

# Answers: Rationalizing the denominator

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## Summary

Answers to questions relating to the guide on rationalizing the denominator.

*These are the answers to [Questions: Rationalizing the denominator](#).*

**Please attempt the questions before reading these answers!**

## Q1

$$1.1. \quad \frac{5}{\sqrt{3}} = \frac{5\sqrt{3}}{3}$$

$$1.2. \quad \frac{7}{2\sqrt{5}} = \frac{7\sqrt{5}}{10}$$

$$1.3. \quad \frac{11}{4\sqrt{7}} = \frac{11\sqrt{7}}{28}$$

$$1.4. \quad \frac{8}{5\sqrt{6}} = \frac{4\sqrt{6}}{15}$$

$$1.5. \quad \frac{3\sqrt{2}}{\sqrt{5}} = \frac{3\sqrt{10}}{5}$$

$$1.6. \quad \frac{9}{\sqrt{10}} = \frac{9\sqrt{10}}{10}$$

$$1.7. \quad \frac{\sqrt{7}}{\sqrt{3}} = \frac{\sqrt{21}}{3}$$

$$1.8. \quad \frac{\sqrt{2}}{\sqrt{6}} = \frac{\sqrt{3}}{3}$$

$$1.9. \quad \frac{12}{\sqrt{11}} = \frac{12\sqrt{11}}{11}$$

$$1.10. \quad \frac{\sqrt{8}}{\sqrt{2}} = 2$$

$$1.11. \quad \frac{15}{3\sqrt{7}} = \frac{5\sqrt{7}}{7}$$

$$1.12. \quad \frac{6\sqrt{3}}{\sqrt{10}} = \frac{3\sqrt{30}}{5}$$

$$1.13. \quad \frac{\sqrt{18}}{\sqrt{9}} = \sqrt{2}$$

$$1.14. \quad \frac{2\sqrt{5}}{\sqrt{12}} = \frac{\sqrt{30}}{3}$$

$$1.15. \quad \frac{4}{\sqrt{2}} = 2\sqrt{2}$$

$$1.16. \quad \frac{10}{5\sqrt{13}} = \frac{2\sqrt{13}}{13}$$


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## Q2

$$2.1. \quad \frac{5}{2 + \sqrt{3}} = 10 - 5\sqrt{3}$$

$$2.2. \quad \frac{7}{4 - \sqrt{2}} = \frac{4 + \sqrt{2}}{2}$$

$$2.3. \quad \frac{3}{\sqrt{5} + 1} = \frac{3\sqrt{5} - 3}{4}$$

$$2.4. \quad \frac{\sqrt{7}}{\sqrt{3} - 1} = \frac{\sqrt{21} + \sqrt{7}}{2}$$

$$2.5. \quad \frac{2 + \sqrt{5}}{1 - \sqrt{2}} = -2 - 2\sqrt{2} - \sqrt{5} - \sqrt{10}$$

$$2.6. \quad \frac{3\sqrt{2} + 5}{4 + \sqrt{6}} = \frac{12\sqrt{2} - 6\sqrt{3} + 20 - 5\sqrt{6}}{10}$$

$$2.7. \quad \frac{8}{3 - \sqrt{7}} = 12 + 4\sqrt{7}$$

$$2.8. \quad \frac{6}{2 + \sqrt{5}} = -12 + 6\sqrt{5}$$

$$2.9. \quad \frac{\sqrt{10}}{\sqrt{2} + 3} = \frac{3\sqrt{10} - 2\sqrt{5}}{7}$$

$$2.10. \quad \frac{2\sqrt{3} + 5}{\sqrt{7} - 1} = \frac{2\sqrt{21} + 5\sqrt{7} + 2\sqrt{3} + 5}{6}$$

$$2.11. \quad \frac{\sqrt{6} - \sqrt{2}}{2 + \sqrt{5}} = -2\sqrt{6} + 2\sqrt{5} + 2\sqrt{2} - \sqrt{10}$$

$$2.12. \quad \frac{4 + \sqrt{3}}{5 - \sqrt{7}} = \frac{4\sqrt{7} + 5\sqrt{3} + \sqrt{21} + 20}{18}$$

$$2.13. \quad \frac{2}{4 - \sqrt{11}} = \frac{8 + 2\sqrt{11}}{5}$$

$$2.14. \quad \frac{\sqrt{8} + \sqrt{3}}{\sqrt{7} - 2} = \frac{2\sqrt{14} + 4\sqrt{2} + \sqrt{21} + 2\sqrt{3}}{3}$$


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### Q3

3.1. To prove this equation, rationalize the denominator of the left hand side of the equation.

Since the denominator contains two square roots you can multiply the numerator and denominator by  $-2\sqrt{3} + \sqrt{5}$  or by  $2\sqrt{3} - \sqrt{5}$  to rationalize the denominator.

If you multiply the numerator and denominator by  $2\sqrt{3} - \sqrt{5}$  you get:

$$\frac{\sqrt{11}}{2\sqrt{3} + \sqrt{5}} \cdot \frac{2\sqrt{3} - \sqrt{5}}{2\sqrt{3} - \sqrt{5}} = \frac{\sqrt{11}(2\sqrt{3} - \sqrt{5})}{(2\sqrt{3})^2 - 2\sqrt{15} + 2\sqrt{15} - (\sqrt{5})^2}$$

Simplifying the denominator and expanding the brackets gives you:

$$\frac{2\sqrt{33} - \sqrt{55}}{4(3) - 5}$$

Simplifying further gives you the final answer and the right hand side of the equation you are proving:

$$\frac{2\sqrt{33} - \sqrt{55}}{7}$$

If you instead multiply the numerator and denominator by  $-2\sqrt{3} + \sqrt{5}$  you get:

$$\frac{\sqrt{11}}{2\sqrt{3} + \sqrt{5}} \cdot \frac{-2\sqrt{3} + \sqrt{5}}{-2\sqrt{3} + \sqrt{5}} = \frac{\sqrt{11}(-2\sqrt{3} + \sqrt{5})}{(\sqrt{5})^2 + (2\sqrt{3})^2 + 2\sqrt{15} - 2\sqrt{15} - (-2\sqrt{3})^2}$$

Simplifying the denominator and expanding the brackets gives you:

$$\frac{-2\sqrt{33} + \sqrt{55}}{5 - 4(3)}$$

Further simplifying the denominator gives you:

$$\frac{-2\sqrt{33} + \sqrt{55}}{-7}$$

To get a positive denominator, multiplying both the numerator and the denominator by  $-1$  gives you the right hand side of the equation you are proving:

$$\frac{2\sqrt{33} - \sqrt{55}}{7}$$

$$3.2. \quad \frac{5 - \sqrt{2}}{\sqrt{10} - \sqrt{3}} = \frac{5\sqrt{10} - 5\sqrt{3} - 2\sqrt{5} + \sqrt{6}}{7}$$

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v1.0: initial version created 09/24 by Maximilian Volmar.

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