

declaration of linked list :-

In linked list, one is variable and second one is pointer variable. we can declare linked list by using user-defined data type called as structure.

```
struct node
```

```
{
```

```
    int data;
```

```
    struct node *next;
```

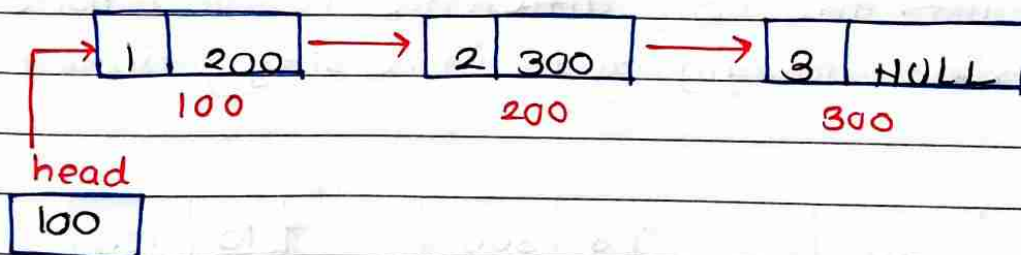
```
}
```

Types of linked list :-

1) singly linked list :-

The singly linked list is most common which consists of data part and address part. The address part in the node is known as a pointer.

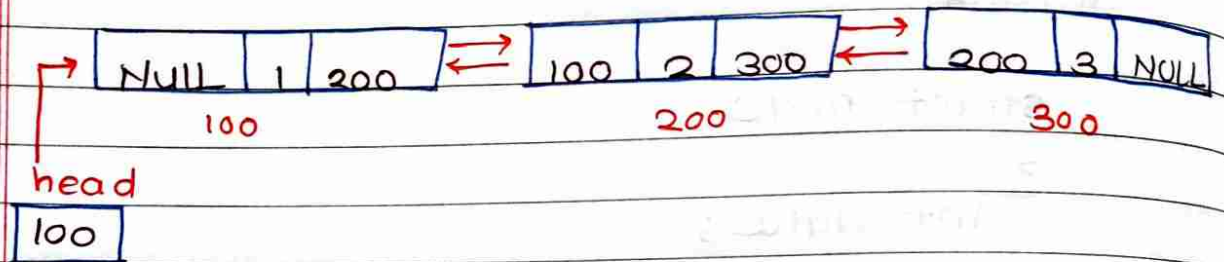
Example :- suppose we have three nodes and addresses of these three nodes are 100, 200 and 300 :



NULL means its address part does not point to any node. The pointer that holds the address of the initial node is known as a head pointer.

2. Doubly linked list :-

As name suggests, the doubly linked list contains two pointers. We define it in three parts the data part and the two address part.



Representation of doubly linked list :-

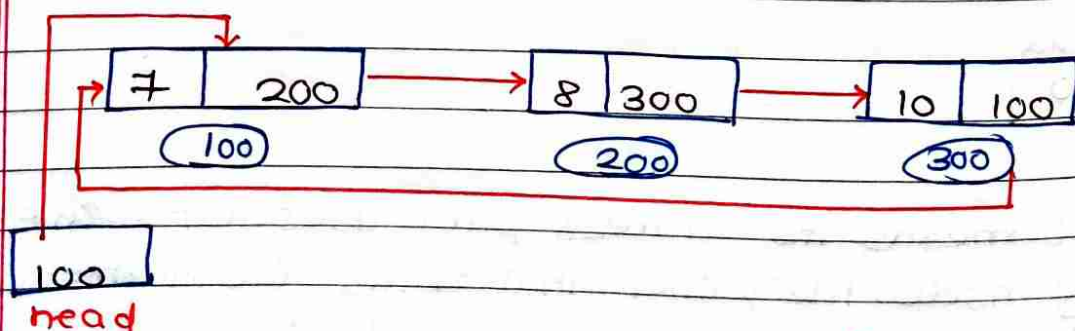
struct node

```

{
    int data ;
    struct node * next ;
    struct node * prev ;
}
    
```

3. Circular linked list :-

A circular linked list is a variation of a singly linked list. The only difference is "last node does not point to any node in a singly linked list".

