The MiniJava Type System

1 What is MiniJava?

MiniJava is a subset of Java. The meaning of a MiniJava program is given by its meaning as a Java program. Overloading is not allowed in MiniJava. The MiniJava statement System.out.println(...); can only print integers. The MiniJava expression e.length only applies to expressions of type int[].

We will now specify MiniJava's syntax and type system. A MiniJava program will type check with the MiniJava type system (as specified below) if and only if it will type check with the Java type system (as specified in the Java Language Specification).

2 Syntax

The grammar below uses the following metanotation:

- Nonterminal symbols are words written in this font.
- Terminal symbols are written in this font, except (IDENTIFIER) and (INTEGER_LITERAL).
- A production is of the form lhs := rhs, where lhs is a nonterminal symbol and rhs is a sequence of nonterminal and terminal symbols, with choices separated by |, and some times using "..." to denote a possibly empty list.
- We will use superscripts and subscripts to distinguish metavariables.

3 Notation for Rules

We will use the following notation:

$$\frac{hypothesis_1}{conclusion} \qquad \frac{hypothesis_2}{conclusion} \dots \quad hypothesis_n$$

This is a *rule* that says that if we can derive all of $hypothesis_1$, $hypothesis_2$, ..., $hypothesis_n$, then we can also derive conclusion.

A special case arises when n = 0: we can write this case as:

 $\overline{conclusion}$

or we can even omit the horizontal bar and write:

conclusion

We can say that this case is a rule with no hypotheses, or we can call it an axiom.

A *derivation* happens when we begin with one or more axioms, then perhaps apply some rules, and finally arrive at a conclusion. Notice that we can organize a derivation as a tree that has the axioms as leaves and the conclusion as the root. We can refer to such as tree as a *derivation tree*.

4 Subtyping

We now define a *subtype* relation on class names. We use \leq to denote the subtype relation. We $t_1 \leq t_2$, we say that t_1 is a subtype of t_2 . We define that \leq is reflexive and transitive, and generated by the "extends" relation among classes.

$$t \le t \tag{1}$$

$$\frac{t_1 \le t_2 \qquad t_2 \le t_3}{t_1 < t_3} \tag{2}$$

$$\frac{\text{class } C \text{ extends } D \dots \text{ is in the program}}{C \le D} \tag{3}$$

5 Type Environments

A type environment is a finite mapping from identifiers to types. We use A to range over type environments. We use dom(A) to denote the domain of A. If id_1, \ldots, id_r are pairwise distinct identifiers, then the notation $[id_1:t_1,\ldots,id_r:t_r]$ denotes a type environment that maps id_i to t_i , for $i \in 1...r$. If A_1, A_2 are type environments, then $A_1 \cdot A_2$ is a type environment defined in the following way:

$$(A_1 \cdot A_2)(id) = \begin{cases} A_2(id) & \text{if } id \in dom(A_2) \\ A_1(id) & \text{otherwise} \end{cases}$$
 (4)

Notice that A_2 takes precedence over A_1 .

6 Helper Functions

6.1 The classname Helper Function

The function *classname* returns the name of a class. The definition of *classname* is:

$$classname(class\ id\ \{\ public\ static\ void\ main\ (String\ []\ id^S)\ \{\dots\}\})=id$$
 (5)

$$classname(\texttt{class}\ id\ \{\ t_1\ id_1;\ \ldots;\ t_f\ id_f;\ m_1\ \ldots\ m_k\ \}) = id \tag{6}$$

$$classname(class\ id\ extends\ id^P\ \{\ t_1\ id_1;\ \ldots;\ t_f\ id_f;\ m_1\ \ldots\ m_k\ \}) = id$$
 (7)

6.2 The methodname Helper Function

The function methodname returns the name of a method definition. The definition of methodname is:

$$methodname(public\ t\ id^M\ (...)\ ...) = id^M$$
 (8)

6.3 The distinct Helper Function

The distinct function checks that the identifiers in a list are pairwise distinct.

$$\frac{\forall i \in 1..n : \forall j \in 1..n : id_i = id_j \Rightarrow i = j}{distinct(id_1, \dots, id_n)}$$

$$(9)$$

6.4 The fields Helper Function

We use the notation fields(C) to denote a type environment constructed from the fields of C and the fields of the superclasses of C. The fields in C take precedence over the fields in the superclasses of C. The definition of fields is:

$$\frac{\text{class } id \ \{ \ t_1 \ id_1; \ \dots; \ t_f \ id_f; \ m_1 \ \dots \ m_k \ \} \quad \text{is in the program}}{fields(id) = [id_1:t_1,\dots,id_f:t_f]}$$
(10)

$$\frac{\text{class } id \text{ extends } id^P \ \{ \ t_1 \ id_1; \ \dots; \ t_f \ id_f; \ m_1 \ \dots \ m_k \ \} \text{ is in the program}}{fields(id) = fields(id^P) \cdot [id_1 : t_1, \dots, id_f : t_f]}$$
(11)

