Introduction to Logarithms: Questions

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Summary

A selection of questions for the study guide on logarithms.

Before attempting these questions, it is highly recommended that you read Guide: Introduction to Logarithms.

Q1

For the following, find the value of x if x is a rational number:

1.1.
$$\log_7(x) = 1$$

1.2.
$$\log_8(x) = 3$$

1.3.
$$\log_{12}(x) = 0$$

1.4.
$$\log_{10}(100) = x$$

1.5.
$$\log_2(17) = x$$

1.6.
$$\log_4(2) = x$$

1.7.
$$\log_3(27) = x$$

1.8.
$$\log_{10}(1) = x$$

1.9.
$$\log_x(16) = 4$$

1.10.
$$\log_x(49) = 2$$

1.11. $\log_x(13) = 4$

1.12. $\log_{2x}(12) = -1$

Q2

Before attempting this question, write out the 5 laws next to their names:

1. The Product Rule:

2. The Quotient Rule:

3. The Power Rule:

4. The Zero Rule:

5. The Identity Rule:

For the following, using the 5 Laws, find the value of \boldsymbol{x} :

2.1. $\log_3\left(\frac{1}{27}\right) = x$

2.2. $\log_4(16) = x$

2.3. $\log_7\left(\frac{2}{49}\right) = x$

2.4. $\log_x(YZ) = M$

2.5. $\log_6(\frac{36}{x}) = 1$

2.6. $\log_5(25) = x$

Q3

Convert the following logarithms to the given base and evaluate

2

3.1. $\log_3(25)$ to base 5

3.2. $\log_4(64)$ to base 16

- 3.3. $\log_e(100)$ to base 10
- 3.4. $\ln(27)$ to base 3
- 3.5. $\log_4(8)$ to base 2

Q4

For the following, find the value of \boldsymbol{x} :

4.1.
$$3^{x+1} = 7^x$$

4.2.
$$17^{2x} = 4^{x-1}$$

4.3.
$$5^{x+1} + 5^x = 12$$

4.4.
$$2^{3x-1} = 10^x$$

4.5.
$$11^x = 122^{(x-1)}$$

4.6.
$$2^{2x} - 8 \cdot 2^x - 16 = 0$$