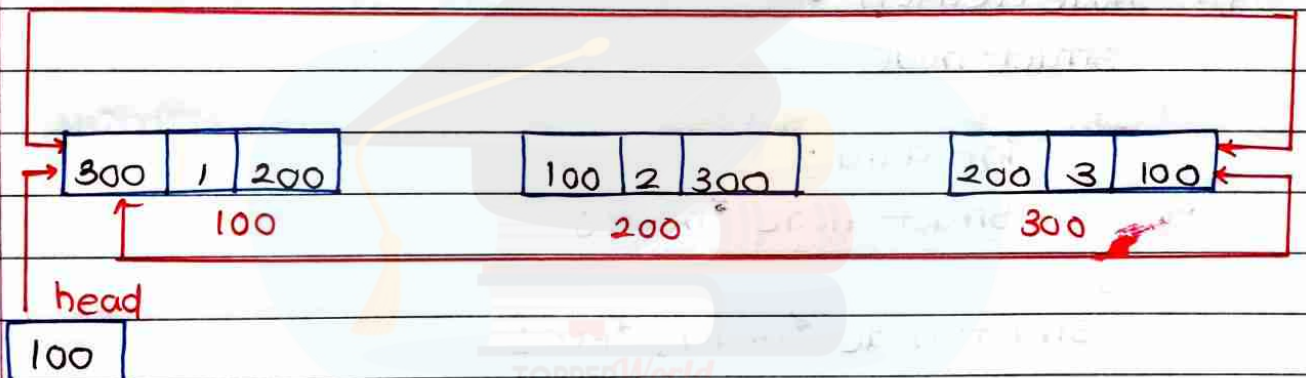


Representation of circular linked list :-

```
struct node
{
    int data;
    struct node *next;
}
```

4. Doubly circular linked list :-

The doubly circular linked list has the features of both the circular linked list and doubly linked list.



The last node is attached to the first node and thus creates a circle.

The main difference is that doubly circular linked list does not contain NULL value in previous field of the node.

Representation of doubly circular linked list :-

```
struct node
{
    int data;
    struct node *next;
    struct node *prev;
}
```

Complexity :-

	Average	Space complexity
Singly linked list	Access $O(n)$ search $O(n)$ Insertion $O(1)$ deletion $O(1)$	Worst $O(n)$
	Worst	
singly linked list	Access $O(n)$ search $O(n)$ Insertion $O(1)$ deletion $O(1)$	

Operations on singly linked list :-

1). Node creation :-

```
struct node
```

```
{
```

```
    int data;
```

```
    struct node *next;
```

```
};
```

```
struct node *head, *ptr;
```

```
ptr = (struct node *) malloc (sizeof (struct node *));
```

2). Insertion :-

① Insertion at beginning :- It involves inserting any element at the front of the list. We just need a few link adjustment to make new node as head of list.

② Insertion at end of list :- The new node can be inserted as the only node in the list / it can be inserted as last one.

③ Insertion after specified node :- we need to skip desired number of nodes in order to reach node after which the new node will be inserted.

3) 3). Deletion and Traversing :-

①. Deletion at beginning :- It just needs few adjustments in the node pointers

②. Deletion at end of list :- The list can either be empty or full. Different logic is implemented for different scenarios.

Traversing :- In traversing, we simply visit each node of the list at least once in order to perform some specific operation in it, for example, printing data part of each node present in the list.

Searching :- In searching, we match each element of the list with the given element. If the element is found on any of the location, that element is returned otherwise null is returned.

Operations on doubly linked list :-

1) Node creation :-

```
struct node
```

```
{
```

```
    struct node *prev;
```

```
    int data;
```

```
    struct node *next;
```

```
};
```

```
struct node *head;
```

2) Insertion :-

①. Insertion at beginning :- Adding the node into the linked list at beginning.

②. Insertion at end :- Adding the node into the linked list to the end.

3>. Deletion and Traversing :-

① Deletion at beginning :- Removing the node from beginning of the list.

