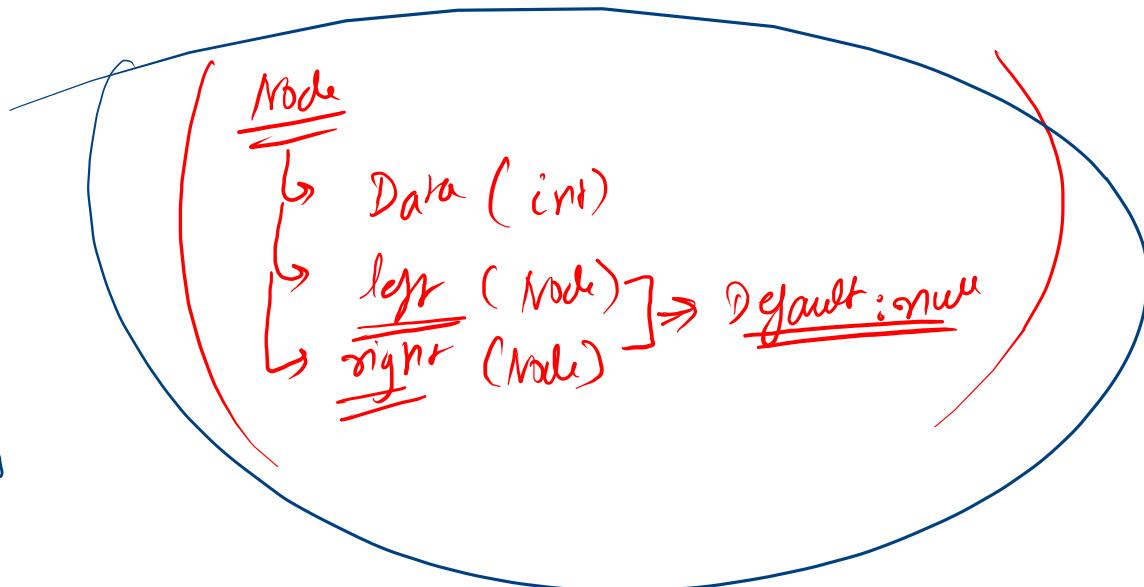
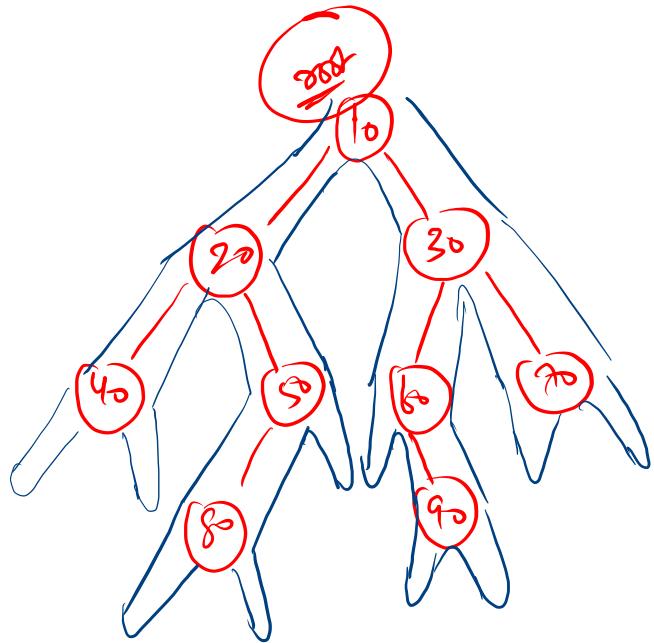


BINARY TREES:

Concept is similar to Binary Tree

Structural limit :- A node can have at most 2 children  
↳ 0, 1, 2



10 20 40 null null 50 80 null null null 30 60 null 90 null null 70 null null



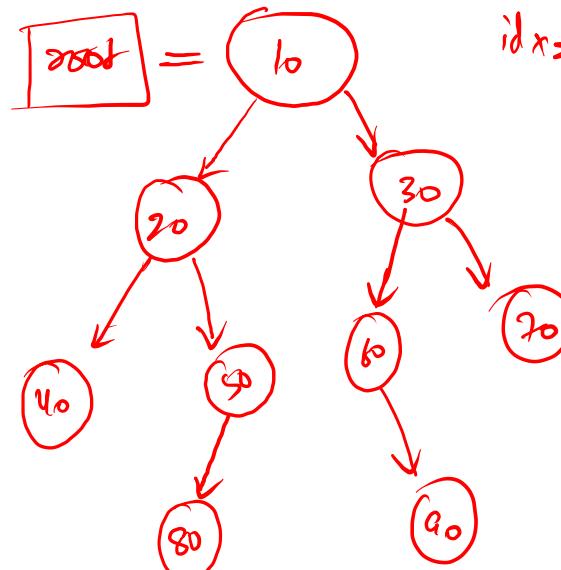
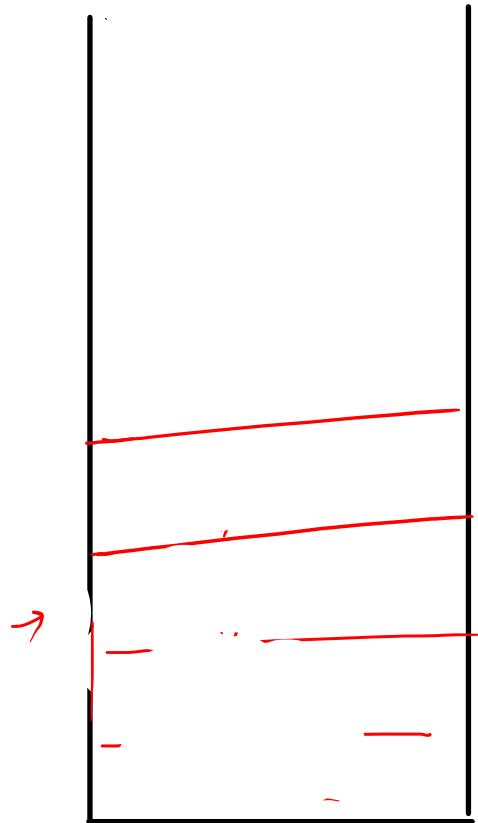
{10,20,40,null,null,50,80,null,null,null,30,60,null,90,null,null,70,null,null};

~~Pair~~  
 ↳ Node  
 ↳ state

Stack  
 0 → left

1 → right

2 → pop

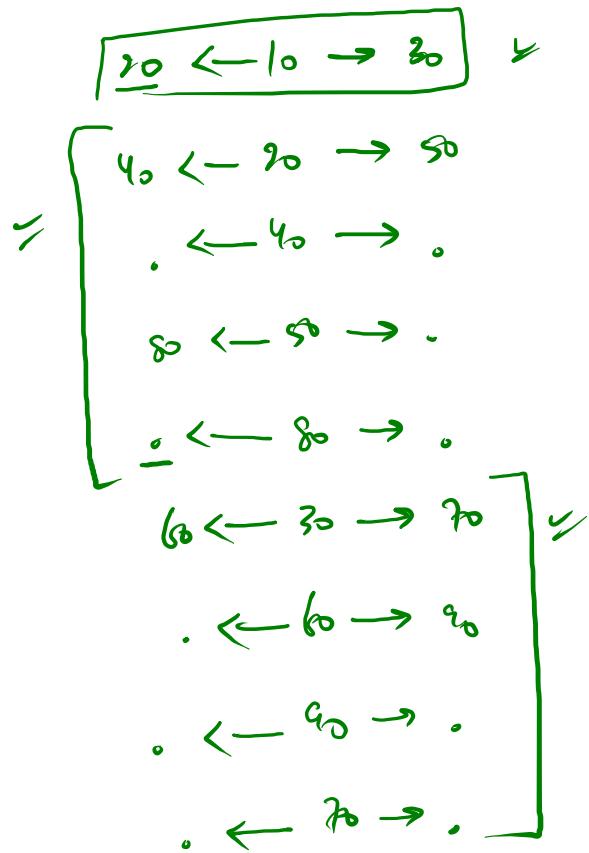
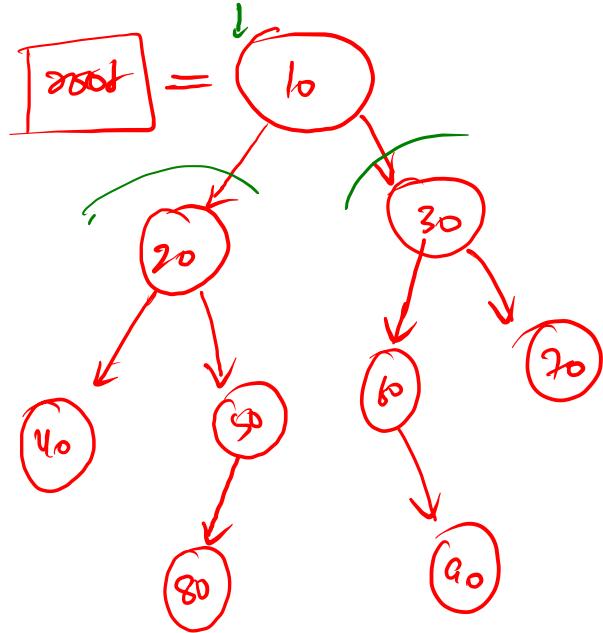


