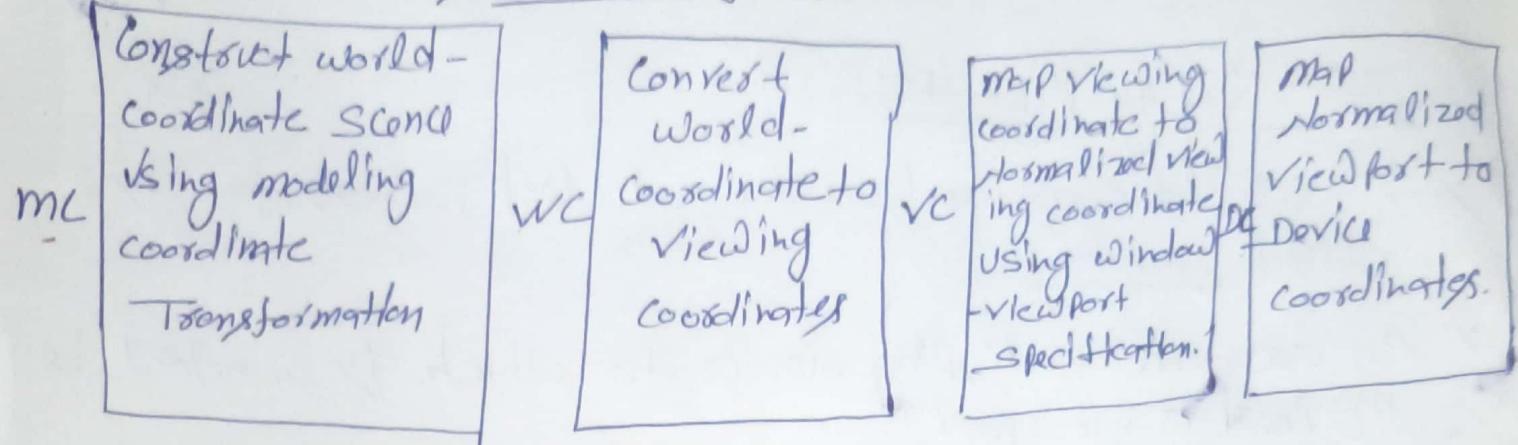
⇒ The viewing pipeline:-

- * The world coordinate area selected for display is called window.
- * An area on a display device to which is window is mapped a viewport.
- * Windows and viewports are rectangular in standard position.
- * In general finding device coordinates of viewport from world coordinate of window is called as viewing transformation.
- * A viewing transformation using standard rectangles for the window and viewport.



→ Now we see steps involved in viewing pipeline.

→ 2 D - Viewing Pipeline

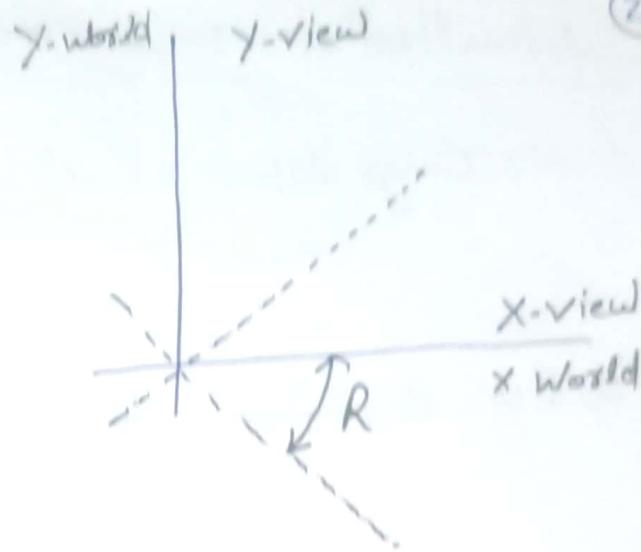
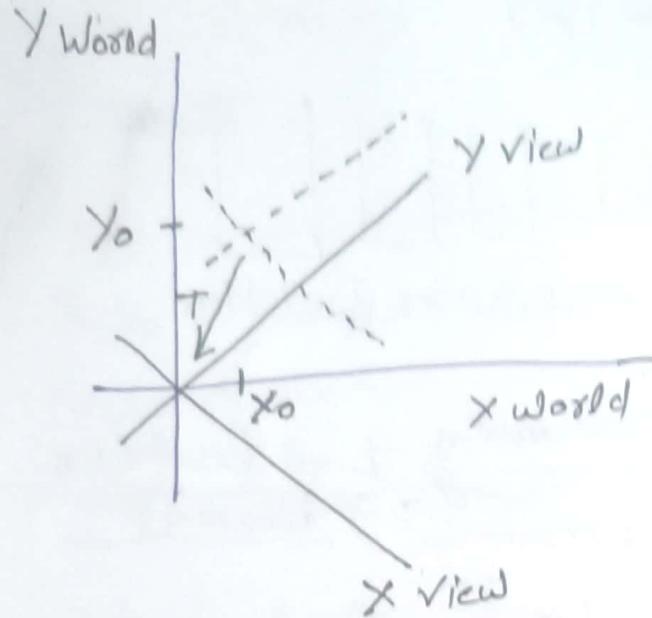


- Finally device-coordinate is used to display image on display screen.
- By changing the viewport position on screen we can see image at different place on the screen.
- By changing the size of the Window and Viewport we can obtain zoom in and zoom out effect as per requirement.
- Fixed size viewport and small size window gives zoom in effect, and fixed size viewport and larger window gives zoom out effect.
- ⇒ Viewing coordinate Reference Frame -
set-up the viewing coordinate.

- 1) origin is selected at some world position $P_0 = (x_0, y_0)$
- 2) Establish the orientation, specify a world vector ✓ that defines the viewing Y direction
- 3) obtain the matrix for converting world to viewing coordinates

