

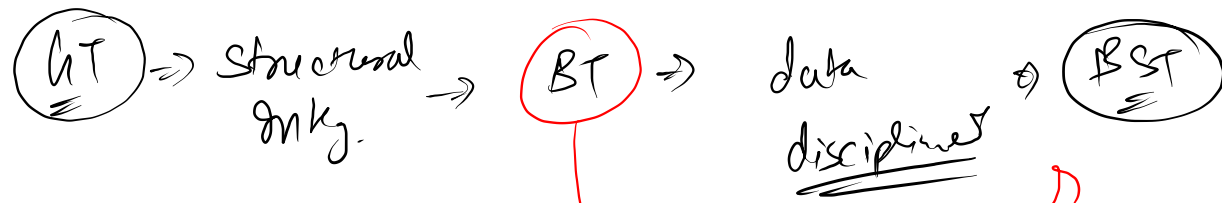
BST



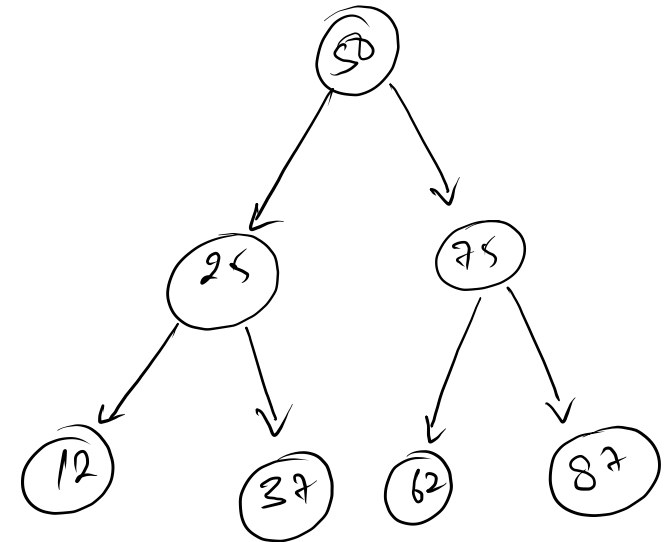
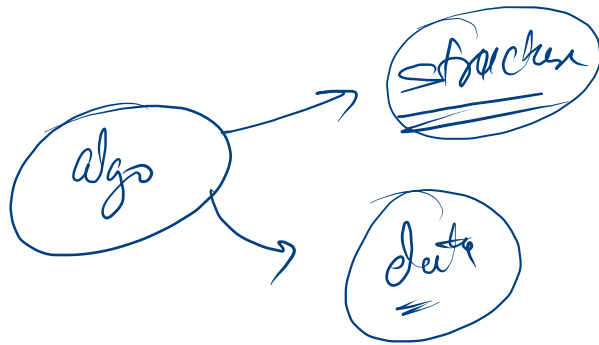
left < root.data < right



BST



BST Properties



	BT	BST
Size	✓	✓
HT	✓	✓
Display	✓	✓
Max	$O(n)$	optimization
Min	$O(n)$	=
find	$O(n)$	=
NTRP	$O(n)$	=
LCA	$O(n)$	=

BT → Construct

1. state → pair class

2. stack ✓

BT Construction ✓

Balanced Tree ?

