Questions: Trigonometric identities (degrees)

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Summary

A selection of questions on trigonometric identities, where angles are measured in degrees.

Before attempting these questions, it is recommended that you read Guide: Trigonometric identities (degrees).

Q1

Using trigonometric identities, find the values of the following expressions:

1.1.
$$2(6\sin^2(\theta)) + 3(4\cos^2(\theta))$$
.

1.2.
$$10(7\sin^2(\theta)) + 14(5\cos^2(\theta))$$
.

1.3.
$$5\left(\frac{6}{\csc^2(\theta)}\right) + 15\left(\frac{2}{\sec^2(\theta)}\right)$$
.

1.4.
$$(\cos^2(\theta)-\sin^2(\theta))^2+4sin^2(\theta)\cos^2(\theta)$$

1.5.
$$2\sin(30)\cos(15) + 2\cos(30)\sin(15)$$

1.6.
$$3\cos(45)\cos(15) - 3\sin(45)\sin(15)$$

1.7.
$$\sin(150) + \sin(30)$$

1.8.
$$\cos(150) + \cos(30)$$

Q2

Simplify the following expressions:

2.1.
$$\tan(\theta)\cos(-\theta)$$

$$2.2 \quad \tan(-\theta)\csc(-\theta)\sec(-\theta)$$

2.3.
$$\tan^{2}(\theta) + \sin^{2}(\theta) + \cos^{2}(\theta)$$

2.4.
$$\frac{2\sin(\theta)}{\cos(\theta)(1-\tan^2(\theta))}$$

2.5.
$$\frac{\sin(7\theta) + \sin(3\theta)}{\cos(7\theta) - \cos(3\theta)}$$

2.6.
$$\frac{\sin(5\theta) - \sin(\theta)}{\cos(5\theta) + \cos(\theta)}$$

Q3

Using trigonometric identities, answer the following questions:

- 3.1. What is the value of $\cos(210^{\circ})$?
- 3.2. What are the values of $\sin(135^{\circ})$ and $\sin(225^{\circ})$?
- 3.3. If $\sin(50^\circ)$ has the value 0.766 (to 3 decimal places), what is the value of $\cos(130^\circ)$ to three decimal places?

Q4

Using trigonometric identities, find exact values of the following:

- 4.1. $\sin(15)$
- 4.2. $\cos(15)$
- 4.3. $\tan(15)$
- 4.4. $\sin(75)$
- 4.5. $\cos(75)$
- 4.6. $\tan(75)$