$$M_{w \rightarrow vc} = R T$$

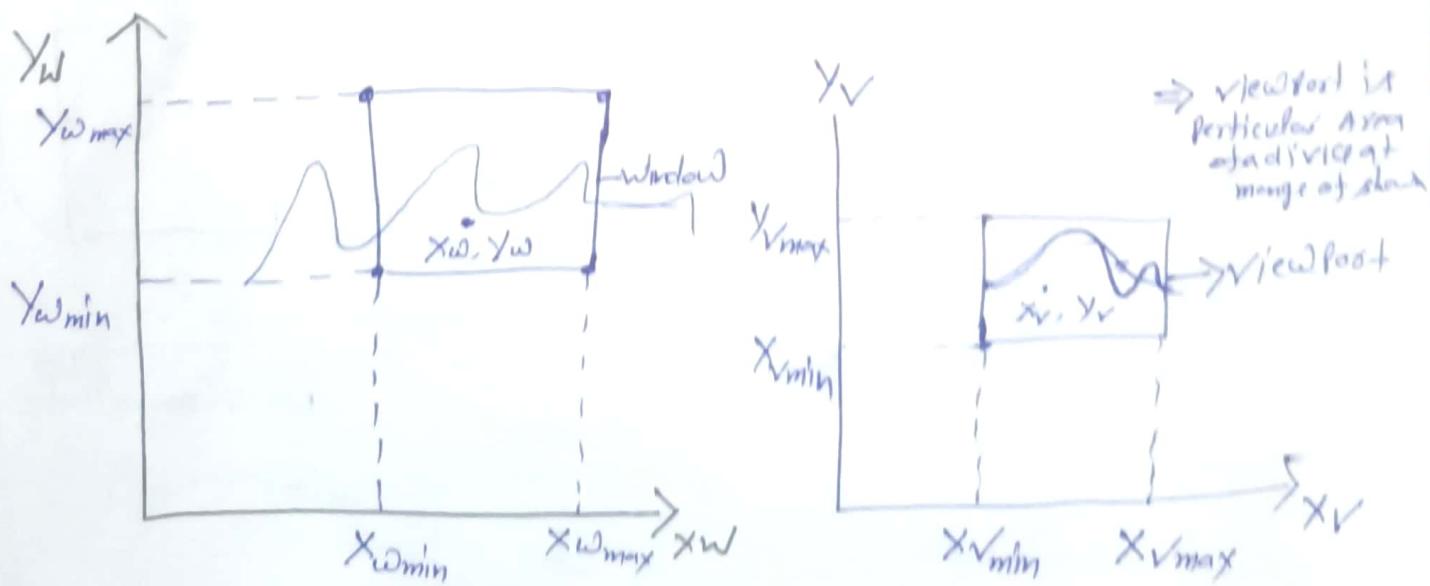
$T = \text{Translate}$, $R = \text{rotate}$



\Rightarrow Window to Viewport coordinate Transformation:-

* Select the viewport in normalized coordinate, and then object description transferred to normalized device coordinate

- 1) \Rightarrow Used to process
normalization $\xrightarrow{\text{Transformation}}$
- 2) Work station Transformation



3

$$\left. \begin{array}{l} x = x_n * x_w \\ y = y_n * y_w \end{array} \right\} \frac{0-1}{\text{Scaling}}$$

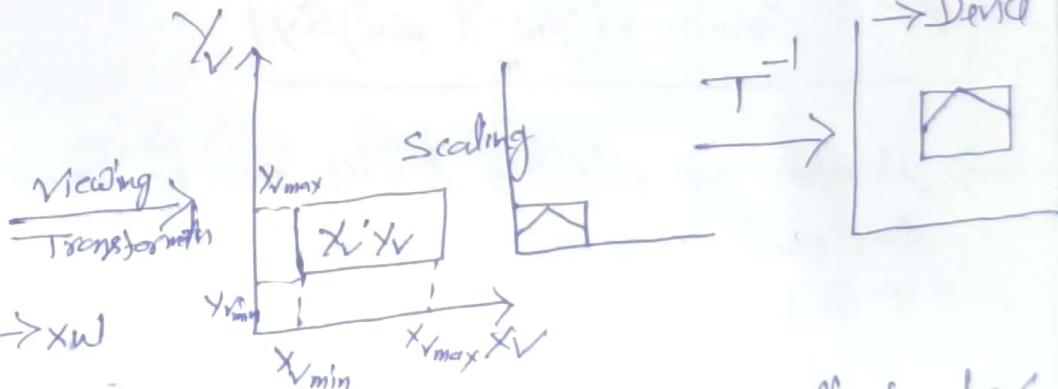
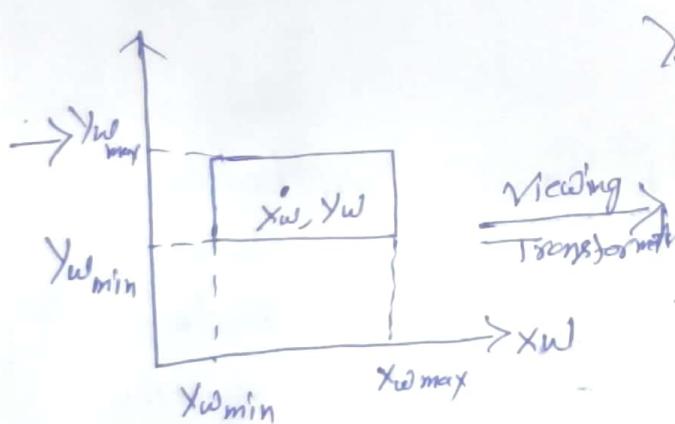
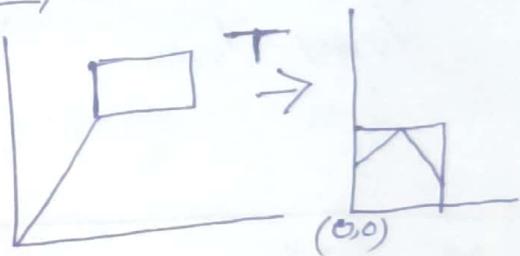
$x, y \rightarrow$ Actual device coordinate
 $x_n, y_n \rightarrow$ normalized coordinate \rightarrow scaling
 $x_w, y_w \rightarrow$ window coordinate

\rightarrow workstation transformation.

World $\xrightarrow{\text{normalize}}$ normalized coordinate $\xrightarrow{\text{workstation}}$ Device coordinate
 \rightarrow window

$$\Rightarrow V = W \cdot W^{-1}$$

$$W = T \cdot S \cdot T^{-1}$$



$$\rightarrow \frac{x_v - x_{v\min}}{x_{v\max} - x_{v\min}} = \frac{x_w - x_{w\min}}{x_{w\max} - x_{w\min}}$$

$$\rightarrow x_v - x_{v\min} = \left(\frac{x_w - x_{w\min}}{x_{w\max} - x_{w\min}} \right) * x_{v\max} - x_{v\min}$$

Scaling factor

$$S_x = \frac{x_{v\max} - x_{v\min}}{x_{w\max} - x_{w\min}}$$

$$S_y = \frac{y_{v\max} - y_{v\min}}{y_{w\max} - y_{w\min}}$$



$$X_V - X_{V\min} = \left(\frac{X_{V\max} - X_{V\min}}{X_{W\max} - X_{W\min}} \right) * X_W - X_{W\min}$$

$$X_V = S_X \cdot (X_W - X_{W\min}) + X_{V\min}$$

$$X_V = X_{V\min} + (X_W - X_{W\min}) S_X$$

\rightarrow Now

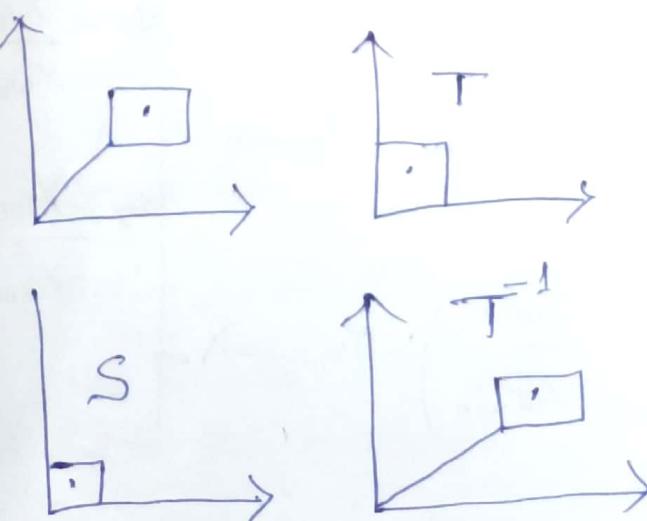
$$\frac{Y_V - Y_{V\min}}{Y_{V\max} - Y_{V\min}} = \frac{Y_W - Y_{W\min}}{Y_{W\max} - Y_{W\min}}$$