② Deletion at end :- Removing the node from end of the list.

Traversing :- visiting each node of the list at least once in order to perform some specific operation like searching, sorting, display etc.

Searching :- comparing each node data with the item to be searched and return location of the item in the list if the item found else return null.

Skip list :-

* What is a skip list ?

A skip list is a probabilistic data structure. The skip list is used to store a linked list of elements or data with a linked list. In one single step, it skips several elements of the entire list, which is why it is known as skip list.

Structure of skip list :-

skip list is built in two layers: The lowest layer and the top layer. The lowest layer of the skip list is a common sorted linked list, and the top layers of the skip list are the like an "express line" where elements are skipped.

complexity table :-

Sr.No.	complexity	Average case	Worst case
1).	Access complexity	$O(\log n)$	$O(n)$
2).	search comple.	$O(\log n)$	$O(n)$
3).	delete comple.	$O(\log n)$	$O(n)$
4).	Insert comple.	$O(\log n)$	$O(n)$
5).	space comple.	-	$O(n \log n)$

Basic operations and its algorithms :-

- 1). Insertion operation :- It is used to add new node to a particular location in a specific situation.
- 2). Deletion operation :- It is used to delete a node in a specific situation.
- 3). search operation :- The search operation is used to search a particular node in a skip list.

Algorithm of insertion operation :-

Insertion (L, key)

local update [0 ... max-level + 1]

$q = L \rightarrow \text{header}$

for $i = L \rightarrow \text{level down to } 0$ do.

while $q \rightarrow \text{forward}[i] \rightarrow \text{key} < \text{forward}[i]$

update $[i] = a$


```

a = a → forward[0]
IV = random-level()
if IV > L → level then
for i = L → level + 1 to IV do
    update[i] = L → header
L → level = IV
a = make node (IV, key, value)
for i = 0 to level do
    a → forward[i] = update[i] → forward[i]
update[i] → forward[i] = a
    
```

Algorithm of deletion operation :-

```

Deletion (L, key)
local update [0... max level + 1]
a = L → header
for i = L → level down 0 to do
    while a → forward[i] → key forward[i]
        update[i] = a
a = a → forward[0]
if a → key = key then
    for i = 0 to L → level do
        if update[i] → forward[i] ? a then break
        update[i] → forward[i] → forward[i]
    free(a)
while L → level > 0 and L → header → forward[L → level]
    = NIL do
    L → level = L → level - 1
    
```


Algorithm of searching operation :-
searching (L, Skey)

$a \leftarrow L \rightarrow \text{header}$

loop invariant : $a \rightarrow \text{key level down to 0 do}$

while $a \rightarrow \text{forward}[i] \rightarrow \text{key forward}[i]$

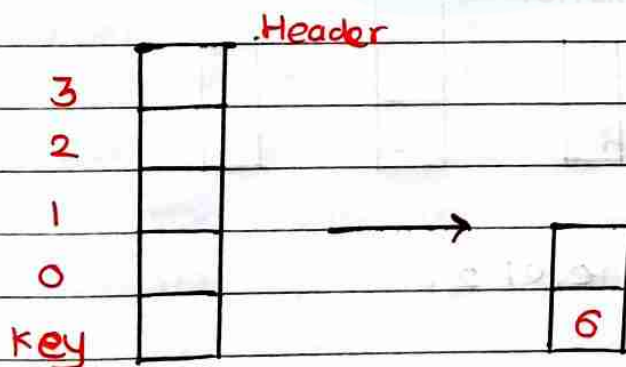
$a \leftarrow a \rightarrow \text{forward}[a]$

if $a \rightarrow \text{key} = \text{Skey}$ then return $a \rightarrow \text{value}$
else return failure.