$idx = 10, 11, 12, 13, 14, 15, 16, 17, 18, 19$

```

while(st.size() > 0){
  Pair top = st.peek();
  if(top.state == 0){
    Integer ele = inp[idx]; // null
    if(ele != null){
      Node newNode = new Node(ele, null, null);
      top.node.left = newNode;
      st.push(new Pair(newNode, 0));
    }
    idx++;
  } else if(top.state == 1){
    Integer ele = inp[idx]; // null
    if(ele != null){
      Node newNode = new Node(ele, null, null);
      top.node.right = newNode;
      st.push(new Pair(newNode, 0));
    }
    idx++;
  } else{
    st.pop();
  }
}
  
```

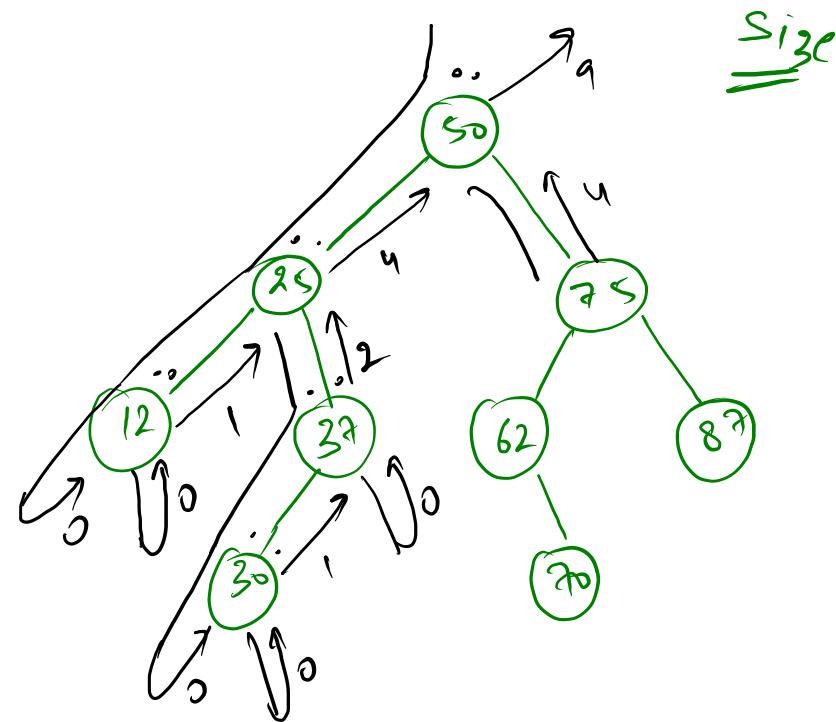
~~Integer~~ inp[] = {10, 20, 40, ~~null~~, ~~null~~, 50, 80, ~~null~~, ~~null~~, ~~null~~, 30, 60, ~~null~~, 90, ~~null~~, ~~null~~, 70, ~~null~~, ~~null~~};



```

public static void display(Node node){
    String str = "";
    str += node.left != null ? node.left.data : ".";
    str += " " + node.data + " ";
    str += node.right != null ? node.right.data : ".";
    System.out.print(str);
    display(node.left);
    display(node.right);
}

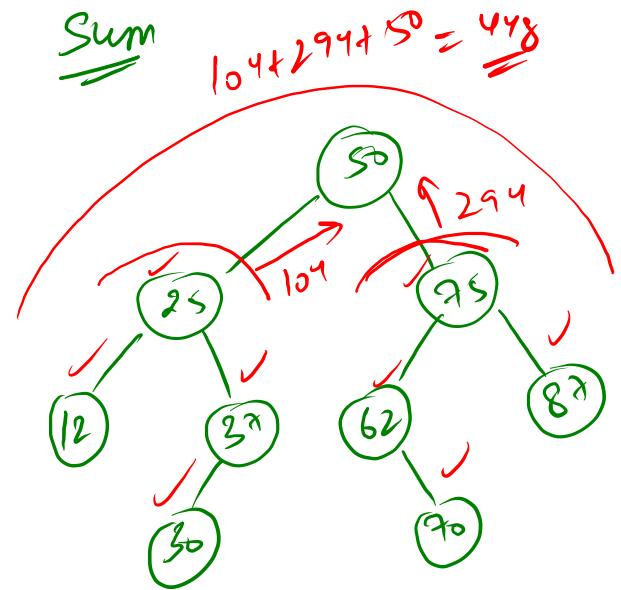
```



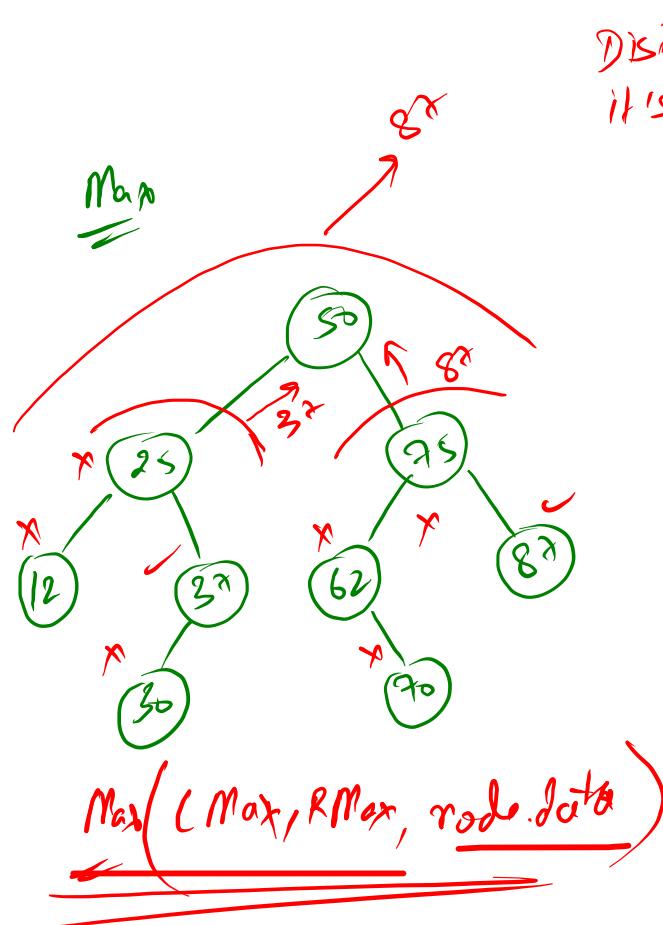
size

```
if(node == null){  
    return 0;  
}
```

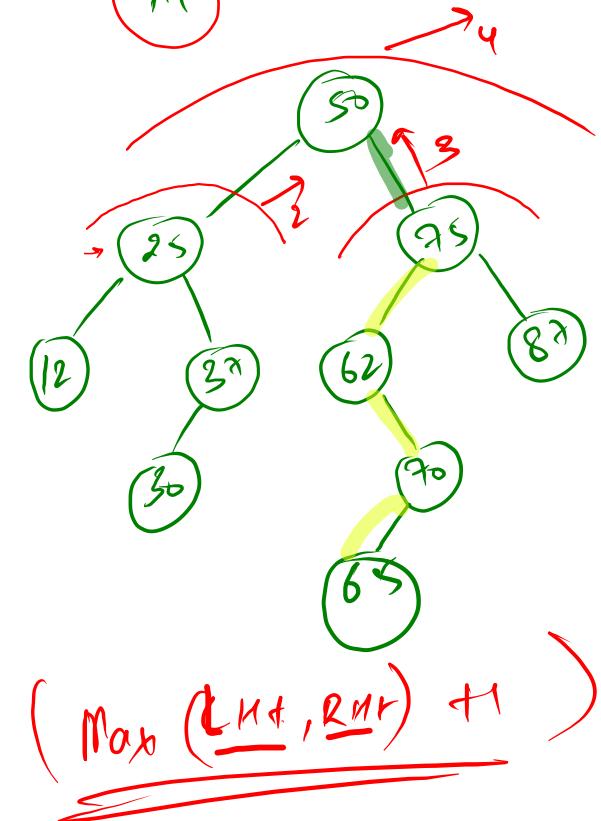
```
public static int size(Node node) {  
    int sizeOfLTree = size(node.left); -1  
    int sizeOfRTree = size(node.right); -2  
  
    return sizeOfLTree+sizeOfRTree+1; -3  
}
```