⋮

$$Y_V = Y_{V\min} + (Y_W - Y_{W\min}) S_Y$$

\rightarrow Number of display device can be used in application and for each we can use different window-to-viewport transformation. This mapping is called the workstation transformation.

$$W = T \cdot S \cdot T^{-1}$$



matrix representation

$$T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ \frac{X_{W\max} - X_{W\min}}{X_{V\max} - X_{V\min}} & 1 \end{bmatrix}$$

$$S = \begin{bmatrix} S_X & 0 & 0 \\ 0 & S_Y & 0 \\ 0 & 0 & 1 \end{bmatrix} \Rightarrow$$

$$T^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ \frac{X_{W\min} - X_{W\max}}{X_{V\max} - X_{V\min}} & 1 \end{bmatrix}$$



GLUT Display window:

$$T \cdot S \cdot T^{-1} = \begin{bmatrix} Sx & 0 & 0 & 0 \\ 0 & Sx & Sy & 0 \\ X_{w_{\min}} - X_{w_{\max}} \cdot Sx & Y_{w_{\min}} - Y_{w_{\max}} \cdot Sy & 1 \end{bmatrix}$$

$$\begin{bmatrix} A' \\ B' \\ C' \end{bmatrix} = \begin{bmatrix} A \\ B \\ C \end{bmatrix} \begin{bmatrix} \text{Transformation} \end{bmatrix}$$

\Rightarrow Viewing function:

\rightarrow OpenGL Two-Dimensional viewing functions.

* We must set the parameters for the clipping window as part of the projection transformation.

* Functions:

`glMatrixMode(GL_Projection);`

* We can also set the initialization as

`glLoadIdentity();`

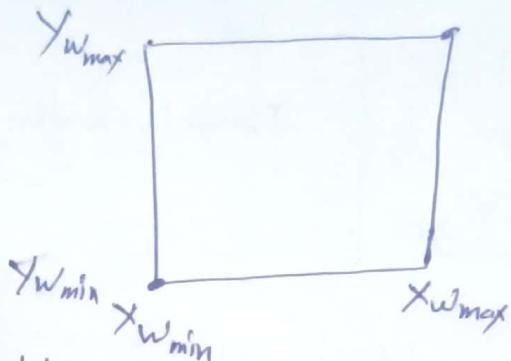
\rightarrow This ensures that each time we enter the projection mode, the matrix will be reset to the identity matrix so that the new viewing parameters are not combined with the previous ones.

\rightarrow GLU Clipping-Window Functions.

* To define a two-dimensional clipping window, we can use the GLU function:

`gluOrtho2D(X_{w_{\min}}, X_{w_{\max}}, Y_{w_{\min}}, Y_{w_{\max}});`

* This function specifies an orthogonal projection for mapping the scene to the screen. The orthogonal projection has no effect on our two-dimensional scene other than to convert object positions to normalized coordinates.



→ OpenGL Viewport function:-

`glViewport(x_{vmin}, y_{vmin}, vpWidth, vpHeight);`

Where -

→ x_{vmin} and y_{vmin} specify the position of the lower-left corner of the viewport relative to the lower-left corner of the display window.

→ $vpWidth$ and $vpHeight$ are pixel width and height of the viewport

→ coordinates for the upper-right corner of the viewport are calculated for this transformation matrix in terms of the viewport width & height.

$$x_{vmax} = x_{vmin} + vpWidth, \quad y_{vmax} = y_{vmin} + vpHeight$$

→ `glGetIntegerv(GL_VIEWPORT, vpArray)`

→ $vpArray$ is a single-subscript, four-element array

→ Relocating and Resizing a GLUT Display window → (6)

* glutPositionWindow(x New Top Left, y New Top Left)

* glutReshapeWindow(dw New Width, dw New Height);

* glutFullScreen();

* glutReshapeFunc(winReshapeFun);

→ Managing multiple GLUT Display windows

* glutIconifyWindow();

* glutSetIconTitle("Icon Name");

* glutSetWindowTitle("New Window Name");

* glutSetWindow(window ID);

* glutPopWindow();

* glutSetWindow(window ID);

* glutPushWindow();

* glutHideWindow();

* glutShowWindow();



→ GLUT Sub window:-

* glutCreateSubWindow(window ID, xBottomLeft, yBottomLeft, width, height);

→ Selecting a Display - window screen - cursor shape

* glutSetCursor(shape);

Where

→ GLUT_CURSOR_UP_DOWN → up-down arrow

→ GLUT_CURSOR_CYCLE → rotatory arrow chosen

→ GLUT_CURSOR_WAIT → a wristwatch shape.

→ GLUT_CURSOR_DESTROY → a skull and crossbones.

→ Viewing Graphics objects in a GLUT - Display window

* glutDisplayFunc(Picture Descrip);

* glutPostRedisplay();

⇒ Cohen-Sutherland line clipping algorithm:-

→ In this Algorithm, we given a region on the screen out of which one region is of the window and the rest 8 regions are around it given by 4 digit binary. The division of the region are based on

$(X_{max}, Y_{max}) \text{ & } (X_{min}, Y_{min})$

→ The central part is the viewing region or window. all the lines which lie within the region are completely visible.