Node

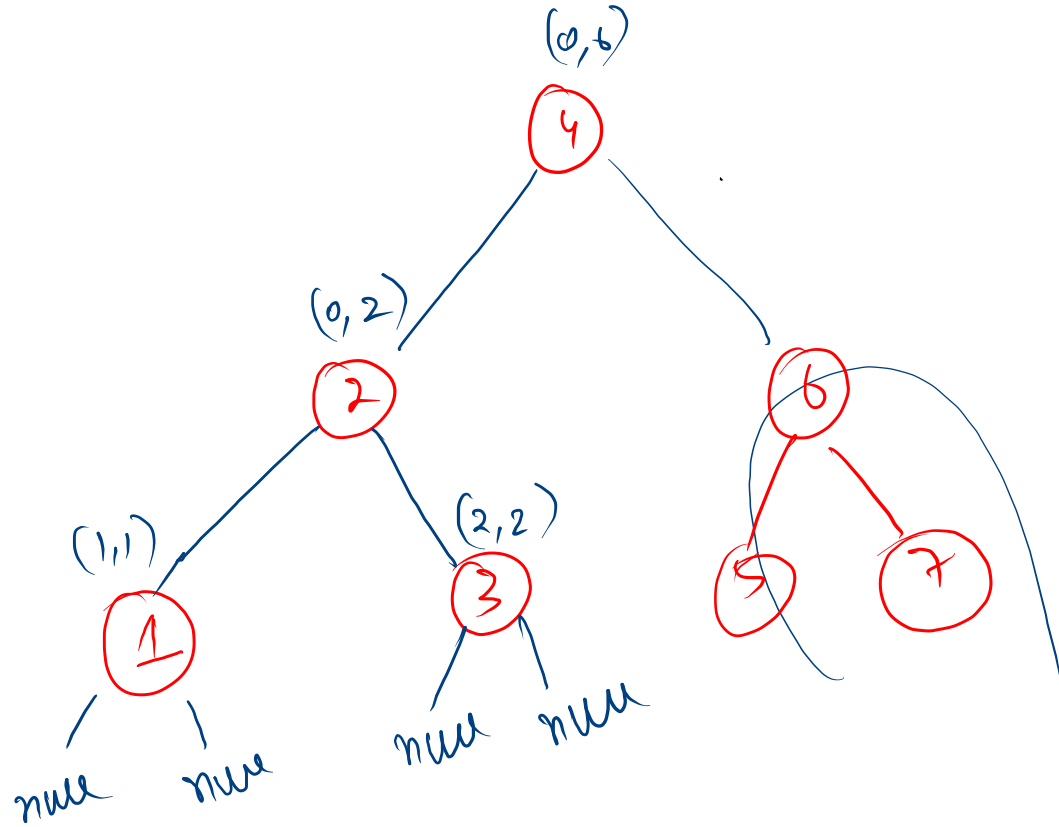
data
left
Right

Index \rightarrow 0 1 2 3 4 5 6 7

val \rightarrow 1 2 3 4 5 6 7

Sorted

Balanced BST

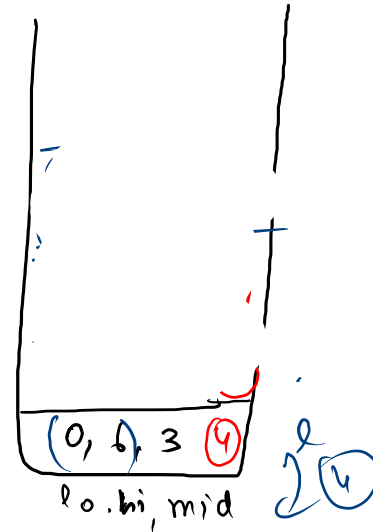


```

public static Node construct(int []inp, int lo, int hi){
    if(lo > hi){
        return null;
    }
    int mid = (lo+hi)/2;
    Node node = new Node(inp[mid]);

    node.left = construct(inp, lo, mid-1);
    node.right = construct(inp, mid+1, hi);

    return node;
}
  