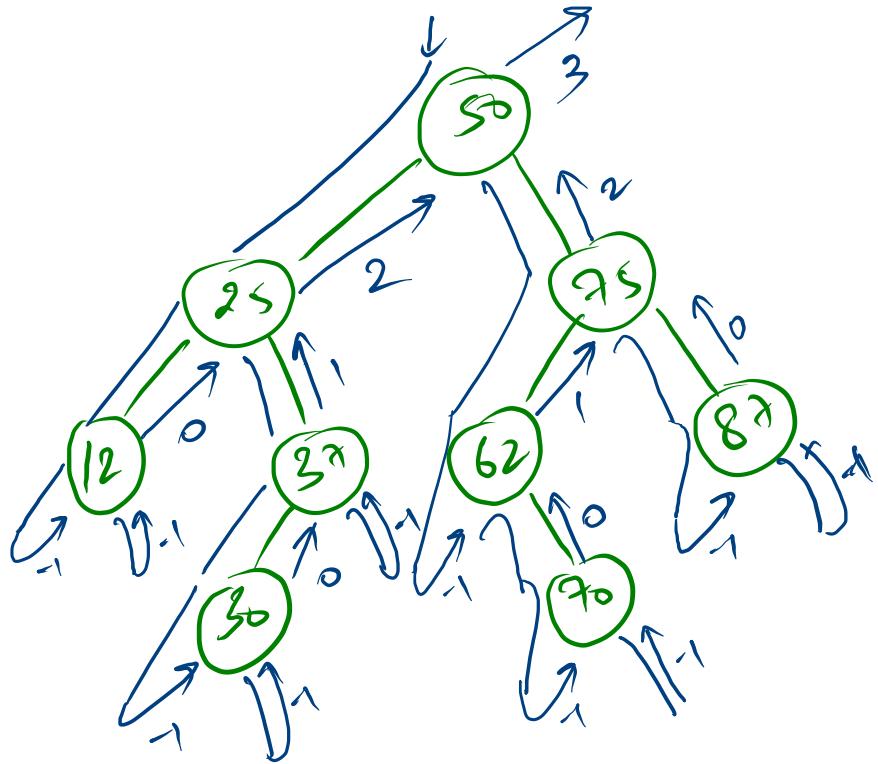
(Sum + Rsum + node.data)



Distance b/w root &  
it's deepest node

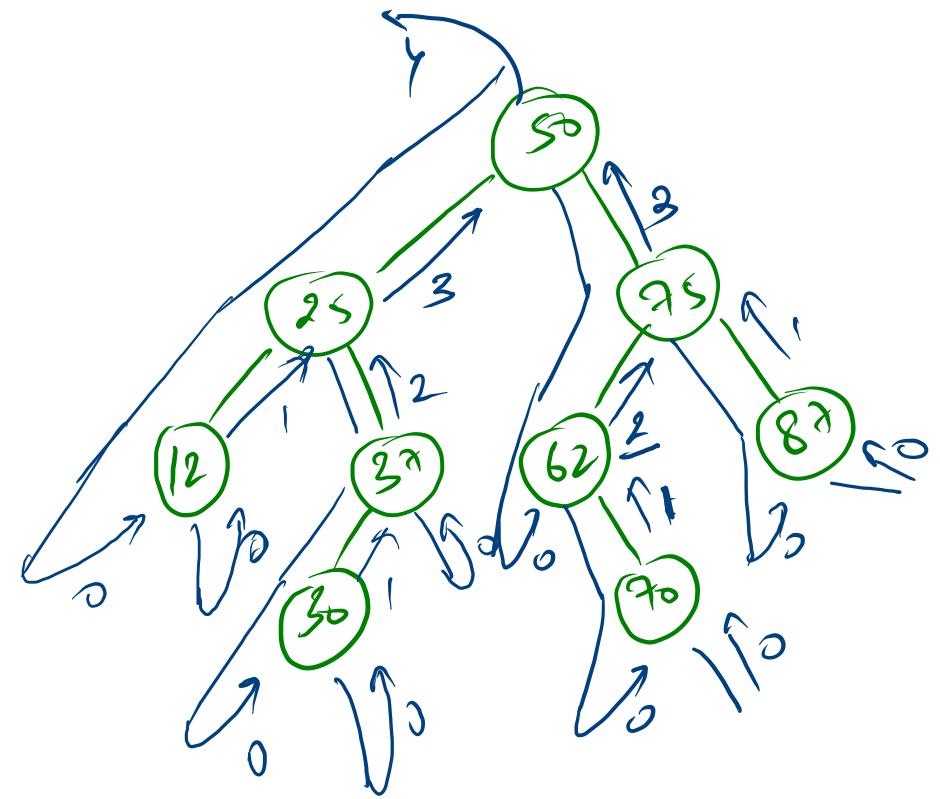


Height  $\Rightarrow$  Distance b/w root & its deepest node.

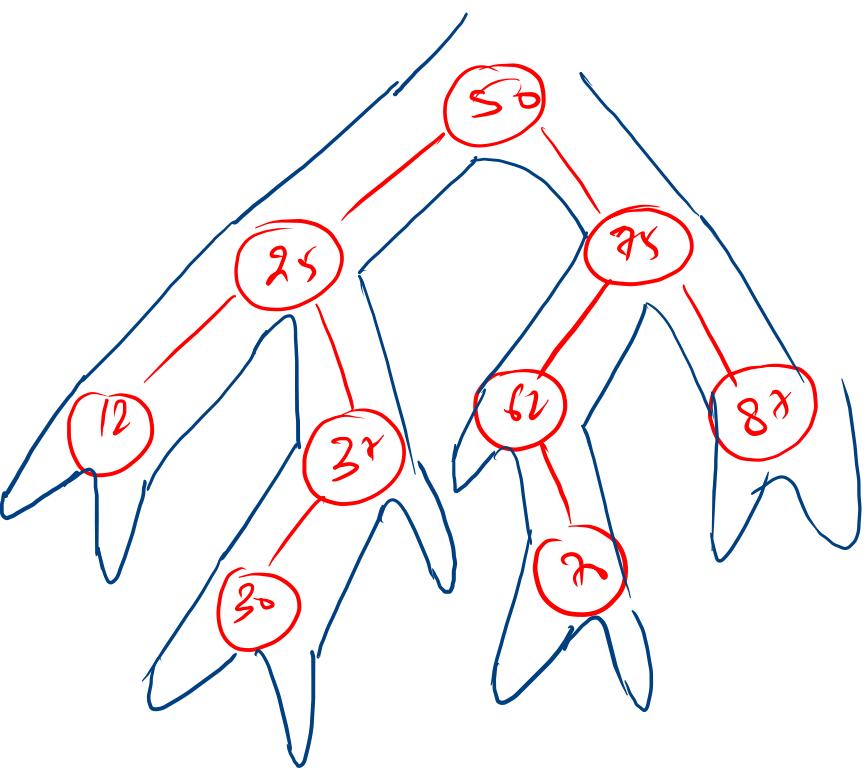


$-1 \Rightarrow$  Height  
on the basis  
of edges

```
public static int height(Node node) {  
    if(node == null){  
        |  
    }  
    int lht = height(node.left);  
    int rht = height(node.right);  
    return Math.max(lht,rht)+1;  
}
```