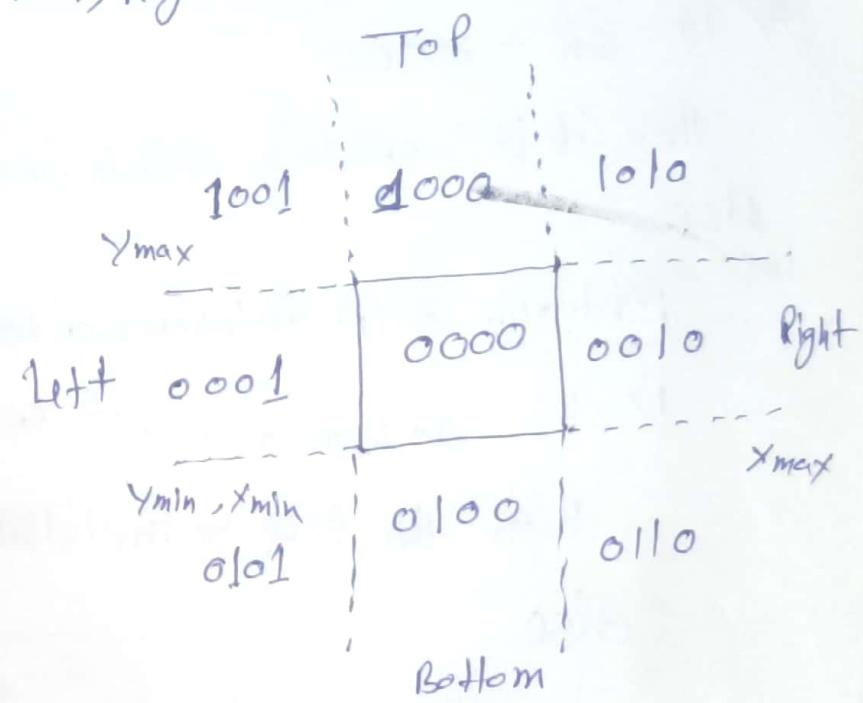
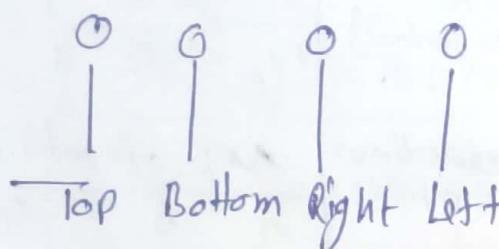
(7)

→ A region code is always assigned to the endpoints of the given line.

→ To check whether the line is visible or not.

⇒ Formula to check binary digits:- T B R L which can be defined as Top, bottom, Right and Left.

Now → TBLR Rule



→ Rule:-

1) Line Inside

All B code is
"0000"

2) outside

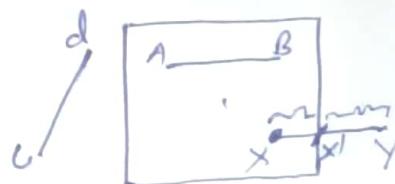
$$c = 0001, d = 0001$$

$$C = \begin{array}{cccc} 0 & 0 & 0 \\ 0 & 0 & 1 \end{array}$$

$$d = \begin{array}{cccc} 0 & 0 & 0 \\ 1 & & \end{array}$$

$$\text{logical AND} = \begin{array}{cccc} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{array}$$

Not
0000



→ Find Intersection point X' .

3) Partially inside the window

$$x = \begin{array}{cccc} 0 & 0 & 0 \\ 0 & 1 & 0 \end{array}$$

$$y = \begin{array}{cccc} 0 & 0 & 1 & 0 \end{array}$$

$$\text{AND} = \begin{array}{cccc} 0 & 0 & 0 & 0 \end{array}$$

→ Algorithms:-

→ Steps:-

- 1) Assign the region codes to both endpoints.
- 2) Perform OR operation on both of those endpoints

- 3) if $OR = 0000$

then it is completely visible (inside the window)
else

Perform AND operation on both ~~of these~~ endpoints

- i) if $AND \neq 0000$

then the line is invisible

else

$$AND = 0000$$

Line is considered to be clipped case
Partially inside the window?

→ Clipping

- 4) After confirming that the line is partially inside the window, then we find intersection with the boundary of the window.

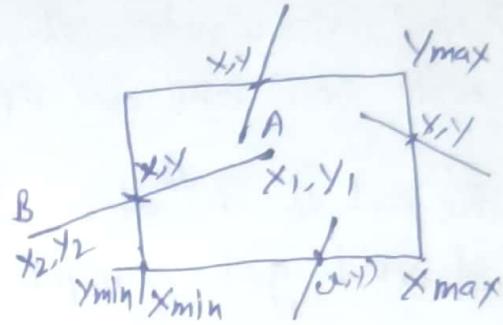
$$\text{Slope } m = \frac{y_2 - y_1}{x_2 - x_1}$$

- a) If the line passes through the left region or the line intersects with the left boundary of the window.

OR operation		
A	B	Q
0	0	0
0	1	1
1	0	1
1	1	1

AND operation		
A	B	Q
0	0	0
0	1	0
1	0	0
1	1	1

(8)



Left: $x = x_{\min}$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{y - y_1}{x - x_1} = \frac{y - y_1}{x_{\min} - x_1}$$

$$y - y_1 = m(x_{\min} - x_1)$$

$$y = y_1 + m(x_{\min} - x_1)$$

b) If the line passes through the Right vertex or the line intersects with the right boundary of the window.

Right: $x = x_{\max}$

$$y = y_1 + m(x_{\max} - x_1)$$

c) If the line passes through top or the line intersects with the top boundary of the window

Top: $y = y_{\max}$

$$m = \frac{y - y_1}{x - x_1} = \frac{y_{\max} - y_1}{x - x_1}$$

$$x = x_1 + (y_{\max} - y_1) / m$$

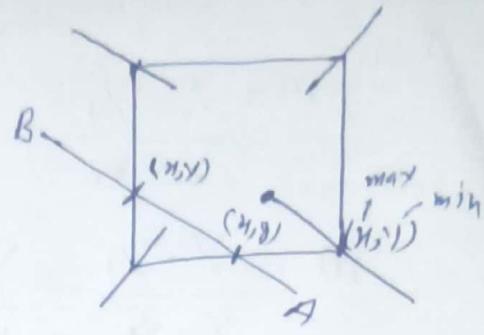
d) If the line passes the bottom or the line intersects with the bottom boundary

Bottom: $y = y_{\min}$

$$x = x_1 + (y_{\min} - y_1) / m$$

5) Now, overwrite the end points with new one and update it.

6) Repeat the 4th step till your line doesn't get completely clipped.