```



```

public static int max(Node node) {
    if (node.right == null) {
        return node.data;
    }

    return max(node.right);
}

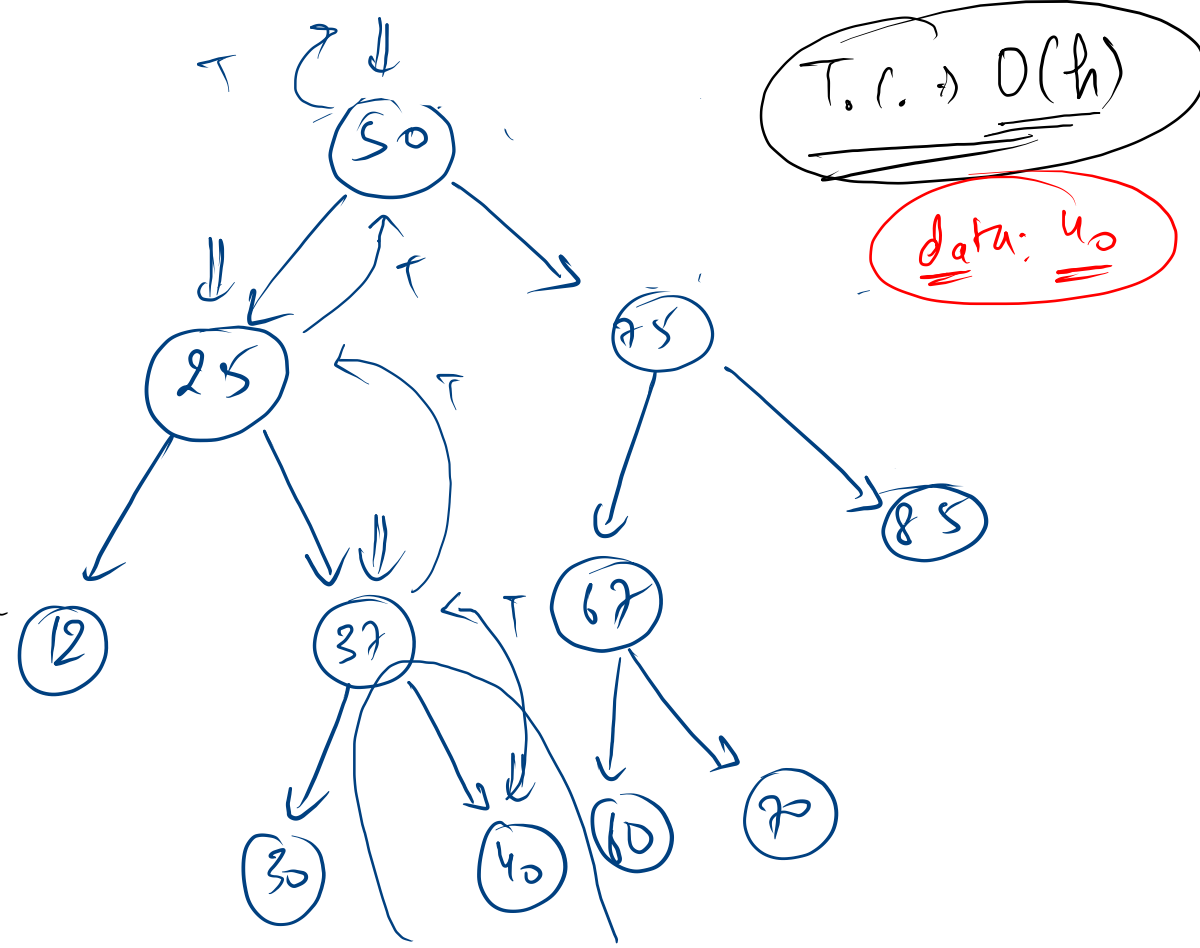
public static int min(Node node) {
    if (node.left == null) {
        return node.data;
    }

    return min(node.left);
}

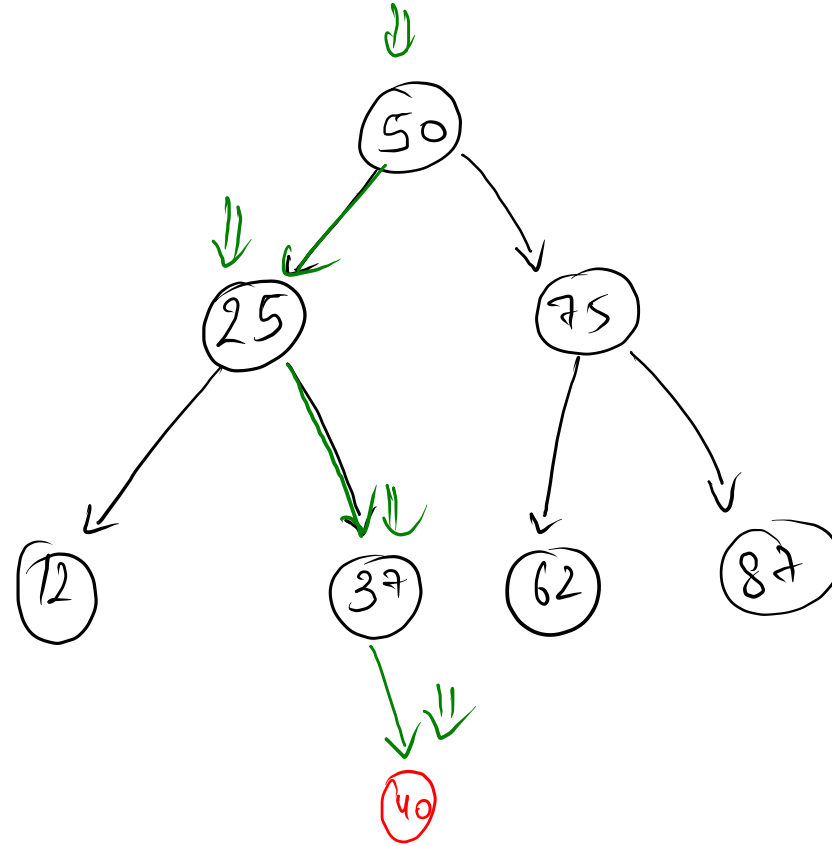
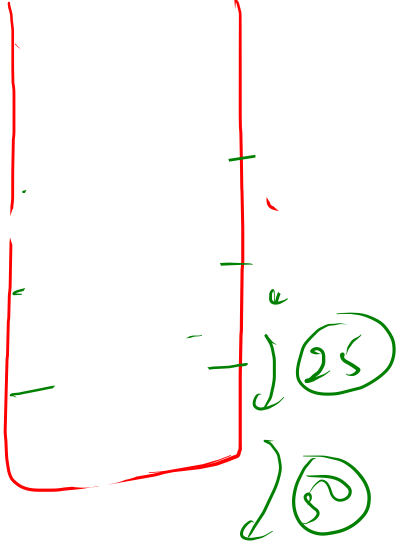