$0 \rightarrow$  Height  
on the basis of  
nodes

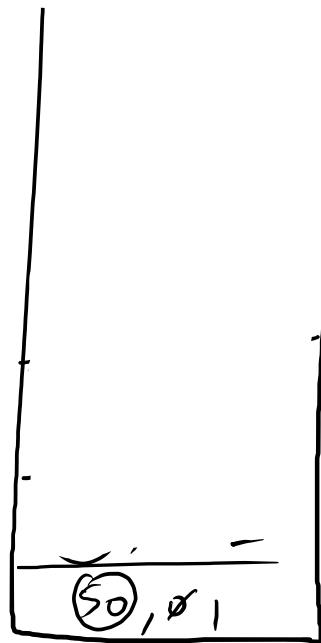
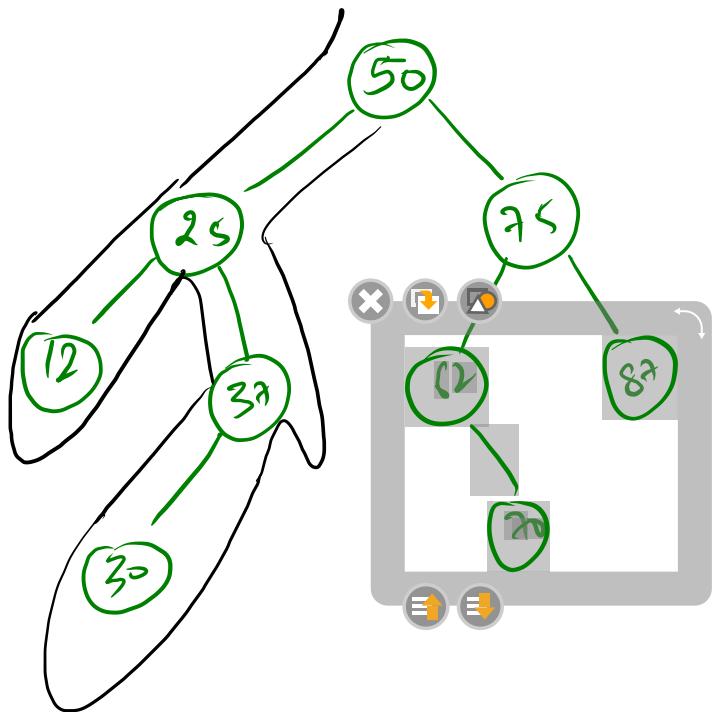


Pre → first  $[N L R]$   
~~In~~ → second  $[L N R]$   
~~Post~~ → last  $[L R N]$

$P_x = 50 \rightarrow 25 \rightarrow 12 \rightarrow 32 \rightarrow 30 \rightarrow 75 \rightarrow 62 \rightarrow 20 \rightarrow 87 \rightarrow .$

$I^n = 12 \rightarrow 25 \rightarrow 30 \rightarrow 32 \rightarrow 50 \rightarrow 62 \rightarrow 20 \rightarrow 75 \rightarrow 87 \rightarrow .$

$Posr = 12 \rightarrow 30 \rightarrow 32 \rightarrow 25 \rightarrow 20 \rightarrow 62 \rightarrow 87 \rightarrow 75 \rightarrow 50 \rightarrow .$



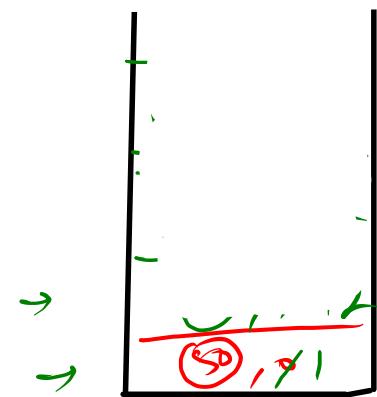
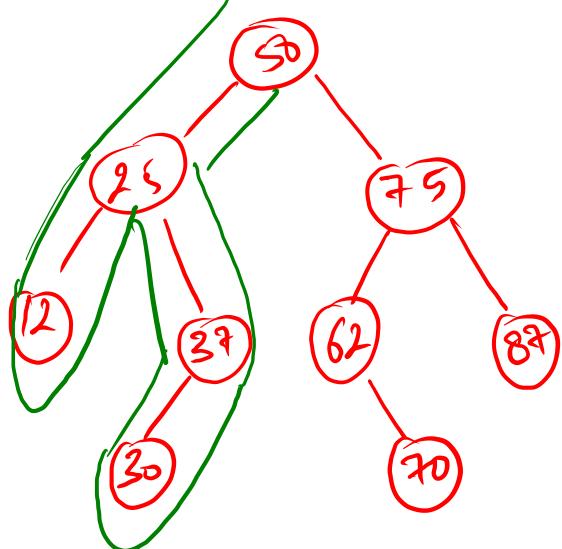
state

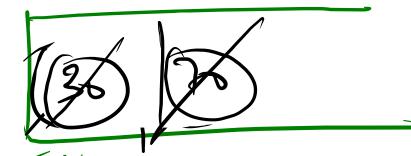
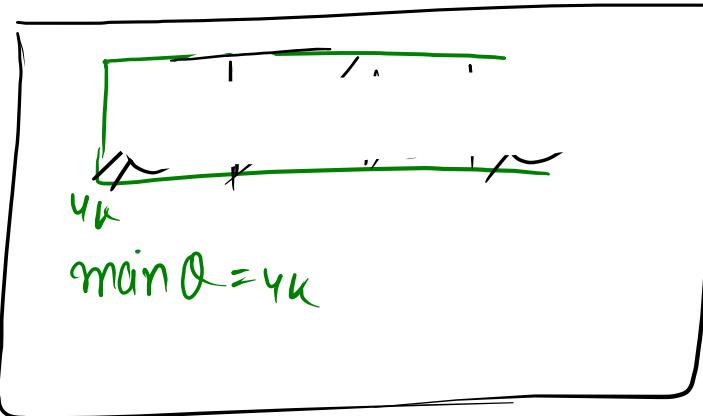
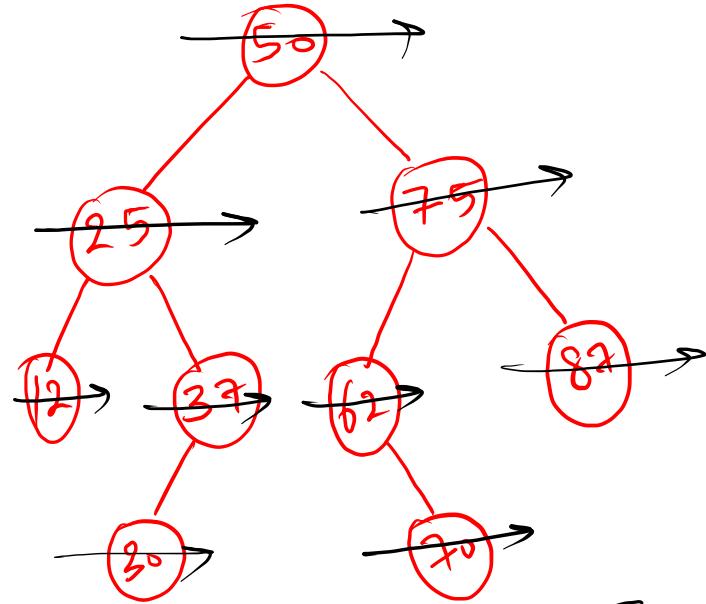
- 0 → pre, left add
- 1 → in, right add
- 2 → post, pop

px      50    25    12    37    30  
 in      12    25    30    37  
 post     12    30    37    25

