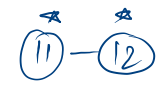
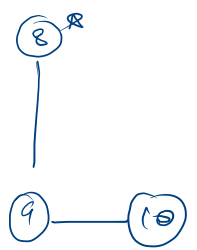
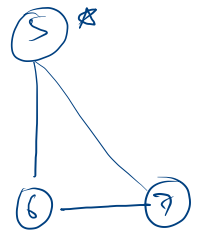
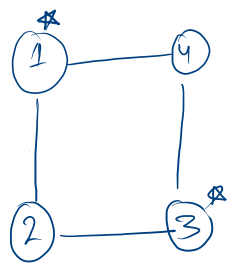


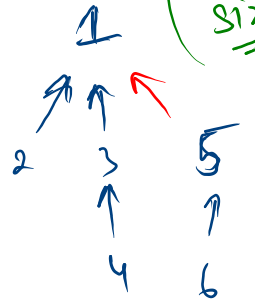
Minimize
Network
SPREAD



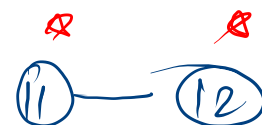
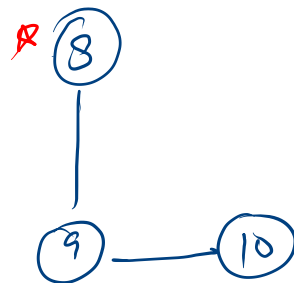
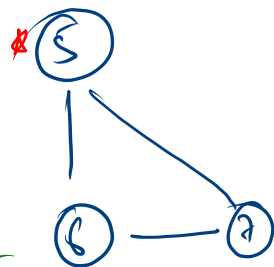
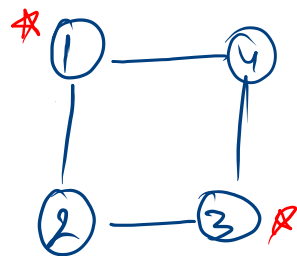
Infected $\rightarrow \{1, 3, 5, 8, 11, 12\}$

Power \rightarrow to disinfect a Person

(Union by Rank \leftrightarrow Union by Size)
(Par Size \rightarrow default = 1)

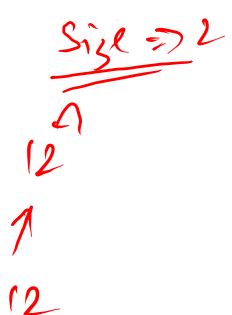
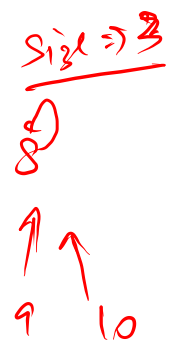
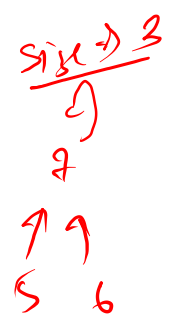
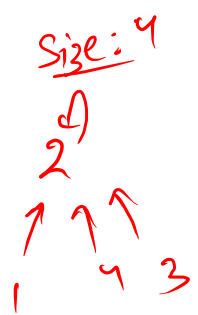


```
public static void Union(int x, int y) {
    int lx = find(x);
    int ly = find(y);
    if (lx != ly) {
        if (size[lx] >= size[ly]) {
            par[ly] = lx;
            size[lx] += size[ly];
        } else if (size[lx] < size[ly]) {
            par[lx] = ly;
            size[ly] += size[lx];
        }
    }
}
```