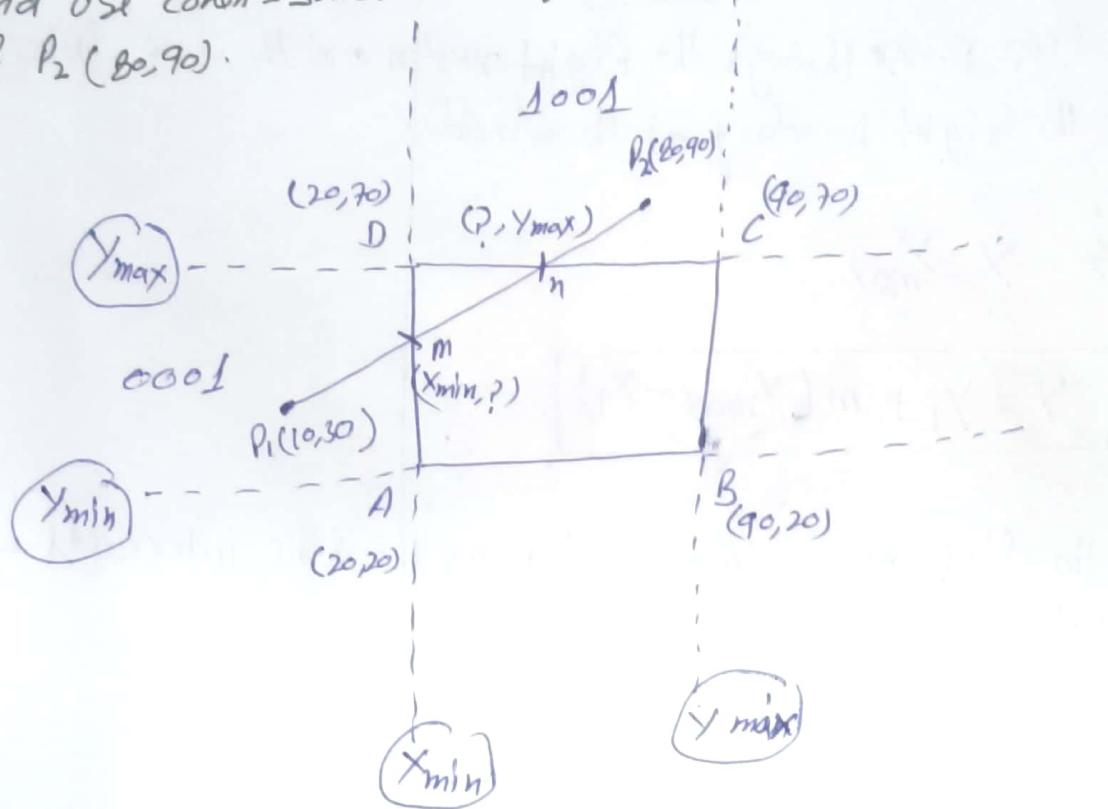


⑨

rsath

Ex: Let ABCD be the rectangular window with A(20,20), B(90,20), C(90,70), and D(20,70). Find region codes for the end points and use Cohen-Sutherland Algo. to clip the line P₁(10,30) & P₂(80,90).

→



→ Finding region code:

$$\textcircled{1} \quad P_1 = 0001 \\ P_2 = 1001$$

AND = 0000 → Line is partially visible (clipping)

$$P_1(10,30) \rightarrow x_1, y_1$$

$$P_2(80,90) \rightarrow x_2, y_2$$

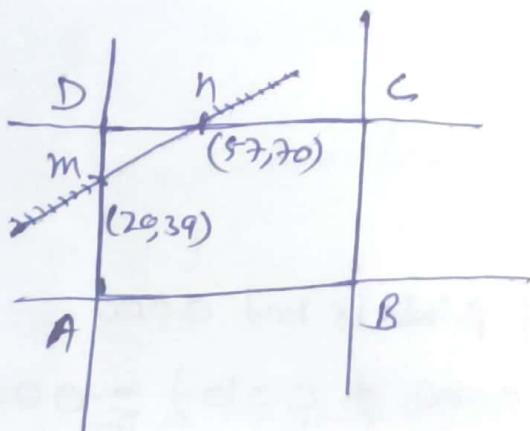
slity
with
corner

$$\textcircled{2} \quad \text{Slope } m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{90 - 30}{80 - 10} = \frac{6}{7} = \underline{\underline{0.857}}$$

→ For Point of intersection m :

$$\begin{aligned} Y &= m(X_{min} - X_1) + Y_1 \\ &= 0.857(20 - 10) + 30 \\ &= 8.57 + 30 \\ &= 38.57 \\ &= 39 \end{aligned}$$

$m(20, 39)$



$$X_{min} = 20$$

$$Y_{max} = 70$$

→ For Point n : - (Intersection)

$$n = \frac{1}{m}(Y_{max} - Y_1) + X_1$$

$$x = \frac{1}{m}(70 - 30) + 10$$

$$= \frac{1}{0.857}(40) + 10$$

$$= 56.67$$

$$x \approx 57$$

$n(57, 70)$

====

~~Desired intersection algorithm~~

→ Formula to calculate the bit code:

* Bit 1 = sign of $(Y - Y_L)$

* sign = 1 → +ve

* Bit 2 = sign of $(Y_R - Y)$

* sign = 0 → -ve

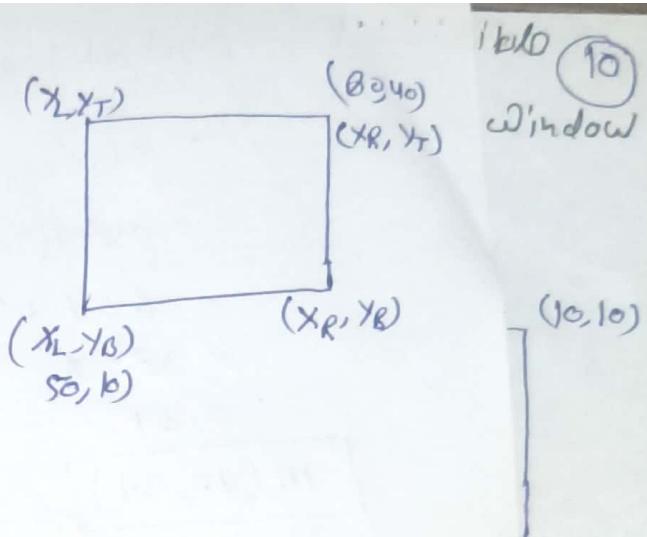
* Bit 3 = sign of $(X - X_R)$

* Bit 4 = sign of $(X_L - X)$

→ Use the Cohen Sutherland algorithm to determine the visibility of a line $P_1 P_2$ $P_1(70, 20)$, $P_2(100, 10)$ against a window with lower left hand corner at $(50, 10)$ and upper right hand corner at $(89, 70)$.



→ Outcode for P_1 : $\rightarrow P_1(70, 20)$
 Bit₁ = $S(20 - 40) = -20 = 0$
 Bit₂ = $S(10 - 20) = -10 = 0$
 Bit₃ = $S(70 - 80) = -10 = 0$
 Bit₄ = $S(50 - 70) = -20 = 0$
 (0000)
 → Outcode for P_2 : $\rightarrow P_2(100, 10)$
 Bit₁ = $S(10 - 40) = -30 = 0$
 Bit₂ = $S(10 - 10) = 0$
 Bit₃ = $S(100 - 80) = 20 \Rightarrow 1$
 Bit₄ = $S(50 - 100) = -50 = 0$
 (0010)

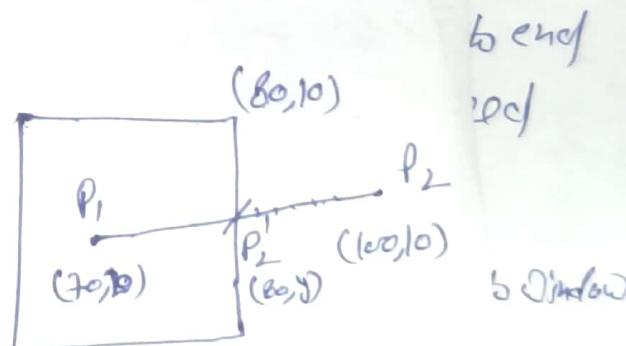


→ As the outcode for both the end point is not 0000
 ∵ the line is partially visible (0000 & 0010) = 0000