public static boolean find(Node node, int data) {
    if (node == null) {
        return false;
    }

    if (node.data == data) {
        return true;
    } else if (data > node.data) { // Larger -> right
        return find(node.right, data);
    } else { // smaller -> left
        return find(node.left, data);
    }
}

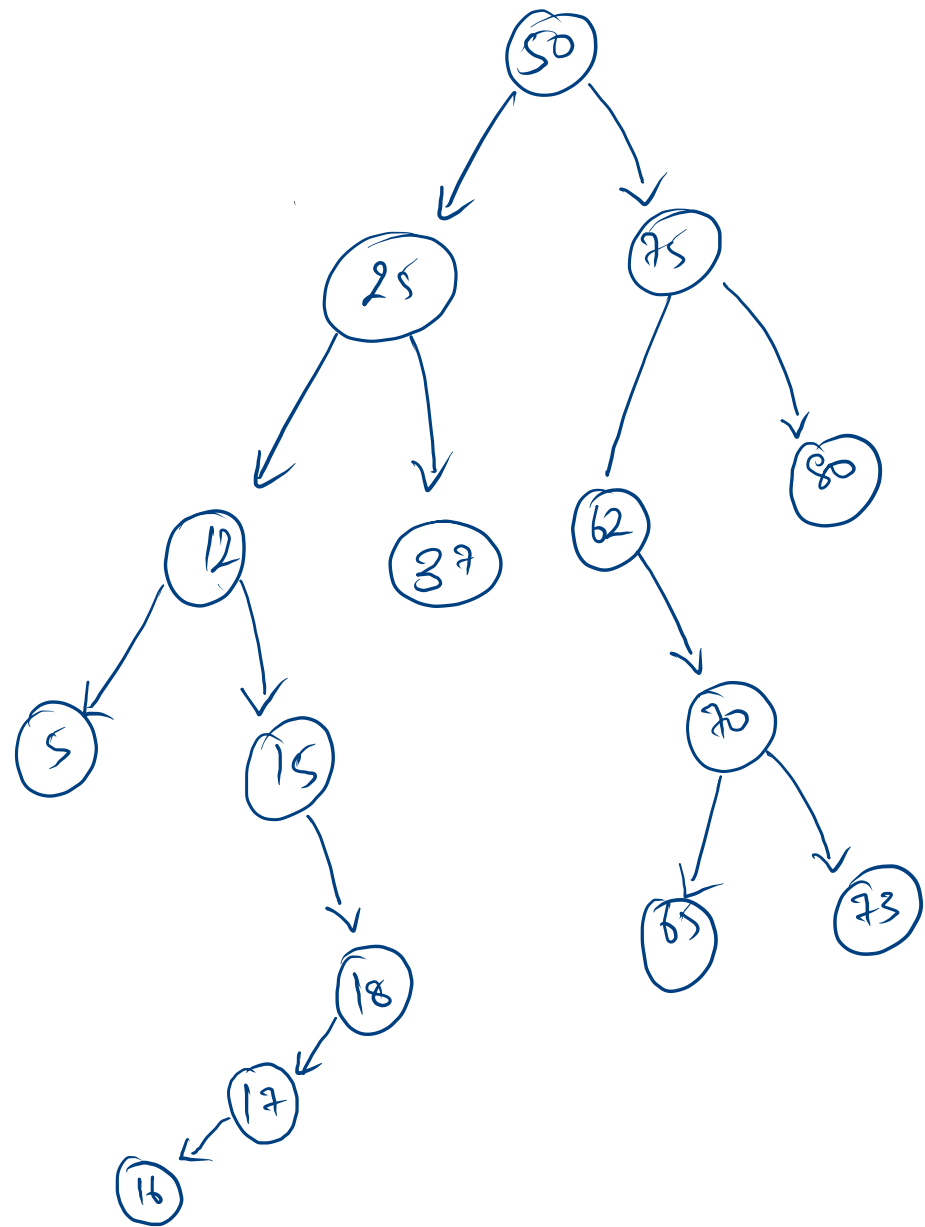
```



