

Mid Term Exam

1. Write code to create a **directed** graph with **100 nodes** where each node is numbered between **2** and **101**. There exists an edge from **node-A** to **node-B** if **node-B** is a multiple of **node-A**. **10**

For example, the node **50** should have directed edges to node **50** and node **100**. (as both 50 and 100 are multiples of 50)

Use **adjacency list** as your graph representation.

2. Can you draw the graph in **problem-1** for **10** nodes where all nodes are numbered from **2** to **11**.

Will this graph be a **DAG** if there are a million nodes? Why or why not?

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3. Can you find the length of the **longest path** in **problem-1**?

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What graph traversal would you use? Can it be solved with both **BFS** and **DFS**?

Finally, **write code** to print the longest path.

4. Given a positive integer **n**, write a **recursive** function to print all combinations of numbers between **1** and **n** having sum **n**.

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For example,

For **n = 5**, the following combinations are possible:

- { 5 }
- { 1, 4 }
- { 2, 3 }
- { 1, 1, 3 }
- { 1, 2, 2 }
- { 1, 1, 1, 2 }
- { 1, 1, 1, 1, 1 }

5. Write code to solve the following problem: [SPOJ.com - Problem ABCPATH](https://www.spoj.com/problems/ABCPATH/)

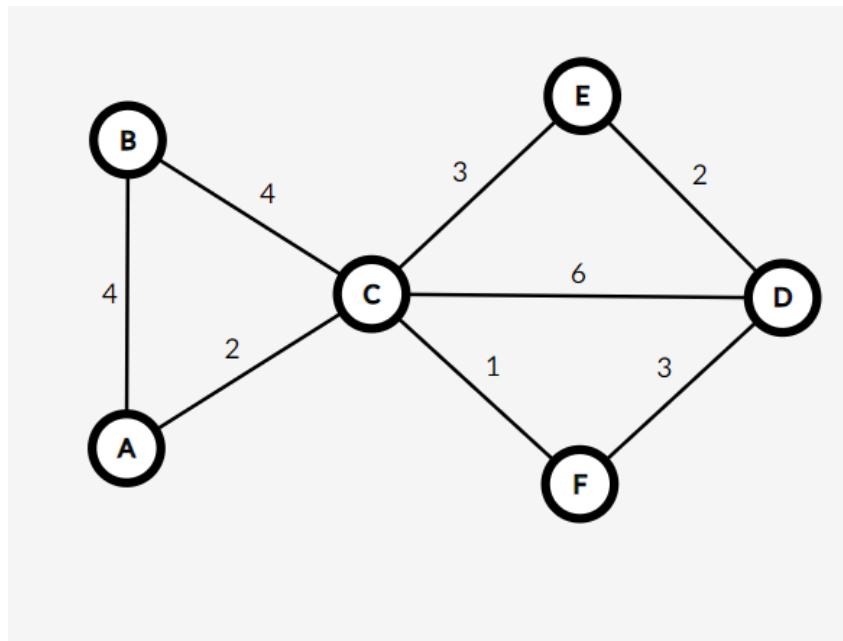
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6. Write code to solve the following problem: [Problem - 580C - Codeforces](#)
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7. Write code to solve the following problem: [Country Roads | LightOJ](#)
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8. Simulate Dijkstra's algorithm (the optimised version) on the following graph:
Use node-B as source.

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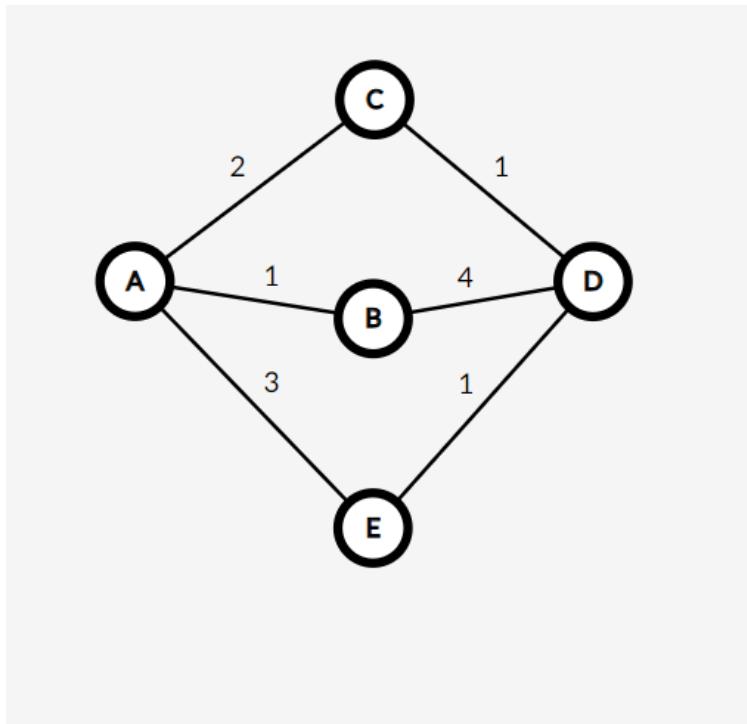
9. We know that in a **weighted graph**, we can detect the **smallest distance** of a node from the source node using **Dijkstra's algorithm**. But can we detect the **2nd smallest distance** of a node from the source node?

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For example, in the following graph the **smallest distance** from node-A to node-D is **3** if we take the path **A -> C -> D**

But the **2nd smallest distance** from node-A to node-D is **4** if we take the path **A -> E -> D**

How can you modify **Dijkstra's algorithm** to solve this problem? (code is not needed.
You can write your idea or pseudocode)



10. Will **Dijkstra's** algorithm give correct output for the following graph?

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Why or why not? The source node is **node-A** and the destination is **node-B**.