→ Now determine the visible portion of this line

→ As the outcode for P_2 is 0010

∴ It is intersecting the right edge of window



→ Determine the intersection point P_{2'}

$$\text{Slope of the line } P_1 P_2 = \frac{10 - 20}{100 - 70} = \frac{-10}{30} = -\frac{1}{3}$$

$$\text{Now } P_2' P_1 \Rightarrow m = \frac{y - 20}{80 - 70} \Rightarrow -\frac{1}{3} = \frac{y - 20}{10}$$

$$\begin{aligned} \Rightarrow 3(y - 20) &= -10 \\ 3y &= 60 - 10 \\ y &= \left(\frac{50}{3}\right) \Rightarrow 16.67 \equiv 17 \end{aligned}$$

→ Outcode for P_1 :

$$\text{Bit}_1 = S(20 - 40) = -20 = 0$$

$$\text{Bit}_2 = S(10 - 20) = -10 = 0$$

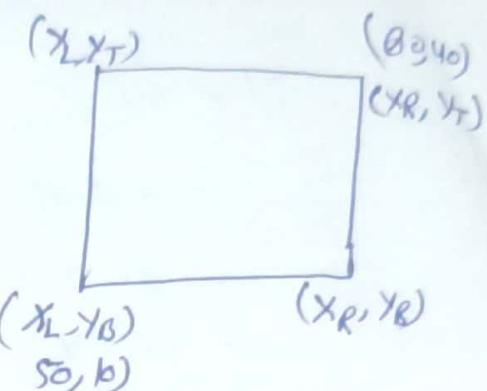
$$\text{Bit}_3 = S(70, -80) = -10 = 0$$

$$\text{Bit}_4 = S(50 - 70) = -10 = 0$$

→ Outcode for P_2 :

(0000)

$P_1(70, 20)$
 x, y



$P_2(100, 10)$
 x, y

$$\text{Bit}_1 = S(10 - 40) = -30 = 0$$

$$\text{Bit}_2 = S(10 - 10) = 0$$

$$\text{Bit}_3 = S(100 - 80) = 20 \Rightarrow 1$$

$$\text{Bit}_4 = S(50 - 100) = -50 = 0$$

(0010)

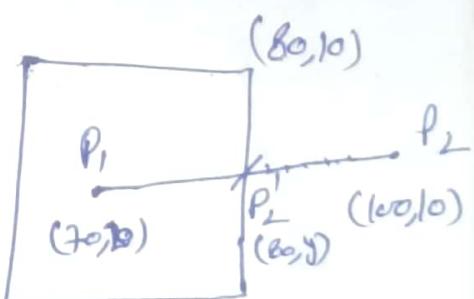
→ As the outcode for both the end point is not 0000

∴ the line is partially visible (0000 & 0010) = 0000

→ How determine the visible portion of this line?

→ As the outcome for P_2 is 0010

∴ It is intersecting the right edge of window



→ Determine the intersection point P_L'

(80, 17)

$$\text{Slope of the line } P_1 P_2 = \frac{10 - 20}{100 - 70} = \frac{-10}{30} = -\frac{1}{3}$$

$$\text{Now } P_2 P_1 \Rightarrow m = \frac{y - 20}{80 - 70} \Rightarrow -\frac{1}{3} = \frac{y - 20}{10}$$

→ $P_1 P_L'$ is the visible portion of line with coordinate (70, 20) & (80, 17)

$$\begin{aligned}
 3(y - 20) &= -10 \\
 3y &= 60 - 10 \\
 y &= \left(\frac{50}{3}\right) \Rightarrow 16.67 \equiv 17
 \end{aligned}$$

Q:- Use the clipping algorithm for calculating the visible portion of the line $P_1(2,7)$, $P_2(8,12)$ against a window where $(X_{min}, Y_{min}) = (5,5)$ & $(X_{max}, Y_{max}) = (10,10)$. 10

$$\rightarrow X_L = 5, X_R = 10, Y_B = 5, Y_T = 10$$

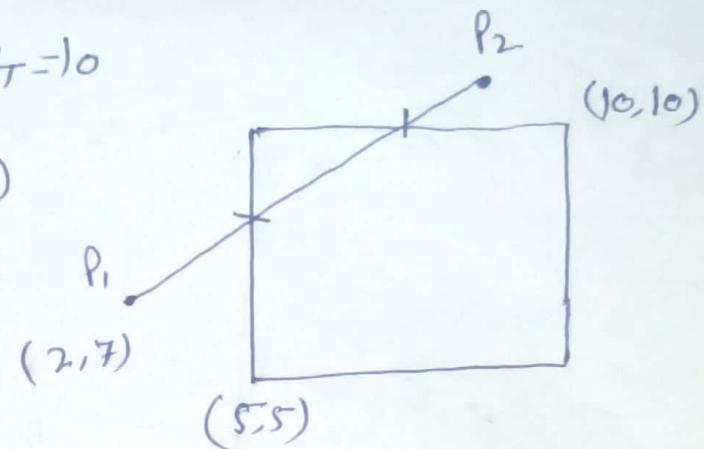
Bit code $P_1(2,7)$ Bit code $P_2(8,12)$

$$B_1 = 7 - 10 = 0 \quad B_1 = 12 - 10 = 1$$

$$B_2 = 5 - 7 = 0 \quad B_2 = 5 - 12 = 0$$

$$B_3 = 2 - 10 = 0 \quad B_3 = 8 - 10 = 0$$

$$B_4 = 5 - 2 = 1 \quad B_4 = 5 - 8 = 0$$



\rightarrow Perform AND operation

$$P_1 = 0001$$

$$P_2 = 1000$$

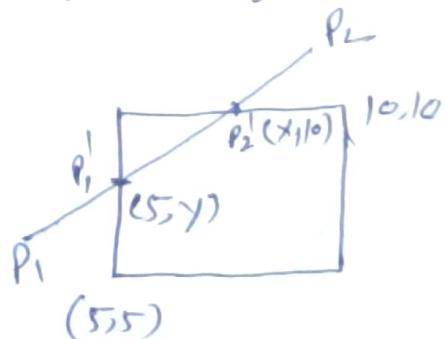
$$\text{AND} - 0000 \rightarrow \text{Line is partially visible}$$

\rightarrow As a result of AND operation for bitcode at both the ends result 0000, so the line is partially visible and need to be clipped.