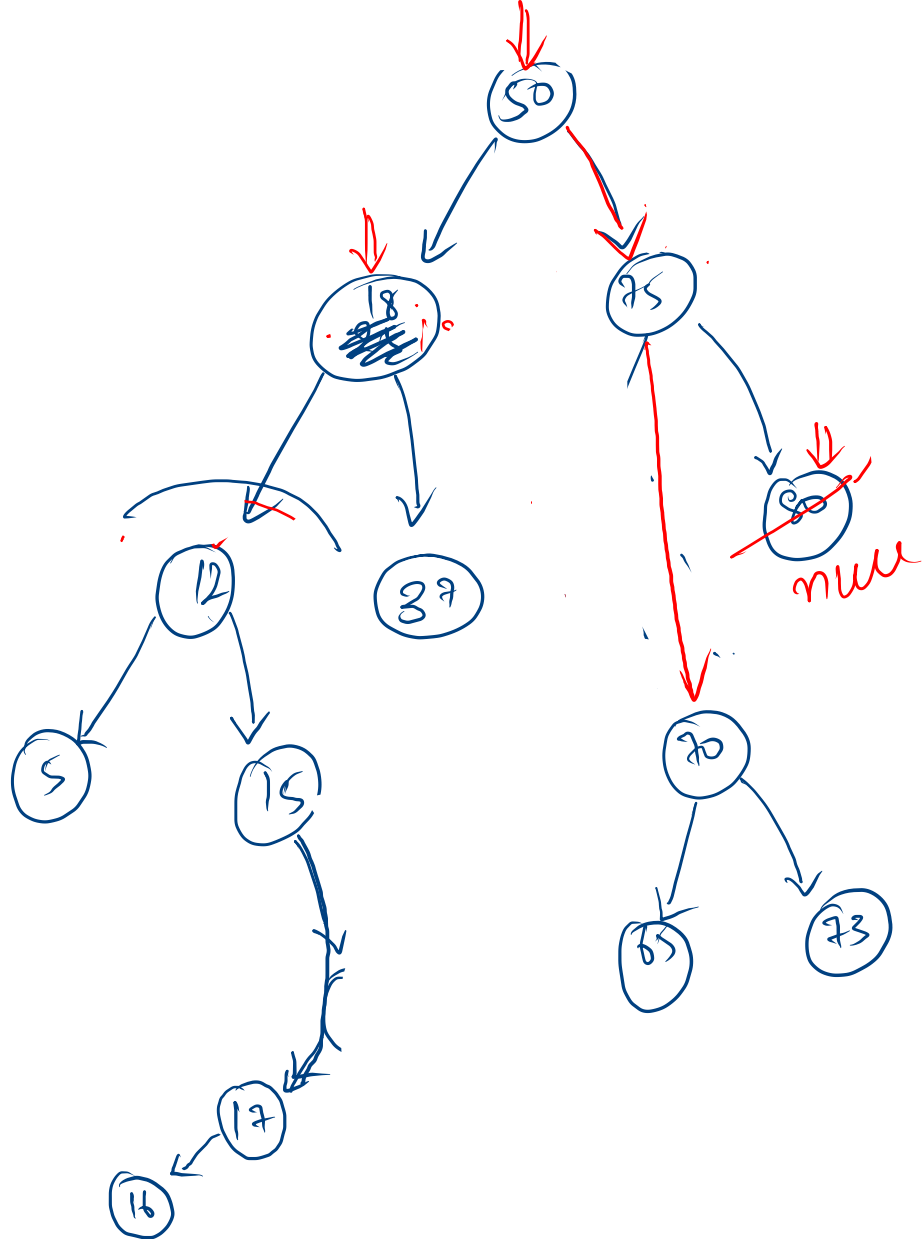
add 40



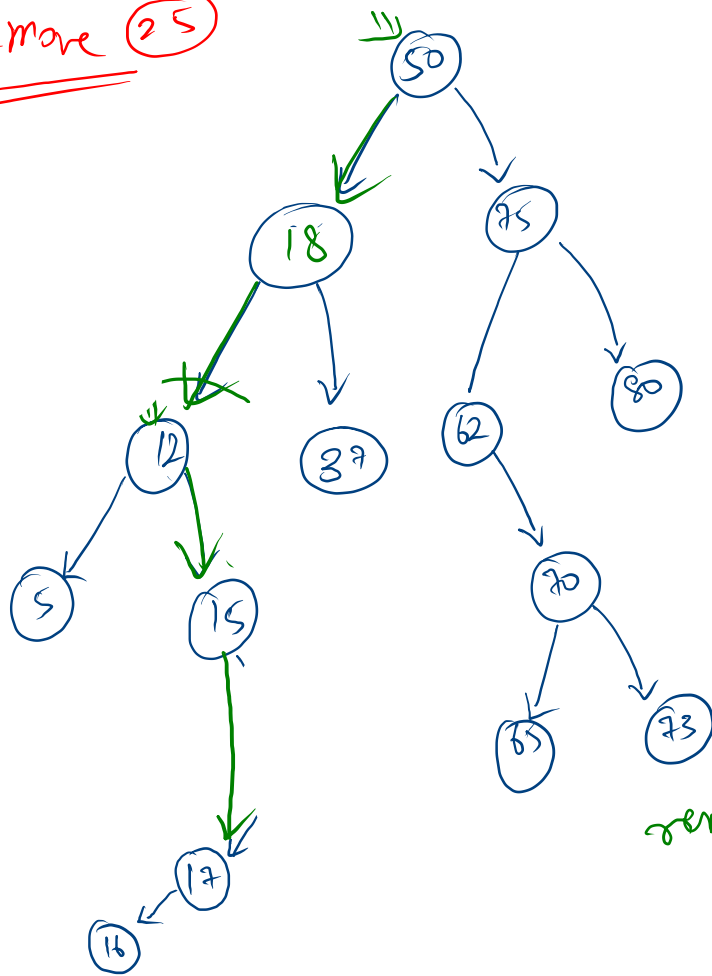
```
public static Node add(Node node, int data) {  
    if(node == null){  
        return new Node(data,null,null);  
    }  
  
    if(data > node.data){  
        node.right = add(node.right,data); → 1  
    }else if(data < node.data){  
        node.left = add(node.left,data); → 2  
    }  
  
    return node;  
}
```



✓ no child ✓ ⇒ (80) null
✓ 1 child ⇒ (62)
2 child ⇒ (25)



remove (25)