6.5 The methodtype Helper Function

We use the notation $method type(id, id^M)$ to denote the list of argument types of the method with name id^M in class id (or a superclass of id) together with the return type (or \bot if no such method exists). The result of method type is of the form $(t_1, \ldots, t_n) \to t$, or \bot . The definition of method type is:

class
$$id \ \{ \dots m_1 \dots m_k \ \}$$
 is in the program for some $j \in 1..k : methodname(m_j) = id^M$
 m_j is of the form public $t id^M$ $(t_1^F id_1^F, \dots, t_n^F id_n^F)$ $\{t_1 id_1; \dots; t_r id_r; s_1 \dots s_q \text{ return } e; \}$
 $methodtype(id, id^M) = (id_1^F : t_1^F, \dots, id_n^F : t_n^F) \to t$

class $id \ \{ \dots m_1 \dots m_k \ \}$ is in the program for all $j \in 1..k : methodname(m_j) \neq id^M$
 $methodtype(id, id^M) = \bot$

class $id \text{ extends } id^P \ \{ \dots m_1 \dots m_k \ \}$ is in the program for some $j \in 1..k : methodname(m_j) = id^M$
 m_j is of the form public $t id^M$ $(t_1^F id_1^F, \dots, t_n^F id_n^F)$ $\{t_1 id_1; \dots; t_r id_r; s_1 \dots s_q \text{ return } e; \}$
 $methodtype(id, id^M) = (id_1^F : t_1^F, \dots, id_n^F : t_n^F) \to t$

class $id \text{ extends } id^P \ \{ \dots m_1 \dots m_k \ \}$ is in the program for all $j \in 1..k : methodname(m_j) \neq id^M$
 $methodtype(id, id^M) = methodtype(id^P, id^M)$
 (15)

6.6 The noOverloading Helper function

$$\frac{methodtype(id^P, id^M) \neq \bot \quad \Rightarrow \quad methodtype(id^P, id^M) = methodtype(id, id^M)}{noOverloading(id, id^P, id^M)} \tag{16}$$

7 Type Rules

7.1 Type Judgments

We will use the following seven forms of type judgments:

We can read a judgment as follows. The judgment $\vdash g$ means "the goal g type checks." The judgment $\vdash mc$ means "the main class mc type checks." The judgment $\vdash d$ means "the type declaration d type checks." The judgment $C \vdash m$ means "if defined in class C, the method declaration m type checks." The judgment $A, C \vdash s$ means "in a type environment A, if written in class C, the statement s type checks." The judgment $A, C \vdash e : t$ means "in a type environment A, if written in class C, the expression e has type e." The judgment e0 in a type environment e1, if written in class e2, the primary expression e3 has type e3.

7.2 Goal

$$\frac{distinct(classname(mc), classname(d_1), \dots, classname(d_n))}{\vdash mc} \\ \frac{\vdash d_i \qquad i \in 1..n}{\vdash mc \ d_1 \ \dots \ d_n}$$

$$(17)$$

7.3 Main Class

7.4 Type Declarations

$$\begin{array}{l} distinct(id_1,\ldots,id_f) \\ distinct(methodname(m_1),\ldots,methodname(m_k)) \\ id \vdash m_i \quad i \in 1..k \\ \vdash \text{class } id \; \{ \; t_1 \; id_1; \; \ldots; \; t_f \; id_f; \; m_1 \; \ldots \; m_k \; \} \end{array}$$

$$\begin{array}{l} distinct(id_1,\ldots,id_f) \\ distinct(methodname(m_1),\ldots,methodname(m_k)) \\ noOverloading(id,id^P,methodname(m_i)) \quad id \vdash m_i \quad i \in 1..k \\ \hline \vdash \text{class } id \; \text{extends } id^P \; \{ \; t_1 \; id_1; \; \ldots; \; t_f \; id_f; \; m_1 \; \ldots \; m_k \; \} \end{array}$$

$$(20)$$

7.5 Method Declarations

$$\begin{aligned} & & & distinct(id_1^F, \dots, id_n^F) \\ & & & & distinct(id_1, \dots, id_r) \\ & & & A = fields(C) \cdot [id_1^F : t_1^F, \dots, id_n^F : t_n^F] \cdot [id_1 : t_1, \dots, id_r : t_r] \\ & & & & A, C \vdash s_i \qquad i \in 1..q \qquad A, C \vdash e : t \\ \hline & & & C \vdash \text{public } t \ id^M \ (t_1^F \ id_1^F, \ \dots, \ t_n^F \ id_n^F) \ \{t_1 \ id_1; \ \dots; \ t_r \ id_r; \ s_1 \ \dots \ s_q \ \text{return } e; \ \} \end{aligned}$$

7.6 Statements

$$\frac{A,C \vdash s_i \qquad i \in 1..q}{A,C \vdash \{s_1 \ldots s_q\}}$$

$$(22)$$

$$\frac{A(id) = t_1 \qquad A, C \vdash e : t_2 \qquad t_2 \le t_1}{A, C \vdash id = e;} \tag{23}$$

$$\frac{A(id) = \operatorname{int}[] \quad A, C \vdash e_1 : \operatorname{int} \quad A, C \vdash e_2 : \operatorname{int}}{A, C \vdash id \ [e_1] = e_2;} \tag{24}$$

$$\frac{A,C \vdash e : \texttt{boolean}}{A,C \vdash \texttt{if (}e \texttt{)} s_1 \texttt{ else } s_2} \tag{25}$$

$$\frac{A,C \vdash e : \texttt{boolean} \qquad A,C \vdash s}{A,C \vdash \texttt{while (}e \texttt{)}s} \tag{26}$$

$$\frac{A, C \vdash e : \mathtt{int}}{A, C \vdash \mathtt{System.out.println(} e \ \mathtt{);}} \tag{27}$$

7.7 Expressions and Primary Expressions

$$\begin{array}{c} A,C \vdash p_1 : \mathtt{boolean} & A,C \vdash p_2 : \mathtt{boolean} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_1 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{int} & A,C \vdash p_2 : \mathtt{int} \\ A,C \vdash p_2 : \mathtt{i$$