\rightarrow The out code P_1 is 0001
 \therefore we can calculate that the line is extending (0001) left edge of the window

$$\rightarrow \text{Line } P_1 P_L: m = \frac{5}{6}$$

$$\text{Line } P_1 P_2: m = \frac{12 - y}{3} = \frac{5}{8} \Rightarrow 9.5$$



→ Now, also finding out code of $P_1'(5, 9.5)$

x, y

$$B_1 = 9.5 - 10 = 0$$

$$B_2 = 5 - 9.5 = 0$$

$$B_3 = 5 - 10 = 0$$

$$B_4 = 5 - 5 = 0$$

→ As 16 bit code of P_1' is 0000
∴ It is inside 16 clipping window

$$P_1 P_2 \quad m = \frac{10 - 9.5}{x - 5} = \frac{5}{6} \quad x = 5.6$$

Finding out code of $P_1'(5.6, 10)$

$$B_1 = 10 - 10 = 0 \quad | \quad B_3 = 5.6 - 10 = 0$$

$$B_2 = 5 - 10 = 0 \quad | \quad B_4 = 5 - 5.6 = 0$$

→ As 16 out code of both 16 end points P_1', P_2' 0000, ∴ Line is completely inside the clipping window & visible portion
 $(5, 9.5)$ & $(5.6, 10)$

⇒ Cyrus-beck line clipping Algorithm

Region code $P_3 P_4 -$

$P_3 - 0101$
$P_4 - 0000$
<hr/>
<u>0000</u>

Partially visible

$$\text{slope } m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{60 - 10}{70 - 10} = \frac{50}{60} = \frac{5}{6} = 0.833.$$

$$i_3(x_{\min}, y) = i_3(20, y).$$

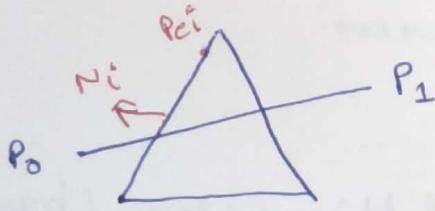
$$y = m(x_{\min} - x_1) + y_1$$

$$= \frac{5}{6}(20 - 10) + 10 = 18.33$$

$$\left\{ \begin{array}{l} \therefore i_3(20, 18.33) \\ \end{array} \right.$$

$$i_4(x, y_{\max}) = \quad \& \quad P_4 \text{ is already } \underline{0000}.$$

Cohen-Sutherland line clipping algorithm



- 1) Dot Product
- 2) Parametric eq. line.
 \downarrow
 $P(t) = P_0 + t(P_1 - P_0)$

(1) Normal vector \rightarrow outward to line

N_i

$i = \text{edge no.}$

(2) Take a point anywhere on line

P_{e_i} : Point at edge $i = 1, 2, 3 \dots$

(1) Dot Product $N_i \cdot (P(t) - P_{e_i})$

$$N_i \cdot (P_0 + t(P_1 - P_0) - P_{e_i}) = 0$$

$$N_i \cdot P_0 + \underline{N_i t P_1} - \underline{N_i t P_0} - N_i P_{e_i} = 0$$

$$\underline{N_i t P_1} - \underline{N_i t P_0} = N_i P_{e_i} - N_i P_0$$

$$t = \frac{N_i P_{e_i} - N_i P_0}{N_i P_1 - N_i P_0} = \frac{N_i (P_{e_i} - P_0)}{N_i (P_1 - P_0)}$$

$$t = \frac{(P_{e_i} - P_0) N_i}{(P_1 - P_0) N_i}$$

→ Nor

B_i

P

$$N_i(P_1 - P_0) = D \quad \{ \text{Denominator}$$

D > 0 leaving point

D < 0 entering point

D = 0

→ Calculate t₁, t₂, t₃

→ make list of entry or leaving point.

→ Pick values ^{highest} in entry point list

→ Pick value lowest in leaving point

→ Put t in.

$$(2) \quad P(t) = P_0 + t(P_1 - P_0)$$

Parametric eq

• cyrus beck is a line clipping algorithm that we allow clipping for non-rectangular.

steps ① firstly find the exterior point on the edge and, which is represent in a general way n(normal vector) which is an edge no.

Step 2 Now take a point on every edge or a vertex which is represent by P_{ei} --- P_{ei} (point at edge)

Step 3 After take a point on every calculating N_i or P_{ei} then by using both values we can calculate the time for every edge of polygon.

$$t = \frac{N_i(P_{ei} - P_0)}{N_i(P_1 - P_0)}$$

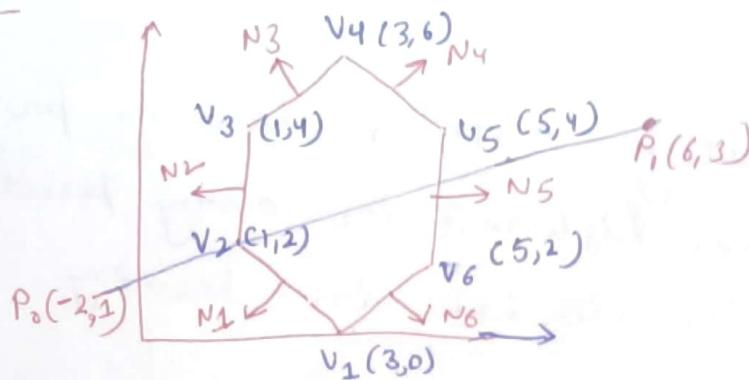


Step 4 After calculating time for all edge by using P_0 and P_1 and use this time by using formula:

$$P(t) = P_0 + t(P_1 - P_0)$$

find out the value of P_{e_0} and P_1 .

Numerical :-



$$N_1 (-1, -1)$$

$$N_2 (-1, 0)$$

$$N_3 (-1, 1)$$

$$N_4 (1, 1)$$

$$N_5 (1, 0)$$

$$N_6 (1, -1)$$

$$P(t) = P_0 + t(P_1 - P_0)$$

$$t_i = \frac{N_i (P_{ei} - P_0)}{N_i (P_1 - P_0)}$$

$$t_1 = \frac{(-1, -1) ((3, 0) - (-2, 1))}{(-1, -1) ((6, 3) - (-2, 1))}$$

$$\Rightarrow \frac{(-1, -1) (3 - (-2), 0 - 1)}{(-1, -1) (6 - (-2), 3 - 1)}$$

$$\Rightarrow \frac{(-1, -1) (5, -1)}{(-1, -1) (8, 2)} = 0.1.$$

$$\Rightarrow \frac{-5 + 1}{-8 - 2} = \frac{-4}{-10}$$

$$t_2 = \frac{(-1, 0) [(1, 2) - (-2, 1)]}{(-1, 0) [(6, 3) - (-2, 2)]} = \frac{(-1, 0) [(1+2), (2-1)]}{(-1, 0) [(6+3), (3-1)]}$$

$$= \frac{(-1, 0) (3, 1)}{(-1, 0) (8, 2)} = \frac{-3}{-8}.$$

$$t_3 = \frac{6}{6} \quad t_4 = \frac{10}{10} \quad t_5 = \frac{7}{8} \quad t_6 = \frac{6}{6}$$