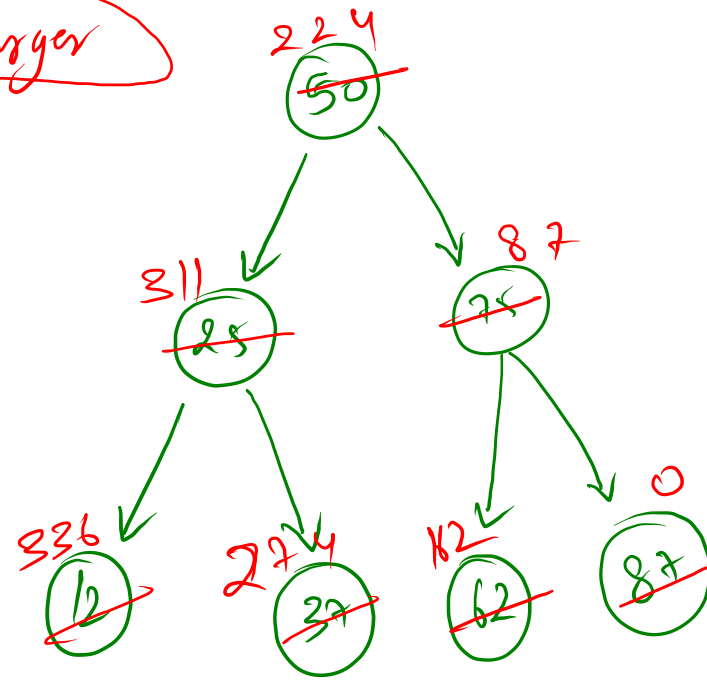


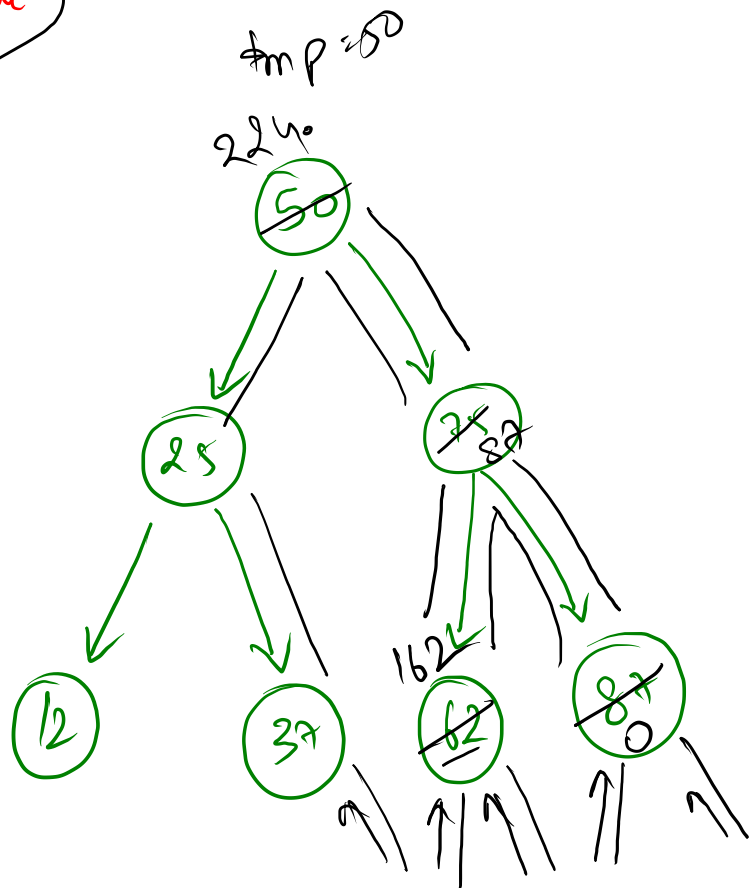
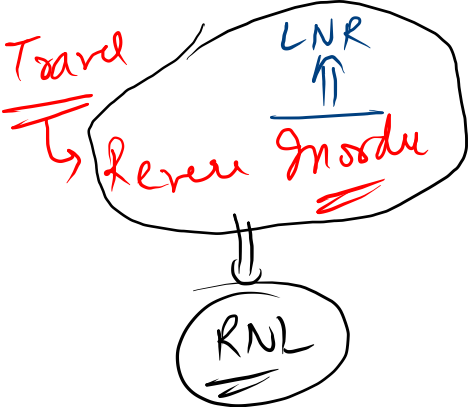
remove (25)

```
public static Node remove(Node node, int data) {  
    if(data > node.data){  
        node.right = remove(node.right,data); → 1  
    }else if(data < node.data){  
        node.left = remove(node.left,data); → 2  
    }else{  
        Node lchild = node.left;  
        Node rchild = node.right;  
  
        if(lchild == null && rchild == null){ // no child  
            return null;  
        }else if(lchild != null && rchild == null){ // only left child  
            return node.left;  
        }else if(lchild == null && rchild != null){ // only right child  
            return node.right;  
        }else{ //both child  
            int max = max(lchild);  
            node.data = max;  
            node.left = remove(lchild,max);  
            return node;  
        }  
    }  
    return node;  
}
```

