IIT Madras Instalnfluencer Fest '25

Hackerrank_link:

Background Story

It's March 2025, and after Shaastra, an **Instainfluencer Fest** is happening at IIT Madras for the first time! This fest is a massive gathering of GenZ influencers, content creators, and fans. Events range from viral dance-offs, meme competitions, podcast sessions, to live-streaming challenges. Each event depends on certain other events being completed first (e.g., you can't have the "Final Dance-Off" without completing the preliminary rounds).

However, drama unfolds when some influencers demand that certain events happen before others, creating complex dependencies. If there is a directed edge between event $u \to v$, then event u must be completed before v. The organizers need your help to:

- 1. Identify if any drama-induced cyclic dependencies exist.
- Find groups of tightly interdependent events (Strongly Connected Components) and the cardinality of the group with the maximal number of events.
- 3. Provide a valid order of events if possible.
- 4. Calculate the maximum "hype score" (don't worry it's described later) achievable from attending events in a valid path.

Problem Statement

You're given a **directed graph** representing events at Instalnfluencer Fest:

- Nodes represent events.
- **Directed edges** represent dependencies (event u must occur before event v).
 - Each event has an associated **"hype score**," indicating its popularity among IIT Madras students.

You must process queries of four types:

Query Type	Description
1	Check if the event schedule has any cyclic dependencies. Output "YES" if cycles exist; otherwise "NO".
2	Output the number of strongly connected components (SCCs) in the event dependency graph and the cardinality of the group with the maximal number of events.
3	Provide a valid topological order for the events if possible. Ensure that independent vertices are sorted lexicographically within their valid topological order. Incase of cycle output "NO".
4	Compute the maximum total hype score achievable by attending events. Identify all SCCs in the graph. Condense each SCC in a single vertex, summing the hypescores of all vertices within the SCC representing the hypescore of this vertex. Now find the path with maximum total hypescore achievable in the condensed graph.

^{*}A **Path** is a sequence of vertices connected by edges connecting two consecutive vertices in the sequence, and vertices are distinct(not repeated).

Input Format

- 1. The first line contains two integers N and M, representing the number of events and dependencies respectively.
- 2. The second line contains N integers h_1 , h_2 , ..., h_N , where h_i is the hype score of event i.
- 3. The next M lines each contain two integers u and v, indicating that event u must precede event v.
- 4. The next line contains an integer Q_t representing the number of queries.
- 5. The next Q lines contain one integer per line indicating query type (1, 2, 3 or 4).

Output Format

For each query:

- For query type 1: Output "YES" or "NO".
- For query type 2: Output two integers separated by space:
 - o The number of SCCs in the graph.
 - o The cardinality of the group with the maximal number of events.
- For query type 3: Output a valid topological order separated by spaces; otherwise output "NO" if no valid order exists due to cycles.
- For query type 4: Output an integer representing maximum total hype score achievable.

Constraints

 $1 \le N, M \le 10^5$

 $1 \le Q \le 10^5$

 $1 \le h_i \le 10^4$

NOTE: The vertices are numbered from 1 to N, where N is the number of vertices.

Requirements

Design Requirements:

- 1. Create a class <code>GraphAlgorithm</code> which has a pure virtual function <code>void Query()</code> that is overloaded by all child classes:
 - o isCycle: Detects cycles in the graph.
 - o indepComponent: Computes SCCs and their cardinalities.
 - validOrder: Computes a valid topological order if possible.
 - o maxHype: Computes maximum hype points on DAGs.
- 2. Implement a **Comparator Functor** .(Not mandatory)
- 3. Include explanatory comments or use self-explanatory variable and function names.

Sample Test Cases

Test Case 1:

Input:

4 4

10 20 30 40

- 1 2
- 2 3
- 3 1
- 3 4
- 4
- 1
- 2
- 3
- 4

Output:

YES

2 3

NO

100

Explanation:

- Query Type 1: A cycle exists $(1 \rightarrow 2 \rightarrow 3 \rightarrow 1)$, so output "YES".
- Query Type 2: Two SCCs are found: $\{1,2,3\}$ with cardinality 3, and $\{4\}$ with cardinality 1. Output is 2 3.
 - Query Type 3: Topological sorting is impossible due to cycles, so output "NO".
- Query Type 4: Maximum hype score comes from attending $\{(1->2->3)->4\}$, which has a hype score of 60+40=100. (1->2->3) is a SCC.

Test Case 2:

Input:

8 8

10 20 10 10 30 40 10 20

- 1 2
- 1 5
- 2 3
- 3 4
- 5 6

```
5 7
```

7 3

7 8

4

4

3

1

2

Output:

80

1 2 5 6 7 3 4 8

NO

8 1

Explanation:

- Query Type 4: Maximum hype score is for the path {1-> 5-> 6} i.e. 80.
- Query Type 3: A valid topological order exists: 1->2->5->6->7->3->4->8. Since there is no cycle. Output is 1 2 5 6 7 3 4 8. After 1->2, there are two possible ways 3,5, but 3 cant be chosen as before 3,7 should be processed, thus will go with 5. similarly we'll process the graph.
- Query Type 1: No cycles exist; output "NO".
- \bullet Query Type 2: All the vertices are individual SCC this number of SCC is 8 and max cardinality is 1.