Injected $\Rightarrow \left\{ \begin{matrix} 2 & 2 & 7 & 8 & 12 & 12 \\ \uparrow & \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\ 1, & 3, & 5, & 5, & 11, & 12 \end{matrix} \right\}$

for size
DSU



5 ✓

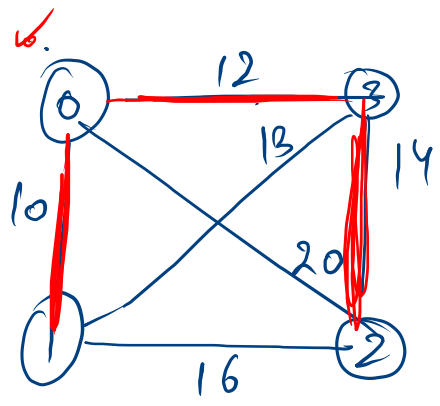
Injected v+x = 5
 Count = 3

Index		Injected Count
x	2	1 2
	7	1
	8	1
x	12	1 2

MST → Prim's

MST USING PO
 Graph

KRUSKAL → MST using DSU

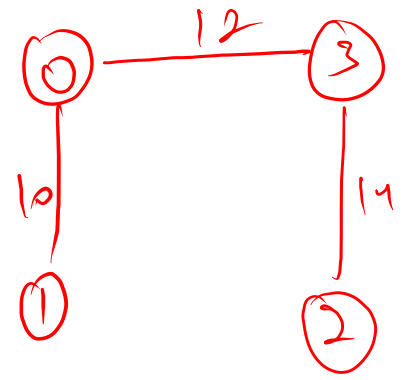


36

u	v	wt
0	3	12
1	3	13
0	2	20
3	2	14
1	2	16
0	1	10

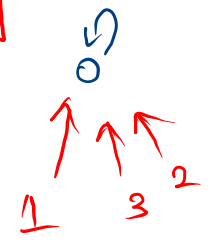
⇒

u	v	wt
✓ 0	1	10
✓ 0	3	12
1	3	13
✓ 3	2	14
1	2	16
0	2	20



Cost → 10 + 12 + 14

→ 36



0-1-10	✓
3-2-14	✓
0-3-12	✓
0-2-20	
1-3-13	X
1-2-16	

\checkmark 0 - 1 - 10 \checkmark
 \checkmark 0 - 3 - 12 \checkmark
 \checkmark 1 - 3 - 13 \times
 \checkmark 3 - 2 - 14 \checkmark
 \checkmark 1 - 2 - 16 \times
 \checkmark 0 - 2 - 20 \times