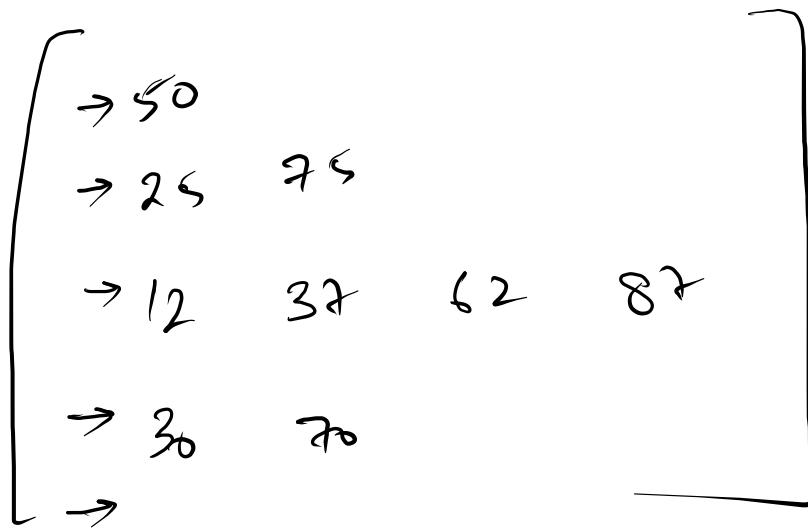
→ Pre = 50 25 12 37 30

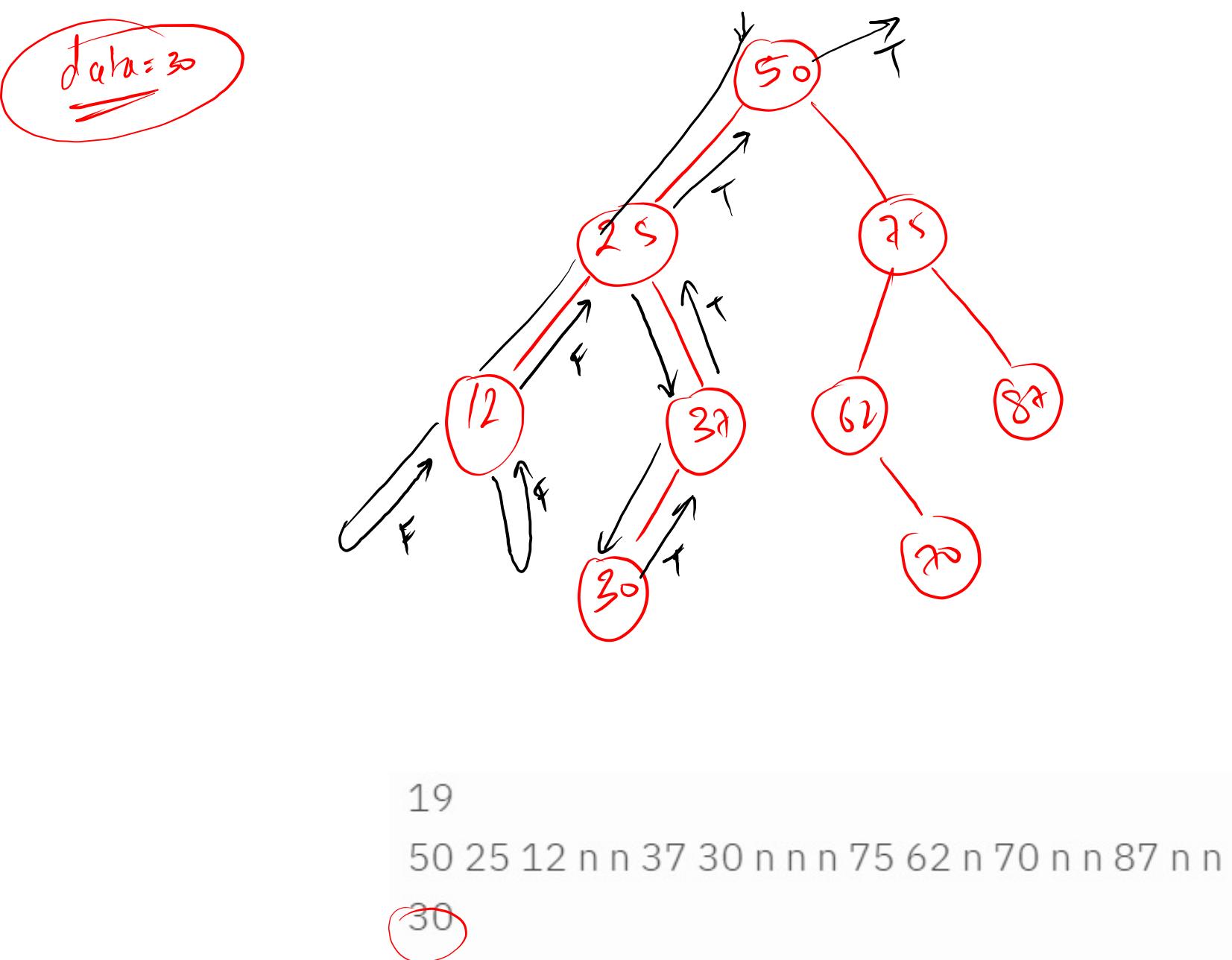
→ In = "12 25 30 37"  
→ Post = "12 30 37 25"



