

Powers and nth roots: questions

Isabella Lewis

Summary

A selection of questions for the study guide on powers and nth roots.

Before attempting these questions, it is highly recommended that you read [Guide: powers and nth roots].

Q1

Simplify the following expressions, leaving your answer as a singular power:

1.1. $(a)^2 \cdot (b)^2$

1.2. $(a)^{-4} \cdot (b)^{-4}$

1.3. $2^2 \cdot 3^2$

1.4. $8^5 \cdot 6^5$

1.5. $12^{11} \cdot 3^{11}$

1.6. $\left(\frac{x^5}{y^5}\right)$

1.7. $\left(\frac{4^5}{2^5}\right)$

1.8. $\left(\frac{2^{-2}}{13^{-2}}\right)$

1.9. $\left(\frac{a}{b}\right)^n \cdot \left(\frac{c}{d}\right)^n$

1.10. $\left(\frac{2}{3}\right)^{14} \cdot \left(\frac{9}{12}\right)^{14}$

$$1.11. (a^{\frac{1}{2}}) \cdot (b^{\frac{1}{2}})$$

Q2

Evaluate the following:

$$2.1. \left(\frac{4^3 \cdot 3^3}{6^3}\right)$$

$$2.2. \left(\frac{4^2 \cdot 8^2}{2^2}\right) \cdot \left(\frac{1}{2}\right)^2$$

$$2.3. \left(\frac{a}{b}\right)^4 \cdot \left(\frac{c}{d}\right)^4 \cdot \left(\frac{e}{f}\right)^4$$

$$2.4. \frac{\left[\left(\frac{-2}{3}\right)^{-3} \cdot \left(\frac{-3}{5}\right)^{-3}\right]}{\left(\left(\frac{2}{3}\right)^{-3}\right)}$$

$$2.5. \frac{5^{x+1} \cdot 6^{x+1}}{3^{x+1}}$$

$$2.6. \frac{\left(\frac{1}{2}\right)^4 \cdot \left(\frac{3}{5}\right)^4}{\left(\frac{8}{3}\right)^4}$$

Q3

For the following, find the value of x :

$$3.1. (4^x) \cdot (2^x) = 64$$

$$3.2. \frac{5^{x+1} \cdot 6^{x+1}}{3^{x+1}} = 100$$

$$3.3. \frac{\left[\left(\frac{1}{2}\right)^x \cdot \left(\frac{-1}{4}\right)^x\right]}{\left(\frac{2}{3}\right)^x} = \frac{-27}{4096}$$

Q4

Simplify the following expressions:

4.1. $\sqrt{8}$

4.2. $\sqrt{3} \cdot \sqrt{7}$

4.3. $(\frac{\sqrt{24}}{\sqrt{6}})$

4.4. $(\sqrt{5})^2$

4.5. $(\sqrt{2})^4$

4.6. $\sqrt{75}$

4.7. $\sqrt{4^3} \cdot \sqrt[3]{8}$

4.8. $\sqrt{6} \cdot \sqrt{15}$

4.9. $\sqrt{75} - \sqrt{27}$

4.10. $(8 + \sqrt{2}) \cdot (3 - \sqrt{2})$

4.11. $(3\sqrt{7})^2(8\sqrt{3})^2$

4.12. $(3 - \sqrt{8})^2$

4.13. $(7 + \sqrt{5}) \cdot (1 + \sqrt{5})$

4.14. $\sqrt{45} + \sqrt{125}$

4.15. $\sqrt{108}$

Q5

Simplify the following:

5.1. $\frac{8}{\sqrt{3}}$

5.2. $\frac{7+\sqrt{5}}{3+\sqrt{5}}$

5.3. $\left(\frac{2-\sqrt{3}}{3+\sqrt{3}}\right)$

5.4. $\frac{21}{2+\sqrt{3}}$

5.5. $\frac{1}{4-\sqrt{8}}$

Please click this link to find the answers.
