

Answers: Trigonometric identities (degrees)

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Summary

A selection of questions on trigonometric identities, using degrees to measure angles.

These are the answers to [Questions: Trigonometric identities \(degrees\)](#).

Please attempt the questions before reading these answers!

Q1

$$1.1. \quad 2(6 \sin^2(\theta)) + 3(4 \cos^2(\theta)) = 12(\sin^2(\theta) + \cos^2(\theta)) = 12$$

$$1.2. \quad 10(7 \sin^2(\theta)) + 14(5 \cos^2(\theta)) = 70$$

$$1.3. \quad 5 \left(\frac{6}{\csc^2(\theta)} \right) + 15 \left(\frac{2}{\sec^2(\theta)} \right) = 30$$

$$1.4. \quad (\cos^2(\theta) - \sin^2(\theta))^2 + 4 \sin^2(\theta) \cos^2(\theta) = \cos^2(2\theta) + \sin^2(2\theta) = 1$$

$$1.5. \quad 2 \sin(30) \cos(15) + 2 \cos(30) \sin(15) = 2 \sin(30 + 15) = 2 \sin(45) = \sqrt{2}$$

$$1.6. \quad 3 \cos(45) \cos(15) - 3 \sin(45) \sin(15) = 3 \cos(60) = \frac{3}{2}$$

$$1.7. \quad \sin(150) + \sin(30) = 2 \sin\left(\frac{180}{2}\right) \cos\left(\frac{120}{2}\right) = 2 \sin(90) \cos(60) = 1$$

$$1.8. \quad \cos(150) + \sin(30) = 2 \cos(90) \cos(60) = 0$$

Q2

$$2.1. \quad \tan(\theta) \cos(-\theta) = \frac{\sin(\theta)}{\cos(\theta)} \cdot \cos(\theta) = \sin(\theta)$$

$$2.2. \quad \tan(-\theta) \csc(-\theta) \sec(-\theta) = \left(-\frac{\sin(\theta)}{\cos(\theta)} \right) \left(\frac{1}{-\sin(\theta)} \right) \left(\frac{1}{\cos(\theta)} \right) = \left(\frac{1}{\cos^2(\theta)} \right) = \sec^2(\theta)$$

$$2.3. \quad \tan^2(\theta) + \sin^2(\theta) + \cos^2(\theta) = \tan^2(\theta) + 1 = \sec^2(\theta)$$

$$2.4. \quad \frac{2 \sin(\theta)}{\cos(\theta)(1 - \tan^2(\theta))} = \tan(2\theta)$$

$$2.5. \quad \frac{\sin(7\theta) + \sin(3\theta)}{\cos(7\theta) - \cos(3\theta)} = \frac{2 \sin(5\theta) \cos(2\theta)}{-2 \sin(5\theta) \sin(2\theta)} = -\cot(\theta)$$

$$2.6. \quad \frac{\sin(5\theta) - \sin(\theta)}{\cos(5\theta) + \cos(\theta)} = \tan(2\theta)$$

Q3

$$3.1. \quad \cos(210) = \frac{\sqrt{3}}{2}$$

$$3.2. \quad \text{Here } \sin(135) = \frac{1}{\sqrt{2}}, \text{ and } \sin(225) = -\frac{1}{\sqrt{2}}.$$

$$3.3. \quad \cos(130) = -0.766 \text{ to three decimal places.}$$

Q4

$$4.1. \quad \sin(15) = \sin(45) \cos(30) - \cos(45) \sin(30) = \frac{\sqrt{3}}{2\sqrt{2}} - \frac{1}{2\sqrt{2}} = \frac{\sqrt{3}-1}{2\sqrt{2}}$$

$$4.2. \quad \cos(15) = \frac{\sqrt{3}+1}{2\sqrt{2}}$$

$$4.3. \quad \tan(15) = \frac{\sqrt{3}-1}{\sqrt{3}+1}$$

$$4.4. \quad \sin(75) = \sin(45) \cos(30) + \cos(45) \sin(30) = \frac{\sqrt{3}+1}{2\sqrt{2}}$$

$$4.5. \quad \cos(75) = \frac{\sqrt{3}-1}{2\sqrt{2}}$$

$$4.6. \quad \tan(75) = \frac{\sqrt{3}+1}{\sqrt{3}-1}$$