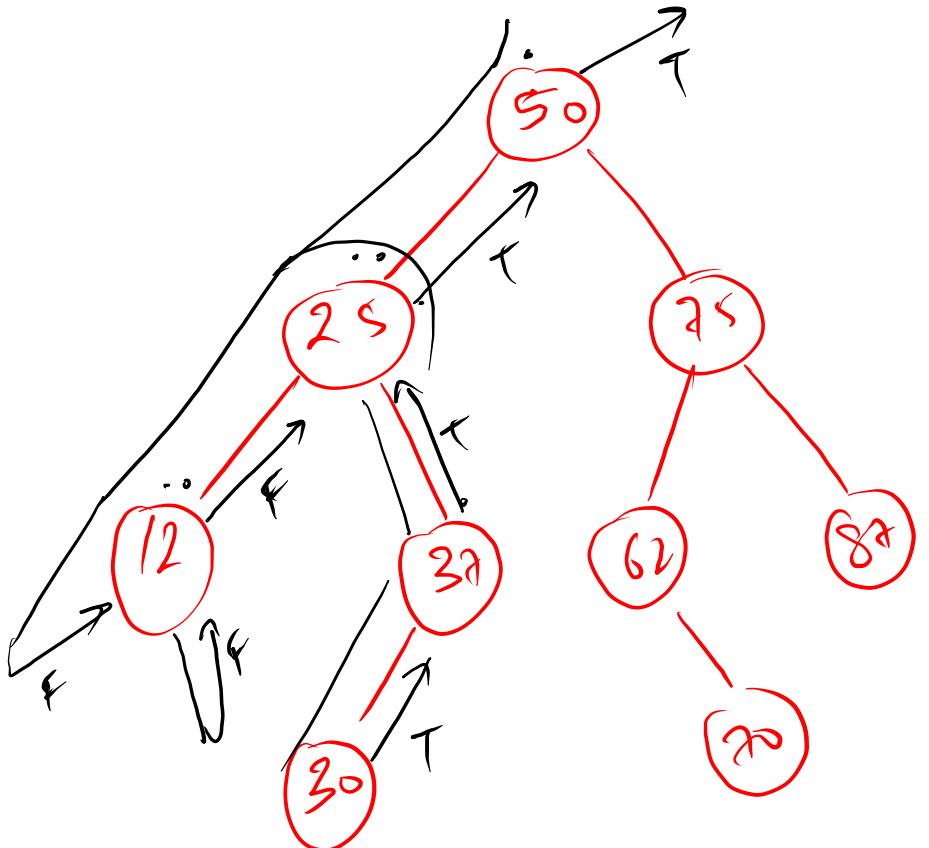


$\text{helperD} = 5K$



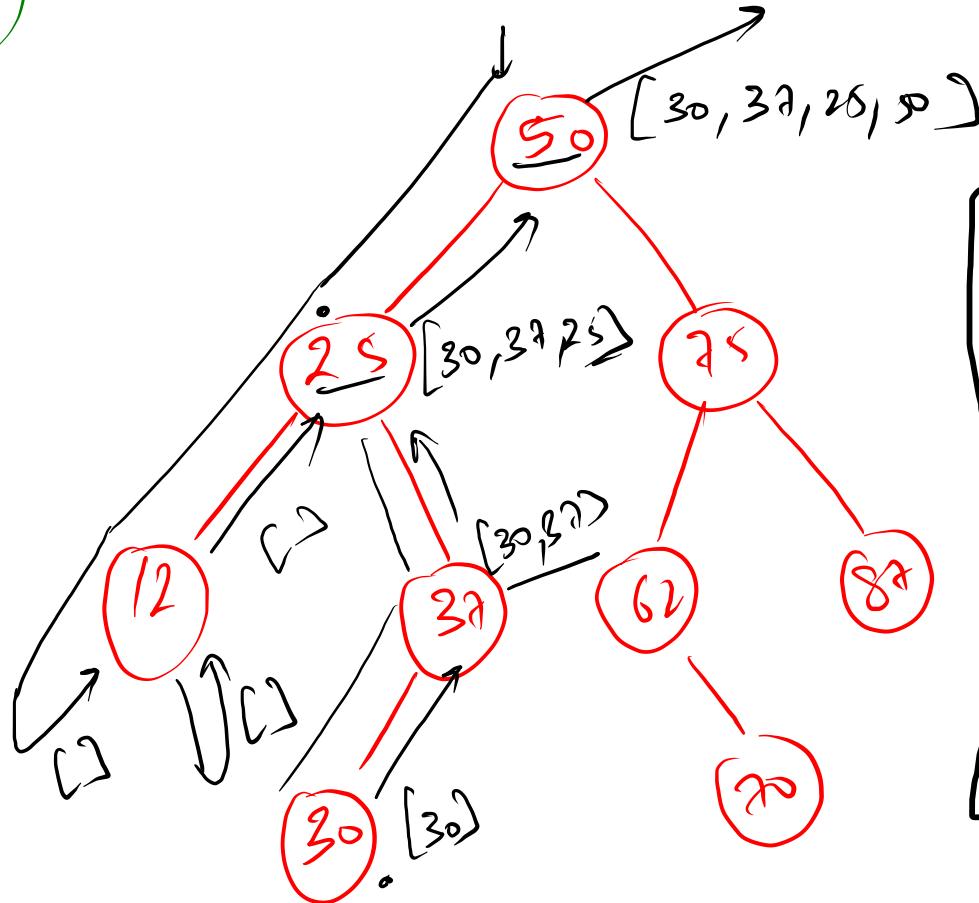


data = 30



```
public static boolean find(Node node, int data){  
    if(node == null){  
        return false;  
    }  
    if(node.data == data){  
        return true;  
    }  
  
    boolean lres = find(node.left,data);  
    if(lres){  
        return true;  
    }  
    boolean rres = find(node.right,data);  
    if(rres){  
        return true;  
    }  
    return false;  
}
```

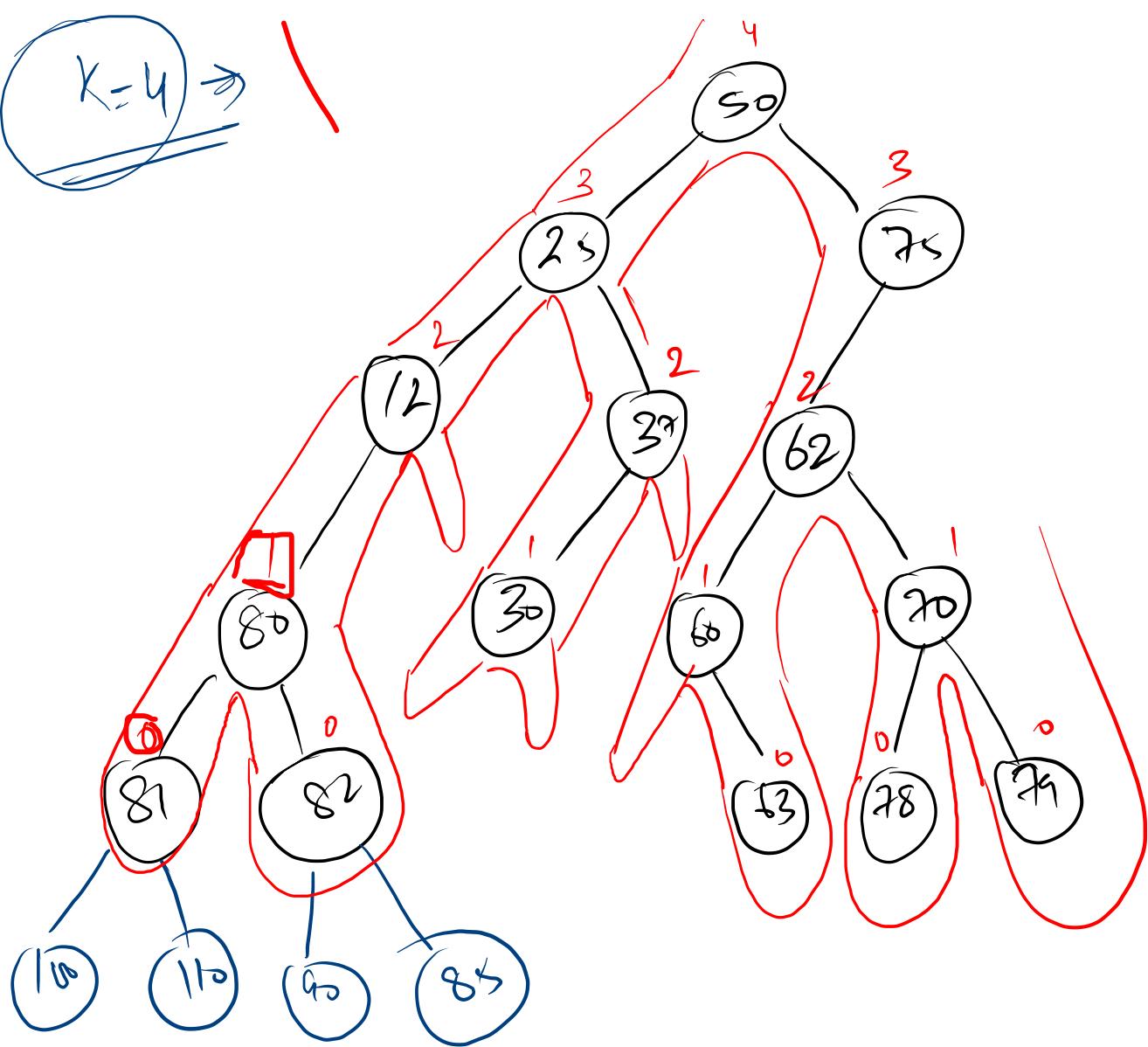
$$\text{data} = 30$$



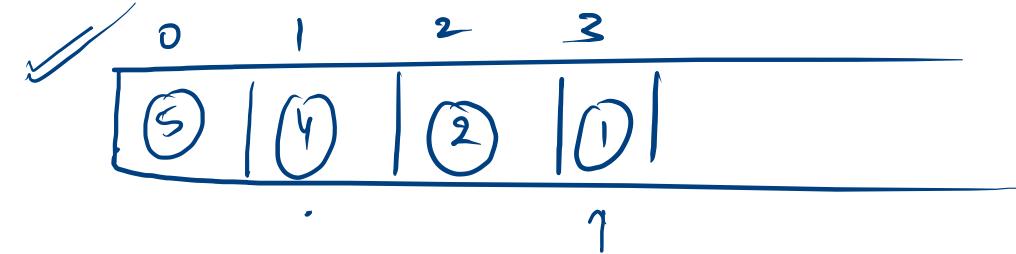
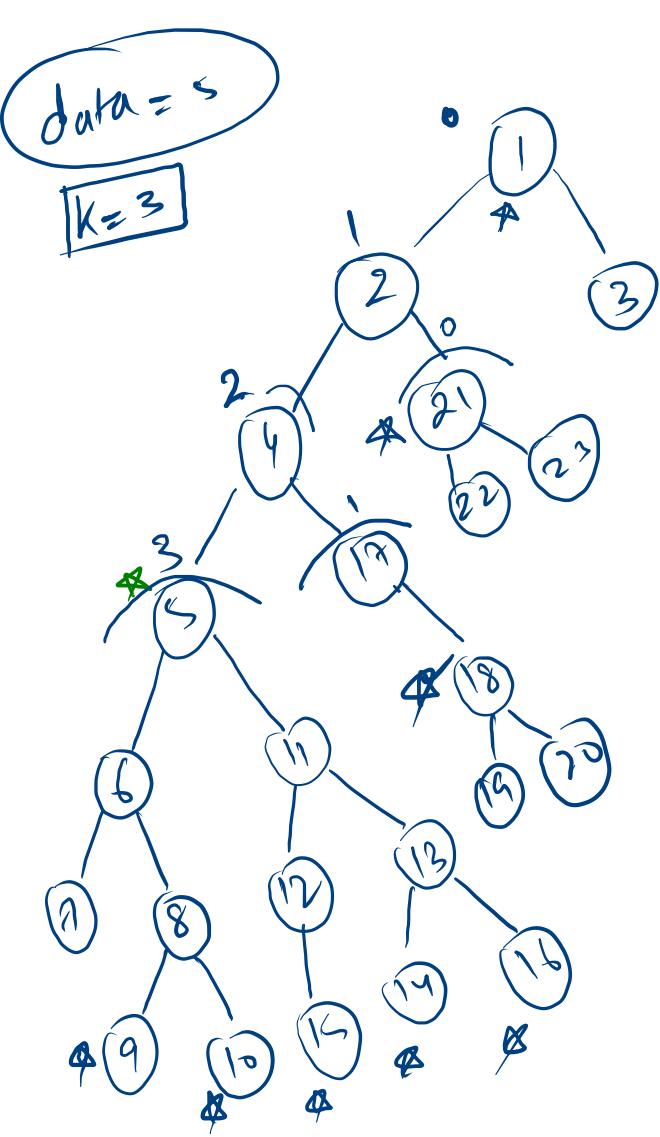
```
public static ArrayList<Integer> nodeToRootPath(Node node, int data){  
    if(node == null){  
        return new ArrayList<>();  
    }  
    if(node.data == data){  
        ArrayList<Integer> al = new ArrayList<>();  
        al.add(data);  
        return al;  
    }  
  
    ArrayList<Integer> lres = nodeToRootPath(node.left,data);  
    if(lres.size() > 0){  
        lres.add(node.data);  
        return lres;  
    }  
    ArrayList<Integer> rres = nodeToRootPath(node.right,data);  
    if(rres.size() > 0){  
        rres.add(node.data);  
        return rres;  
    }  
    return new ArrayList<>();  
}
```

```
public static ArrayList<Integer> nodeToRootPath(Node node, int data){  
    if(node == null){  
        return new ArrayList<>();  
    }  
    if(node.data == data){  
        ArrayList<Integer> al = new ArrayList<>();  
        al.add(data);  
        return al;  
    }  
  
    ArrayList<Integer> lres = nodeToRootPath(node.left,data);  
    if(lres.size() > 0){  
        lres.add(node.data);  
        return lres;  
    }  
    ArrayList<Integer> rres = nodeToRootPath(node.right,data);  
    if(rres.size() > 0){  
        rres.add(node.data);  
        return rres;  
    }  
    return new ArrayList<>();  
}
```