50

Replace with sum of larger





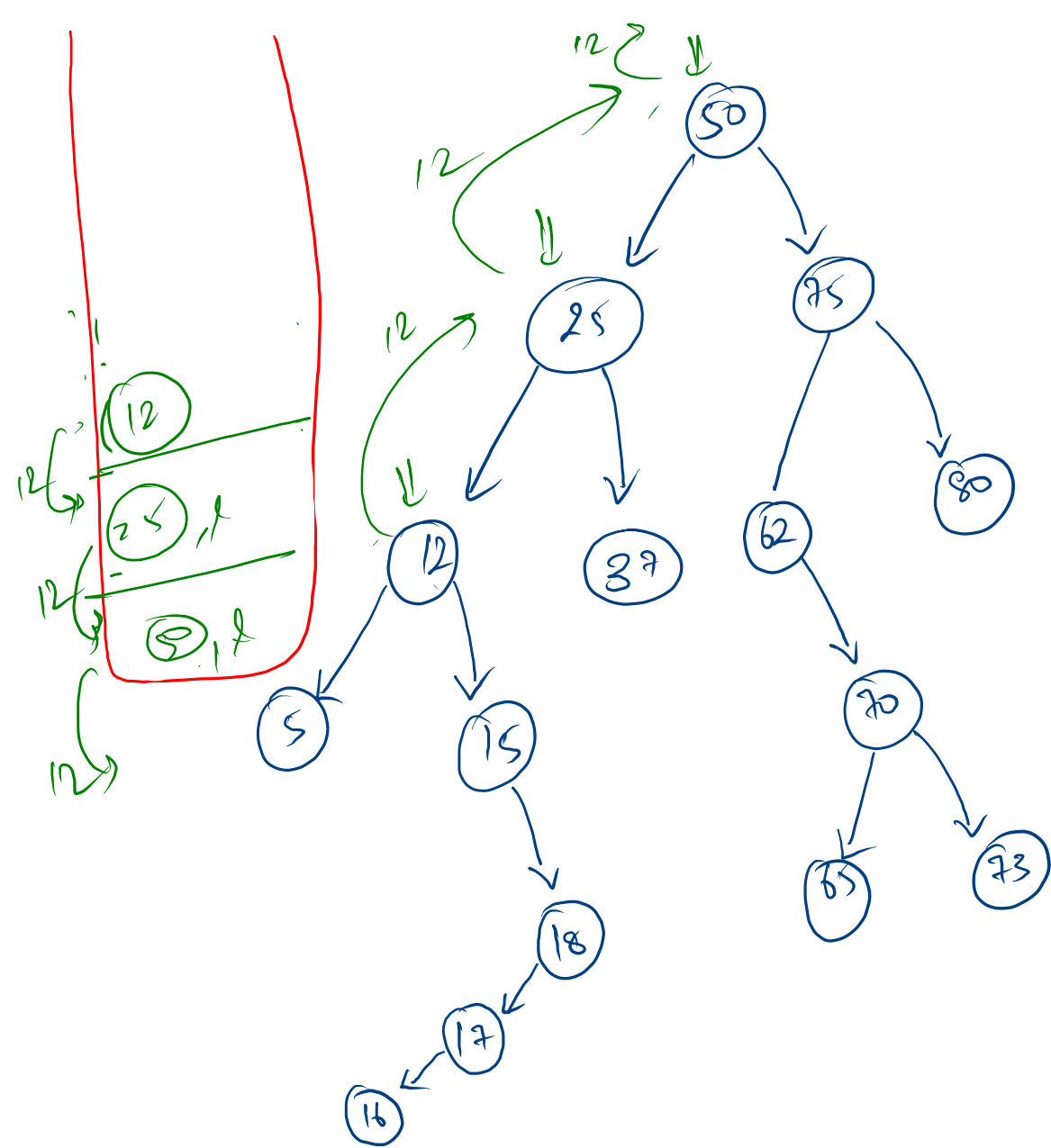
$$\text{Sum} = 0 + 87 + 75 + 62 + 50$$

logger

```
static int sum = 0;
public static void rwsol(Node node){
    if(node == null){
        return;
    }
    rwsol(node.right);

    int tmp = node.data;
    node.data = sum;
    sum += tmp;

    rwsol(node.left);
}
```



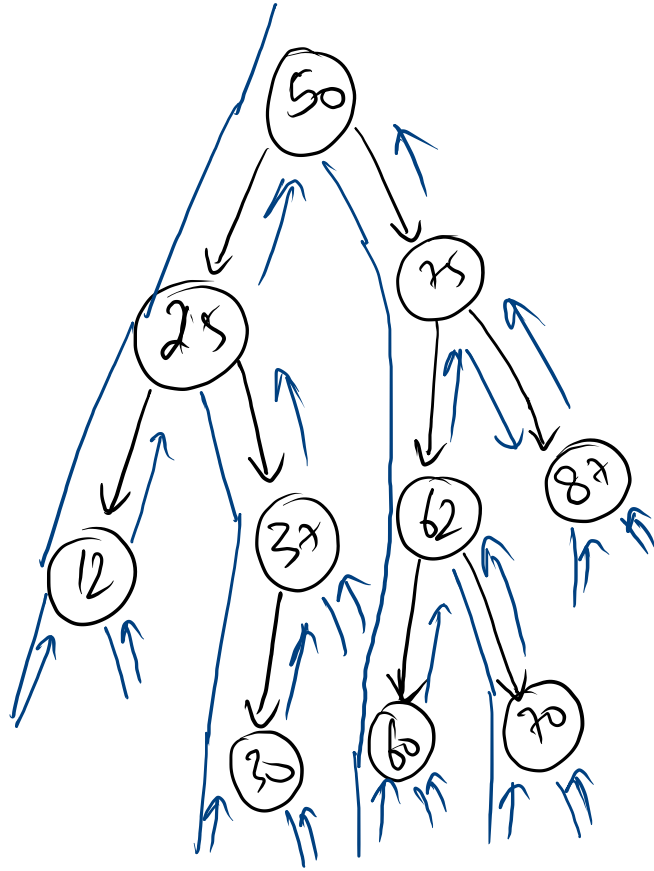
(LCA)

$d_1 = 5$

$d_2 = 15$

```

public static int lca(Node node, int d1, int d2) {
    if(d1 < node.data && d2 < node.data){
        return lca(node.left, d1, d2);
    } else if(d1 > node.data && d2 > node.data){
        return lca(node.right, d1, d2);
    } else{
        return node.data;
    }
}
  
```



✓ 25 25
✓ 30 30

	val	cval	<	Find
x	12	88	T	F
✓	25	75	T	T
✓	30	70	T	T
x	37	63	F	F
x	50	50	F	T
x	60	40	F	F
x	62	38	F	F
x	70	30	F	T
x	75	25	F	T
x	87	13	F	F

data ⇒ 100

100

```
public static void tsp(Node node, Node root, int total){
    if(node == null){
        return;
    }
    tsp(node.left, root, total);

    int val = node.data;
    int cval = total - node.data;
    if(val < cval && find(root, cval)){
        System.out.println(val+" "+cval);
    }
    tsp(node.right, root, total);
}
```