0 - 3 - 12
1 - 3 - 13
0 - 2 - 20
3 - 2 - 14
1 - 2 - 16
0 - 1 - 10

Cost: 0 + 10 + 12 + 14

```

public static void main (String[] args) throws java.lang.Exception
{
    Scanner scn = new Scanner(System.in);

    int vtces = scn.nextInt();
    int n = scn.nextInt();
    Edge edges[] = new Edge[n];
    for(int i = 0 ; i < n ; i++){
        int u = scn.nextInt();
        int v = scn.nextInt();
        int wt = scn.nextInt();
        edges[i] = new Edge(u,v,wt);
    }

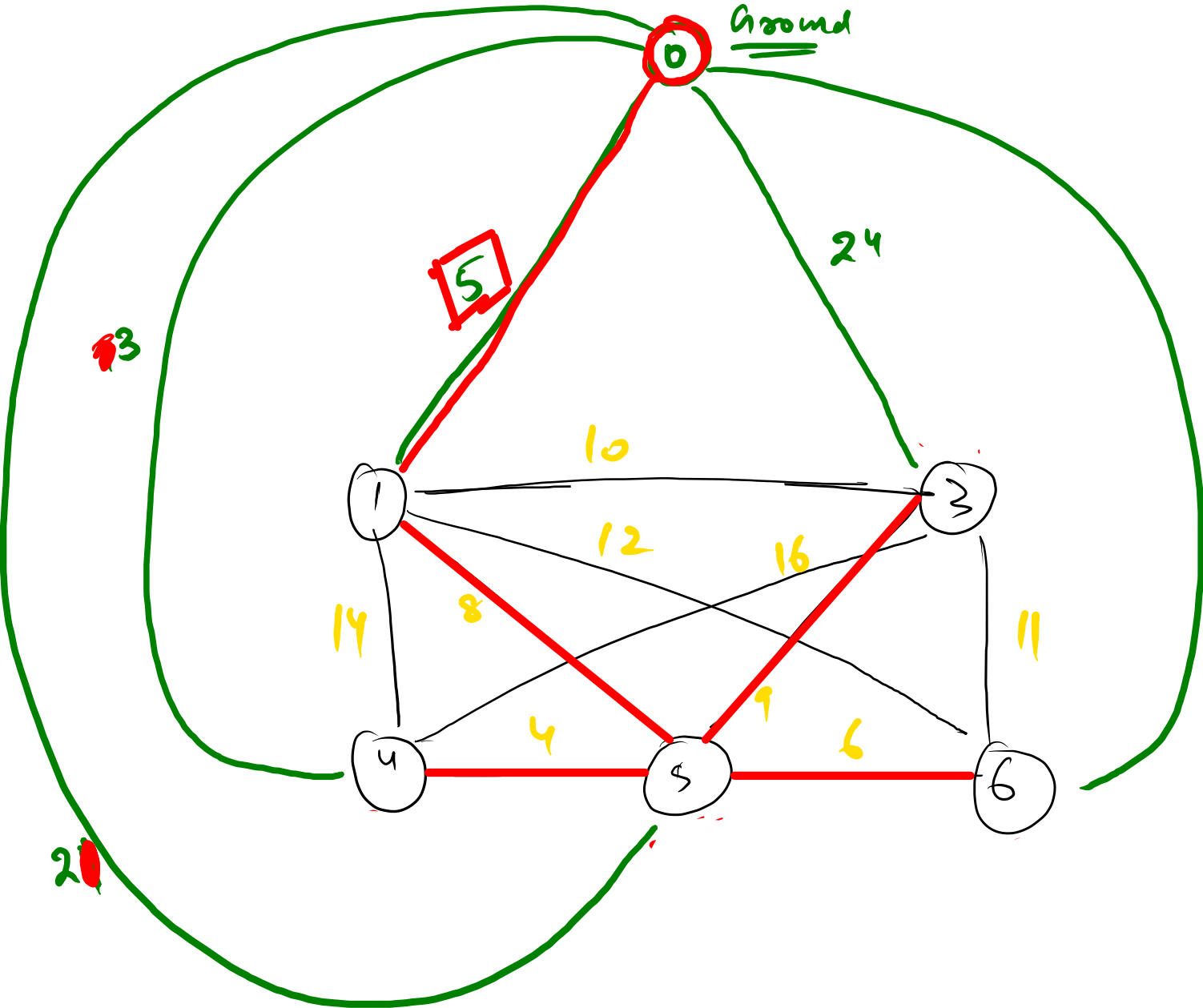
    Arrays.sort(edges);

    UnionFind uf = new UnionFind(vtces+1);
    long cost = 0;
    for(Edge e : edges){
        if(uf.union(e.u,e.v)){
            cost += e.wt;
        }
    }

    System.out.println(cost);
}

public boolean union(int vtx1,int vtx2){
    int rootv1 = find(vtx1);
    int rootv2 = find(vtx2);

    if(rootv1 != rootv2){
        int rankv1 = rank[vtx1];
        int rankv2 = rank[vtx2];
        if(rankv1 > rankv2){
            par[rootv2] = rootv1;
        }else if(rankv1 < rankv2){
            par[rootv1] = rootv2;
        }else{
            par[rootv2] = rootv1;
            rank[rootv1]++;
        }
        return true;
    }
    return false;
}
  