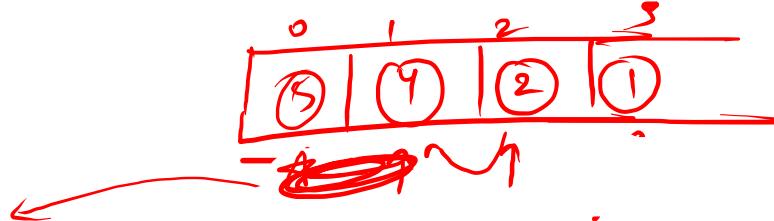
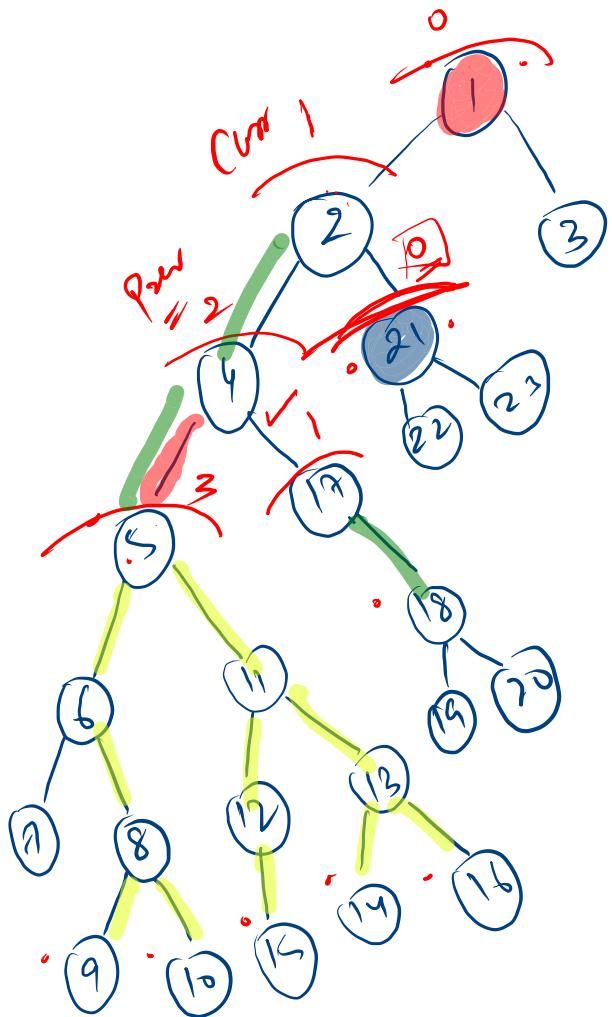
```
public static boolean find(Node node, int data){  
    if(node == null){  
        return false;  
    }  
    if(node.data == data){  
        return true;  
    }  
  
    boolean lres = find(node.left,data);  
    if(lres){  
        return true;  
    }  
    boolean rres = find(node.right,data);  
    if(rres){  
        return true;  
    }  
    return false;  
}
```



81  
82  
63  
78  
29



~~remDist~~  $\Rightarrow$  K-idx



$\text{remDist} = 0$        $d=5, k=3$

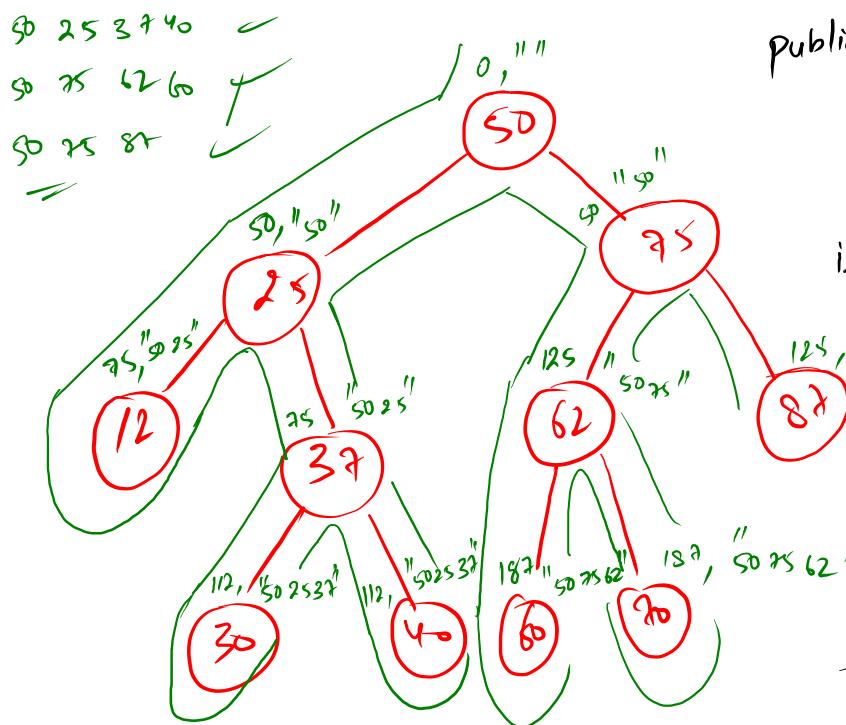
9  
10  
15  
14  
16  
18  
 $\neq 21$   
1

```
ArrayList<Node> list = nodeToRootPath(node,data);
printKLevelsDown(list.get(0),k);
```

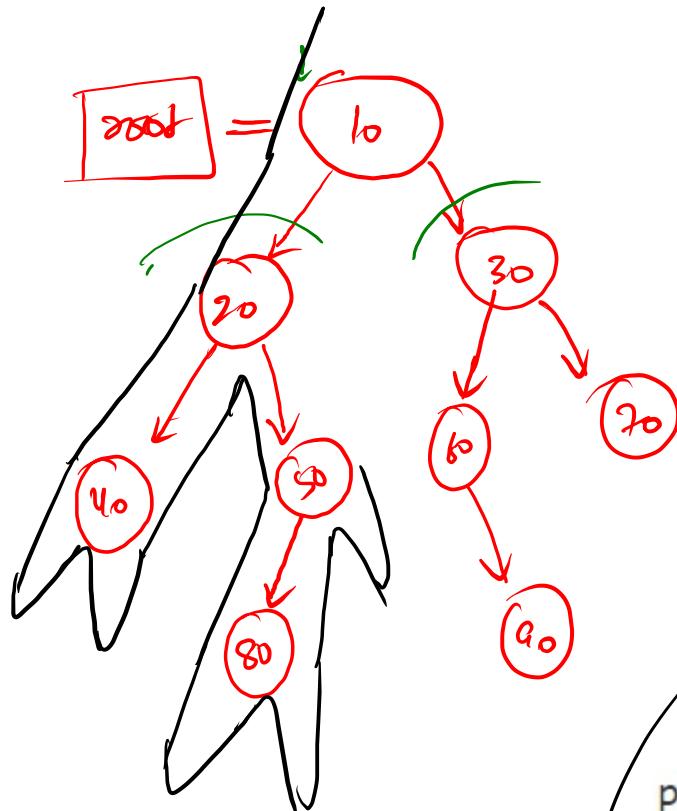
```
for(int idx = 1 ; idx < list.size() ; idx++){
    int remDist = k - idx;
    Node curr = list.get(idx);
    Node prev = list.get(idx-1);
    if(remDist == 0){
        System.out.println(curr.data);
        break;
    }else{
        if(curr.left == prev){
            printKLevelsDown(curr.right , remDist-1);
        }else if(curr.right == prev){
            printKLevelsDown(curr.left , remDist-1);
        }
    }
}
```