Entering point = t_1, t_2, t_3

leaving point = t_4, t_5, t_6

$$P(t) = P_0 + t(P_1 - P_0)$$

$$= (-2, 1) + \left(\frac{4}{10} \right) ((6, 3) - (-2, 1))$$

$$= (-2, 1) + \frac{4}{10} ((6 - (-2), 3 - 1))$$

$$= (-2, 1) + \left(\frac{4^2}{10} \times 2, \frac{4}{10} \times 2 \right)$$

$$= (-2, 1) + \left(\frac{16}{5}, \frac{4}{5} \right)$$

$$\left(-2 + \frac{16}{5}, 1 + \frac{4}{5} \right) = \boxed{\left(\frac{6}{5}, \frac{9}{5} \right)}$$

$$\checkmark P(t) = (-2, 1) + \frac{7}{8} (2, 2)$$

$$= (-2, 1) + \frac{7}{8} \times 2, \frac{7}{8} \times 2$$

$$= (-2, 1) + \left(7, \frac{7}{4} \right) \Rightarrow \left(-2 + 7, 1 + \frac{7}{4} \right)$$

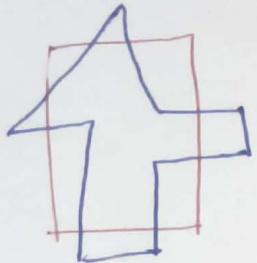
$$\boxed{\left(5, \frac{11}{4} \right)}$$

Sutherland-Hodgeman Polygon clipping algorithm

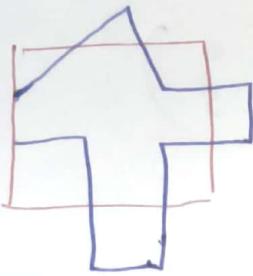
The Sutherland-Hodgeman algorithm performs clipping of a polygon against each window in turn.

The order to clip the polygons should be:

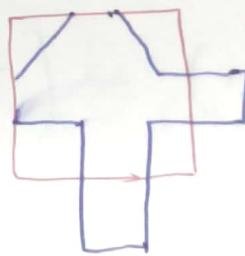
1. clipping against the left side of the window.
2. clipping against the top side of the window.
3. clipping against the right side of the window.
4. clipping against the bottom side of the window.



Before clipping



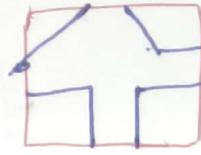
(a)



(b)



(c)

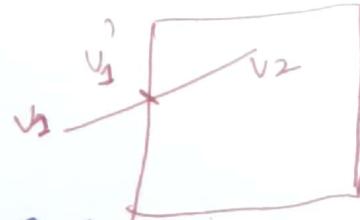


(d)

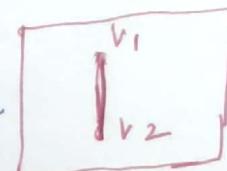
It consists of four cases:-

- ① If the first vertex is outside the window, second vertex is inside then the intersection point of the polygon edge with the window boundary and second vertex are added to the output vertex list.

Save { v_1 and v_2 }



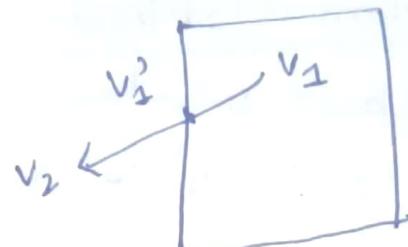
- ② If both vertices of edge are inside the window. Then only second vertex is added to the output vertex list.



Save { v_2 }

③ If the first vertex of the edge is inside and second is outside then only the intersection point of the polygon boundary and window boundary is added to the window boundary the output vertex list.

Save $\{v_1'\}$

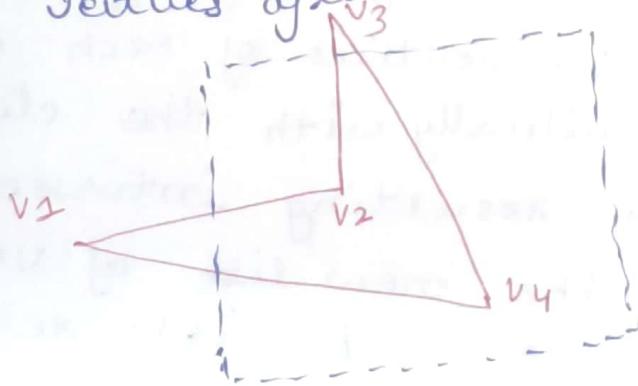


④ If both vertices of the edge are outside the window. Then nothing is added.

Save $\{\emptyset\}$



Ques for a polygon and clipping window. give the list of vertices after each boundary clipping.

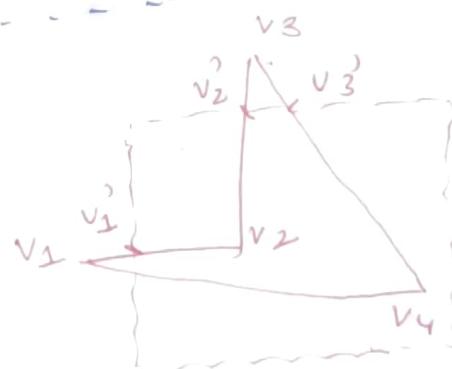


Solution

① left clipped

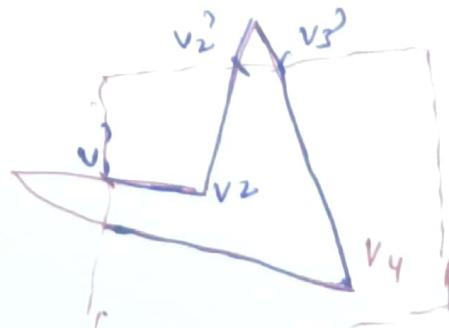
output vertex -

$\{v_2', v_2, v_2', v_3, v_3', v_4, v_4'\}$



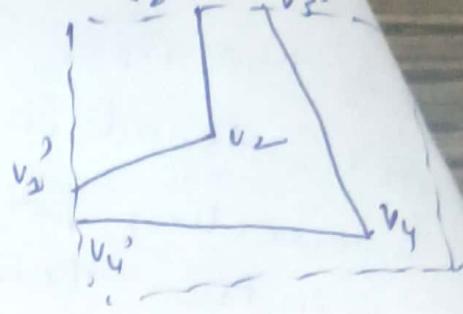
② Top clipped

$\{v_2', v_2, v_2', v_3, v_4, v_4'\}$



③ Right clipped :-

output vertex =
 $\{v_1', v_2, v_2', v_3', v_4, v_4'\}$



④ Bottom clipped :-

output vertex =
 $\{v_1', v_2, v_2', v_3', v_4, v_4'\}$

final clipped polygon =

$\{v_1', v_2, v_2', v_3', v_4, v_4'\}$

Algorithm, ① Read coordinates of all vertices of the polygon.

② Read coordinates of the clipping window.

③ consider the left edge of the window.

④ compare the vertices of each edge of the polygon, individually with the clipping plane.

⑤ save the resulting intersections and vertices in the new list of vertices according to four possible relationships between the edge and clipping boundary.

⑥ repeat step ④ & ⑤ for remaining edges of the clipping window.

⑦ stop.