```



8

MST + choice
multiple choices

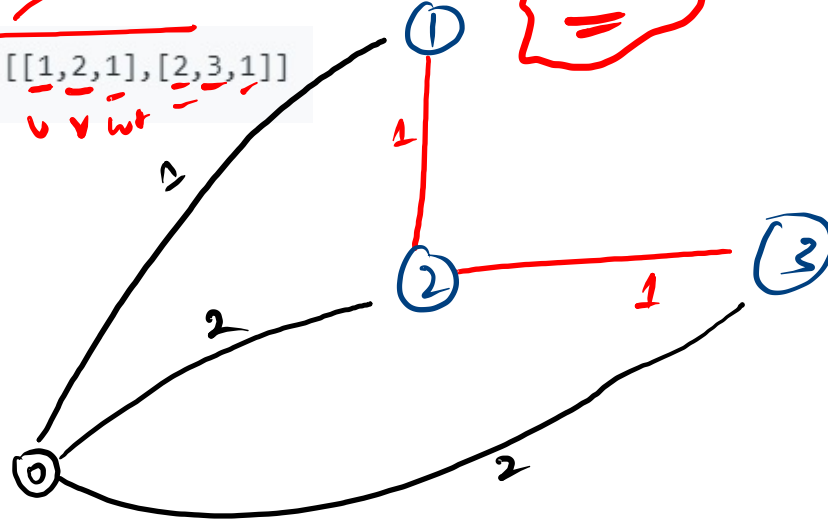
↓

MST =

1 2 3
wells = [1, 2, 2], pipes = [[1, 2, 1], [2, 3, 1]]

Level 1

H.W.



Graph

Transform

Wells

MST

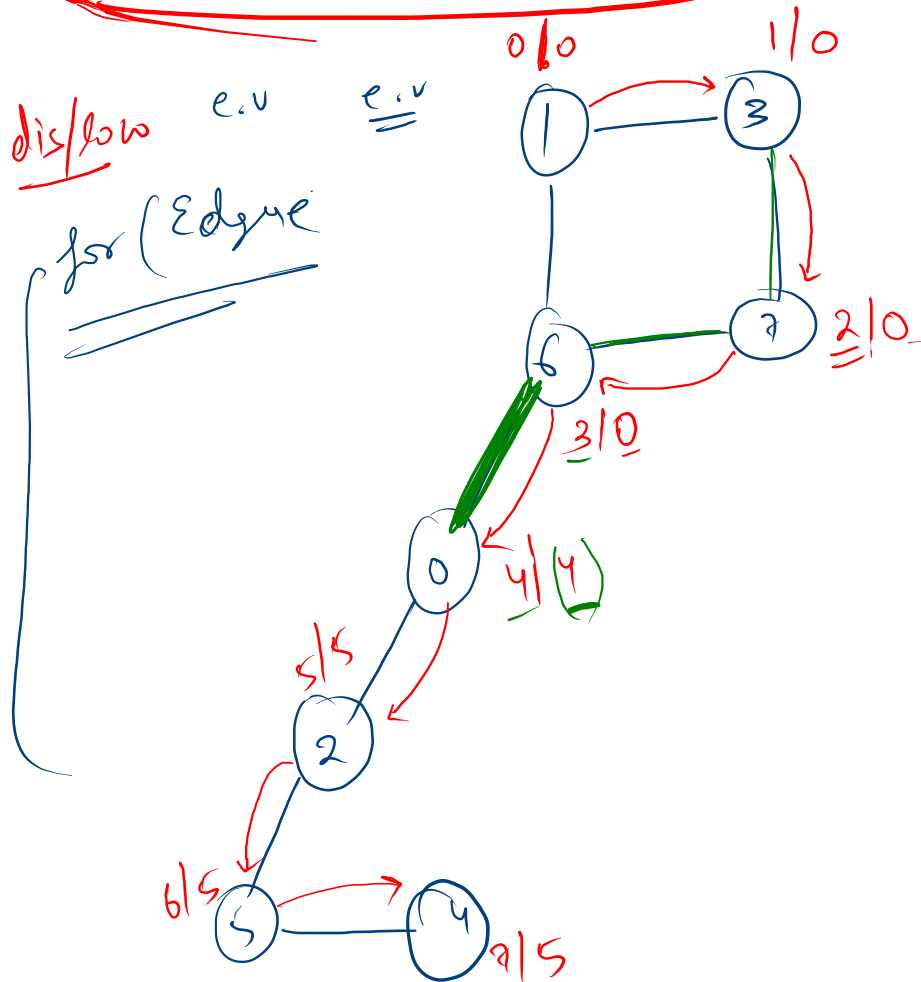
Prims ✓

Kruskal ✓

Level 1

Revision

ARTICULATION POINT :



A point which generates disconnected graph
if removed (1) Low, disc (2) AP

visited

Parent Continue

Non Parent

$low[u] = \min(low[u], disc[v])$

unvisited

djs call()

$\{ \text{if } (low[v] \geq disc[u]) \{$

$\text{ap}[u] = \text{true}$

$\text{low}[u] = \min(low[u], low[v])$