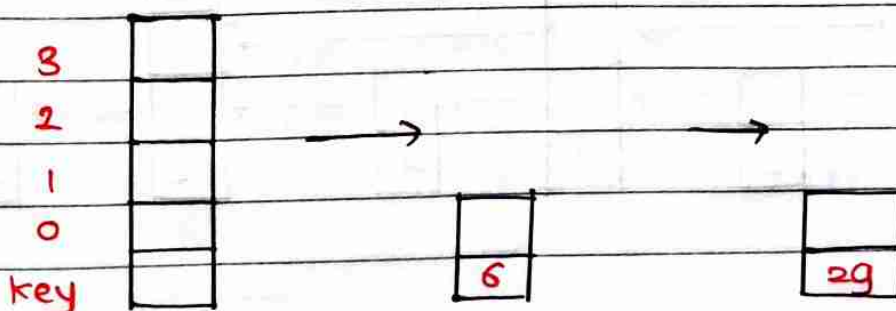
Example : create a skip list, we want to insert those following keys in empty skip list

1. 6 with level 1
2. 29 with level 1
3. 22 with level 4.
4. 9 with level 3.
5. 17 with level 1.
6. 4 with level 2.

→ Solution :- Insert 6 with level 1.

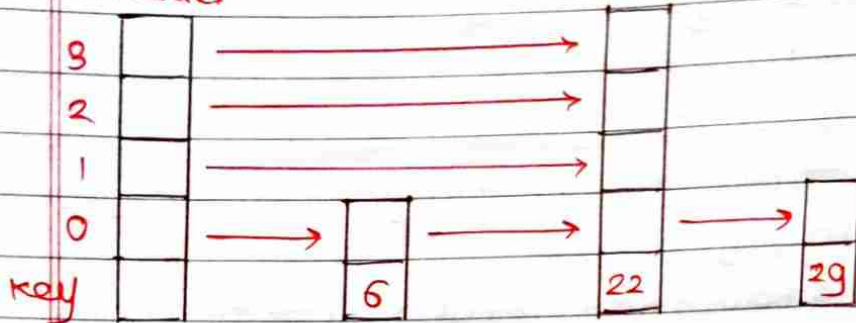


step 2 :- Insert 29 with level 1.

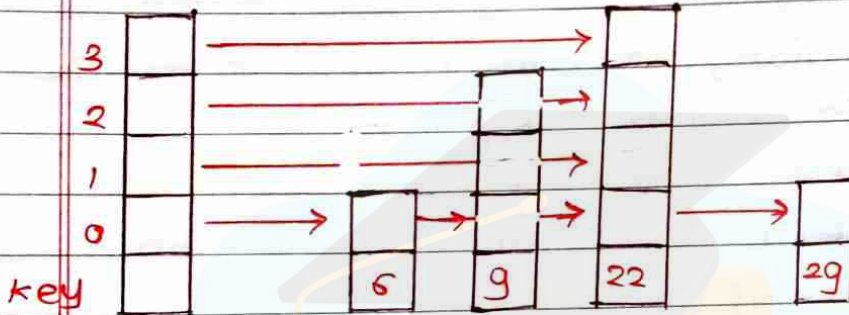


Step 3: Insert 22 with level 4.

Header

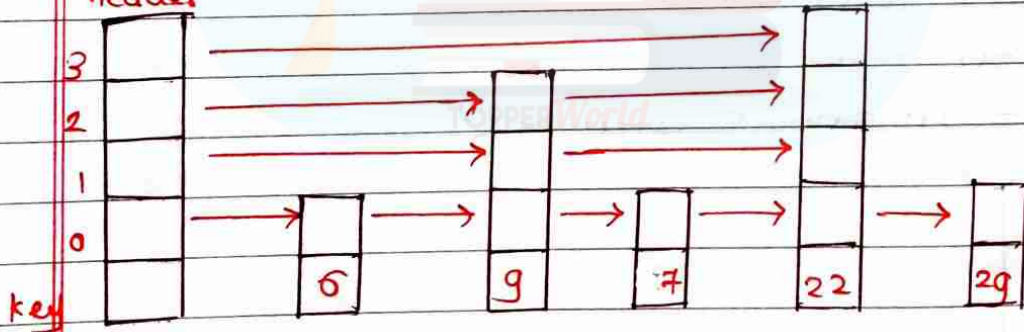


Step 4: Insert 9 with level 3.



Step 5: Insert 17 with level 1

header



Step 6: Insert 4 with level 2.

header