$$l_0 = 150$$
  
$$h_i = 250$$



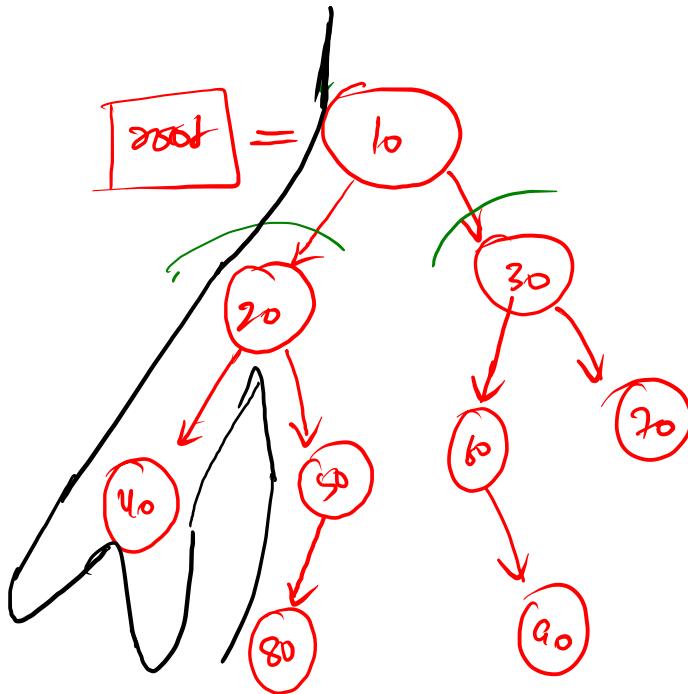
```
public static void fun(Node node, int sum, String path, int lo, int hi) {  
    if (node == null){  
        return;  
    }  
    if (node.left == null & node.right == null){  
        sum += node.data;  
        path += node.data;  
        if (sum >= lo & sum <= hi){  
            print(path);  
        }  
        return;  
    }  
    fun(node.left, sum + node.data, path + node.data + " ", lo, hi);  
    fun(node.right, sum + node.data, path + node.data + " ", lo, hi);  
}
```



pre : 10 -> 20 -> 40 -> 50 -> 80 -> 30 -> 60 -> 90 -> 70 -> .

in : 40 -> 20 -> 80 -> 50 -> 10 -> 60 -> 90 -> 30 -> 70 -> .

post : 40 -> 80 -> 50 -> 20 -> 90 -> 60 -> 70 -> 30 -> 10 -> .



$20 \leftarrow 10 \rightarrow 30$

$40 \leftarrow 20 \rightarrow 50$

$\cdot \leftarrow 40 \rightarrow \cdot$

```

if (node == null) {
    return;
}

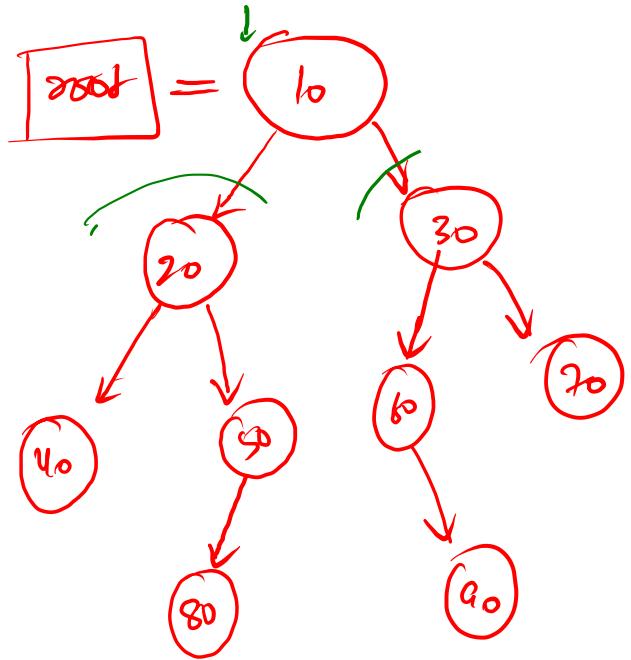
```

```

public static void display(Node node){
    String str = "";
    str += node.left != null ? node.left.data : ".";
    str += " <- " + node.data + " -> ";
    str += node.right != null ? node.right.data : ".";
    System.out.println(str);
    → display(node.left);
    display(node.right);
}

```

$80 \leftarrow 50 \rightarrow \cdot$



20 <- 10 -> 30

40 <- 20 -> 50

. <- 40 -> .

80 <- 50 -> .

. <- 80 -> .

60 <- 30 -> 70

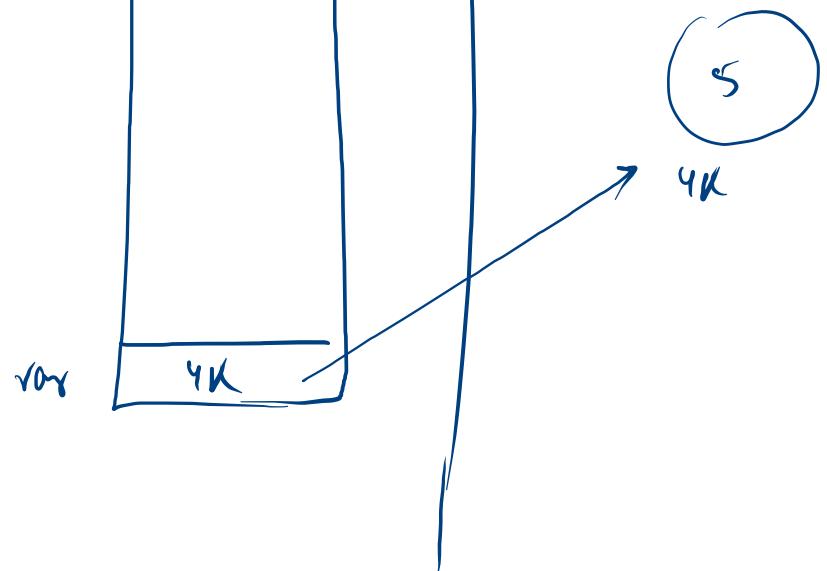
. <- 60 -> 90

. <- 90 -> .

. <- 70 -> .

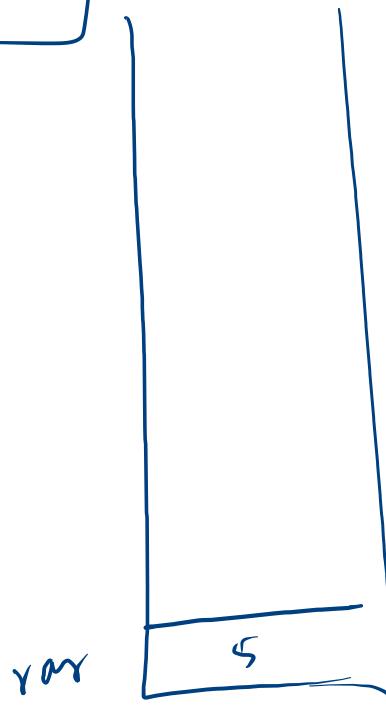
Integer  
→ wrapper Class of int

Integer var = 5;



int (polymorphic)

int var = s



~~s(1)~~  
~~s(2)~~  
~~s(8)~~  
~~s(6)~~  
~~y(4)~~  
~~z(3)~~  
~~2(1)~~  
~~H(F)~~  
~~e(5)~~

0	1	2	3	4	5	6	7	8
5	8	1	0	3	4	6	8	2

0	1	2	3	4	5	6	7	8
7	8	3	4	6	8	-1	-1	-1

